

<https://www.chegg.com/homework-help/questions-and-answers/question-based-strassen-s-matrix-multiplication-algorithm-got-answer-wrong-answer-apparentl-q27035906>

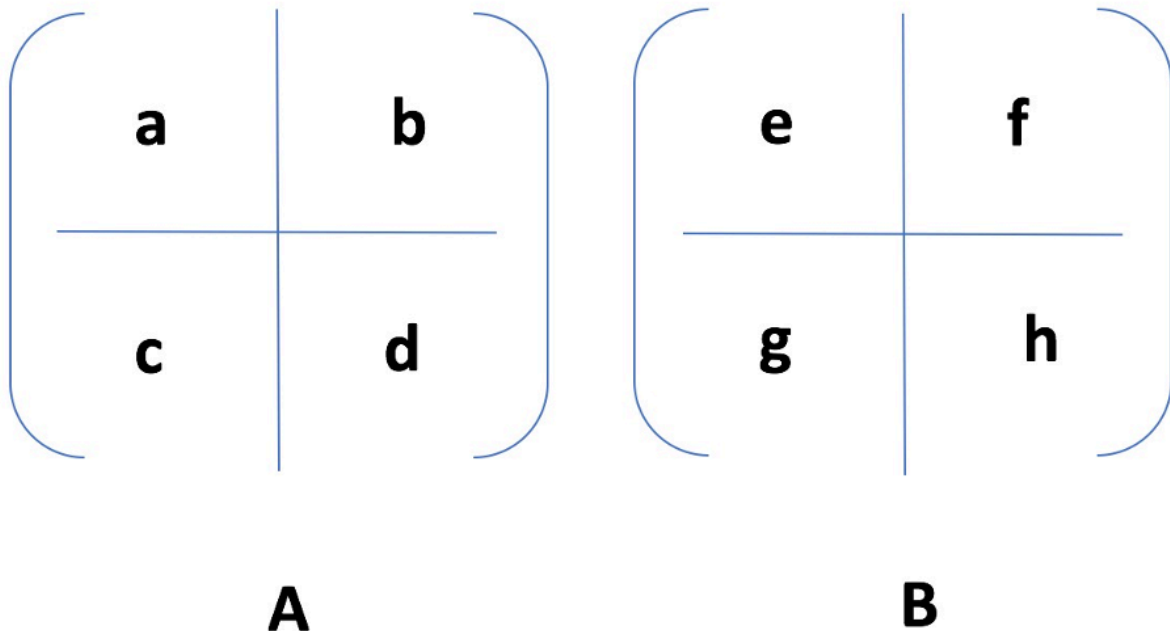
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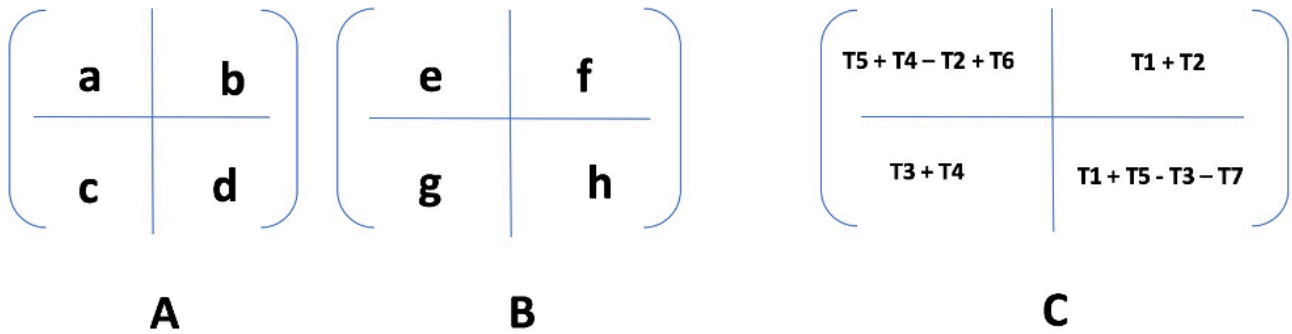
Divide and Conquer technique is used in Strassen Matrix multiplication. In which, the matrices ($N \times N$) is divided into 4 submatrices of size ($N/2 \times N/2$).

Suppose we have 2 matrix of size ($N \times N$) as A and B. Divide both of them into sub matrices as $A(a,b,c,d)$ and $B(e,f,g,h)$

like this



In traditional divide and conquer method, at every recursive call there are 8 multiplications and 4 additions, but in Strassen it is reduced to 7 multiplication at every step.



$$\begin{aligned}
 T1 &= a(f - h) & T2 &= (a + b)h & T3 &= (c + d)e & T4 &= d(g - e) & T5 &= (a + d)(e + h) \\
 T6 &= (b - d)(g + h) & T7 &= (a - c)(e + f)
 \end{aligned}$$

So as you can see from above diagram, we can see the recursive call equation is: **$P(N) = 7P(N/2) + O(N^2)$**

So at every recursive we are multiplying matrices 7 times instead of 8 times.

When $N=2$, there will be 7 multiplications of (1×1) matrices and every (1×1) matrix takes only one operations. = 7 multiplications

when $N=4$, there will be 7 multiplications of (2×2) matrices and every (2×2) matrix takes 7 multiplications so total number of multiplications = 49.

when $N=8$, there will be 7 multiplications of (4×4) matrices and every (4×4) matrix takes 49 multiplications so total number of multiplications = $7 * 49 = 343$.

when $N=16$, there will be 7 multiplications of (8×8) matrices and every (8×8) matrix takes 343 multiplications so total number of multiplications = $7 * 343 = 2401$

Hence the total number of multiplications are 2401 for 16×16 matrix.