# **Answer Script**

# **Question No. 01**

Fibonacci Number

20

```
Memoization Method:
```

```
#include<bits/stdc++.h>
using namespace std;
const int N = 101;
int dp[N];
int fib(int n)
       if(n <= 2) return 1;
       if(dp[n] != -1) {
       return dp[n];
       int ans = fib(n-1) + fib(n-2);
       dp[n] = ans;
       return ans;
int main()
{
       int n;
       cin >> n;
       for(int i = 1; i \le n; i++) {
       dp[i] = -1;
       cout<< fib(n) << endl;
       return 0;
}
```

```
Tabulation Method:
#include<bits/stdc++.h>
using namespace std;
const int N = 101;
int dp[N];
int main()
{
     int n;
     cin >> n;
     dp[1] = 1;
     dp[2] = 1;

     for(int i = 3 ; i <= n ; i++) {
        dp[i] = dp[i-1] + dp[i-2];
      }
      cout << dp[n] << endl;
     return 0;
}</pre>
```

# **Question No. 02**

FARIDA 20

```
Memoization Method:
```

```
#include<bits/stdc++.h>
using namespace std;
vector<long long int> dp(1000000);
long long int maxloot(vector<int> &loot, int n)
       if (n == 0)
       return 0;
       if (n == 1)
       return loot[0];
       if (n == 2)
       return max(loot[0], loot[1]);
       if (dp[n] != -1)
       return dp[n];
       long long int take = loot[n - 1] + maxloot(loot, n - 2);
       long long int leave = maxloot(loot, n - 1);
       return dp[n] = max(take, leave);
int main()
       int t;
       cin >> t;
       int p = 1;
       while (t--)
       {
       int n;
       cin >> n;
       vector<int> loot;
       for (int i = 0; i < n; i++)
```

```
int temp;
      cin >> temp;
      loot.push_back(temp);
      dp.assign(1000000, -1);
      cout << "Case " << p << ": " << maxloot(loot, n) << endl;
      p++;
      dp.clear();
Tabulation Method:
#include<bits/stdc++.h>
using namespace std;
int main()
{
      int T, N, c;
      long long tmp, dp[4];
      cin >> T;
      for(int tc=1; tc <= T; ++tc) {
      cin >> N;
      c = 0;
      for(int i=0; i<4; ++i)
      dp[i] = 0;
      for(int i=0; i<N; ++i) {
      cin >> tmp;
      dp[c] = tmp + max(dp[(c+2)\%4], dp[(c+1)\%4]);
      c = (c+1)\%4;
      tmp = max(dp[(c+2)\%4], dp[(c+3)\%4]);
      cout << "Case " << tc << ": " << tmp << "\n";
      return 0;
```

# **Question No. 03**

Boredom 20

```
Memoization Method:
```

```
#include <bits/stdc++.h>
using namespace std;
int n;
map<int, int> m;
vector<pair<int, int>> v;
long long f[111111];
int nextInt()
{
       int x = 0, p = 1;
       char c;
       do {
       c = getchar();
       ) while (c <= 32);
       if (c == '-') {
       p = -1;
       c = getchar();
       while (c >= '0' && c <= '9') {
       x = x * 10 + c - '0';
       c = getchar();
       return x * p;
long long solve(int idx)
       if (idx == 0) return 1LL * v[idx].first * v[idx].second;
       if (f[idx] != -1) return f[idx];
       int pr = idx - 1;
```

```
while (pr \geq 0 && v[pr].first + 1 == v[idx].first) pr--;
       if (pr == -1)
       f[idx] = 1LL * v[idx].first * v[idx].second;
       else
       f[idx] = solve(pr) + 1LL * v[idx].first * v[idx].second;
       f[idx] = max(f[idx], solve(idx - 1));
       return f[idx];
int main()
{
       n = nextInt();
       while (n--) {
       int x = nextInt();
       m[x]++;
       for (map<int, int>::iterator it = m.begin(); it != m.end(); it++) {
       v.push_back(make_pair(it->first, it->second));
       }
       memset(f, -1, sizeof(f));
       cout << solve(v.size() - 1) << "\n";
       return 0;
Tabulation Method:
#include <bits/stdc++.h>
using namespace std;
int n;
map<int, int> m;
vector<pair<int, int>> v;
long long f[111111];
int nextInt()
```

```
int x = 0, p = 1;
       char c;
       do {
       c = getchar();
       } while (c <= 32);
       if (c == '-') {
       p = -1;
       c = getchar();
       while (c >= '0' && c <= '9') {
       x = x * 10 + c - '0';
       c = getchar();
       return x * p;
int main()
       n = nextInt();
       while (n--) {
       int x = nextInt();
       m[x]++;
       for (map<int, int>::iterator it = m.begin(); it != m.end(); it++) {
       v.push_back(make_pair(it->first, it->second));
       f[0] = 1LL * v[0].first * v[0].second;
       for (int i = 1; i < v.size(); i++) {
       int pr = i - 1;
       while (pr \ge 0 \&\& v[pr].first + 1 == v[i].first) pr--;
       if (pr == -1)
       f[i] = 1LL * v[i].first * v[i].second;
       else
       f[i] = f[pr] + 1LL * v[i].first * v[i].second;
       f[i] = max(f[i], f[i - 1]);
```

```
cout << f[v.size() - 1] << "\n";
return 0;
}
```

# N-th Tribonacci Number

```
Memoization Method:
#include<bits/stdc++.h>
using namespace std;
vector<int> dp(101, -1);
int tribonacciMemo(int n)
{
       if (n \le 0)
       return 0;
       if (n == 1 || n == 2)
       return 1;
       if (dp[n] != -1)
       return dp[n];
       dp[n] = tribonacciMemo(n - 1) + tribonacciMemo(n - 2) + tribonacciMemo(n
- 3);
       return dp[n];
int main()
{
       int n;
       cin >> n;
       int tribN = tribonacciMemo(n);
       cout << tribN << "\n";
       return 0;
Tabulation Method:
#include<bits/stdc++.h>
using namespace std;
int tribonacciTab(int n)
```

```
{
    vector<int> dp(n + 1);
    dp[0] = 0;
    dp[1] = 1;
    dp[2] = 1;
    for (int i = 3; i <= n; i++)
    {
        dp[i] = dp[i - 1] + dp[i - 2] + dp[i - 3];
        }
        return dp[n];
}

int main()
{
        int n;
        cin >> n;
        int tribN = tribonacciTab(n);
        cout << tribN << "\n";
        return 0;
}</pre>
```

#### Question No. 05

You are given an integer n.You can perform any of the following operations on it as many times you want -

- Subtract 1 from it
- If it is divisible by 2 divide by 2
- If it is divisible by 3 divide by 3

Find the minimum number of operations to make n=1

# **Constraints** -

1<=n<=10^5

# Output -

Print a single integer, the minimum number of operations to make n=1

Sample Input-	Sample Output-
7	3
11	4

# **Explanation-**

When n = 7,

By using 3 operations we can go from 7 to 1.

- >> 1st step -> subtract 1 from 7 then it became 6
- >> 2nd step -> 6 is divisible by 3 hence we can divide it by 3 and it became 2
- >> 3rd step -> 2 is divisible by 2 hence we can divide it by 2 and it became 1

#### Answer No. 05

#### **Memoization Method:**

```
#include<bits/stdc++.h>
using namespace std;
unordered_map<int, int> dp;
int minOperations(int n) {
       if (n == 1) {
       return 0;
       if (dp.find(n) != dp.end()) {
       return dp[n];
       }
       int ans = 1 + \min Operations(n - 1);
       if (n % 2 == 0) {
       ans = min(ans, 1 + minOperations(n / 2));
       if (n \% 3 == 0) {
       ans = min(ans, 1 + minOperations(n / 3));
       }
       dp[n] = ans;
       return ans;
int main() {
       int n;
       cin >> n;
       int ans = minOperations(n);
       cout << ans << "\n";
       return 0;
Tabulation Method:
#include<bits/stdc++.h>
using namespace std;
int minOperations(int n) {
```

```
vector<int> dp(n + 1, 0);

for (int i = 2; i <= n; i++) {
    dp[i] = 1 + dp[i - 1];

    if (i % 2 == 0) {
        dp[i] = min(dp[i], 1 + dp[i / 2]);
    }

    if (i % 3 == 0) {
        dp[i] = min(dp[i], 1 + dp[i / 3]);
    }
    }
    return dp[n];
}

int main() {
    int n;
    cin >> n;
    int ans = minOperations(n);
    cout << ans << "\n";
    return 0;
}</pre>
```