



Let the universe set  $U = \{1, 2, 3, ..., 10\}$ .

Let 
$$A=\{1,4,7,10\}$$
  $B=\{1,2,3,4,5\}$   $C=\{2,4,6,8\}$ 

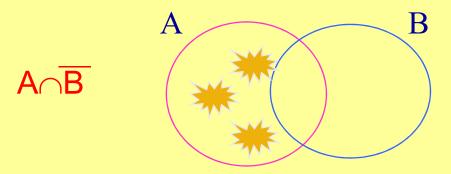
List the elements of each set.

A
$$\cup$$
B= {1,2,3,4,7,5,10}  
B-A= {2,3,5}  
 $\overline{U}$ = Ø  
A $\cup$  U= U  
 $\overline{B} \cap (C-A)$ ={6,8}  
(A $\cup$ B)-(C-B)={1,2,3,4,5,7,10}

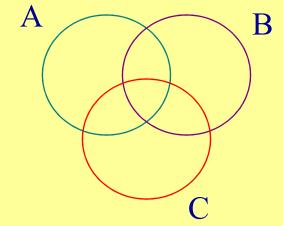




## Draw a Venn diagram and shade the given set.



$$((C \cap A) - (\overline{B} - \overline{A})) \cap C$$

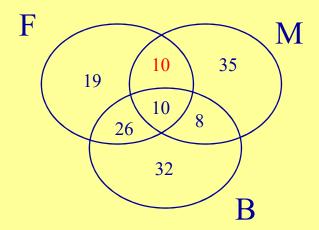






There is a group of 191 students. 10 students are taking French, Business and Music; 36 are taking French and Business; 20 are taking French and Music; 18 are taking Business and Music; 65 are taking French; 76 are taking Business and 63 are taking Music.

How many are taking French and Music not Business?

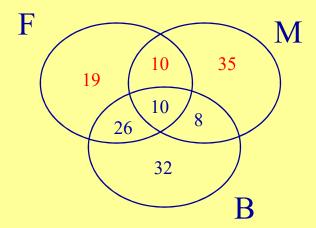






There is a group of 191 students. 10 students are taking French, Business and Music; 36 are taking French and Business; 20 are taking French and Music; 18 are taking Business and Music; 65 are taking French; 76 are taking Business and 63 are taking Music.

How many are taking Music or French (or both) but not Business?







Write "true" if the statement is true; otherwise give a counterexample. The sets X, Y and Z are subsets of a universal set U. Assume that the universe for Cartesian products is UxU.

 $(X \cap Y) \cup (Y-X) = X$  for all sets X and Y

False

$$X=\{1\}$$
  $Y=\{1,2\}$ 



## For the sequence a defined by



$$a_i = i^2 - 3i + 3$$
 i  $\ge 1$ 

Find 
$$\sum_{i=1}^{4} a_i = 12$$

$$\operatorname{Find} \prod_{i=3}^{4} a_i = 21$$



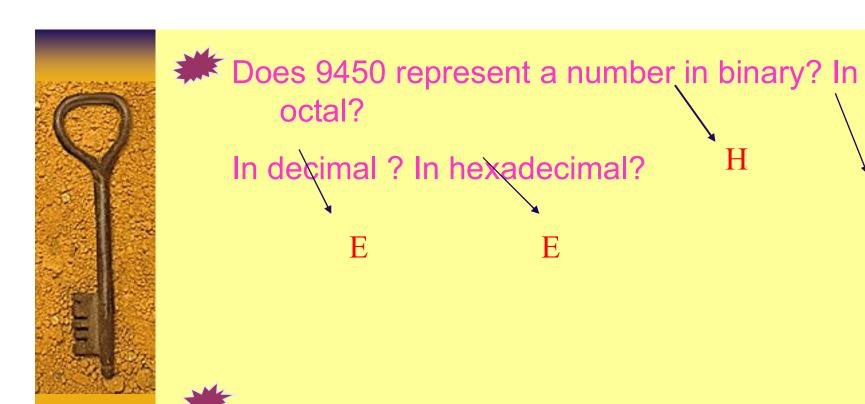


## Using the sequences y and z defined by

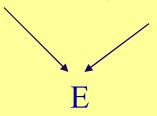
$$y_i = 2^i - 1$$
$$z_i = i(i - 1)$$

Find 
$$\left(\sum_{i=1}^{3} y_i\right) \left(\sum_{i=1}^{3} z_i\right) = 88$$

Find 
$$\left(\sum_{i=1}^{4} y_i\right) \left(\prod_{i=2}^{4} z_i\right) = 3744$$



1101010 represents in decimal, in hexadecimal.



H



# For the relation R on the set $\{1,2,3,4,5\}$ defined by the rule $(x,y) \in R$ if $x+y \le 6$

#### List the elements of R

$$R = \{(1,1)(1,3)(1,2)(1,4)(1,5)(2,2)(2,1)(2,3)(2,4)(3,3)(3,2)$$

$$(3,1)(4,1)(4,2)(5,1)\}$$

### Find the range of R

$$R = \{1,2,3,4,5\}$$

### Find the range of R<sup>-1</sup>

$$Dom(R)=Rng(R)=Rng(R^{-1})=\{1,2,3,4,5\}$$



# Give examples of relations on {1,2,3,4} having the properties specified

Reflexive, symmetric and non transitive

$$R = \{(1,1)(2,2)(3,3)(4,4)(1,2)(2,1)(2,3)(3,2)\}$$

Non reflexive, symmetric, not antisymmetric and transitive

$$R = \{(1,1)(1,2)(2,1)(2,2)\}$$



Let R and S be relations on X. Determine statement is true or false?

If the statement is false give a counterexample

If R and S are antisymmetric, then  $R \cup S$  is antisymmetric

#### **FALSE**

$$R=\{(1,2)\}\ S=\{(2,1)\}\ R\cup S=\{(1,2)(2,1)\}$$





Determine whether the given relation is an equivalence relation on {1,2,3,4,5}. Given relation is true or false?

{(1,1)(2,2)(3,3)(4,4)(5,5)(1,5)(5,1)(3,5)(5,3)(1,3)(3,1) TRUE

 $\{(x,y) \mid 3 \text{ divides } x+y\}$ 

**FALSE** 





#### Each function is one-to-one. Find each inverse function

$$f(x) = 4x + 2$$

$$f(x)^{-1}=(x-2)/4$$

$$f(x)=3+1/x$$

$$f(x)^{-1}=1/(x-3)$$