Cache Memory

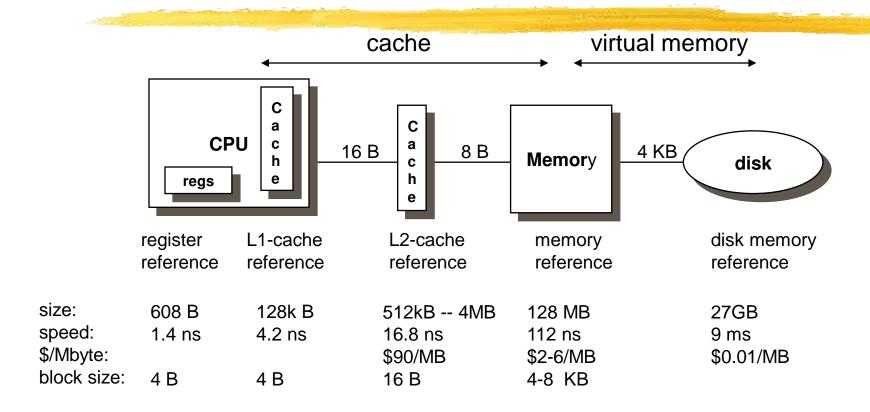
Outline

- Memory Hierarchy
- Direct-Mapped Cache
- □ Write-Through, Write-Back
- Cache replacement policy
- Examples

Principal of Locality

- Cache work on a principal known as locality of reference. This principal states asserts that programs continually use and re-use the same locations.
 - -Instructions: Loops, common subroutines
 - -Data: Look-up Tables, data sets(arrays)
- Temporal Locality (locality in time):Same location will be referenced again soon
- Spatial Locality (locality in space): Nearby locations will be referenced soon

The Tradeoff

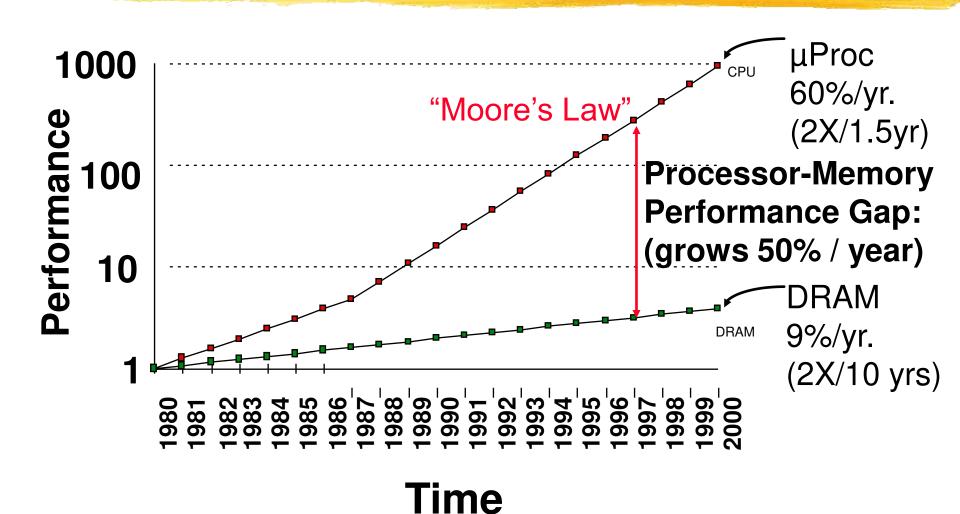


larger, slower, cheaper

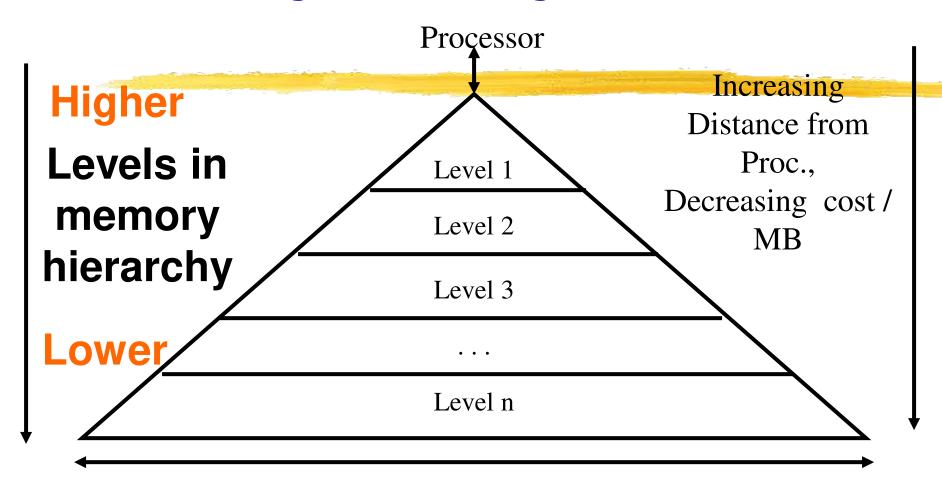
(Numbers are for a DEC Alpha 21264 at 700MHz)

MOORE's LAW

Processor-DRAM Memory Gap (latency)



Memory Hierarchy



Size of memory at each level

Cache Design

- How do we organize cache?
- Where does each memory address map to? (Remember that cache is subset of memory, so multiple memory addresses map to the same cache location.)
- How do we know which elements are in cache?
- How do we quickly locate them?

Cache mappings

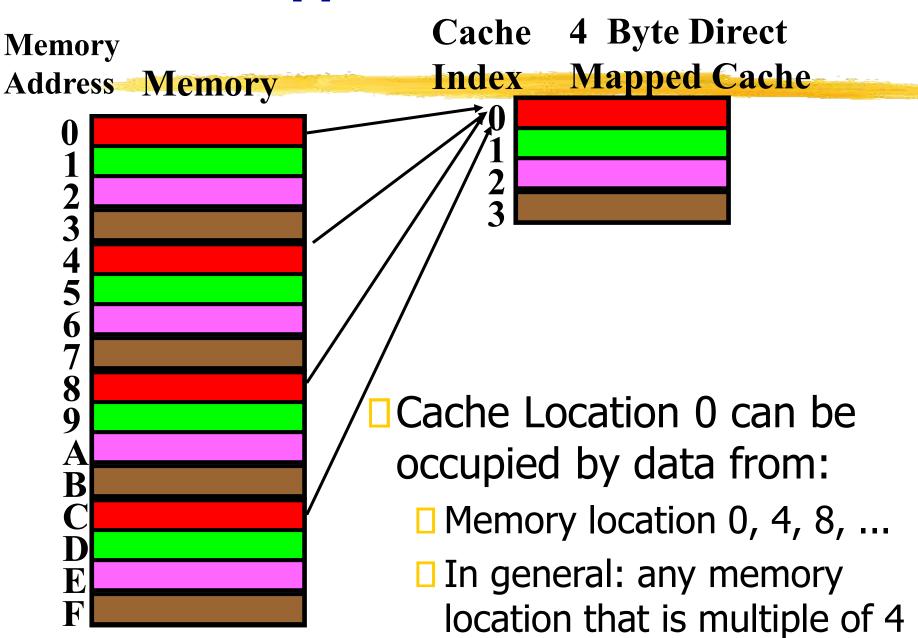
□ There are three types of methods for mapping between the main memory addresses and the cache addresses.

- Fully associative cache
- Direct mapped cache
- Set associative cache

Direct-Mapped Cache

- In a <u>direct-mapped cache</u>, each memory address is associated with one possible <u>block</u> within the cache
 - □ Therefore, we only need to look in a single location in the cache for the data if it exists in the cache
 - Block is the unit of transfer between cache and memory

Direct-Mapped Cache



Issues with Direct-Mapped

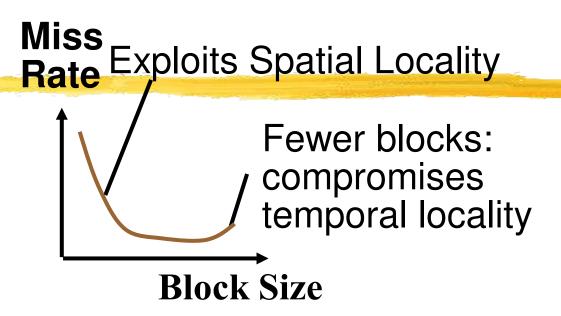
- Since multiple memory addresses map to same cache index, how do we tell which one is in there?
- What if we have a block size > 1 byte?
- Result: divide memory address into three fields

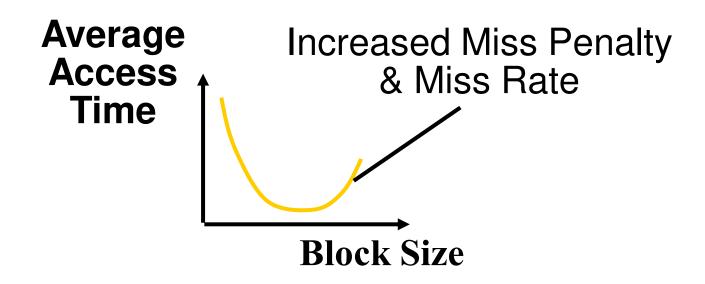
ttttttttttt	iiiiiiiii	0000
tag	index	byte
to check	to	offset
if have	select	within
correct block	block	block

Direct-Mapped Cache Terminology

- All fields are read as unsigned integers.
- Index: specifies the cache index (which "row" of the cache we should look in)
- Offset: once we've found correct block, specifies which byte within the block we want
- □ Tag: the remaining bits after offset and index are determined; these are used to distinguish between all the memory addresses that map to the same location

Block Size Tradeoff Conclusions





Direct-Mapped Cache Example

- Suppose we have a 16KB of data in a directmapped cache with 4 word blocks
- □ Determine the size of the tag, index and offset fields if we're using a 32-bit architecture
- Offset
 - need to specify correct byte within a block
 - □ block contains 4 words = 16 bytes = 2⁴ bytes
 - □ need <u>4 bits</u> to specify correct byte

Direct-Mapped Cache Example

- □ Index: (~index into an "array of blocks")
 - need to specify correct row in cache
 - \square cache contains 16 KB = 2^{14} bytes
 - □ block contains 2⁴ bytes (4 words)

 - = <u>bytes/cache</u> bytes/row
 - = 2¹⁴ bytes/cache 2⁴ bytes/row
 - = 2¹⁰ rows/cache need 10 bits to specify this many rows

Direct-Mapped Cache Example

- □ Tag: use remaining bits as tag
 - □ tag length = mem addr length offset index

- □ so tag is leftmost <u>18 bits</u> of memory address
- Why not full 32 bit address as tag?
 - □ All bytes within block need same address (-4b)
 - □ Index must be same for every address within a block, so its redundant in tag check, thus can leave off to save memory (- 10 bits in this example)

Accessing data in a direct mapped cache

Memory

- Ex.: 16KB of data, directmapped,4 word blocks
- □Read 4 addresses
 - □0x00000014, 0x0000001C, 0x00000034, 0x00008014
- ■Memory values on right:
 - only cache/memory level of hierarchy

Address (hex)	Value of Word
0000010	a
00000014	b
00000018	C
000001C	d
•••	•••
0000030	е
00000034	f
00000038	g
000003C	h
•••	•••
00008010	i
00008014	
00008018	k
0000801C	
•••	•••

Accessing data in a direct mapped cache

4 Addresses:

- □0x00000014, 0x0000001C, 0x00000034, 0x00008014
- 4 Addresses divided (for convenience) into Tag, Index, Byte Offset fields

```
      000000000000000000
      0000000000
      0100

      0000000000000000
      000000000
      1100

      0000000000000000
      000000001
      0100

      0000000000000000
      000000000
      0100

      Tag
      Index
      Offset
```

Accessing data in a direct mapped cache

- □So lets go through accessing some data in this cache
 - □16KB data, direct-mapped, 4 word blocks
- □Will see 4 types of events:
- Cache loading: Before any words and tags have been loaded into the cache, all locations contains invalid information. As lines are fetched from main memory into the cache, cache entries become valid. To represent this structure a valid bit added to each cache entry.
- <u>cache miss</u>: nothing in cache in appropriate block, so fetch from memory
- <u>cache hit</u>: cache block is valid and contains proper address, so read desired word
- <u>cache miss, block replacement</u>: wrong data is in cache at appropriate block, so discard it and fetch desired data from memory

Cache Loading

- Before any words and tags have been loaded into the cache, all locations contains invalid information. As lines are fetched from main memory into the cache, cache entries become valid. To represent this structure a valid bit added to each cache entry. This valid bit indicates that the associated cache line is valid(1) or invalid(0).
- ☐ If the valid bit is 0, then a cache miss occurs even if the tag matches the address from CPU, required addressed word to be taken from main memory.

16 KB Direct Mapped Cache, 16B blocks

□ Valid bit: determines whether anything is stored in that row (when computer initially turned on, all entries are invalid)

Example Block 0x8-b 0xc-f Valid 0x4-7 $0 \times 0 - 3$ Index Tag 1234567 1022

Read 0x00000014 = 0...00 0..001 0100

Tag field

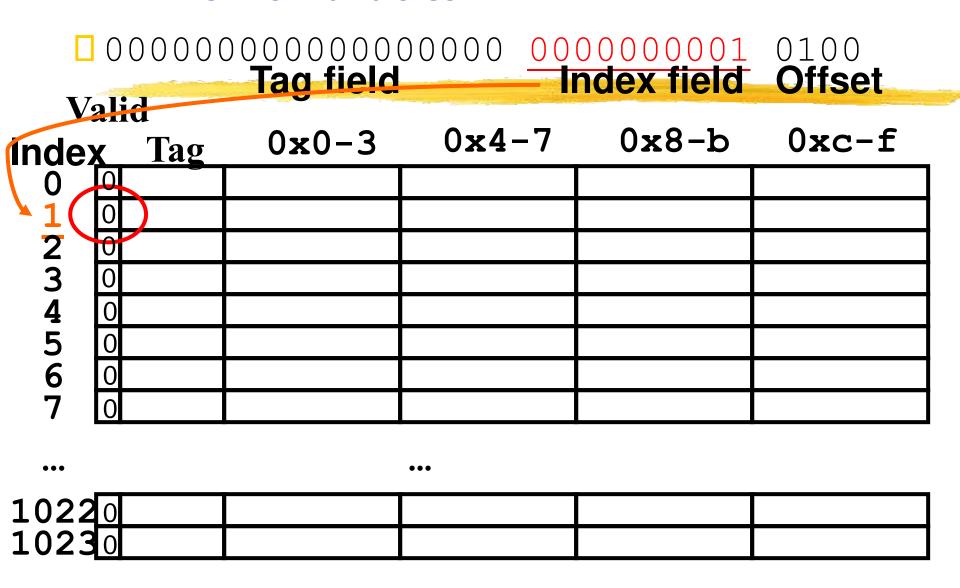
Index field Offset

Va Index	alid	Tag	0 x 0-3	0x4-7	0x8-b	0xc-f
0123456	0					
1	0					
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
•••				•••		
1022	0					
1023						

So we read block 1 (000000001)

Tag field Index field Offset Valid 0x4-70x8-b0x0-30xc-f Tag Index. **1**234567 **1022**0 **1023**0

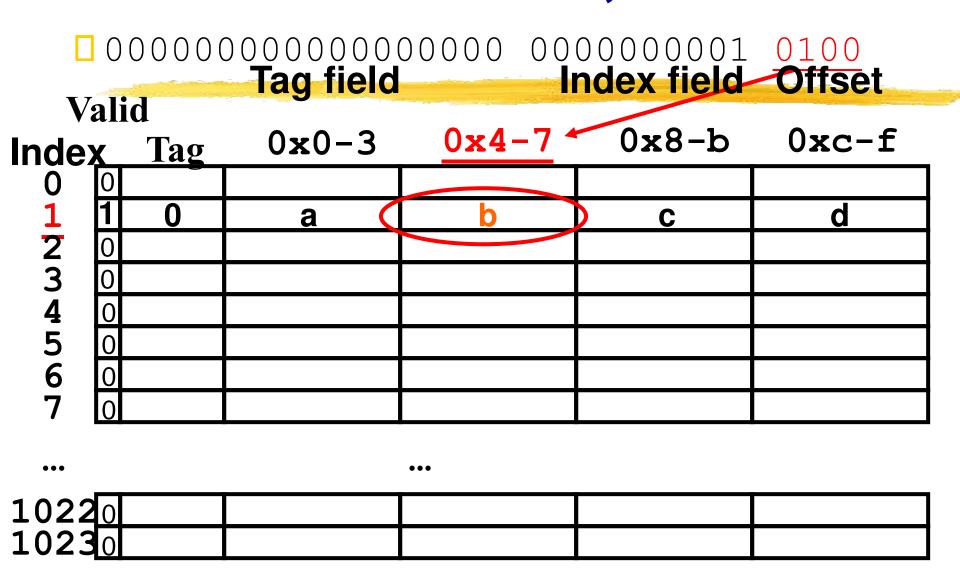
No valid data



So load that data into cache, setting tag, valid

Tag field Valid Index field Offset 0x4-70x0-3Index **Tag** 01234567 a 10220 **1023**0

Read from cache at offset, return word b



Read 0x000001C = 0...00 0..001 1100

 \square 00000000000000000 000000001 1100 Index field Offset Tag field Valid 0x4-70x8-b 0xc-f0x0-3Index Tag 1234567 b a **1022**0 10230

Data valid, tag OK, so read offset return word d

□ 0000000000000000 000000001 11,00 0x8-b0x4-70xc-f 0x0-3Index Tag **1**234567 b a **1022**0 10230

Read 0x00000034 = 0...00 0..011 0100

	000	0000	000000000 Tag field	0000 0000 Inc	0000011 lex field	0100 Offset
V	an	a	0x0-3	0x4-7		0xc-f
0	0 1	0	а	b	С	d
1 2 3 4 5 6	0					
4 5	0					
6 7	0					
•••				•••		
1022 1023						

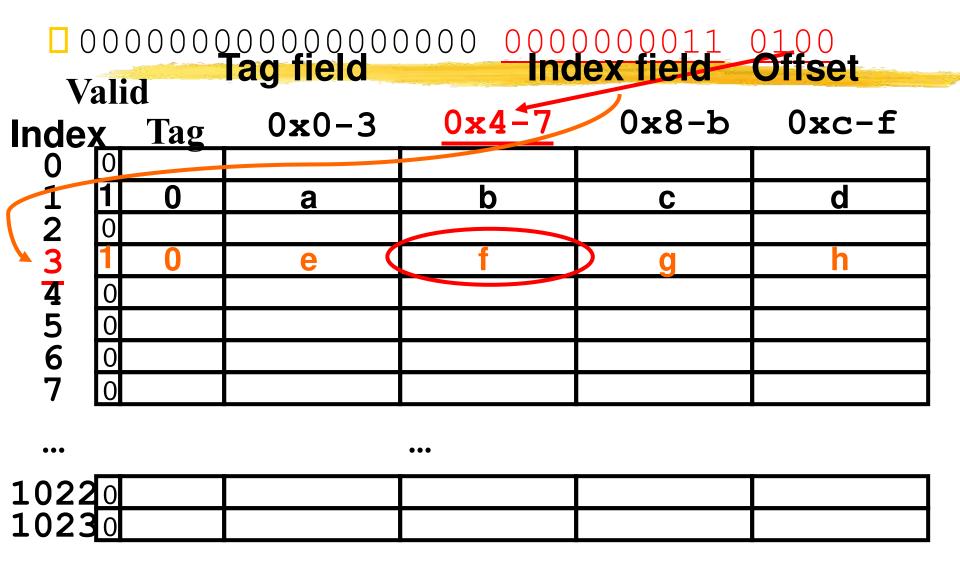
So read block 3

	00	0000	000000000 Tag field		0000011 lex field	0100 Offset
V	an	a	0x0-3	0x4-7	0x8-b	0xc-f
0	0	0	а	b	С	d
2 3 4 5 6 7	0					
4 5	0					
6 7	0					
•••				•••		
1022						
1023	0					

No valid data

00000 Tag	0000000 field	000 0000 Ind	000011 (ex field	0100 Offset
		0x4-7	0x8-b	0xc-f
0	а	b	С	d
•	••	•		
	_		ag 0x0-3 0x4-7	

Load that cache block, return word f



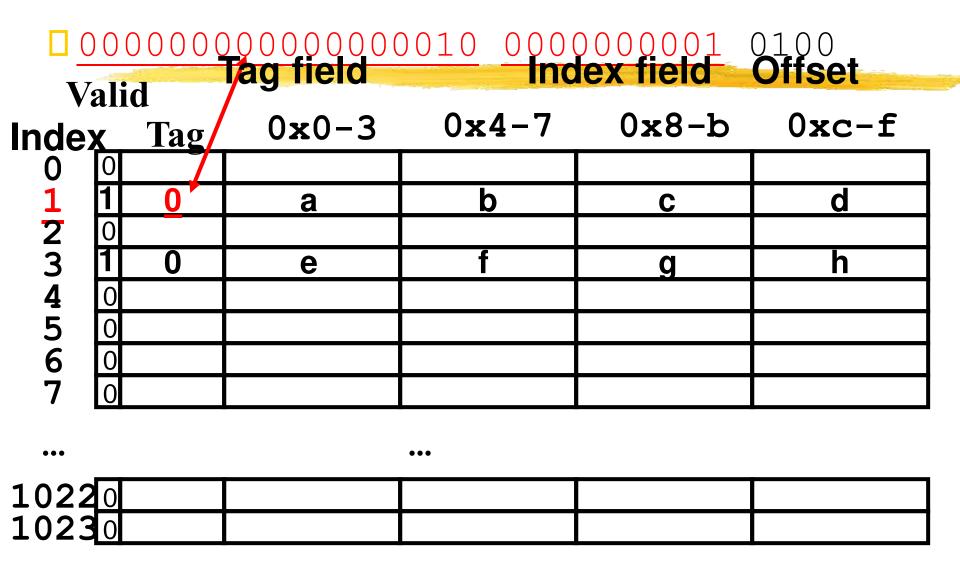
Read 0x00008014 = 0...10 0..001 0100

	0(0000	000000000 Tag field	0010 0000 Inc	0000001 lex field	0100 Offset
V	an	a	0x0-3		0x8-b	0xc-f
0	0	0	а	b	С	d
1 2 3 4 5 6 7	0	0	e	f	a	h
4	0			•	9	- ''
6	0					
•	0					
1022	0					
1023	0			_	_	

So read Cache Block 1, Data is Valid

0x4-70x8-b 0xc-f0x0-3Index Tag **1**234567 b a C a 10220 10230

Cache Block 1 Tag does not match (0 != 2)



Miss, so replace block 1 with new data & tag

	000	0000	000000000 Tag field	0010 0000	000001	0100
V	an	u				
Inde	X Ioi	<u>Tag</u>	0x0-3	UX4-/	0x8-b	0xc-f
1	1	2	i	i	k	
2				£		
1 2 3 4 5 6	0	0	е	T	g	h
5	0					
6 7	0					
•	U					
				•••		
1022 1023						

And return word j

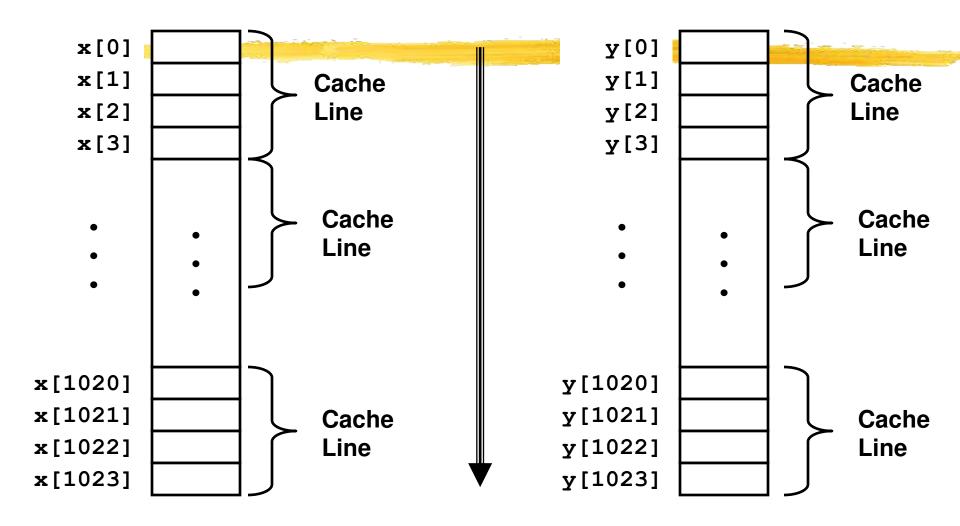
	0 (0000	000000000 Tag field	010 000	0000001 iex field	0100 Offset
Inde	211	d Tag	0x0-3	0x4-7	0x8-b	
	0 1	2	i		k	
0 1 2 3 4 5 6	0	0	е	f	g	h
4 5	0					
6 7	0					
•••				•••		
1022 1023						

Vector Product Example

```
float dot_prod(float x[1024], y[1024])
{
   float sum = 0.0;
   int i;
   for (i = 0; i < 1024; i++)
      sum += x[i]*y[i];
   return sum;
}</pre>
```

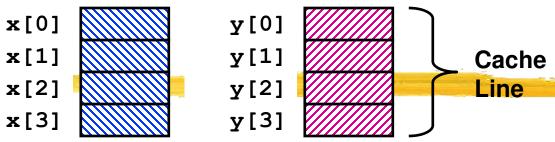
- Machine
 - □ DEC Station 5000
 - MIPS Processor with 64KB direct-mapped cache, 16 B line size
- Performance
 - ☐ Good case: 24 cycles / element
 - ☐ Bad case: 66 cycles / element

Thrashing Example



 Access one element from each array per iteration

Thrashing Example: Good Case

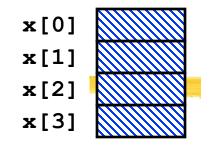


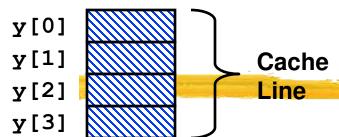
- ☐ Access Sequence
 - Read x[0]
 - x[0], x[1], x[2], x[3] loaded
 - Read y[0]
 - □ y[0], y[1], y[2], y[3] loaded
 - Read x[1]
 - Hit
 - Read y[1]
 - Hit

 - ☐ 2 misses / 8 reads

- Analysis
 - x[i] and y[i] map to different cache lines
 - ☐ Miss rate = 25%
 - Two memory accesses / iteration
 - On every 4th iteration have two misses

Thrashing Example: Bad Case





- Access Pattern
 - Read x[0]
 - □ x[0], x[1], x[2], x[3] loaded
 - Read y[0]
 - □ y[0], y[1], y[2], y[3] loaded
 - Read x[1]
 - □ x[0], x[1], x[2], x[3] loaded
 - Read y[1]
 - □ y[0], y[1], y[2], y[3] loaded
 - □ 8 misses / 8 reads

- Analysis
 - x[i] and y[i] map to same cache lines
 - ☐ Miss rate = 100%
 - Two memory accesses / iteration
 - On *every* iteration have two misses

- Average access time
- Average access time, ta, given by:
- \Box ta = tc + (1 h)tm
- assuming again that the first access must be to the cache before an access is made to the main memory. Only read requests are consider so far.
- Example
- If hit ratio is 0.85 (a typical value), main memory access time is 50 ns and cache access time is 5 ns, then average access time is 5+0.15*50 = 12.5 ns.
- THROUGHOUT tc is the time to access the cache, get (or write) the data if a hit or recognize a miss. In practice, these times could be different.

Example-1

- Assume
 - ☐ Hit Time = 1 cycle
 - ☐ Miss rate = 5%
 - ☐ Miss penalty = 20 cycles
- Average memory access time=t_c+m*t_m
 (m:miss rate, h:hit rate,
 t_m: main memory access time, t_c: Cache access time)
 Average memory access time = 1 + 0.05 x 20=2 cycle

or

$$= t_c*h+(t_m+t_c)*m$$
1x0.95 + 21x0.05=2 cycle

Example-2

- Assume
 - ☐ L1 Hit Time = 1 cycle
 - □ L1 Miss rate = 5%
 - ☐ L2 Hit Time = 5 cycles
 - ☐ L2 Miss rate = 15% (% L1 misses that miss)
 - ☐ L2 Miss Penalty = <u>100 cycles</u>
- \square L1 miss penalty = 5 + 0.15 * 100 = 20
- Average memory access time = 1 + 0.05 x 20= 2 cycle

Replacement Algorithms

- □ When a block is fetched, which block in the target set should be replaced?
- Optimal algorithm:
 - replace the block that will not be used for the longest time (must know the future)
- ☐ Usage based algorithms:
 - Least recently used (LRU)
 - replace the block that has been referenced least recently
 - hard to implement
- Non-usage based algorithms:
 - ☐ First-in First-out (FIFO)
 - treat the set as a circular queue, replace head of queue.
 - easy to implement
 - ☐ Random (RAND)
 - replace a random block in the set
 - even easier to implement

Implementing RAND and FIFO

FIFO:

- maintain a modulo E counter for each set.
 - counter in each set points to next block for replacement.
 - increment counter with each replacement.

RAND:

- maintain a single modulo E counter.
- counter points to next block for replacement in any set.
- increment counter according to some schedule:
 - each clock cycle, each mem reference, or each replacement.

LRU

- Need state machine for each set
- Encodes usage ordering of each element in set
- \square E! possibilities ==> \sim E log E bits of state

What Happens on a Write?

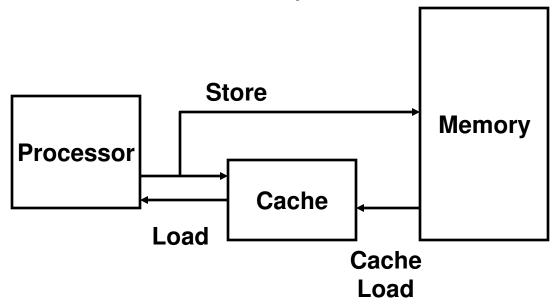
- Need to keep cache consistent with the main memory
 - □ Reads are easy require no modification
 - Writes- when does the update occur
- Write-Through
 - On cache write- always update main memory as well
- Write-Back
 - On cache write- remember that block is modified (dirty)
 - Update main memory when dirty block is replaced
 - Sometimes need to flush cache (I/O, multiprocessing)

What to do on a write hit?

- Write-through
 - update the word in cache block and corresponding word in memory
- □ Write-back
 - update word in cache block
 - allow memory word to be "stale"
 - => add 'dirty' bit to each line indicating that memory needs to be updated when block is replaced
 - => OS flushes cache before I/O !!!
- Performance trade-offs?

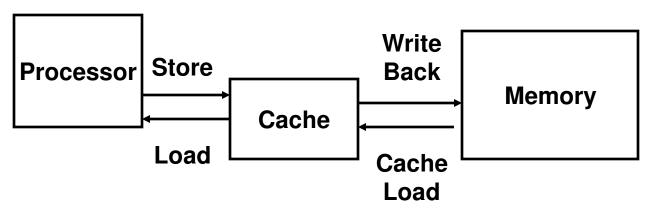
Write Through

- □Store by processor updates cache *and* memory
- Memory always consistent with cache
- □~2X more loads than stores
- WT always combined with write buffers so that don't wait for lower level memory



Write Back

- Store by processor only updates cache line
- Modified line written to memory only when it is evicted
 - □ Requires "dirty bit" for each line
 - Set when line in cache is modified
 - Indicates that line in memory is stale
- Memory not always consistent with cache
- □No writes of repeated writes



Store Miss?

- Write-Allocate
 - Bring written block into cache
 - Update word in block
 - Anticipate further use of block
- No-write Allocate
 - Main memory is updated
 - Cache contents unmodified

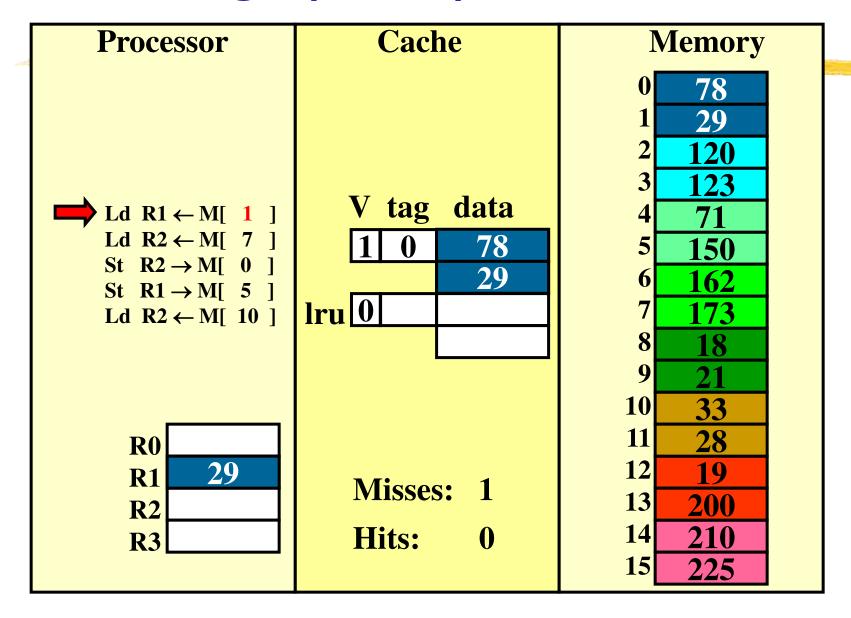
Handling stores (write-through)

Processor	Cache	Memory
Ld R1 ← M[1] Ld R2 ← M[7] St R2 → M[0] St R1 → M[5] Ld R2 ← M[10]	V tag data 0	0 78 1 29 2 120 3 123 4 71 5 150 6 162 7 173 8 18 9 21
R0	Misses: 0 Hits: 0	10 33 11 28 12 19 13 200 14 210 15 225

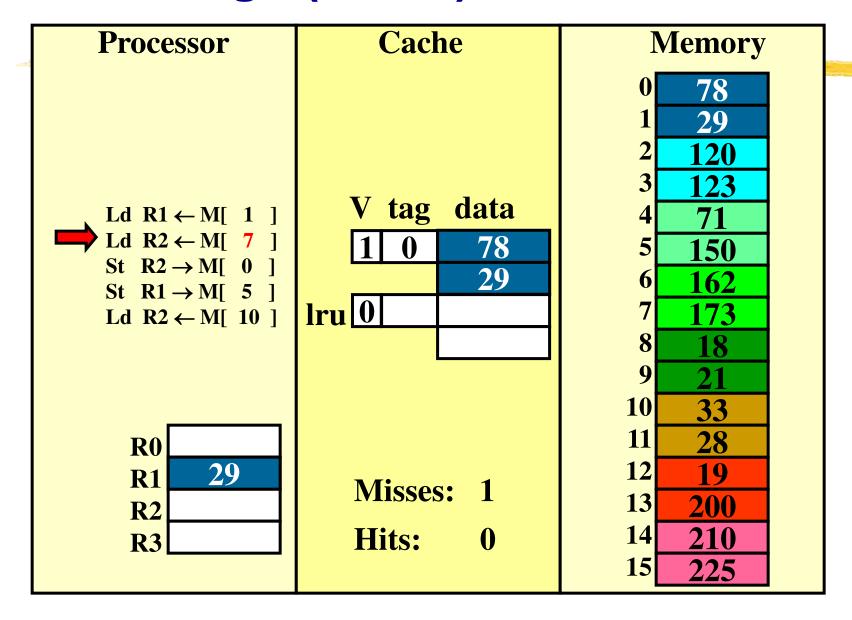
write-through (REF 1)

Processor	Cache	Memory
Ld R1 ← M[1] Ld R2 ← M[7] St R2 → M[0] St R1 → M[5] Ld R2 ← M[10] R0 R1 R2 R2	V tag data 0 0 0 Misses: 0	0 78 1 29 2 120 3 123 4 71 5 150 6 162 7 173 8 18 9 21 10 33 11 28 12 19 13 200
R3	Hits: 0	14 210 15 225

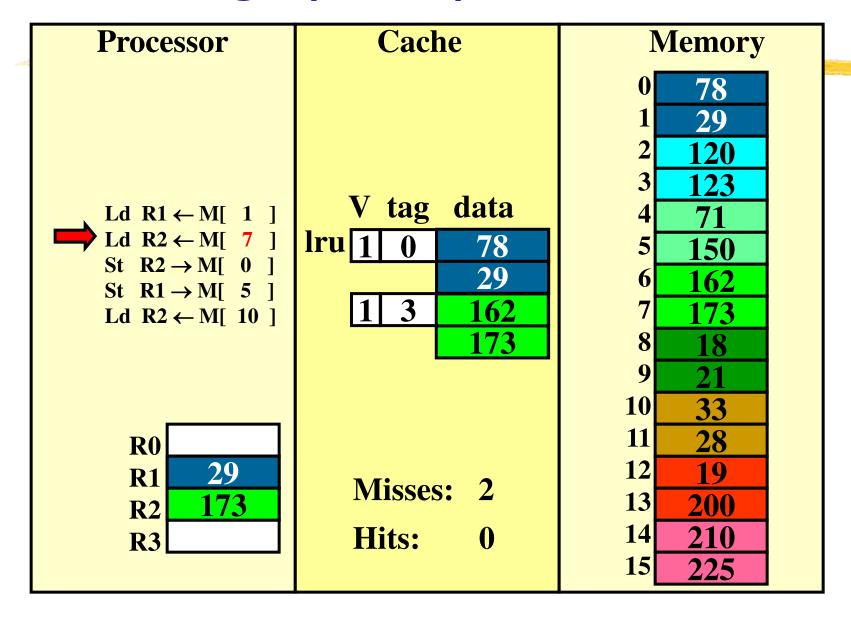
write-through (REF 1)



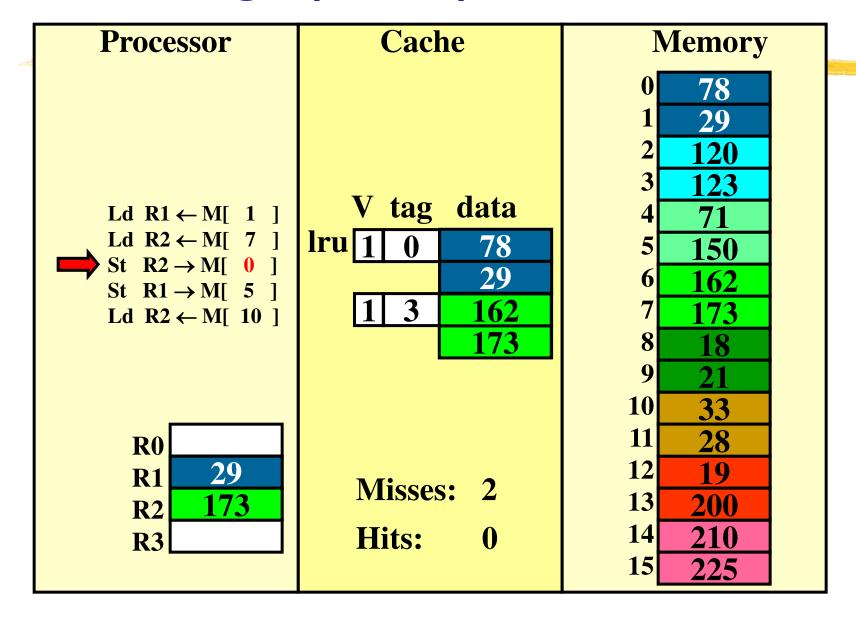
write-through (REF 2)



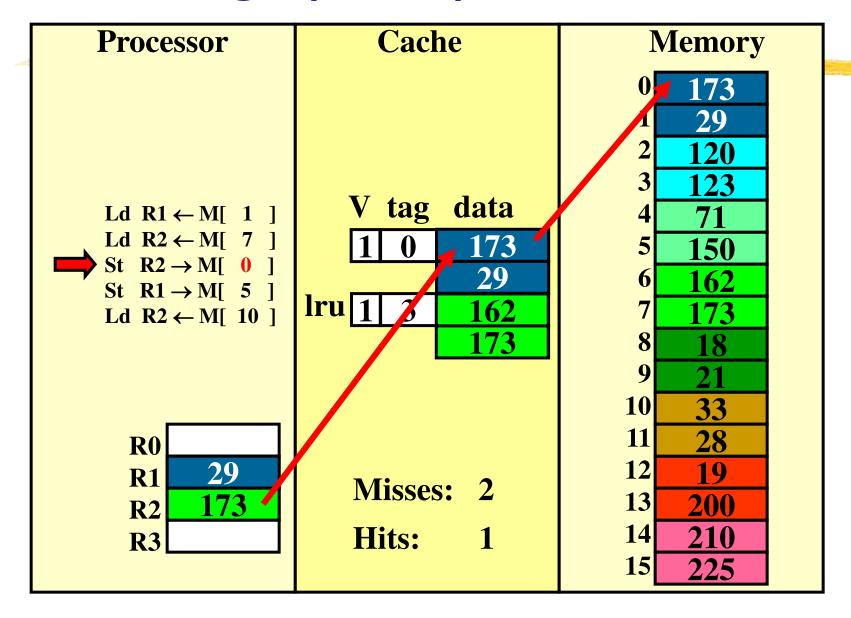
write-through (REF 2)



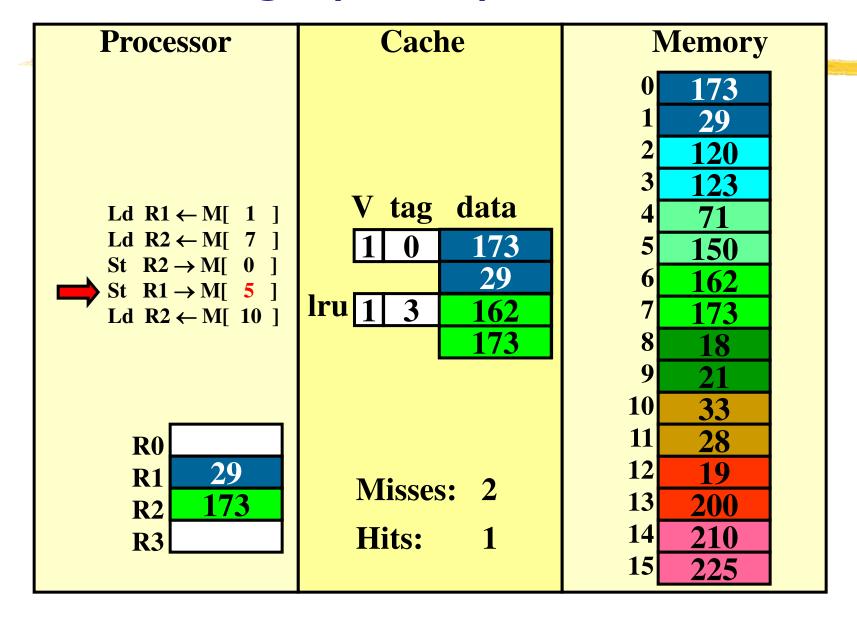
write-through (REF 3)



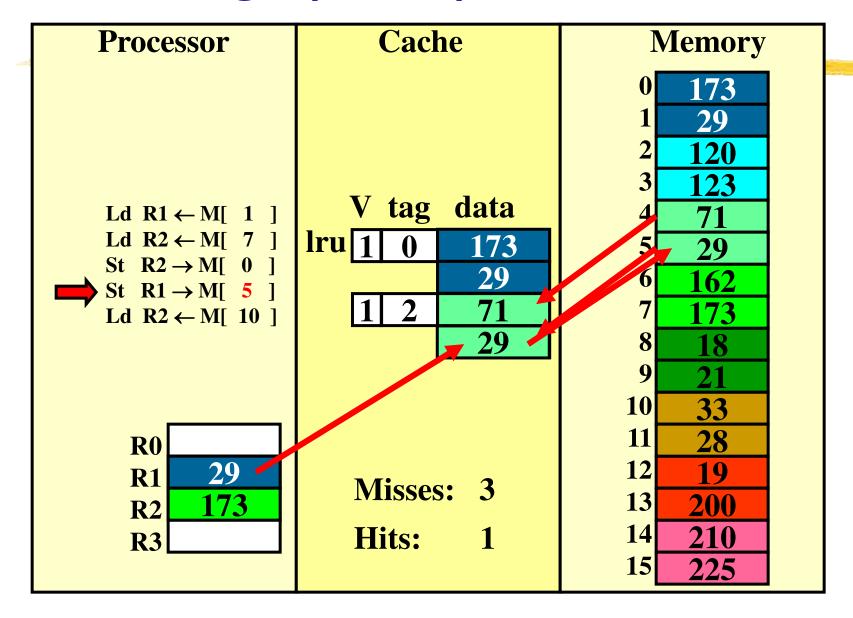
write-through (REF 3)



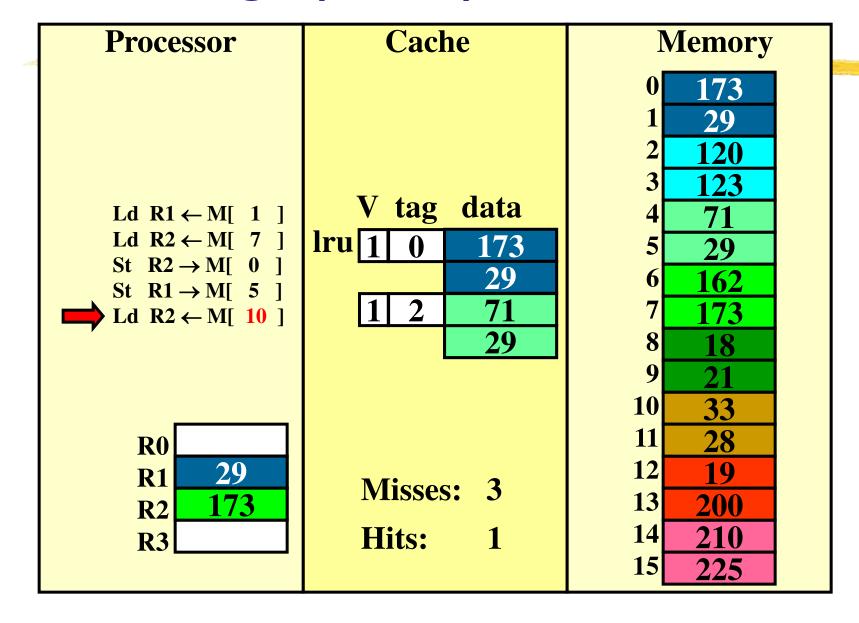
write-through (REF 4)



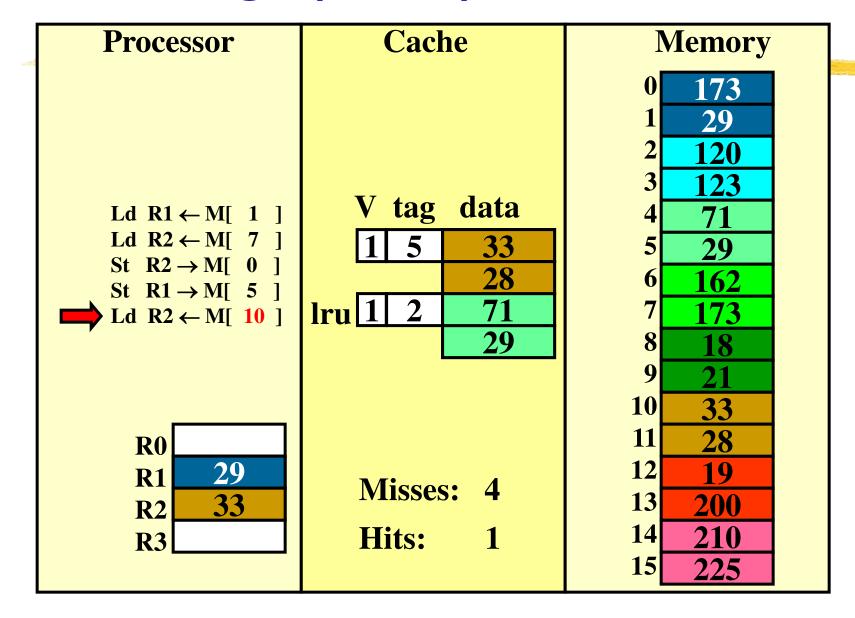
write-through (REF 4)



write-through (REF 5)



write-through (REF 5)



How many memory references?

- ☐ Each miss reads a block
 - ☐ 2 bytes in this cache
- □ Each store writes a byte
- □ Total reads: 8 bytes
- ☐ Total writes: 2 bytes

but caches generally miss < 20%

Write-through vs. write-back

- □ D the cache to NOT write all stores to memory immediately?
 - □ Keep the most current copy in the cache and update the memory when that data is evicted from the cache (a write-back policy).
 - □ write-back all evicted lines?
 - No, only blocks that have been stored into
 - Keep a "dirty bit", reset when the line is allocated, set when the block is stored into. If a block is "dirty" when evicted, write its data back into memory.

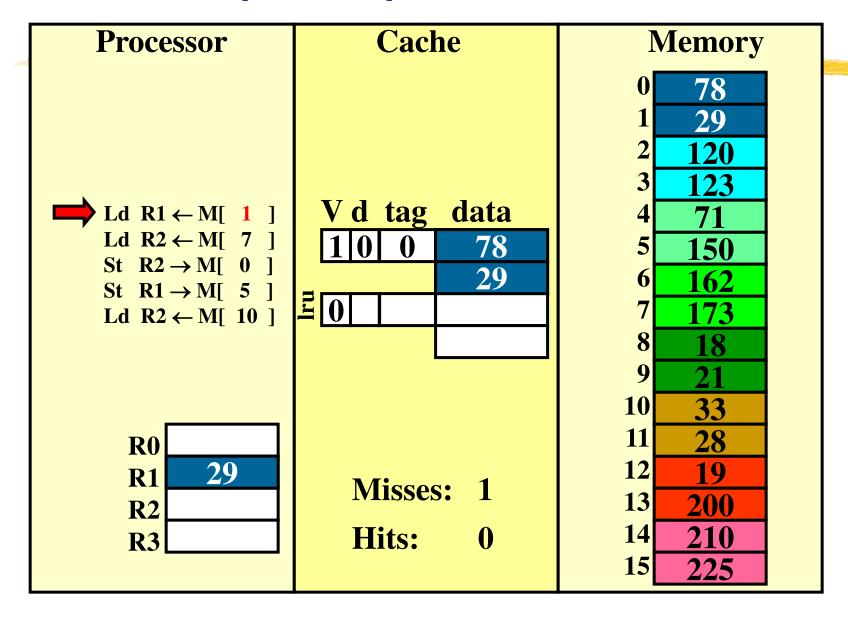
Handling stores (write-back)

Processor	Cache	Memory
Ld R1 ← M[1] Ld R2 ← M[7] St R2 → M[0] St R1 → M[5] Ld R2 ← M[10]	V d tag data 0	0 78 1 29 2 120 3 123 4 71 5 150 6 162 7 173 8 18 9 21
R0 R1 R2 R3	Misses: 0 Hits: 0	10 33 11 28 12 19 13 200 14 210 15 225

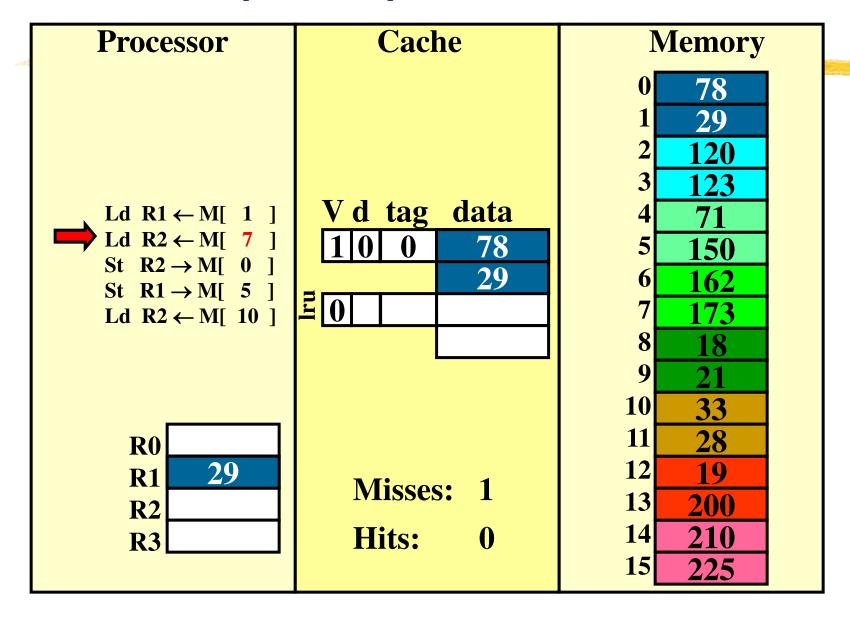
write-back (REF 1)

Processor	Cache	Memory
Ld R1 ← M[1] Ld R2 ← M[7] St R2 → M[0] St R1 → M[5] Ld R2 ← M[10] R0 R1 R2 R3	V d tag data O O O O O O O O O O O O O O O O O O O	0 78 1 29 2 120 3 123 4 71 5 150 6 162 7 173 8 18 9 21 10 33 11 28 12 19 13 200 14 210 15 225

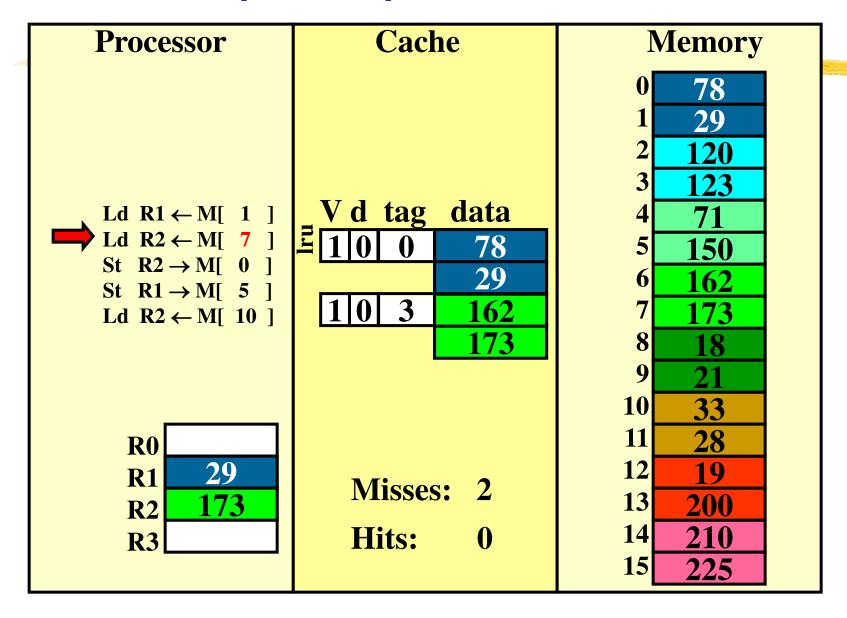
write-back (REF 1)



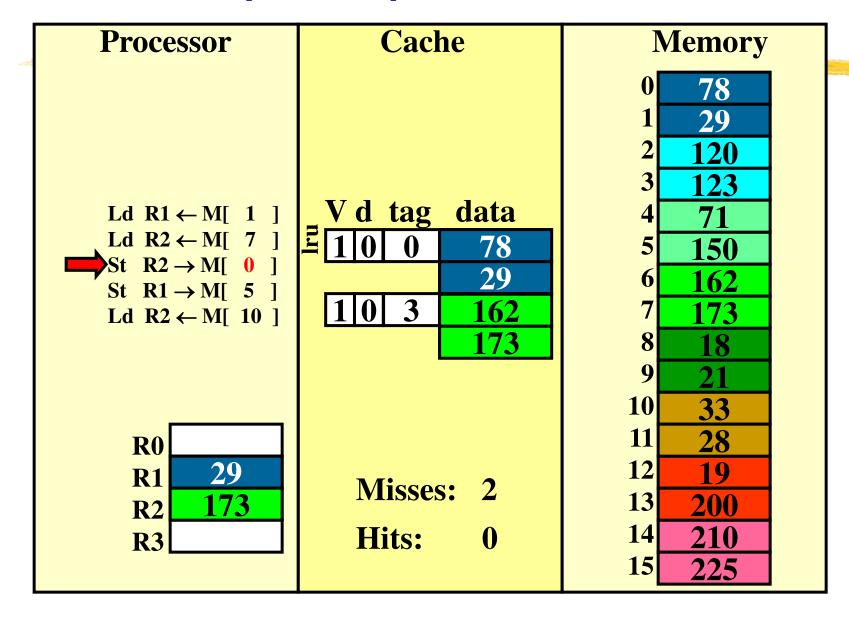
write-back (REF 2)



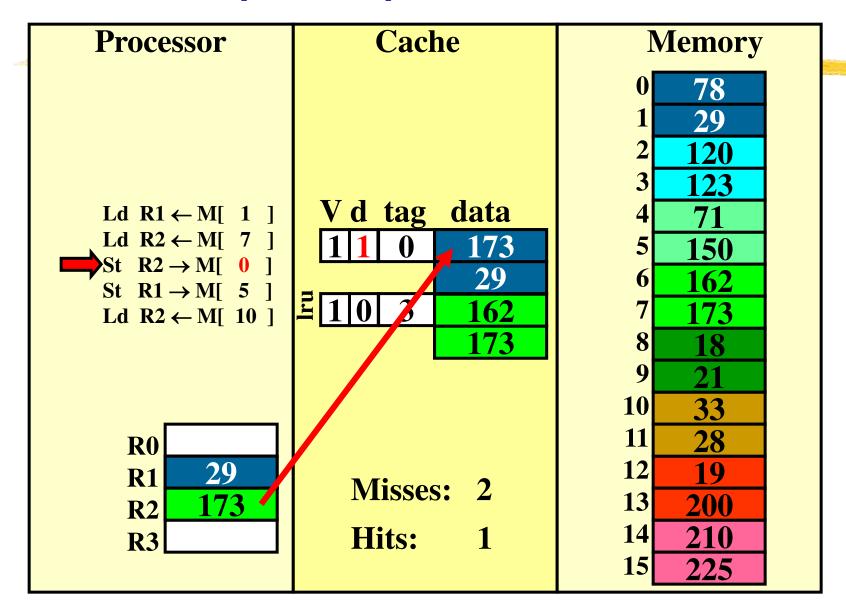
write-back (REF 2)



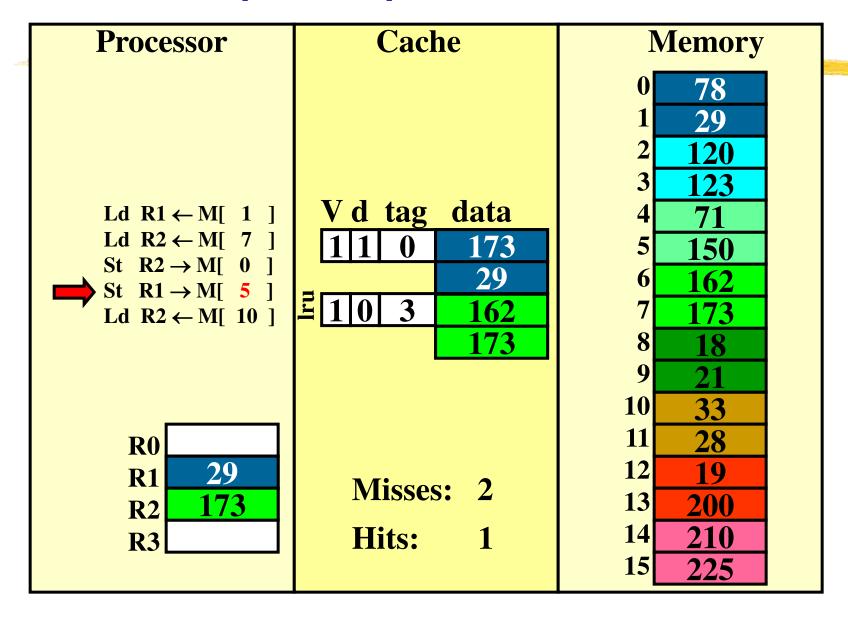
write-back (REF 3)



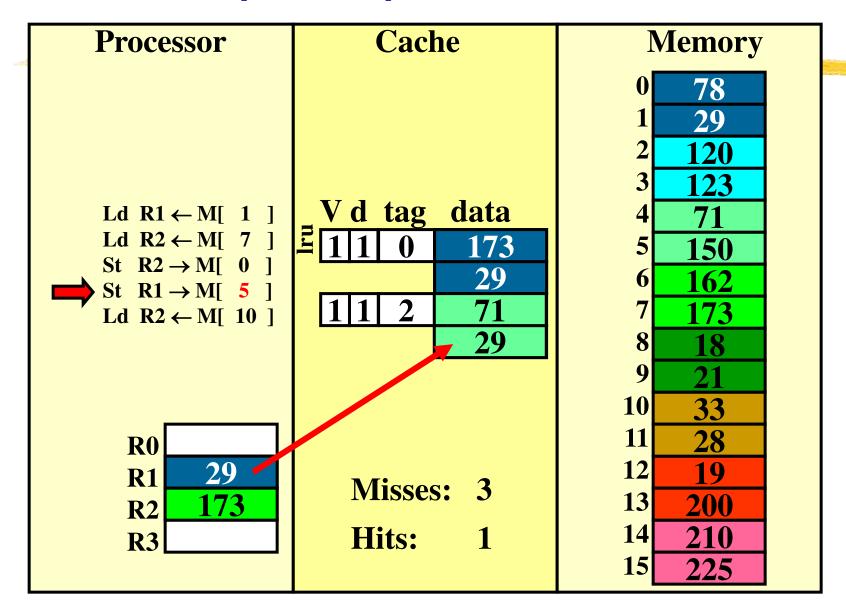
write-back (REF 3)



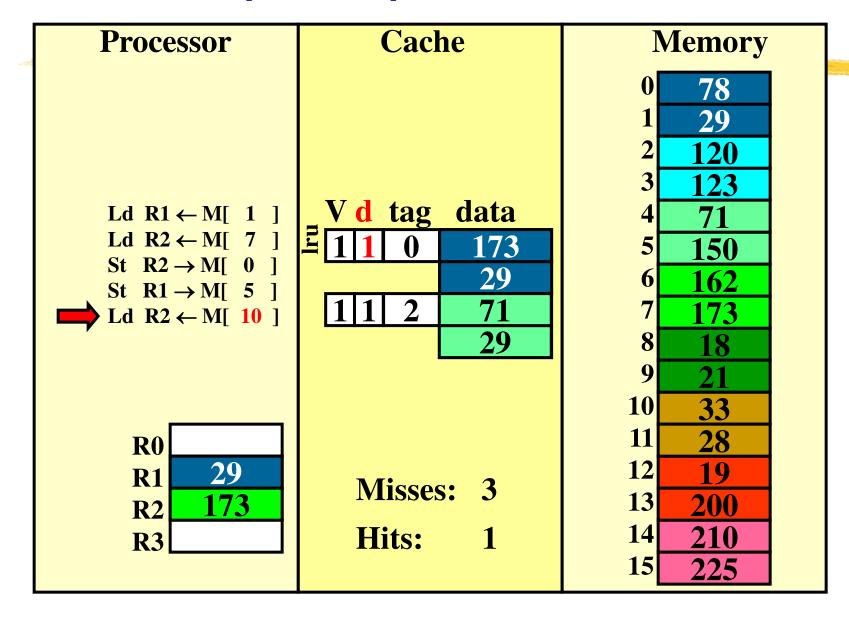
write-back (REF 4)



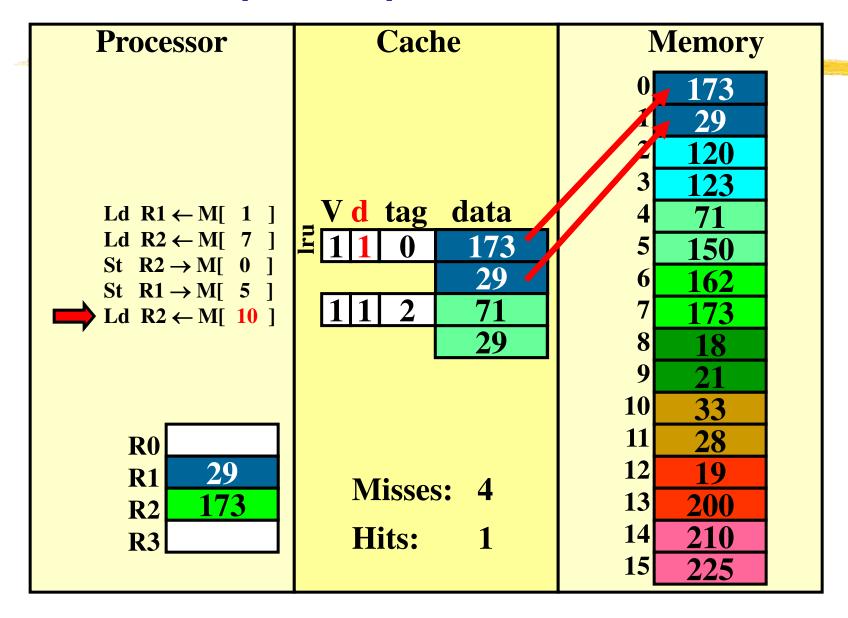
write-back (REF 4)



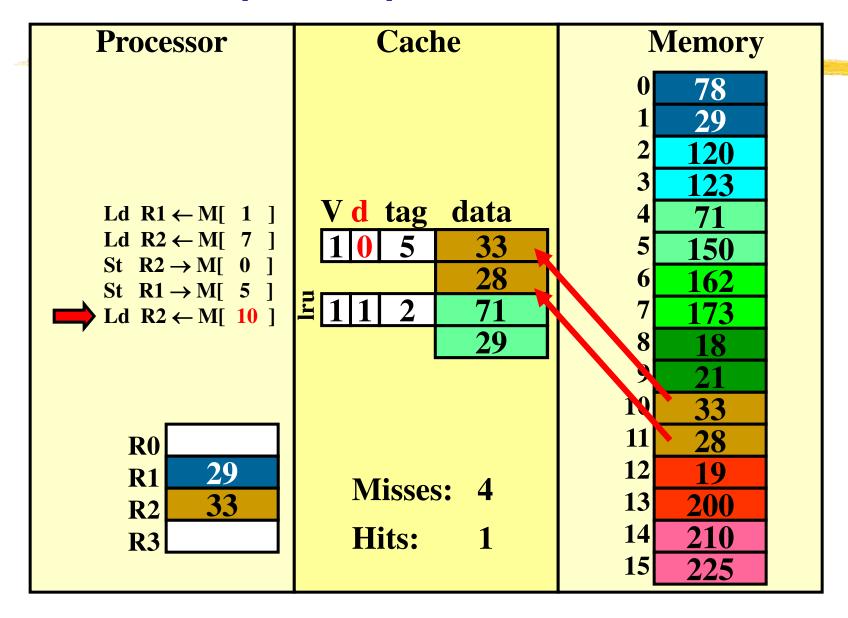
write-back (REF 5)



write-back (REF 5)



write-back (REF 5)



How many memory references?

- ☐ Each miss reads a block
 - □ 2 bytes in this cache
- □ Each evicted dirty cache line writes a block
- ☐ Total reads: 8 bytes
- □ Total writes: 4 bytes (after final eviction)

Choose write-back or write-through?