# **Cache Memory**

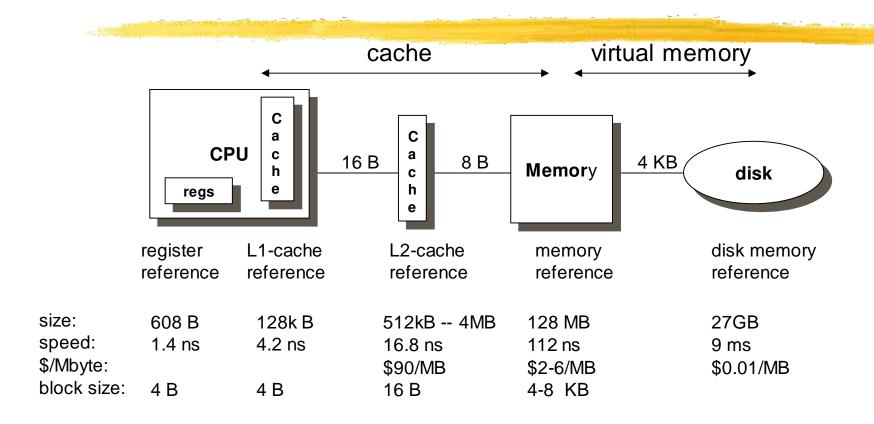
#### **Outline**

- Memory Hierarchy
- Direct-Mapped Cache
- □ Write-Through, Write-Back
- Cache replacement policy
- Examples

# **Principal of Locality**

- Cache work on a principal known as locality of reference. This principal states asserts that programs continually use and re-use the same locations.
  - -Instructions: Loops, common subroutines
  - -Data: Look-up Tables, data sets(arrays)
- Temporal Locality (locality in time):Same location will be referenced again soon
- Spatial Locality (locality in space): Nearby locations will be referenced soon

# **The Tradeoff**

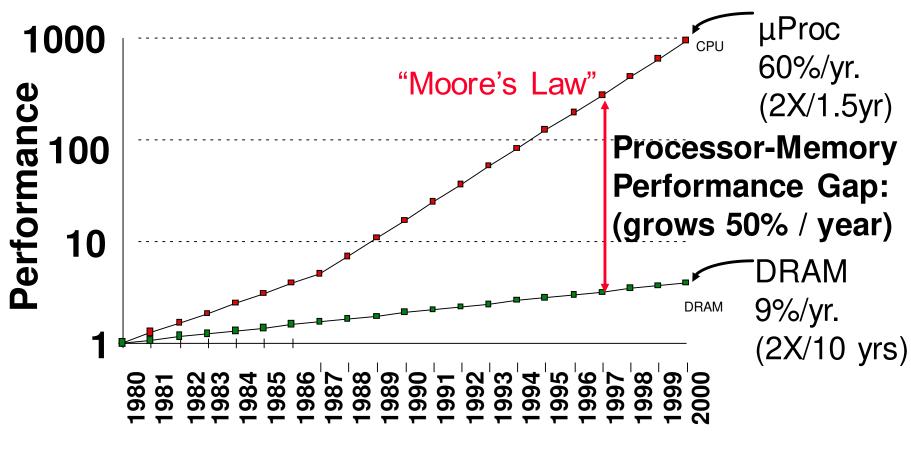


larger, slower, cheaper

(Numbers are for a DEC Alpha 21264 at 700MHz)

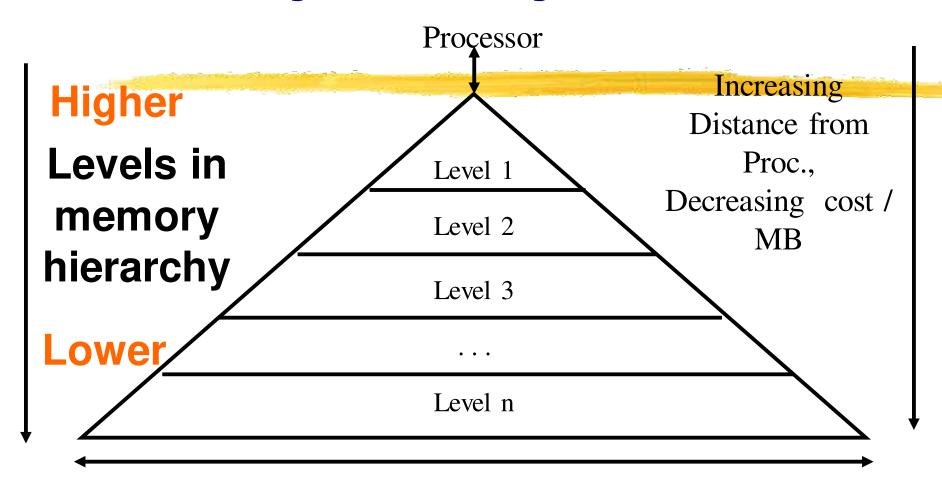
# **MOORE's LAW**

**Processor-DRAM Memory Gap (latency)** 



Time

# **Memory Hierarchy**



Size of memory at each level

# **Cache Design**

- How do we organize cache?
- □ Where does each memory address map to? (Remember that cache is subset of memory, so multiple memory addresses map to the same cache location.)
- How do we know which elements are in cache?
- How do we quickly locate them?

# **Cache mappings**

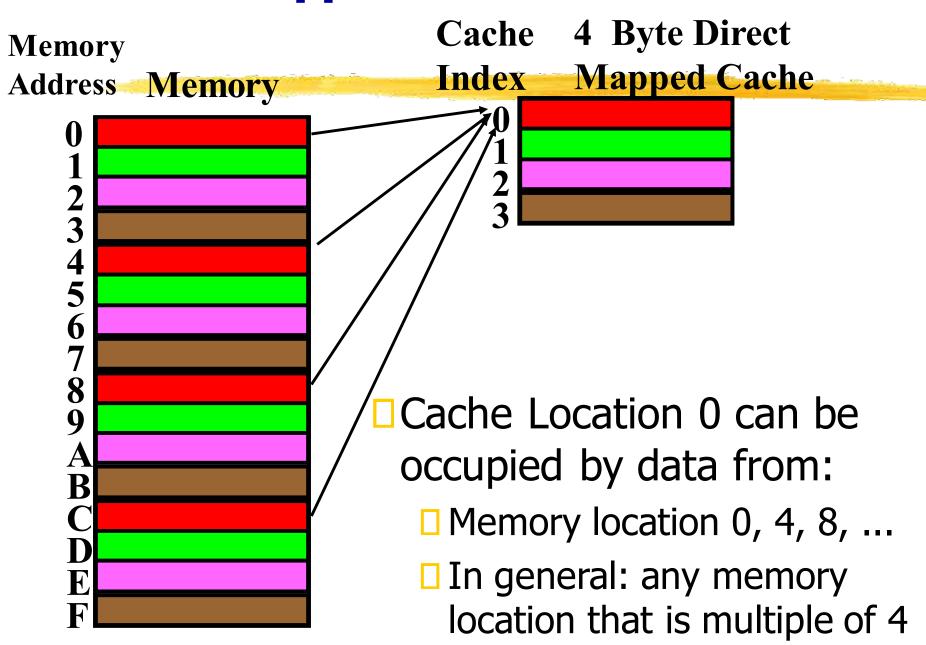
□ There are three types of methods for mapping between the main memory addresses and the cache addresses.

- Fully associative cache
- Direct mapped cache
- Set associative cache

#### **Direct-Mapped Cache**

- In a <u>direct-mapped cache</u>, each memory address is associated with one possible <u>block</u> within the cache
  - □ Therefore, we only need to look in a single location in the cache for the data if it exists in the cache
  - Block is the unit of transfer between cache and memory

### **Direct-Mapped Cache**



### **Issues with Direct-Mapped**

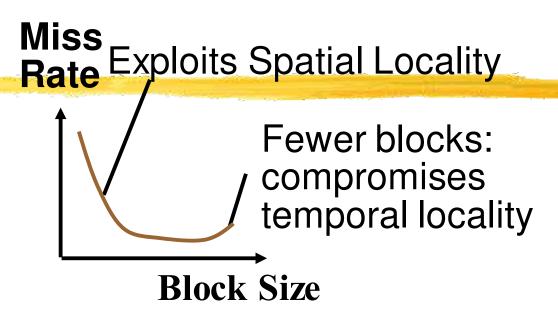
- Since multiple memory addresses map to same cache index, how do we tell which one is in there?
- What if we have a block size > 1 byte?
- Result: divide memory address into three fields

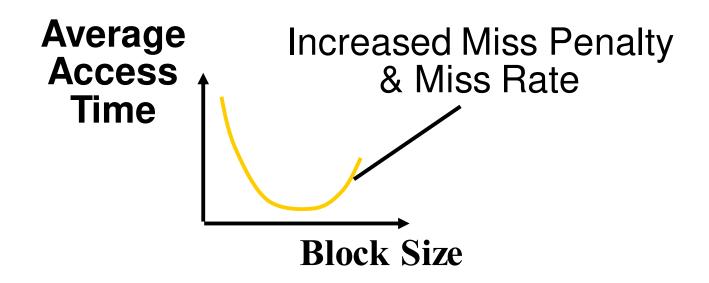
ttttttttttt	iiiiiiiii	0000
tag	index	byte
to check	to	offset
if have	select	within
correct block	block	block

# **Direct-Mapped Cache Terminology**

- All fields are read as unsigned integers.
- Index: specifies the cache index (which "row" of the cache we should look in)
- Offset: once we've found correct block, specifies which byte within the block we want
- Tag: the remaining bits after offset and index are determined; these are used to distinguish between all the memory addresses that map to the same location

#### **Block Size Tradeoff Conclusions**





# **Direct-Mapped Cache Example**

- Suppose we have a 16KB of data in a directmapped cache with 4 word blocks
- □ Determine the size of the tag, index and offset fields if we're using a 32-bit architecture
- Offset
  - need to specify correct byte within a block
  - □ block contains 4 words = 16 bytes = 2<sup>4</sup> bytes
  - □ need <u>4 bits</u> to specify correct byte

# **Direct-Mapped Cache Example**

- □ Index: (~index into an "array of blocks")
  - need to specify correct row in cache
    - $\square$  cache contains 16 KB =  $2^{14}$  bytes
  - □ block contains 2<sup>4</sup> bytes (4 words)
  - # rows/cache =# blocks/cache (since there's one block/row)
  - = <u>bytes/cache</u> bytes/row
  - = 2<sup>14</sup> <u>bytes/cache</u> 2<sup>4</sup> bytes/row
  - = 2<sup>10</sup> rows/cache need <u>10 bits</u> to specify this many rows

# **Direct-Mapped Cache Example**

- Tag: use remaining bits as tag
  - □ tag length = mem addr length offset index

- □ so tag is leftmost <u>18 bits</u> of memory address
- Why not full 32 bit address as tag?
  - □ All bytes within block need same address (-4b)
  - □ Index must be same for every address within a block, so its redundant in tag check, thus can leave off to save memory (- 10 bits in this example)

#### Accessing data in a direct mapped cache

#### **Memory**

- Ex.: 16KB of data, directmapped,4 word blocks
- □Read 4 addresses
  - □0x00000014, 0x0000001C, 0x00000034, 0x00008014
- Memory values on right:
  - only cache/memory level of hierarchy

Address (hex) 00000010 0000014	Value of Word
00000018 0000001C	c d
 00000030 00000034 00000038	e f g
0000003C  00008010 00008014	i i
00008018 0000801C	K

#### Accessing data in a direct mapped cache

- 4 Addresses:
  - □0x00000014, 0x0000001C, 0x00000034, 0x00008014
- □4 Addresses divided (for convenience) into Tag, Index, Byte Offset fields

```
      000000000000000000
      0000000000
      0100

      0000000000000000
      000000000
      1100

      0000000000000000
      000000001
      0100

      0000000000000000
      000000000
      0100

      Tag
      Index
      Offset
```

# Accessing data in a direct mapped cache

- ☐So lets go through accessing some data in this cache
  - □16KB data, direct-mapped, 4 word blocks
- □Will see 4 types of events:
- Cache loading: Before any words and tags have been loaded into the cache, all locations contains invalid information. As lines are fetched from main memory into the cache, cache entries become valid. To represent this structure a valid bit added to each cache entry.
- <u>cache miss</u>: nothing in cache in appropriate block, so fetch from memory
- <u>cache hit</u>: cache block is valid and contains proper address, so read desired word
- <u>cache miss, block replacement</u>: wrong data is in cache at appropriate block, so discard it and fetch desired data from memory

#### **Cache Loading**

- Before any words and tags have been loaded into the cache, all locations contains invalid information. As lines are fetched from main memory into the cache, cache entries become valid. To represent this structure a **valid bit** added to each cache entry. This valid bit indicates that the associated cache line is valid(1) or invalid(0).
- ☐ If the valid bit is 0, then a cache miss occurs even if the tag matches the address from CPU, required addressed word to be taken from main memory.

#### 16 KB Direct Mapped Cache, 16B blocks

□ Valid bit: determines whether anything is stored in that row (when computer initially turned on, all entries are invalid)

Example Block 0x8-b 0xc-f Valid 0x4 - 7 $0 \times 0 - 3$ Index Tag 1234567 1022

#### Read 0x00000014 = 0...00 0..001 0100

Tag field

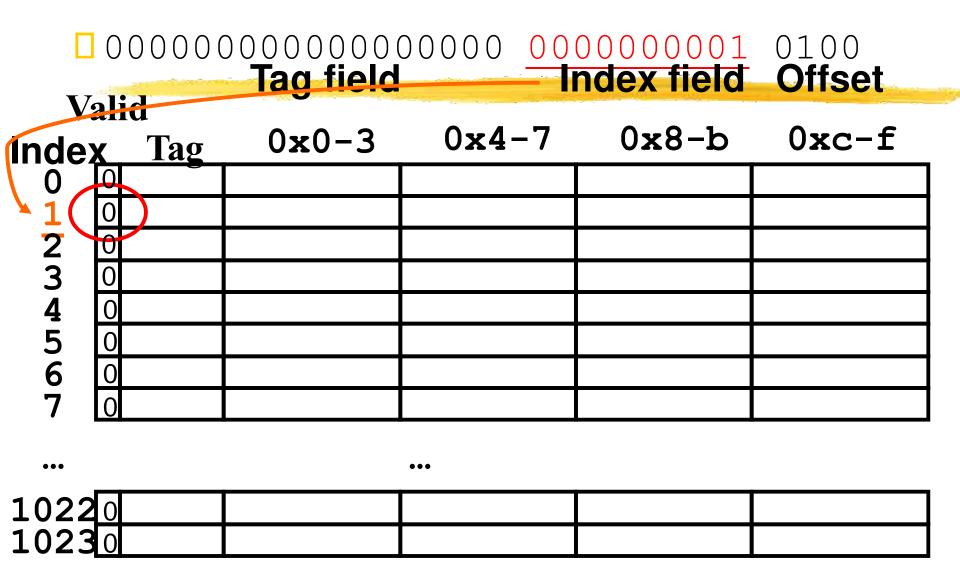
Index field Offset

Valid					
Index	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0				
1	0				
2	0				
01234567	0				
4	0				
5	0				
6	0				
7	0				
•••			•••		
1022 1023	0				
1023					

#### So we read block 1 (000000001)

Tag field Index field Offset Valid 0x4-7 $0 \times 0 - 3$ 0x8-b0xc-f Tag Index **1**234567 **1022**0 **1023**0

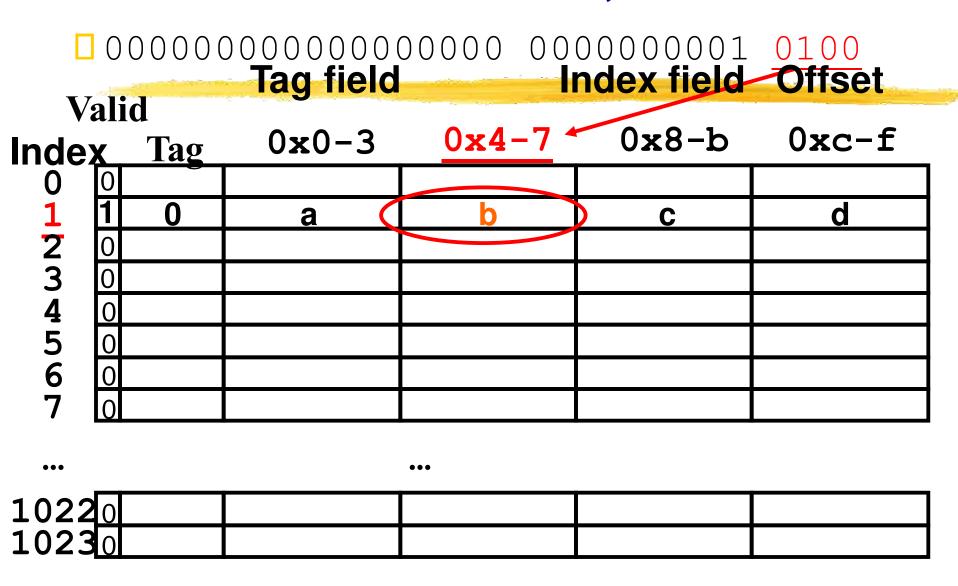
#### No valid data



# So load that data into cache, setting tag, valid

0100 Tag field Valid Index field Offset 0x0-30x4-7Index **Tag** 1234567 **1022**0 10230

#### Read from cache at offset, return word b



#### Read 0x000001C = 0...00 0..001 1100

 $\square$  00000000000000000 000000001 1100 Index field Offset Tag field Valid 0x4-70x0-30x8-b 0xc-fIndex Tag 1234567 b a **1022**0 **1023**0

# Data valid, tag OK, so read offset return word d

0x8-b0x4-70xc-f 0x0-3Index **Tag 1**234567 b a **1022**0 10230

#### Read 0x00000034 = 0...00 0..011 0100

	000	0000	00000000 Tag field	000	0000011	0100 <b>Offset</b>
V Inde	anc	1	0x0-3	0x4-7	0x8-b	0xc-f
0		0	а	b	С	d
1 2 3 4 5 6	0		a			<u>u</u>
3 4 5	0					
5 6 7	0					
,	0					
1022	0			•••		
1023						

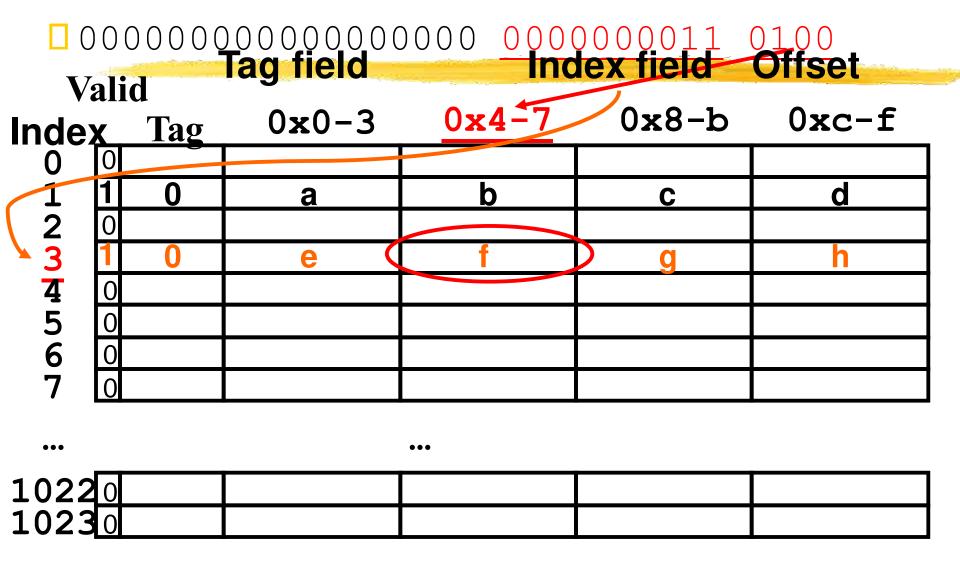
#### So read block 3

	000	0000	000000000 Tag field	000 0000	0000011 lex field	0100 <b>Offset</b>
V Inde	an	a	0x0-3	0x4-7	0x8-b	0xc-f
0	0	0	a	b	С	d
2 3 4 5 6 7	0					
<b>4</b> 5	0					
6 7	0					
•••				•••		
1022 1023	0					

### No valid data

et c-f
d

# Load that cache block, return word f



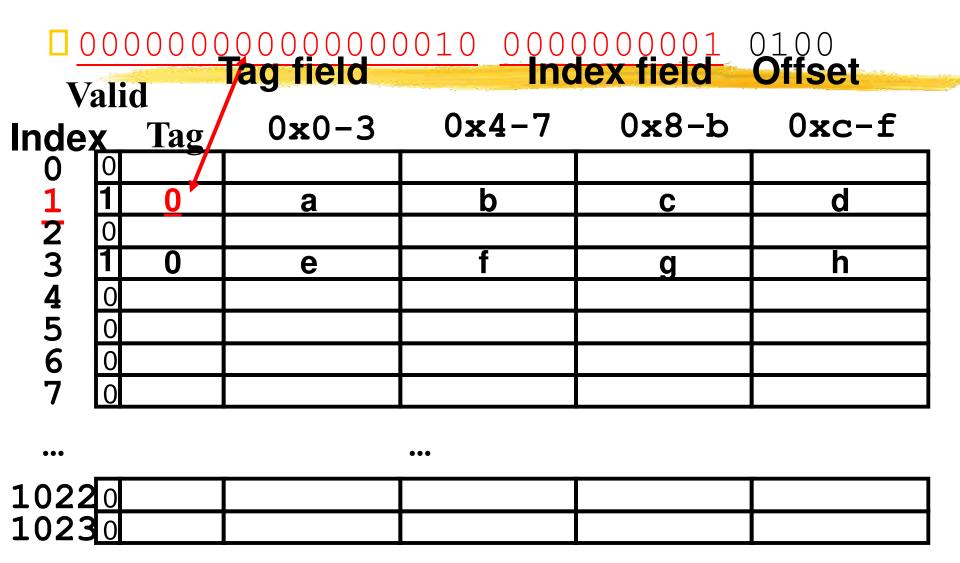
#### Read 0x00008014 = 0...10 0..001 0100

Tag field Index field Offset						
V	an	a	0x0-3	0x4-7		0xc-f
Inde 0		0	а	b	С	d
2	Ō		a			u
1 2 3 4 5 6 7	<b>1</b>	0	е	f	g	h
5	0					
6 7	0					
•						
1022	ار اد			•••		
1023	0					

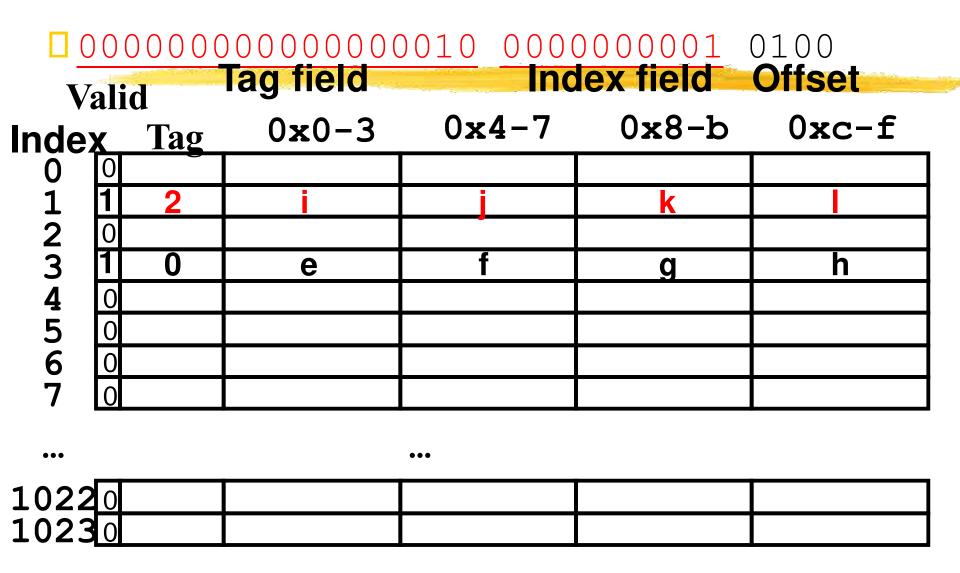
# So read Cache Block 1, Data is Valid

Valid 0x0-30x4-70x8-b 0xc-f**Tag** Index 01234567 b d a a 10220 10230

#### Cache Block 1 Tag does not match (0 != 2)



#### Miss, so replace block 1 with new data & tag



## And return word j

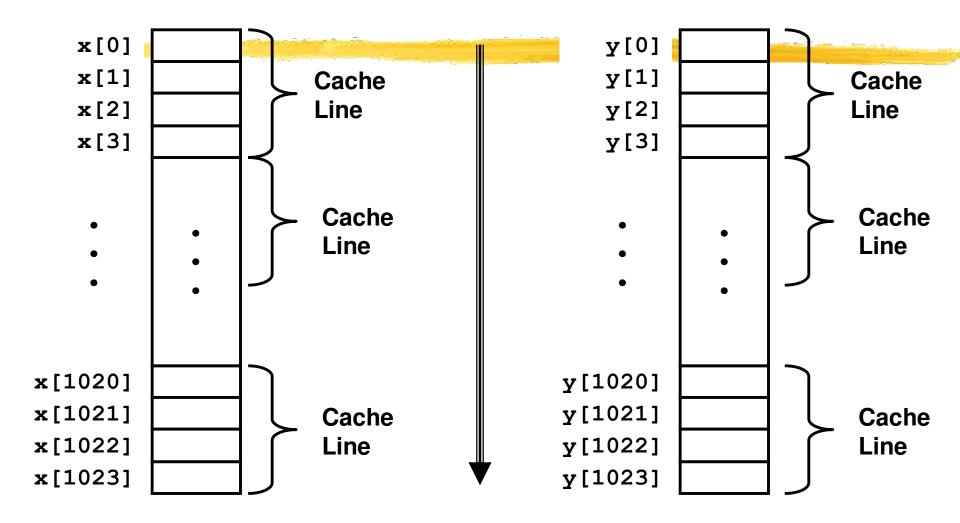
	) () (	0000	000000000 <b>Tag field</b>	010 000	0000001	0100
V Inde		d Tag	0x0-3	0x4-7	0x8-b	
	0 1	2	i		k	I
0 1 2 3 4 5 6	0 <b>1</b>	0	е	f	g	h
<b>4 5</b>	0					
6 7	0 0					
•••				•••		
1022 1023	0					

#### **Vector Product Example**

```
float dot_prod(float x[1024], y[1024])
{
  float sum = 0.0;
  int i;
  for (i = 0; i < 1024; i++)
     sum += x[i]*y[i];
  return sum;
}</pre>
```

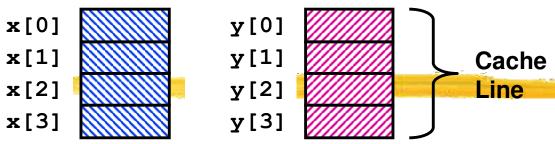
- Machine
  - □ DEC Station 5000
  - □ MIPS Processor with 64KB direct-mapped cache, 16 B line size
- Performance
  - ☐ Good case: 24 cycles / element
  - ☐ Bad case: 66 cycles / element

#### **Thrashing Example**



Access one element from each array per iteration

#### **Thrashing Example: Good Case**

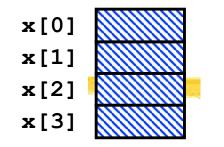


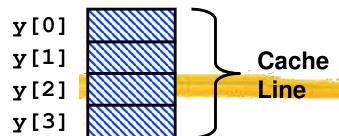
- Access Sequence
  - □ Read x[0]
    - x[0], x[1], x[2], x[3]loaded
  - Read y[0]
    - y[0], y[1], y[2], y[3] loaded
  - Read x[1]
    - Hit
  - Read y[1]
    - Hit

  - □ 2 misses / 8 reads

- Analysis
  - x[i] and y[i] map to different cache lines
  - ☐ Miss rate = 25%
    - Two memory accesses / iteration
    - On every 4th iteration have two misses

#### **Thrashing Example: Bad Case**





- Access Pattern
  - Read x[0]
    - x[0], x[1], x[2], x[3]
      loaded
  - Read y[0]
    - □ y[0], y[1], y[2], y[3] loaded
  - Read x[1]
    - x[0], x[1], x[2], x[3]
      loaded
  - Read y[1]
    - □ y[0], y[1], y[2], y[3] loaded
  - □ 8 misses / 8 reads

- Analysis
  - x[i] and y[i] map to same cache lines
  - ☐ Miss rate = 100%
    - Two memory accesses / iteration
    - On *every* iteration have two misses

- Average access time
- Average access time, ta, given by:
- assuming again that the first access must be to the cache before an access is made to the main memory. Only read requests are consider so far.
- Example
- If hit ratio is 0.85 (a typical value), main memory access time is 50 ns and cache access time is 5 ns, then average access time is 5+0.15\*50 = 12.5 ns.
- THROUGHOUT tc is the time to access the cache, get (or write) the data if a hit or recognize a miss. In practice, these times could be different.

#### **Example-1**

- Assume
  - ☐ Hit Time = 1 cycle
  - ☐ Miss rate = 5%
  - ☐ Miss penalty = 20 cycles
- Average memory access time=t<sub>c</sub>+m\*t<sub>m</sub>
   (m:miss rate, h:hit rate,
   t<sub>m</sub>: main memory access time, t<sub>c</sub>: Cache access time)
   Average memory access time = 1 + 0.05 x 20=2 cycle

or

$$= t_c*h+(t_m+t_c)*m$$
1x0.95 + 21x0.05=2 cycle

#### **Example-2**

- Assume
  - ☐ L1 Hit Time = 1 cycle
  - L1 Miss rate = 5%
  - ☐ L2 Hit Time = 5 cycles
  - □ L2 Miss rate = 15% (% L1 misses that miss)
  - ☐ L2 Miss Penalty = <u>100 cycles</u>
- $\square$  L1 miss penalty = 5 + 0.15 \* 100 = 20
- Average memory access time = 1 + 0.05 x 20= 2 cycle

#### **Replacement Algorithms**

- □ When a block is fetched, which block in the target set should be replaced?
- Optimal algorithm:
  - replace the block that will not be used for the longest time (must know the future)
- Usage based algorithms:
  - Least recently used (LRU)
    - replace the block that has been referenced least recently
    - hard to implement
- Non-usage based algorithms:
  - ☐ First-in First-out (FIFO)
    - treat the set as a circular queue, replace head of queue.
    - easy to implement
  - ☐ Random (RAND)
    - replace a random block in the set
    - even easier to implement

#### Implementing RAND and FIFO

#### □FIFO:

- maintain a modulo E counter for each set.
  - counter in each set points to next block for replacement.
  - □ increment counter with each replacement.

#### □RAND:

- maintain a single modulo E counter.
- counter points to next block for replacement in any set.
- increment counter according to some schedule:
  - each clock cycle, each mem reference, or each replacement.

#### **LRU**

- Need state machine for each set
- Encodes usage ordering of each element in set
- $\square$  E! possibilities ==>  $\sim$  E log E bits of state

#### What Happens on a Write?

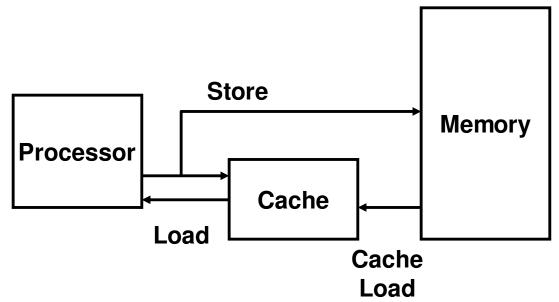
- Need to keep cache consistent with the main memory
  - □ Reads are easy require no modification
  - Writes- when does the update occur
- Write-Through
  - On cache write- always update main memory as well
- Write-Back
  - On cache write- remember that block is modified (dirty)
  - Update main memory when dirty block is replaced
  - □ Sometimes need to flush cache (I/O, multiprocessing)

#### What to do on a write hit?

- Write-through
  - update the word in cache block and corresponding word in memory
- □ Write-back
  - update word in cache block
  - allow memory word to be "stale"
  - => add 'dirty' bit to each line indicating that memory needs to be updated when block is replaced
  - => OS flushes cache before I/O !!!
- Performance trade-offs?

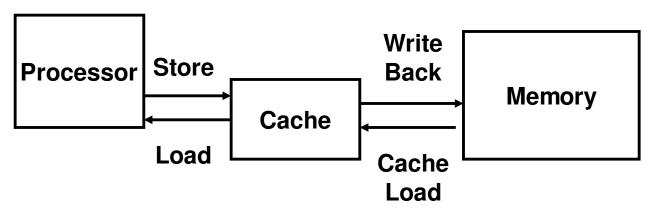
#### **Write Through**

- □Store by processor updates cache *and* memory
- Memory always consistent with cache
- □~2X more loads than stores
- □WT always combined with write buffers so that don't wait for lower level memory



#### **Write Back**

- Store by processor only updates cache line
- ■Modified line written to memory only when it is evicted
  - □ Requires "dirty bit" for each line
    - Set when line in cache is modified
    - Indicates that line in memory is stale
- Memory not always consistent with cache
- ■No writes of repeated writes



#### **Store Miss?**

- Write-Allocate
  - Bring written block into cache
  - Update word in block
  - Anticipate further use of block
- No-write Allocate
  - Main memory is updated
  - Cache contents unmodified

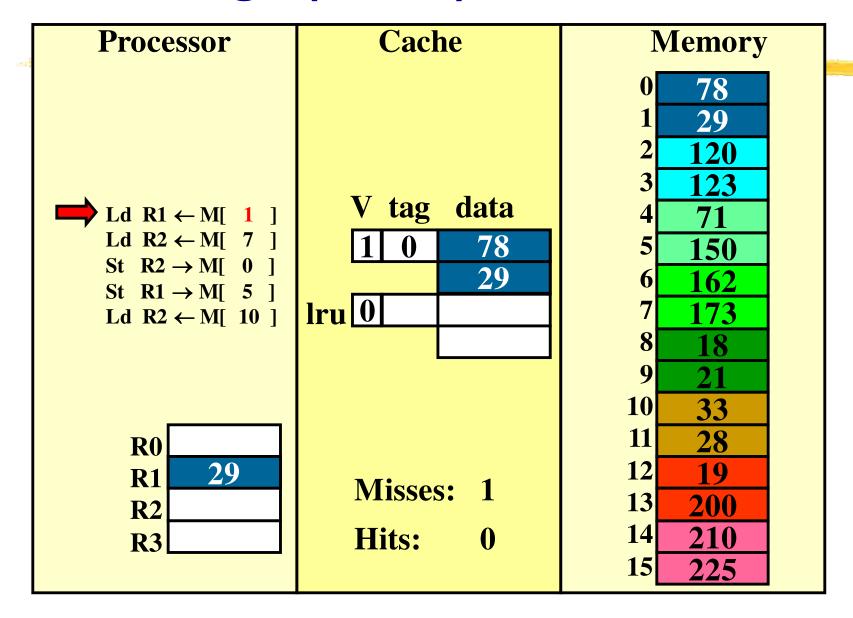
# **Handling stores (write-through)**

 Processor	Cache	Memory
Ld R1 ← M[ 1 ]  Ld R2 ← M[ 7 ]  St R2 → M[ 0 ]  St R1 → M[ 5 ]  Ld R2 ← M[ 10 ]	V tag data 0	0       78         1       29         2       120         3       123         4       71         5       150         6       162         7       173         8       18         9       21
R0 R1 R2 R3	Misses: 0 Hits: 0	10       33         11       28         12       19         13       200         14       210         15       225

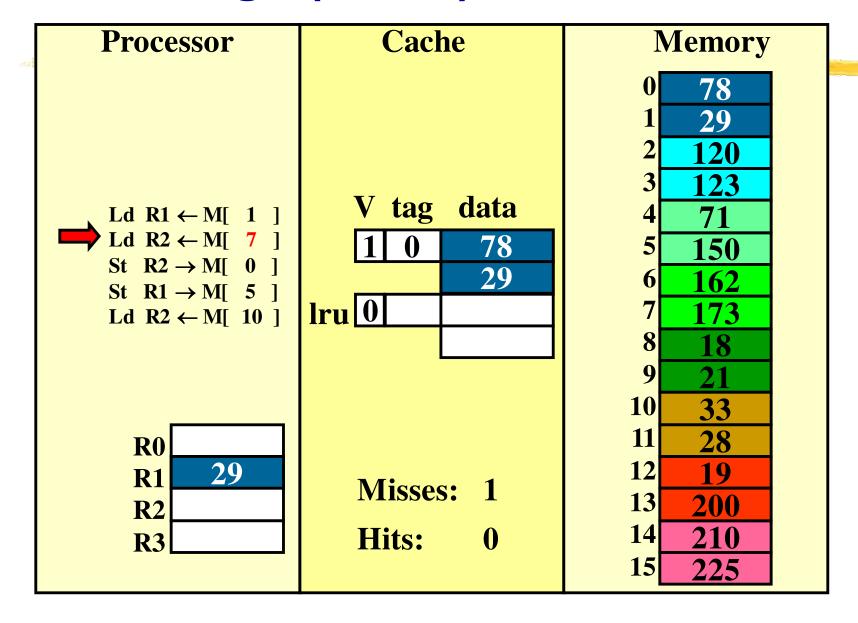
# write-through (REF 1)

Processor	Cache	Memory	
Ld R1 ← M[ 1 ]  Ld R2 ← M[ 7 ]  St R2 → M[ 0 ]  St R1 → M[ 5 ]  Ld R2 ← M[ 10 ]		0       78         1       29         2       120         3       123         4       71         5       150         6       162         7       173         8       18         9       21         10       33	
R0 R1 R2 R3	Misses: 0 Hits: 0	11 28 12 19 13 200 14 210 15 225	

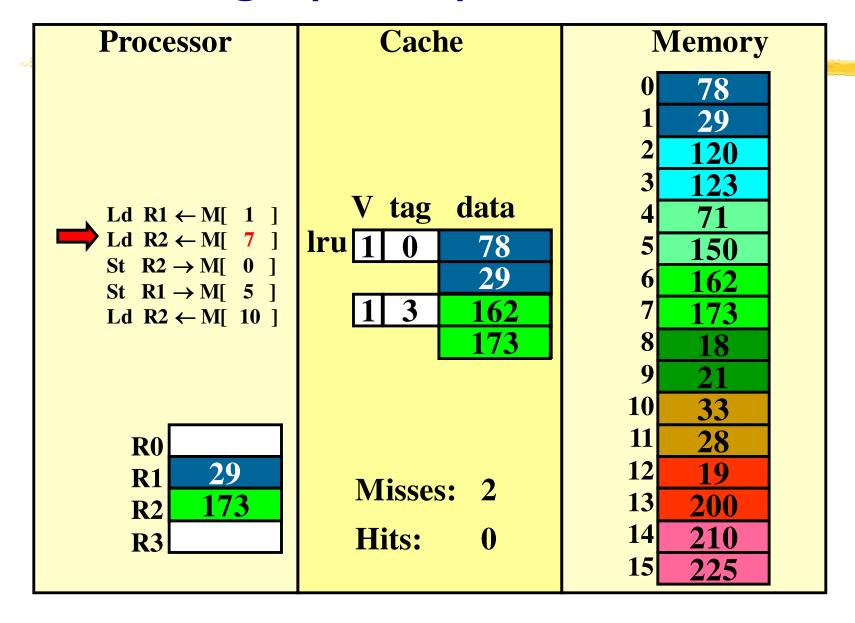
#### write-through (REF 1)



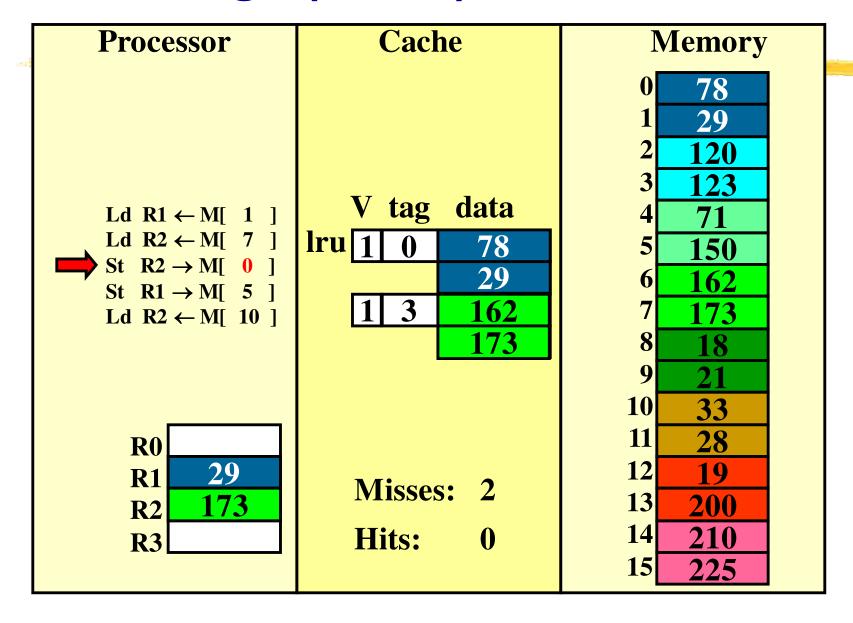
#### write-through (REF 2)



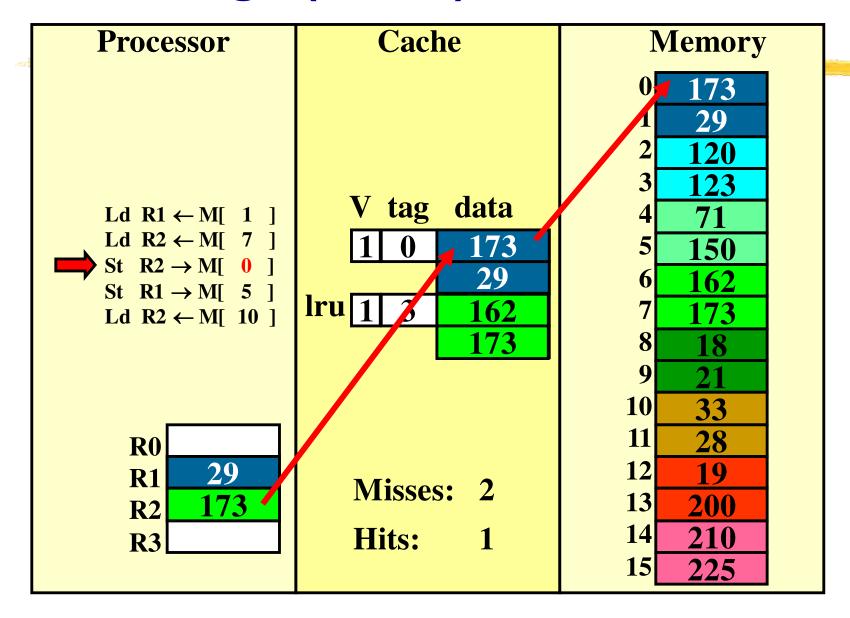
#### write-through (REF 2)



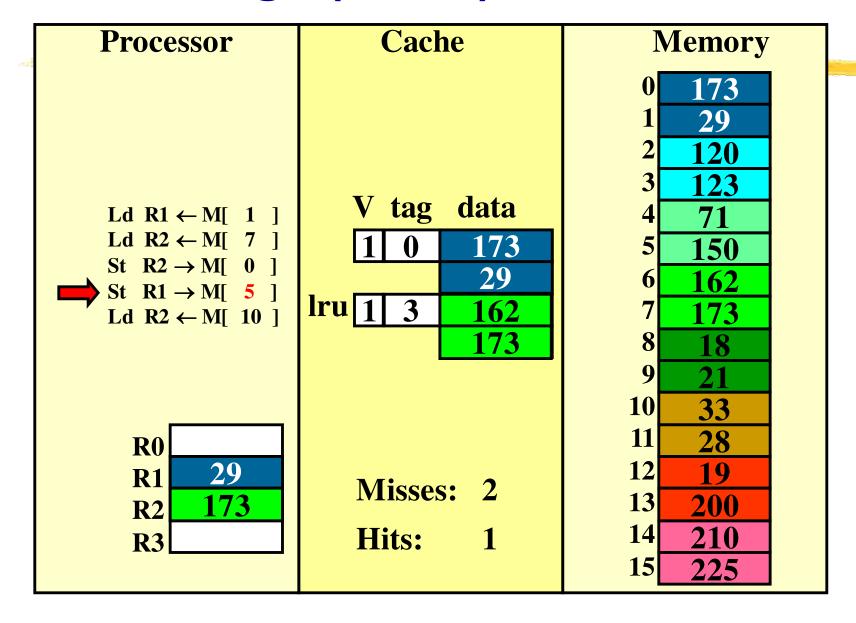
#### write-through (REF 3)



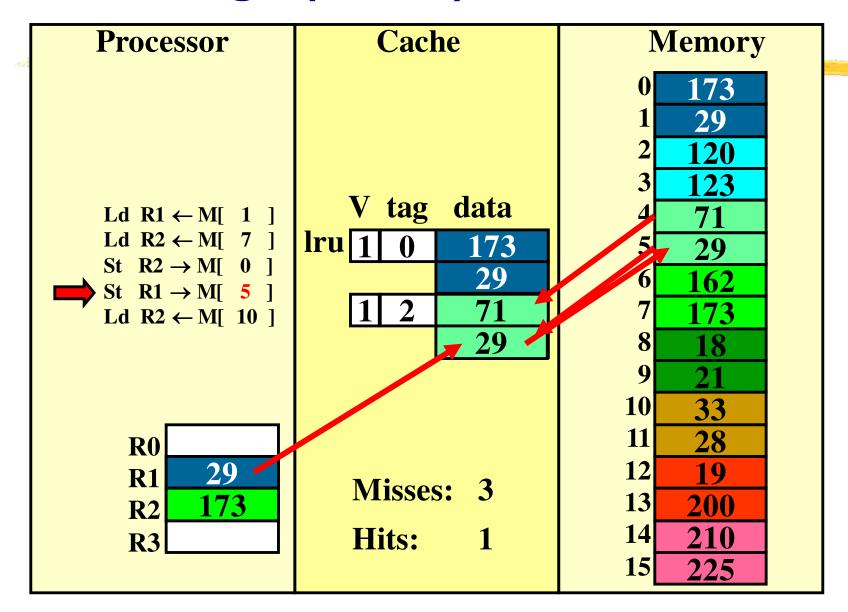
#### write-through (REF 3)



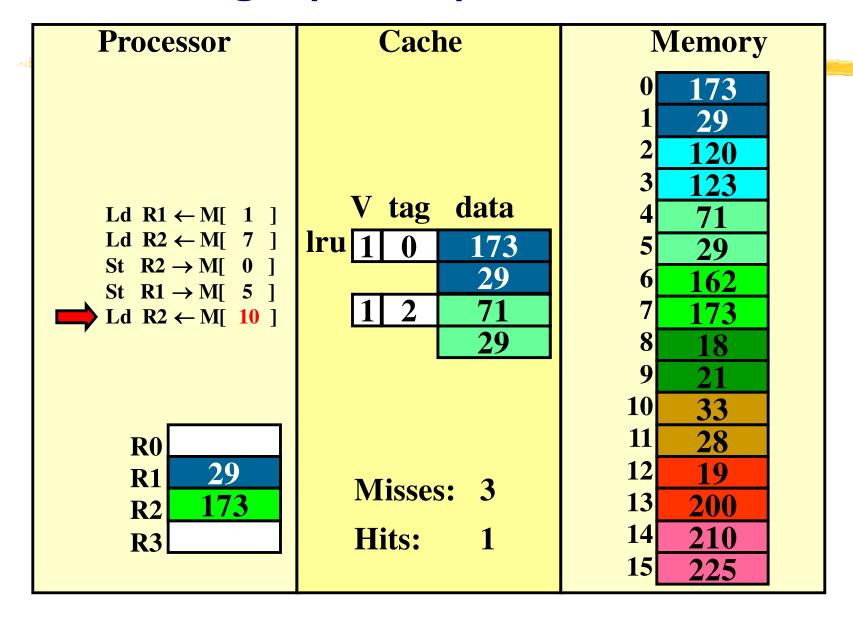
#### write-through (REF 4)



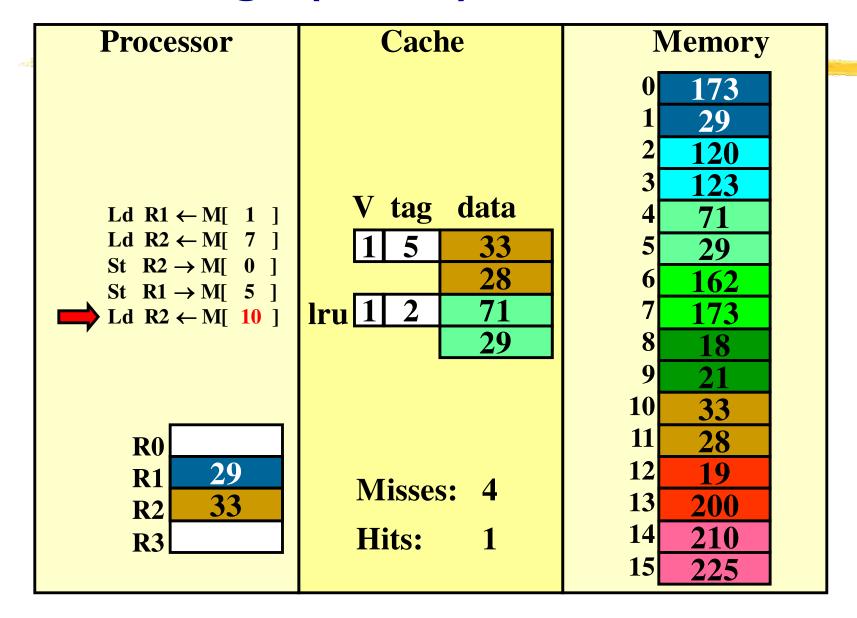
#### write-through (REF 4)



#### write-through (REF 5)



#### write-through (REF 5)



#### How many memory references?

- ☐ Each miss reads a block
  - ☐ 2 bytes in this cache
- ☐ Each store writes a byte
- ☐ Total reads: 8 bytes
- ☐ Total writes: 2 bytes

but caches generally miss < 20%

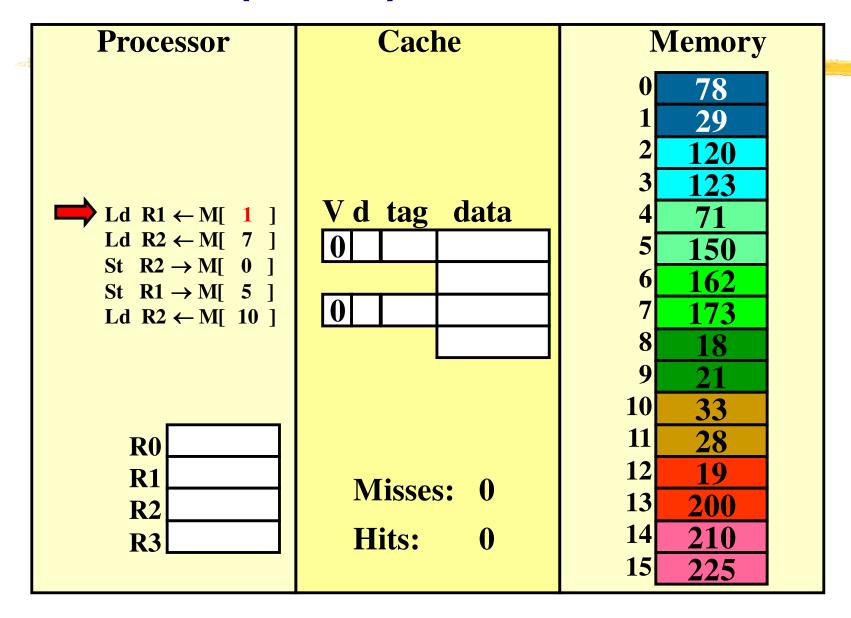
#### Write-through vs. write-back

- □ D the cache to NOT write all stores to memory immediately?
  - ☐ Keep the most current copy in the cache and update the memory when that data is evicted from the cache (a write-back policy).
    - □ write-back all evicted lines?
      - No, only blocks that have been stored into
        - Keep a "dirty bit", reset when the line is allocated, set when the block is stored into. If a block is "dirty" when evicted, write its data back into memory.

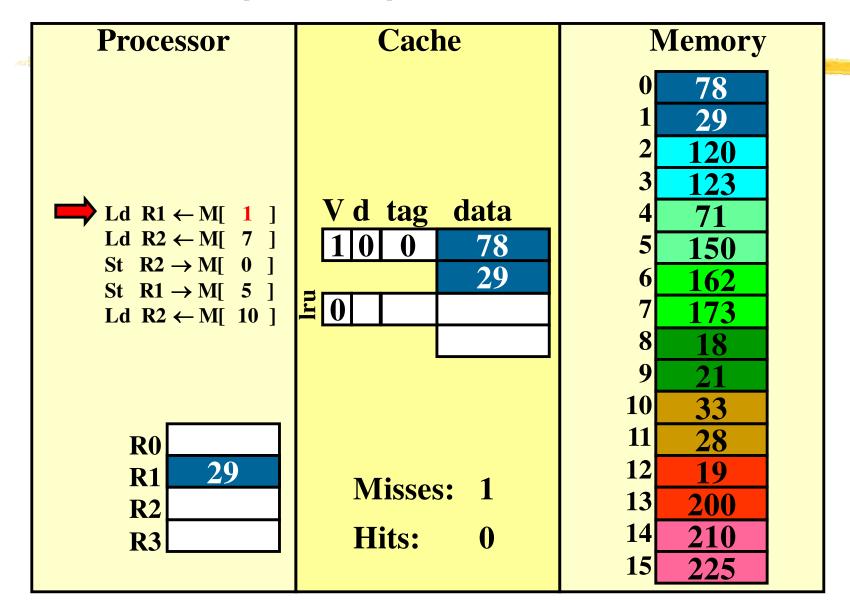
# **Handling stores (write-back)**

Processor	Cache	Memory
Ld R1 $\leftarrow$ M[ 1 ]  Ld R2 $\leftarrow$ M[ 7 ]  St R2 $\rightarrow$ M[ 0 ]  St R1 $\rightarrow$ M[ 5 ]  Ld R2 $\leftarrow$ M[ 10 ]   R0  R1  R2  R3	V d tag data  O O O O O O O O O O O O O O O O O O O	0       78         1       29         2       120         3       123         4       71         5       150         6       162         7       173         8       18         9       21         10       33         11       28         12       19         13       200         14       210         15       225

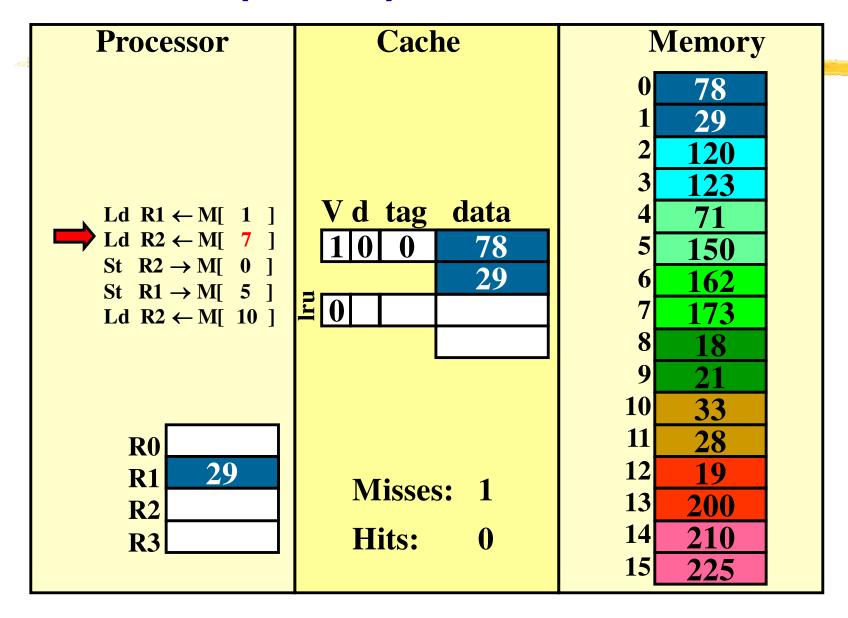
#### write-back (REF 1)



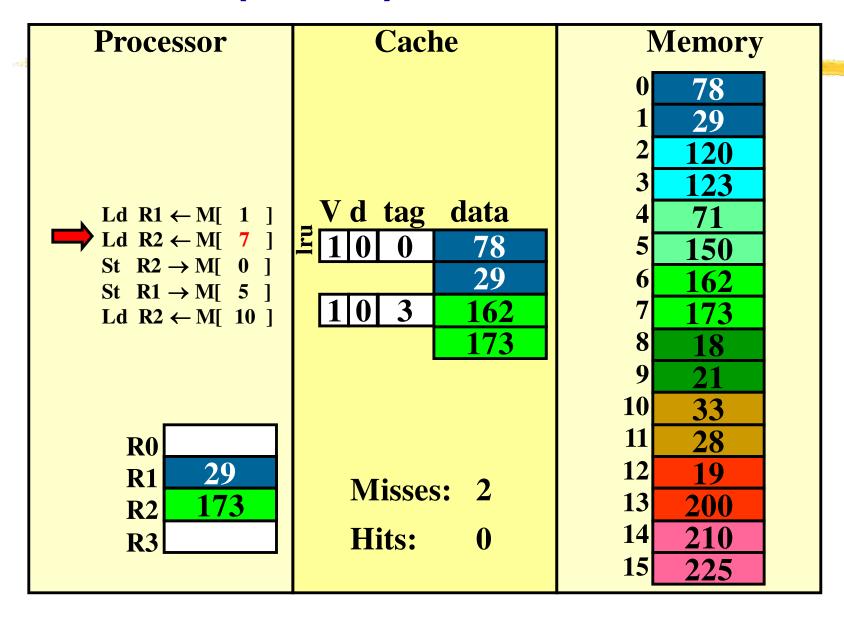
### write-back (REF 1)



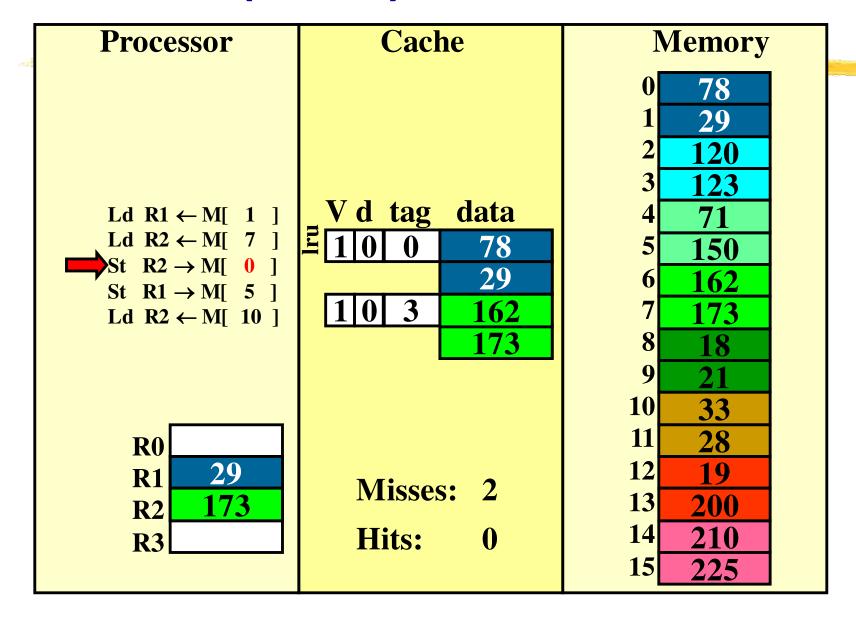
### write-back (REF 2)



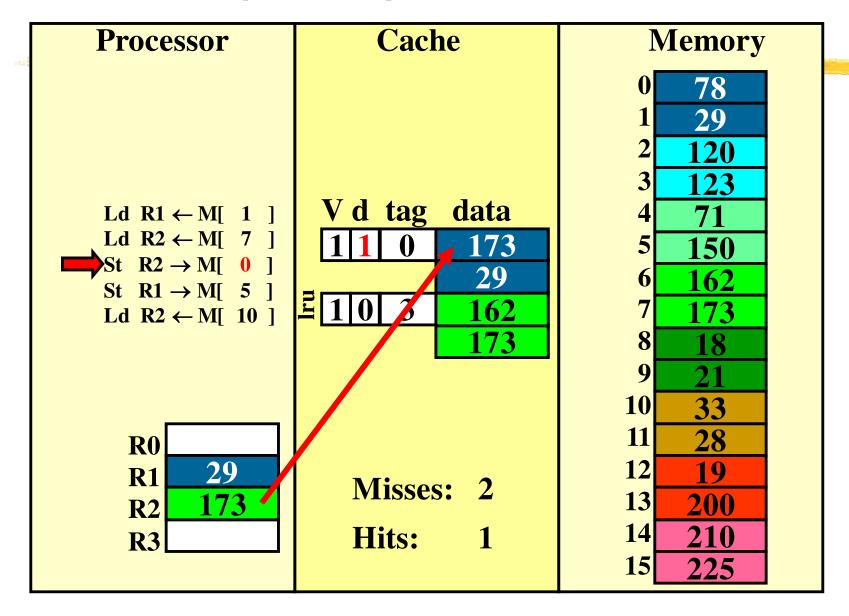
#### write-back (REF 2)



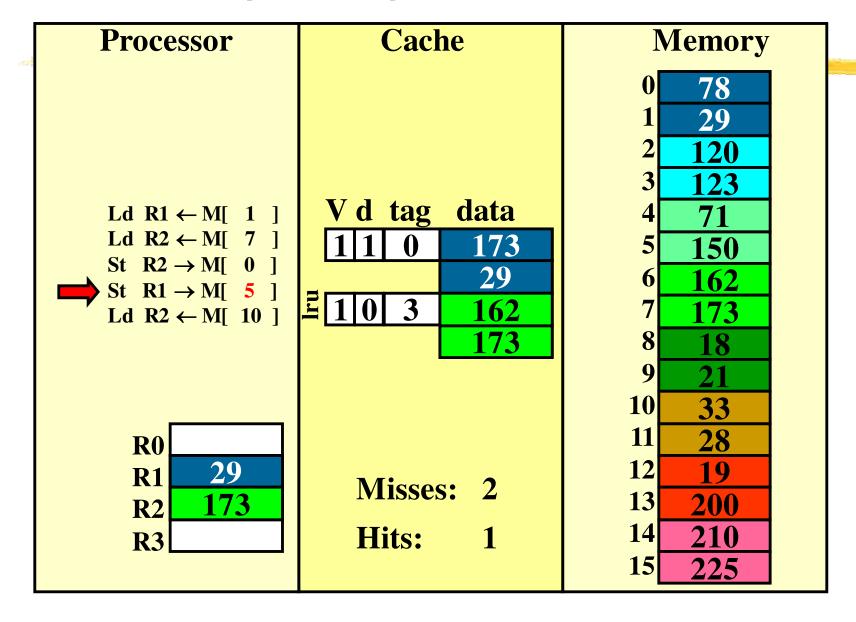
## write-back (REF 3)



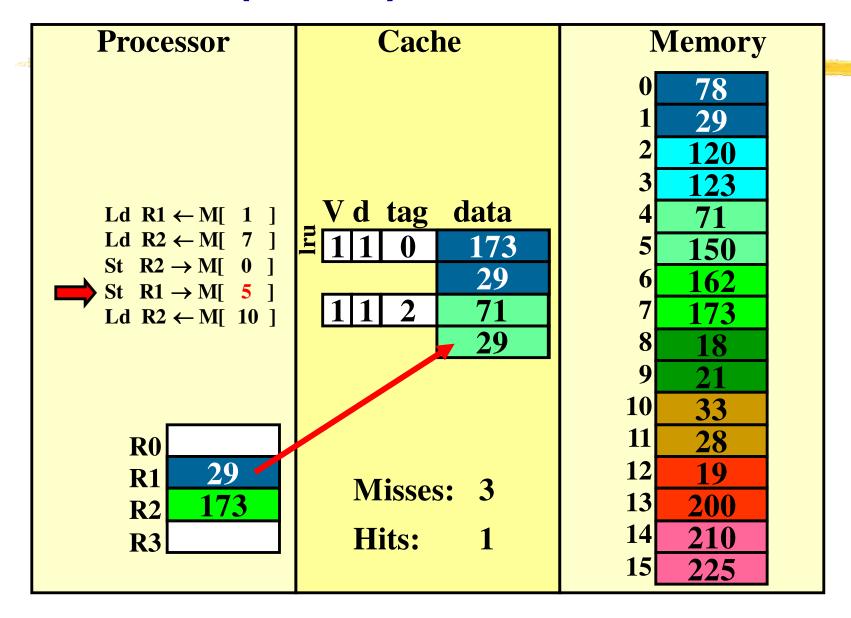
## write-back (REF 3)



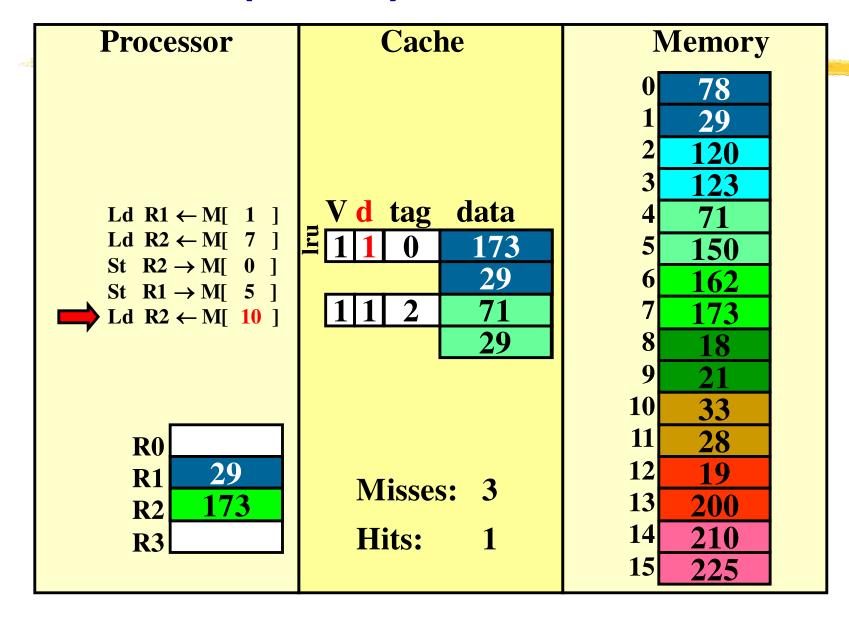
### write-back (REF 4)



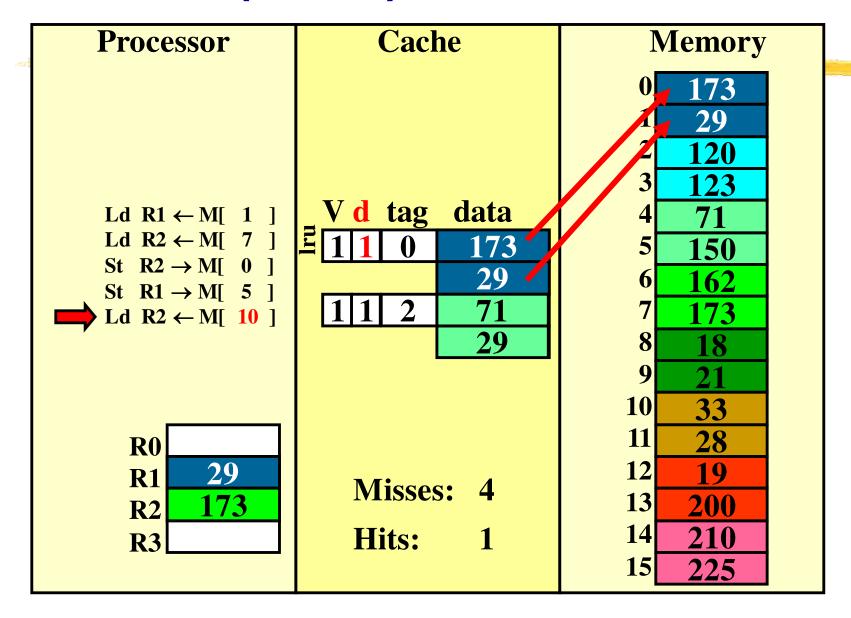
#### write-back (REF 4)



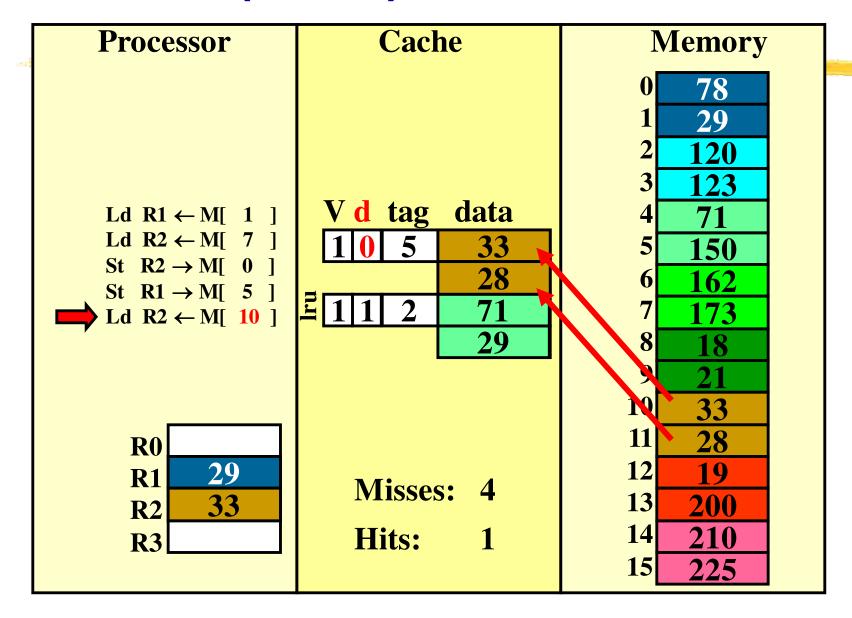
#### write-back (REF 5)



#### write-back (REF 5)



#### write-back (REF 5)



#### How many memory references?

- ☐ Each miss reads a block
  - ☐ 2 bytes in this cache
- □ Each evicted dirty cache line writes a block
- ☐ Total reads: 8 bytes
- ☐ Total writes: 4 bytes (after final eviction)

Choose write-back or write-through?