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let $x(t)$ be the signal

$$x(t) = [10 + 5 \cdot \cos(2000\pi t + \pi/5)] \cdot \cos(10000\pi t)$$

Q-1) Use the Euler's relation to expand $x(t)$ as a sum of complex exponential signals and show that it can be expressed in the Fourier series form

$$x(t) = \sum_{k=-\infty}^{\infty} a_k e^{j k \omega_0 t}$$

My signal is $\rightarrow x(t) = [10 + 5 \cdot \cos(2000\pi t + \pi/5)] \cdot \cos(10000\pi t)$

Euler formula $\rightarrow \cos(\theta) = \frac{1}{2}(e^{j\theta} + e^{-j\theta})$ jetlinde ifade edilir
first step:

$$\cos(2000\pi t + \pi/5) \rightarrow \cos(2000\pi t + \pi/5) = \frac{1}{2} (e^{j(2000\pi t + \pi/5)} + e^{-j(2000\pi t + \pi/5)})$$

Second step:

$$\cos(10000\pi t) \rightarrow \cos \rightarrow \frac{1}{2} (e^{j10000\pi t} + e^{-j10000\pi t})$$

result

$$x(t) = \left[10 + \frac{5}{2} (e^{j(2000\pi t + \pi/5)} + e^{-j(2000\pi t + \pi/5)}) \right] \cdot \frac{1}{2} (e^{j10000\pi t} + e^{-j10000\pi t})$$

$$\frac{1}{2} (e^{j10000\pi t} + e^{-j10000\pi t})$$