

YILDIZ TEKNİK ÜNİVERSİTESİ

BİLGİSAYAR MÜHENDİSLİĞİ BÖLÜMÜ

SAYISAL ANALİZ

DÖNEM PROJE RAPORU

Yusuf Mert ÇELİKARSLAN

19011042

l1119042@std.yildiz.edu.tr

Eğitmen : Prof. Dr. Banu DİRİ

İçindekiler:

3
6
7
9
12
16
19
23
25
27
29
33

Bisection Metodu

```
#include<stdio.h>
#include<math.h>
float bisection(float ,float ,float );
float equat(float ,int [],int );
int main(){
      float x1,x2,kok,mistake;
      printf("Enter the x1 that is value of y1:");
      scanf("%f",&x1);
      printf("Enter the x2 that is value of y2:");
      scanf("%f",&x2);
      printf("Enter the mistake:");
      scanf("%f",&mistake);
      kok=bisection(x1,x2,mistake);
      printf("X~~%f",kok);
      return 0;
}
float bisection(float a,float b,float k){
      float Hata=k+1,fa,fb,fc,c;
      int derece,kat[100],i,iteration=0;
      printf("Denklemin derecesini giriniz:");
      scanf("%d",&derece);
```

```
for(i=derece;i>=0;i--){
      printf("Enter x^%d. parameter of term:",i);
      scanf("%d",&kat[i]);
}
fa=equat(a,kat,derece);
fb=equat(b,kat,derece);
if((fa*fb)>0){
      printf("You entered wrong index!");
      return -1;
}
else if(fa==0){
      return a;
}
else if(fb==0){
      return b;
}
while((fa*fb)<0 \&\& Hata>k){
      iteration++;
      Hata=fabs(a-b)/pow(2,iteration);
      //Hata=fabs(b-a);
      printf("Mistake:%f\n",Hata);
      c=(a+b)/2;
      fc=equat(c,kat,derece);
      if(fa*fc<0){
            b=c;
            fb=fc;
      }
```

```
else if(fa*fc>0){
                  a=c;
                  fa=fc;
            }
            else{
                  printf("Iteration:%d\n",iteration);
                  return c;
            }
      }
      printf("Iteration:%d\n",iteration);
      if(Hata<=k){
            return c;
      }
}
float equat(float x,int kat[],int derece){
      float denklem=0;
      int i;
      for(i=derece;i>=0;i--){
            denklem=denklem+kat[i]*pow(x,i);
      return denklem;
}
```

Bisection Ekran Çıktısı

$x^3-7x^2+14x-6=0$

```
Enter the x1 that is value of y1:0
Enter the x2 that is value of y2:1
Enter the mistake:0.01
Denklemin derecesini giriniz:3
Enter x^3. parameter of term:1
Enter x^2. parameter of term:-7
Enter x^1. parameter of term:14
Enter x^0. parameter of term:-6
Mistake:0.500000
Mistake:0.125000
Mistake:0.031250
Mistake:0.007813
Iteration:4
X~~0.562500
Process exited after 45.92 seconds with return value 0
Press any key to continue . . .
🖽 🔑 Aramak için buraya yazın 📑 👩 🚍 💼 🚺 💋 🗃 💆 🎹
```

$x^2+2x-15=0$

```
Enter the x1 that is value of y1:-5
Enter the x2 that is value of y2:3
Enter the mistake:0.001
Denklemin derecesini giriniz:2
Enter x^2. parameter of term:1
Enter x^1. parameter of term:2
Enter x^0. parameter of term:-15
X~~-5.000000

Process exited after 14.27 seconds with return value 0
Press any key to continue . . .
```

Regula-Falsi Metodu

```
#include<stdio.h>
#include<math.h>
float regula_falsi(float a,float b,float k);
float equat(float ,int [],int );
int main(){
      float x1,x2,kok,mistake;
      printf("Enter the x1 that is value of y1:");
      scanf("%f",&x1);
      printf("Enter the x2 that is value of y2:");
      scanf("%f",&x2);
      printf("Enter the mistake:");
      scanf("%f",&mistake);
      kok=regula_falsi(x1,x2,mistake);
      printf("X~~%f",kok);
      return 0;
}
float regula_falsi(float a,float b,float k){
      float Hata=k+1,fa,fb,fc,c;
      int derece,kat[100],i,iteration=0;
      printf("Denklemin derecesini giriniz:");
```

```
scanf("%d",&derece);
for(i=derece;i>=0;i--){
      printf("Enter x^%d. parameter of term:",i);
      scanf("%d",&kat[i]);
}
fa=equat(a,kat,derece);
fb=equat(b,kat,derece);
if((fa*fb)>=0){
      printf("You entered wrong index!---");
      return -1;
}
while((fa*fb)<0 \&\& Hata>k){
      iteration++;
      Hata=fabs(b-a)/pow(2,iteration);
      printf("Mistake:%f\n",Hata);
      c=(b*fa-a*fb)/(fa-fb);
      fc=equat(c,kat,derece);
      if(fa*fc<0){
            b=c;
            fb=fc;
      }
      else if(fa*fc>0){
            a=c;
            fa=fc;
      }
      else{
            printf("Iteration:%d\n",iteration);
```

```
return c;
}

if(Hata<=k){
    return c;
}

float equat(float x,int kat[],int derece){
    float denklem=0;
    int i;
    for(i=derece;i>=0;i--){
        denklem=denklem+kat[i]*pow(x,i);
    }
    return denklem;
}
```

Newton-Raphson Metodu

```
#include<stdio.h>
#include<math.h>
float newton_raphson(float a,float k);
float derivative(float x,int kat[],int derece);
float equat(float x,int kat[],int derece);
int main(){
    float x1,x2,kok,initiate,mistake;
    char join;
```

```
printf("Enter the x1 that is value of y1:");
      scanf("%f",&x1);
      printf("Enter the x2 that is value of y2:");
      scanf("%f",&x2);
      printf("Do you want to assign an initial value:(Y/N)");
      scanf(" %c",&join);
      printf("Enter the mistake:");
      scanf("%f",&mistake);
      if(join=='Y' || join=='y'){
            printf("Initial Value:");
            scanf("%f",&initiate);
            kok=newton_raphson(initiate,mistake);
      }
      else if(x1< x2)
            kok=newton_raphson(x1,mistake);
      else
            kok=newton_raphson(x2,mistake);
      printf("X~~%f",kok);
      return 0;
float newton_raphson(float a,float k){
      float Hata=k+1,fa,ga,c;
      int derece, kat [100], i;
      printf("Denklemin derecesini giriniz:");
      scanf("%d",&derece);
```

}

```
for(i=derece;i>=0;i--){
      printf("Enter x^%d. parameter of term:",i);
      scanf("%d",&kat[i]);
}
fa=equat(a,kat,derece);
ga=derivative(a,kat,derece);
if(ga==0){
      a+=k;
      ga=derivative(a,kat,derece);
}
printf("denklem=%f --- turev=%f\n",fa,ga);
while(Hata>k){
     c=a-(fa/ga);
      printf("C:%f\n",c);
      Hata=fabs(c-a);//x1-x0
      printf("Mistake:%f\n",Hata);
      a=c; //a=x1
      fa=equat(a,kat,derece);
      ga=derivative(a,kat,derece);
      if(ga==0){
            a+=k;
            ga=derivative(a,kat,derece);
      }
}
//printf("Iteration:%d\n",iteration);
if(Hata<=k){
      return c;
```

```
}
}
float equat(float x,int kat[],int derece){
      float denklem=0,deriv=0;
      int i;
      for(i=derece;i>=0;i--){
            denklem=denklem+kat[i]*pow(x,i);
      return denklem;
float derivative(float x,int kat[],int derece){
      float deriv=0;
      int i;
      for(i=derece;i>0;i--){
            deriv=deriv+(kat[i]*i*pow(x,i-1));
      }
      return deriv;
}
```

Matris Inversi

```
#include<stdio.h>
#define MAX 100
int main(){
    float matrix[MAX][MAX];
    int row,column,i,j;
```

```
printf("ROW LENGTH:");
      scanf("%d",&row);
      printf("COLUMN LENGTH:");
      scanf("%d",&column);
      scan(matrix,row,column);
      for(i=0;i<row;i++){
            for(j=column;j<column*2;j++){</pre>
                  if(i==(j-column)){
                        matrix[i][j]=1;
                  }
                  else{
                        matrix[i][j]=0;
                  }
            }
      }
      print(matrix,row,column*2);
      eliminasyon(matrix,row,column*2);
      printf("Invers A matrix:\n");
      for(i=0;i<row;i++){
            for(j=column;j<column*2;j++){</pre>
                  printf("%-0.3f ",matrix[i][j]);
            }
            printf("\n");
      }
}
void eliminasyon(float a[][MAX],int r,int c){
```

```
int i,j,p,k;
float hold,tmp;
i=0;
while(i<r){//1.satır
      p=i+1;
      while(a[i][i]==0 && p<r){
             for(k=0;k<c;k++){
                   tmp=a[p][k];
                   a[p][k]=a[i][k];
                   a[i][k]=tmp;
             }
             p++;
      }
      hold=a[i][i];
      for(k=i;k<c;k++){
             a[i][k]/=hold;
      }
      for(j=0;j< r;j++){
             hold=a[j][i];
             if(j!=i){
                   for(p=i;p<c;p++){
                          a[j][p]=a[j][p]-(hold*a[i][p]);
                   }
             }
             printf("\n");
      }
      print(a,r,c);
```

```
j++;
      }
}
void print(float a[][MAX],int r,int c){
      int i,j;
      for(i=0;i< r;i++){
             for(j=0;j<c;j++){
                    printf("%0.3f ",a[i][j]);
             }
             printf("\n");
      }
      printf("\n");
}
void scan(float a[][MAX],int r,int c){
      int i,j;
      for(i=0;i< r;i++){
             for(j=0;j<c;j++){
                    printf("[%d][%d]=",i,j);
                    scanf("%f",&a[i][j]);
             }
      }
}
```

Gauss Eleminasyon

```
#include<stdio.h>
#define MAX 100
int main(){
     float extcoefmatrix[MAX][MAX],variables[MAX]={0};
     int row,column,i;
      printf("Denklem sayisini giriniz:");
      scanf("%d",&row);
      printf("Degisken sayisini giriniz:");
      scanf("%d",&column);
      column++;
      scan(extcoefmatrix,row,column);
      print(extcoefmatrix,row,column);
      eliminasyon(extcoefmatrix,row,column);
      print(extcoefmatrix,row,column);
     variable(extcoefmatrix, variables, row, column);
     for(i=0;i<column-1;i++){</pre>
           printf("x%d= %0.3f\t",i+1,variables[i]);
      }
}
void eliminasyon(float a[][MAX],int r,int c){
     int i,j,p,k;
     float hold,tmp;
```

```
i=0;
while(i<r){//1.satır
      p=i+1;
      while(a[i][i]==0 && p<r){
             for(k=0;k<c;k++){
                   tmp=a[p][k];
                   a[p][k]=a[i][k];
                   a[i][k]=tmp;
            }
             p++;
      }
      hold=a[i][i];
      for(k=i;k<c;k++){
             a[i][k]/=hold;
      }
      for(j=i+1;j< r;j++){
             hold=a[j][i];
             for(p=i;p<c;p++){
                   a[j][p]=a[j][p]-(hold*a[i][p]);
            }
      }
      printf("\n\n");
      print(a,r,c);
      j++;
}
```

}

```
void variable(float a[][MAX],float arr[],int r,int c){
      int i,j;
      arr[c-2]=a[r-1][c-1];
      for(i=r-2;i>=0;i--){
             for(j=c-2;j>i;j--){
                    arr[i]=arr[i]+(arr[j]*a[i][j]);
             }
             arr[i]=a[i][c-1]-arr[i];
      }
}
void print(float a[][MAX],int r,int c){
      int i,j;
      for(i=0;i<r;i++){
             for(j=0;j<c;j++){
                    printf("%0.2f ",a[i][j]);
             }
             printf("\n");
      }
      printf("\n");
}
void scan(float a[][MAX],int r,int c){
      int i,j;
      for(i=0;i<r;i++){
             printf("%d. denklemi giriniz:\n",(i+1));
             for(j=0;j<c;j++){
```

Gauss Seidal

```
#include<stdio.h>
#include<math.h>
#define MAX 100
int mistake(float hata[],float E,int n);
void max_diagonal(float a[][MAX],int m,int n,float c[]);
void find_root(float hata[],float a[][MAX],float x[],float c[],int m,int n,float E);
int main(){
    float variables[MAX],katsayi[MAX][MAX],result[MAX],delta[MAX];
    float hata;
    int row,column,i,j;
    printf("Degisken sayisini giriniz:");
    scanf("%d",&column);
    printf("Denklem sayisini giriniz:");
```

```
scanf("%d",&row);
for(i=0;i<row;i++){</pre>
      printf("%d.denklemin katsayilarini giriniz:",i+1);
      for(j=0;j<column;j++){</pre>
            scanf("%f",&katsayi[i][j]);
      }
      printf("%d.denklemin sabit terimini giriniz:",i+1);
      scanf("%f",&result[i]);
}
printf("Degiskenlerin ilk degerlerini giriniz:");
for(i=0;i<column;i++){</pre>
      scanf("%f",&variables[i]);
}
printf("Hatayi giriniz:");
scanf("%f",&hata);
for(i=0;i<column;i++){</pre>
      delta[i]=hata+1000;
}
max_diagonal(katsayi,row,column,result);
for(i=0;i<column;i++){</pre>
      printf(" x\%d\t\t",i+1);
}
printf("\n");
do{
      find_root(delta,katsayi,variables,result,row,column,hata);
}while(mistake(delta,hata,column));
for(i=0;i<column;i++){</pre>
```

```
printf("x\%d = \%0.2f\t",i+1,variables[i]);
      }
}
int mistake(float hata[],float E,int n){
      int i=0;
      while(hata[i]<=E && i<n){
             j++;
      }
      if(i==n){
             return 0;
      }
      return 1;
}
void find_root(float hata[],float a[][MAX],float x[],float c[],int m,int n,float
E){
      int i,j;
      float sum, hold;
      for(i=0;i< m;i++){
             sum=0;
             if(hata[i]>E){
             for(j=0;j< n;j++){
                   if(i!=j){
                         sum+=(a[i][j]*x[j]);
                   }
             }
```

```
hold=x[i];
            x[i]=1.0*(c[i]-sum)/a[i][i];
            hata[i]=fabs(x[i]-hold);
            printf("%0.3f ",x[i]);
            printf("%0.3f\t",hata[i]);
            }
      }
      printf("\n");
}
void max_diagonal(float a[][MAX],int m,int n,float c[]){
      float prod=1,tmp;
      int max,i,j,k;
      for(i=0;i<n;i++){
            max=0;
            for(j=1;j<m;j++){
                   if(fabs(a[j][i])>fabs(a[max][i])){
                         max=j;
                   }
            }
            tmp=c[i];
            c[i]=c[max];
            c[max]=tmp;
            for(k=0;k<n;k++){
                  tmp=a[i][k];
                   a[i][k]=a[max][k];
                   a[max][k]=tmp;
```

```
}
}
```

Sayısal Türev

```
#include<stdio.h>
#include<math.h>
#define MAX 100

float turev(float x,float h,float kat[],int mode,int mode2,int mertebe);
float equation(float t,float kat[],int derece);
int main(){
    float kat[MAX]={0},value,h,deriv;
    int mode,mertebe,i,mode2;
    do{
        printf("Turev hesaplama metodunu seciniz:\n(1)Ilerifark\n(2)Gerifark\n(3)Merkezifark\nMode:");
        scanf("%d",&mode);
    }while(mode<1 || mode>3);
    printf("Deger ve hassasiyet miktarini giriniz:");
```

```
scanf("%f%f",&value,&h);
      deriv=turev(value,h,kat,mode,mode2,mertebe);
      printf("TUREV:%0.4f",deriv);
}
float turev(float x,float h,float kat[],int mode,int mode2,int mertebe){
     float f1,fxi,fx0,fx1,fx2,fx3;
      int derece,i;
     printf("Derece:");
     scanf("%d",&derece);
      for(i=derece;i>=0;i--){
            printf("x^%d. terimin katsayisini giriniz:",i);
            scanf("%f",&kat[i]);
      }
     switch(mode){
            case 1://ileri fark
                  fxi=equation(x+h,kat,derece);
                  fx0=equation(x,kat,derece);
                  f1=(fxi-fx0)/h*1.0;
                  break;
            case 2:// geri fark
                  fxi=equation(x-h,kat,derece);
                  fx0=equation(x,kat,derece);
                  f1=(fx0-fxi)/h*1.0;
                  break;
            case 3:// merkezi fark
                  fxi=equation(x+h,kat,derece);
```

```
fx0=equation(x-h,kat,derece);
                  f1=(fxi-fx0)/(h*2.0);
                  break;
            default:
                  printf("Mode is not correct.");
      }
      return f1;
}
float equation(float t,float kat[],int derece){
      int i;
      float denk=0;
      for(i=derece;i>=0;i--){
            denk+=(pow((double)t,(double)i)*kat[i]);
      }
      return denk;
}
```

Simpson Metodu

```
#include<stdio.h>
#include<math.h>
#define MAX 100
float integral(float kat[],float xn,float x0,int n,int ,int);
float equation(float t,float kat[],int derece,int );
int main(){
```

```
float kat[MAX],a,b;
      int N, derece, i;
      printf("Limit degerlerini kucukten buyuge giriniz:");
      scanf("%f%f",&a,&b);
      printf("N:");
      scanf("%d",&N);
      printf("Derece:");
      scanf("%d",&derece);
      for(i=0;i<=derece;i++){</pre>
            printf("x^%d. terimin katsayisini giriniz:",i);
            scanf("%f",&kat[i]);
      }
      printf("Integral|%0.f to %0.f =
%0.2f\n",a,b,integral(kat,b,a,N,1,derece));
      printf("Area|%0.f to %0.f = %0.2f",a,b,integral(kat,b,a,N,-1,derece));
}
float integral(float kat[],float xn,float x0,int n,int sign,int derece){
      float h,S=0;
      int i;
      h=fabs(1.0*(xn-x0)/n);
      S=equation(x0,kat,derece,sign)+equation(xn,kat,derece,sign);
      for(i=1;i<=n-1;i+=2){
            //printf("%f\n",S);
            S=S+4*equation(x0+i*h,kat,derece,sign);
      }
      for(i=2;i<=n-2;i+=2)
```

```
//printf("%f\n",S);
            S=S+2*equation(x0+i*h,kat,derece,sign);
      }
      S=(h/3)*S;
      return S;
}
float equation(float t,float kat[],int derece,int sign){
      int i;
      float denk=0;
      for(i=0;i<=derece;i++){</pre>
            denk+=(pow((double)t,(double)i)*kat[i]);
      }
      if(denk<0){
            denk=denk*sign;
      return denk;
}
```

Trapez Metodu

```
#include<stdio.h>
#include<math.h>
#define MAX 100

float integral(float kat[],float xn,float x0,int n,int ,int);
float equation(float t,float kat[],int derece,int );
int main(){
```

```
float kat[MAX],a,b;
      int N, derece, i;
      printf("Limit degerlerini giriniz:");
      scanf("%f%f",&a,&b);
      printf("N:");
      scanf("%d",&N);
      printf("Derece:");
      scanf("%d",&derece);
      for(i=0;i<=derece;i++){</pre>
            printf("x^%d. terimin katsayisini giriniz:",i);
            scanf("%f",&kat[i]);
      }
    printf("Integral|%0.f to %0.f = %0.2f\n",a,b,integral(kat,b,a,N,1,derece));
    printf("Area|\%0.f to \%0.f = \%0.2f",a,b,integral(kat,b,a,N,-1,derece));
}
float integral(float kat[],float xn,float x0,int n,int sign,int derece){
      float h,S=0;
      int i;
      h=fabs(1.0*(xn-x0)/n);
      S=(equation(x0,kat,derece,sign)+equation(xn,kat,derece,sign))/2;
      for(i=1;i<n;i++){
            //printf("%f\n",S);
            S=S+equation(x0+i*h,kat,derece,sign);
      }
```

```
S=h*S;
return S;
}

float equation(float t,float kat[],int derece,int sign){
   int i;
   float denk=0;
   for(i=0;i<=derece;i++){
        denk+=(pow((double)t,(double)i)*kat[i]);
   }
   if(denk<0){
        denk=denk*sign;
   }
   return denk;
}</pre>
```

Gregory-Newton Entepolasyonu

```
#include<stdio.h>
#define MAX 100

void gregory_newton(float a[][2],int size,float x,int);
float pow(float a,int b);
int fakt(int f);
int ileri_fark(float a[][2],int size);
```

```
int esitmi(float dizi[],int a,int n);
float kok(float x,int kere,float a[][2]);
int main(){
      float deger[MAX][2];
      int i,j,cozum,exit;
      float value;
      printf("Gireceginiz ornek sayisini yaziniz:");
      scanf("%d",&cozum);
      for(i=0;i<cozum;i++){</pre>
                  printf("%d. index degerini giriniz:",i+1);
                  scanf("%f",&deger[i][0]);
                  printf("%d. fonksiyon degerini giriniz:",i+1);
                  scanf("%f",&deger[i][1]);
      }
      i=0;
      do{
            printf("f(x) fonksiyonu icin x degerini giriniz:");
            scanf("%f",&value);
            gregory_newton(deger,cozum,value,i);
            printf("(1)Tekrar deger girmek icin 1'e basiniz\n(2)Cikmak icin
0'a basiniz\nEnter:");
            scanf("%d",&exit);
            j++;
      }while(exit);
      return 0;
}
```

```
void gregory_newton(float a[][2],int size,float x,int sayi){
      float h=a[1][0]-a[0][0];
      static int sinir;
      int i;
      float denk=a[0][1];
      if(sayi==0){
             sinir=ileri_fark(a,size);
      }
      for(i=1;i<=sinir;i++){</pre>
             denk+=((a[i][1]*kok(x,i,a))/(pow(h,i)*1.0*fakt(i)));
      }
      printf("f(\%.2f) = %f\n",x,denk);
}
float kok(float x,int kere,float a[][2]){
      int i;
      float kuad=1;
      for(i=0;i<kere;i++){</pre>
             kuad*=(x-a[i][0]);
      }
      return kuad;
}
float pow(float a,int b){
      int k;
      if(b==0)
             return 1;
```

```
}
      else{
             k=pow(a,b/2);
             if(b%2==1)
                    return a*k*k;
             else
                    return k*k;
      }
}
int fakt(int f){
      if(f==1 || f==0)
             return 1;
      else
             return f*fakt(f-1);
}
int ileri_fark(float a[][2],int size){
      int i,j=0;
      float gecici[size];
      do{
             for(i=j;i<size;i++){</pre>
                    gecici[i+1]=a[i+1][1]-a[i][1];
             }
             printf("%d. ileri fark:\n",j+1);
             for(i=j+1;i<size;i++){</pre>
                    a[i][1]=gecici[i];
                    printf("%.f\n",a[i][1]);
             }
```

```
j++;
    }while(esitmi(gecici,j,size));
    return j;
}
int esitmi(float dizi[],int a,int n){
    int i=a;
    while(i<n-1 && dizi[i]==dizi[i+1]){
        i++;
    }
    if(i==(n-1))
        return 0;
    else
        return 1;
}</pre>
```

Gregory-Newton Entepolasyonu Ekran Çıktısı

```
Gireceginiz ornek sayisini yaziniz:5
1. index degerini giriniz:2
      fonksiyon degerini giriniz:10
index degerini giriniz:10
fonksiyon degerini giriniz:50
index degerini giriniz:6
              fonksiyon degerini giriniz:122
index degerini giriniz:8
                fonksiyon degerini giriniz:226
  5. index degerini giriniz:10
5. fonksiyon degerini giriniz:362
f(x) fonksiyonu icin x degerini giriniz:4
               ileri fark:
2. ileri fark:
32
  f(4.00) = 50.000000
   (1)Tekrar deger girmek icin 1'e basiniz
   (2)Cikmak icin 0'a basiniz
   f(x) fonksiyonu icin x degerini giriniz:5
 f(5.00) = 82.000000
(1)Tekrar deger girmek icin 1'e basiniz
(2)Cikmak icin 0'a basiniz
   Enter:0
   Process exited after 73.61 seconds with return value 0
        ress any key to continue

    □ □ □ □ □ 0 □ □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ □ 4 □ 4 □ □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4 □ 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Prizde A = 10 40 10:23
```