27-July-2021 Shift-1

EE24BTECH11035 - KOTHAPALLI AKHIL

- 1) If the mean and variance of the following data: 6, 10, 7, 13, a, 12, b, 12 are 9 and $\frac{37}{4}$ respectively, then $(a - b)^2$ is equal to:
 - a) 24
 - b) 12
 - c) 32
 - d) 16
- 2) The value of

$$\lim_{n \to \infty} \frac{1}{n} \sum_{j=1}^{n} \frac{(2j-1) + 8n}{(2j-1) + 4n} \tag{2.1}$$

is equal to:

- a) $5 + \log_e\left(\frac{3}{2}\right)$ b) $2 \log_e\left(\frac{2}{3}\right)$
- c) $3 + 2\log_e(\frac{2}{3})$ d) $1 + 2\log_e(\frac{3}{2})$
- 3) Let $\mathbf{a} = \hat{i} + \hat{j} + 2\hat{k}$ and $\mathbf{b} = -\hat{i} + 2\hat{j} + 3\hat{k}$. Then the vector product

$$(\mathbf{a} + \mathbf{b}) \times ((\mathbf{a} \times (\mathbf{a} - \mathbf{b}) \times \mathbf{b}) \times \mathbf{b})$$
(3.1)

is equal to:

- a) $5(34\hat{i} 5\hat{j} + 3\hat{k})$
- b) $7(34\hat{i} 5\hat{j} + 3\hat{k})$
- c) $7(30\hat{i} 5\hat{j} + 7\hat{k})$
- d) $5(30\hat{i} 5\hat{j} + 7\hat{k})$
- 4) The value of the definite integral

$$\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{dx}{(1 + e^{\cos^3 x})(\sin^4 x + \cos^4 x)}$$
 (4.1)

is equal to:

- 5) Let C be the set of all complex numbers. Let $S_1 = \{z \in \mathbb{C} \mid |z 3 2i| = 8\}$, $S_2 =$ $\{z \in \mathbb{C} \mid \text{Re}(z) \ge 5\}, \quad S_3 = \{z \in \mathbb{C} \mid |z - \overline{z}| \ge 8\}$ Then the number of elements in $S_1 \cap S_2 \cap S_3$ is equal to:
 - a) 1

- b) 0
- c) 2
- d) Infinite
- 6) If the area of the bounded region $R = \{(x, y) : \max\{0, \log_2 x\} \le y \le 2^x, \frac{1}{2} \le x \le 2\}$ is $\alpha(\log_2 2)^{-1} + \beta(\log_2 2) + \gamma$, then the value of $(\alpha + \beta 2\gamma)^2$ is equal to:
 - a) 8
 - b) 2
 - c) 4
 - d) 1
- 7) A ray of light through (2,1) is reflected at a point P on the y-axis and then passes through the point (5,3). If this reflected ray is the directrix of an ellipse with eccentricity $\frac{1}{3}$ and the distance of the nearer focus from this directrix is $\frac{8}{\sqrt{53}}$, then the equation of the other directrix can be:
 - a) 11x + 7y + 8 = 0 or 11x + 7y 15 = 0
 - b) 11x 7y 8 = 0 or 11x + 7y + 15 = 0
 - c) 2x 7y + 29 = 0 or 2x 7y 7 = 0
 - d) 2x 7y 39 = 0 or 2x 7y 7 = 0
- 8) If the coefficients of x^7 in $\left(x^2 + \frac{1}{bx^2}\right)^{11}$ and x^{-7} in $\left(x \frac{1}{bx^2}\right)^{11}$, $b \ne 0$ are equal, then the value of b is equal to:
 - a) 2
 - b) -1
 - c) 1
 - d) -2
- 9) The compound statement $(P \lor Q) \land (\sim P) \implies Q$ is equivalent to:
 - a) $P \vee Q$
 - b) $P \wedge \sim Q$
 - c) $\sim (P \implies Q)$
 - $\mathrm{d}) \sim (P \implies Q) \Leftrightarrow P \wedge \sim Q$
- 10) If $\sin \theta + \cos \theta = \frac{1}{2}$, then $16(\sin 2\theta + \cos 4\theta + \sin 6\theta)$ is equal to:
 - a) 23
 - b) -27
 - c) -23
 - d) 27
- 11) $Let\begin{pmatrix} 1 & 2 \\ -1 & 4 \end{pmatrix}$ If $A^{-1} = \alpha I + \beta A$, $\alpha, \beta \in \mathbb{R}$. If I is a 2×2 identity matrix, then $4(\alpha \beta)$ is equal to:
 - a) 5
 - b) $\frac{8}{3}$
 - c) 2
 - d) 4

12) Let $f: \left(-\frac{\pi}{4}, \frac{4}{4}\right) \to \mathbb{R}$ be defined as

$$f(x) = \begin{cases} (1 + |\sin x|) \cdot \frac{3}{\pi} &, & -\frac{\pi}{4} < x < 0 \\ b &, & x = 0 \\ e^{\cot(4/x \cdot 2x)} &, & 0 < x < \frac{\pi}{4} \end{cases}$$
 (12.1)

If f is continuous at x = 0, then the value of $6a + b^2$ is equal to:

- a) 1 e
- b) 2e 1
- c) 1 + e
- d) 4e
- 13) Let y = y(x) be the solution of the differential equation

$$\log_e\left(\frac{dy}{dx}\right) = 3x + 4y, \quad y(0) = 0.$$
 (13.1)

If $y(-\frac{2}{3}\log_2 2) = \alpha \log_2 2$, then the value of α is equal to:

- a) $-\frac{1}{4}$ b) $\frac{1}{4}$
- c) 2
- d) $-\frac{1}{2}$
- 14) Let the plane passing through the point (-1,0,-2) and perpendicular to each of the planes 2x + y - z = 2 and x - y - z = 3 be ax + by + cz + 8 = 0. Then the value of a + b + c is equal to:
 - a) 3
 - b) 8
 - c) 5
 - d) 4
- 15) Two tangents are drawn from the point P(-1, 1) to the circle $x^2 + y^2 2x 6y + 6 = 0$. If these tangents touch the circle at points A and B, and if D is a point on the circle such that the lengths of the segments AB and AD are equal, then the area of the triangle ABD is equal to:
 - a) 2
 - b) $2\sqrt{3} + 2$

 - c) 4 d) $3\sqrt{2} 1$