Homework 3 (Due October 24, 2016, 9:00 AM)
BLM 1541: Statistics and Probability — Fall 2016
Print family (or last) name:
Print given (or first) name:
Print given student number:
I see that this homework has 5 questions in total.
I agree that I have to submit my homework solution before the deadline (October 24, 2016, 9 AM) otherwise my homework solution will not be graded.
I accept that <i>I will add the signed version of this instruction page as a first page into my homework solution</i> ; otherwise my homework solution will not be graded.
I know that <i>I have to give my solutions written on white A4-sized pages that are stapled on the left-up corner</i> ; otherwise my homework solution will not be graded.
I will take care of the readability of my solutions, from which I may lose 10 points.
For any proofs, I am sure to provide a step-by-step argument, with justifications for every step.
I understand that, during solving this homework, it is prohibited to exchange information about solutions with any other person in any way, including by talking or ex-changing solutions / papers
I know that the course book is "Probability and Statistics for Computer Scientists, by Michael Baron (2nd Edition)".
I have read, understand and accept all of the instructions above. On my honor, I pledge that I have not violated the provisions of the Academic Integrity Code of Yıldız Technical University.
Signature and Date

Problem 1 [20 Points]: By the end of the course BLM1541: Statistics and Probability (Fall'16), a group of students, consisting 4 male and 2 female students, is selected according to student's performance. As a researcher. I would like to pick three students from this group in order to study and analyze the performance of unmanned air vehicles (UAVs) in extreme situations (Hint: Three students are picked from the group without any replacement).

a) Two male students are randomly selected without replacement from the group. Find the probability that at least two of the selected students are male students.

Let X be the random variable that represents the number of picked male students.

- b) Find and plot the probability mass function (PMF) of the random variable X.
- c) Find and the cumulative distribution function, F, of the random variable X.
- d) Compute the expected value and variance of X.
- e) Compute the expected value of $\ln(X)$, which is the entropy obtained for diversity benefits in the project.

Problem 2 [20 Points]: In Davutpasa housing compound of Yıldız Technical University, the heating systems are provided from three companies.

- Company A has installed its system into 60% of houses and 8% of its products are defective
- Company B has installed its system into 30% of houses and 6% of its products are defective
- Company C has installed its system into 10% of houses and 10% of its products are defective

With these information,

- a) What's the probability that the heating system in a house is defective?
- b) Given that it is defective, how likely was it to have been produced by Company C?

Problem 3 [20 Points]: Toss a coin 20 times, and let X be the number of heads that turn up. What is the probability that X is divisible by 2, given that X is divisible by 3?

Problem 4 [20 Points]: In Besiktas, when I asked the traffic police what the average number of car accidents is in Besiktas per day, he answered me 5 car accidents per day. What is the probability that in any given day the number of car accidents in Beşiktaş will exceed 4? Be sure to explain your reasoning.

Problem 5 [20 Points]: Decide about whether each of the following statements is TRUE or FALSE, and shortly explain your explanation of why:

- a) ______: If events X and Y are independent, then knowing P(X) and P(Y) allows one to compute
- b) ______: Mutually exclusive events are not always (in fact almost never) independent.
- c) _____: A student comes up a discrete function in his/her research like that

$$f(x_i) = \begin{cases} \alpha \ (1 + x_i - {x_i}^2), & x_i = -3, -2, -1, 0, 1, 2, 3 \\ 0, & \text{othewise} \end{cases}$$
 with $\alpha \in \mathbb{R}$. Could this function be a valid PMF, with an appropriate choice of α .

- d) ______: If discrete random variables X and Y are independent, then $\mathbb{E}[XY] = \mathbb{E}[X]\mathbb{E}[Y]$.
- e) : Let X be a random variable with sample space Ω . If $P(A \cup B) = \Omega$, can A and B be independent?
- f) _____: If X is a discrete random variable and c is a constant, the following all properties of the variance are valid:
 - var(c) = 0
 - var(X + c) = var(X)
 - $var(cX) = c^2 var(X)$