ARIMA Practice

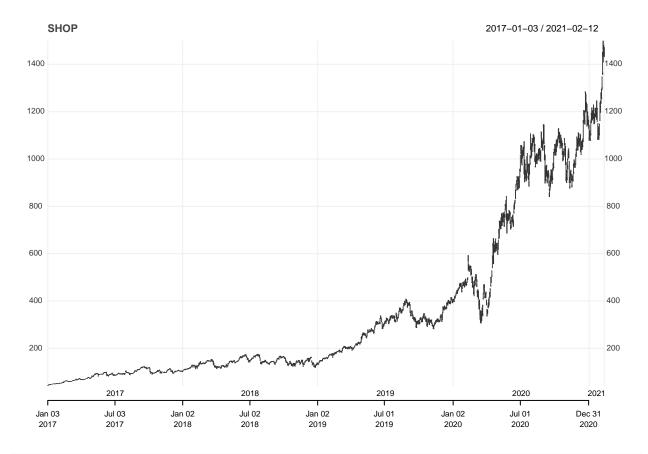
Anyi Fu

09/02/2021

Explore Data

```
summary(SHOP)
```

```
##
        Index
                           SHOP.Open
                                              SHOP.High
                                                                 SHOP.Low
           :2017-01-03
                         Min.
                                : 43.26
                                            Min.
                                                 : 43.46
                                                                    : 42.13
                         1st Qu.: 118.84
                                            1st Qu.: 120.81
    1st Qu.:2018-01-11
                                                              1st Qu.: 115.92
##
                                            Median : 173.38
    Median :2019-01-24
                         Median: 169.90
                                                              Median: 167.05
##
    Mean
           :2019-01-23
                               : 352.55
                                                  : 360.40
                                                                     : 344.31
                         Mean
                                            Mean
                                                              Mean
    3rd Qu.:2020-02-04
                         3rd Qu.: 423.20
                                            3rd Qu.: 435.81
                                                              3rd Qu.: 412.26
##
    Max.
           :2021-02-12
                         Max.
                                :1475.63
                                            Max.
                                                   :1499.75
                                                                     :1438.03
                                                              Max.
      SHOP.Close
                       SHOP. Volume
                                          SHOP.Adjusted
##
                             : 403700
   Min.
          : 42.82
                      Min.
                                          Min.
                                                 : 42.82
    1st Qu.: 118.64
                      1st Qu.: 1195900
                                          1st Qu.: 118.64
##
   Median : 171.18
                      Median: 1669100
                                          Median: 171.18
##
    Mean
          : 353.03
                      Mean
                            : 2029440
                                          Mean
                                                 : 353.03
##
    3rd Qu.: 421.79
                      3rd Qu.: 2404225
                                          3rd Qu.: 421.79
           :1463.31
                             :20895900
##
    Max.
                      Max.
                                          Max.
                                                 :1463.31
p1 = chart_Series(SHOP)
p1
```



#The data is clearly non-stationary, hence we will find the log returns of it

```
##MA
SHOP <- subset(SHOP_Ori, index(SHOP_Ori) >= "2019-01-01")
##two MA using 10 and 30 days of windows,
SHOP_mm10 <- rollmean(SHOP[,6], 10, fill = list(NA, NULL, NA), align = "right")
SHOP_mm30 <- rollmean(SHOP[,6], 30, fill = list(NA, NULL, NA), align = "right")

ggplot(SHOP, aes(x = index(SHOP))) +
   geom_line(aes(y = SHOP[,6], color = "PBR")) + ggtitle("Shopify prices series 2019-2021") +
   geom_line(aes(y = SHOP_mm10, color = "MM10")) +
   geom_line(aes(y = SHOP_mm30, color = "MM30")) + xlab("Date") + ylab("Price") +
   theme(plot.title = element_text(hjust = 0.5), panel.border = element_blank()) +
   scale_x_date(date_labels = "%b %y", date_breaks = "3 months") +
   scale_colour_manual("Series", values=c("PBR"="gray40", "MM10"="firebrick4", "MM30"="darkcyan"))</pre>
```

- ## Don't know how to automatically pick scale for object of type xts/zoo. Defaulting to continuous.
- ## Warning: Removed 9 row(s) containing missing values (geom_path).
- ## Warning: Removed 29 row(s) containing missing values (geom_path).

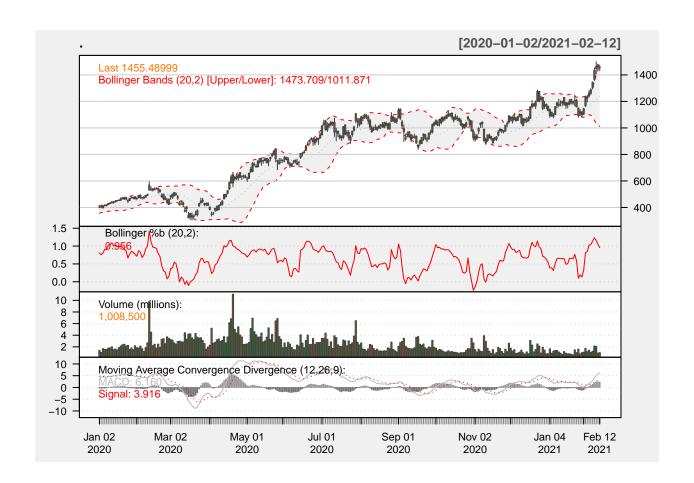
Shopify prices series 2019–2021



```
myTheme<-chart_theme()
myTheme$col$up.col<-'darkgreen'
myTheme$col$dn.col<-'darkred'
myTheme$col$dn.border <- 'black'
myTheme$col$up.border <- 'black'
myTheme$rylab <- FALSE
myTheme$rylab <- "lightgrey"

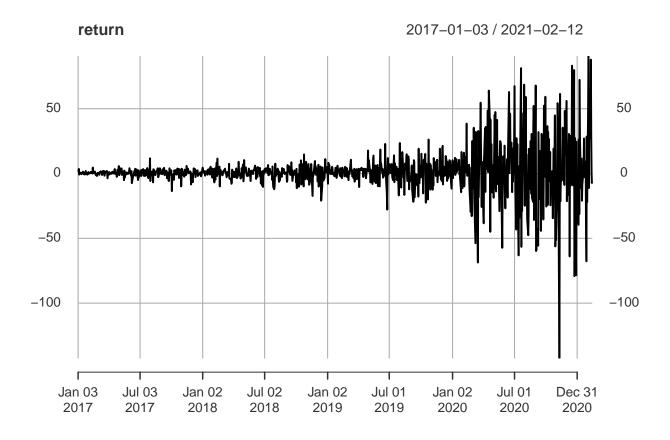
p2 = chart_Series(SHOP['2020-12/2021-02'], theme = myTheme)
SHOP_Ori <- SHOP
p2</pre>
```





Return and log Return

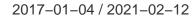
```
return = diff(adj_prices,lag=1)
plot(return)
```

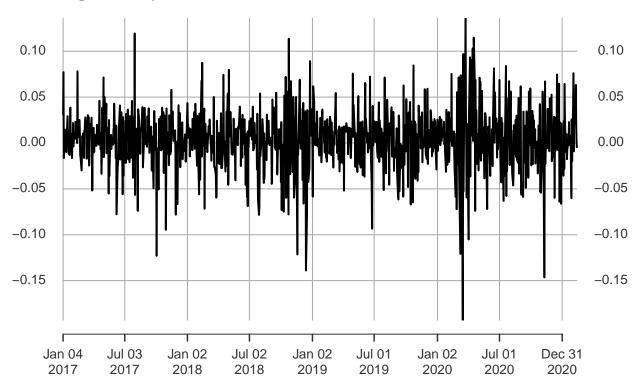


The series is obviously not stationary

```
# Compute the log returns for the stock
logR = diff(log(adj_prices),lag=1)
logR = logR[!is.na(logR)]
# Plot log returns
plot(logR, type='l', main='log returns plot')
```

log returns plot





summary(logR)

```
##
        Index
                        SHOP.Adjusted
          :2017-01-04
                               :-0.193000
   1st Qu.:2018-01-14
                        1st Qu.:-0.013119
##
   Median :2019-01-25
                        Median: 0.004968
##
                              : 0.003407
##
   Mean
           :2019-01-23
                        Mean
##
    3rd Qu.:2020-02-04
                         3rd Qu.: 0.022101
##
  Max.
           :2021-02-12
                        Max. : 0.135820
```

skewness(logR)

```
## [1] -0.4345547
## attr(,"method")
## [1] "moment"
```

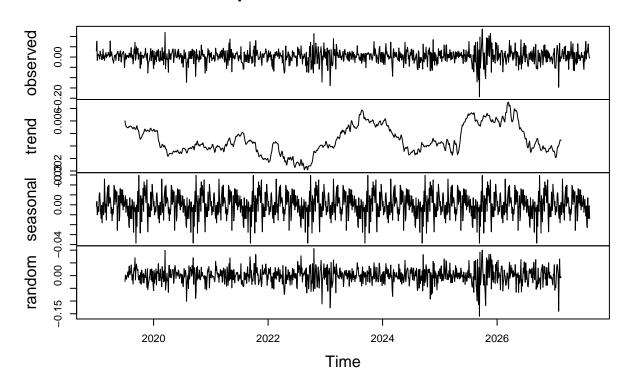
kurtosis(logR)

```
## [1] 2.788449
## attr(,"method")
## [1] "excess"
```

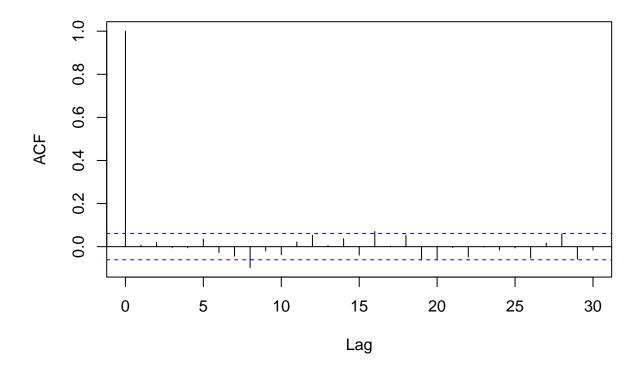
```
#skewness is -0.4351852 which implies a slightly negative skewness #kurtosis is 5.799651 which is much higher than 3 since it is a log function
```

```
#Trend
##Check for the trend
summary(ur.df(logR, type='trend', lags=20, selectlags="BIC"))
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression trend
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 + 1 + tt + z.diff.lag)
##
## Residuals:
        Min
                  1Q
                        Median
## -0.194703 -0.016286  0.001515  0.018636  0.130803
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 2.357e-03 2.176e-03
                                   1.083
                                            0.279
             -9.731e-01 4.432e-02 -21.958
                                           <2e-16 ***
## z.lag.1
              1.580e-06 3.603e-06
## tt
                                   0.439
                                            0.661
## z.diff.lag -1.952e-02 3.146e-02 -0.621
                                            0.535
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.03358 on 1010 degrees of freedom
## Multiple R-squared: 0.4965, Adjusted R-squared: 0.495
## F-statistic: 332 on 3 and 1010 DF, p-value: < 2.2e-16
##
## Value of test-statistic is: -21.9578 160.7161 241.0737
##
## Critical values for test statistics:
##
        1pct 5pct 10pct
## tau3 -3.96 -3.41 -3.12
## phi2 6.09 4.68 4.03
## phi3 8.27 6.25 5.34
logR_mm10 <- rollmean(logR, 10, fill = list(NA, NULL, NA), align = "right")
logR_mm30 <- rollmean(logR, 30, fill = list(NA, NULL, NA), align = "right")
## weights for moving avg
#Decomposition
logR_ts <- ts(logR, frequency = 120 , start = 2019 )</pre>
logR de <- decompose(logR ts)</pre>
plot(logR_de)
```

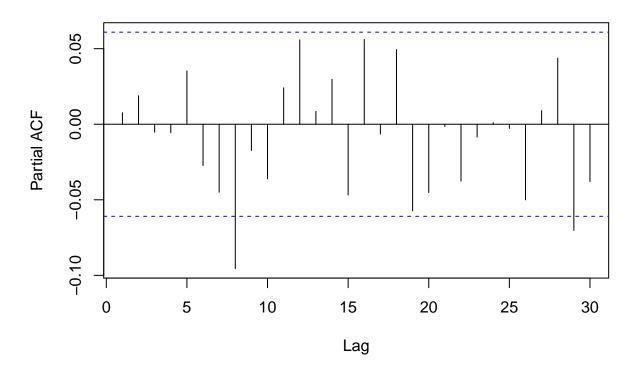
Decomposition of additive time series



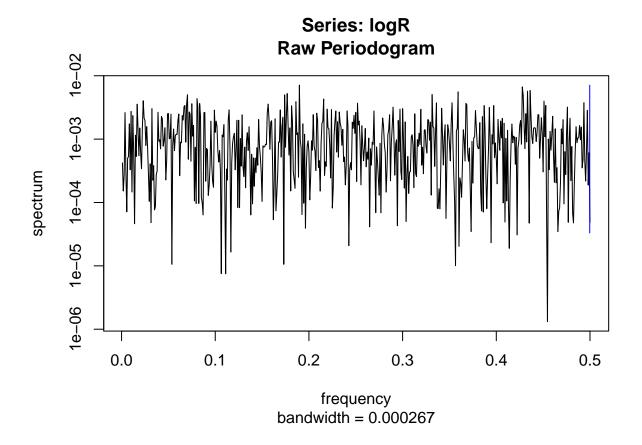
##Check for the seasonality
acf(logR)



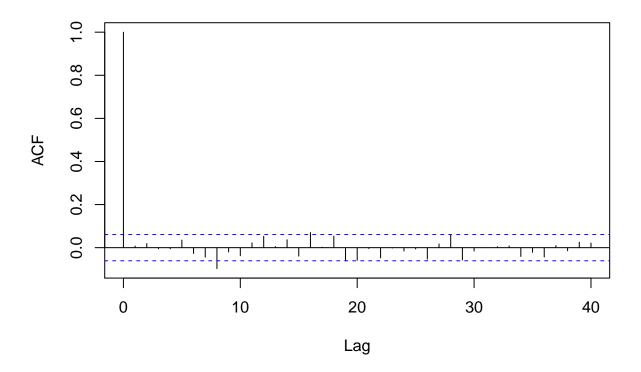
pacf(logR)



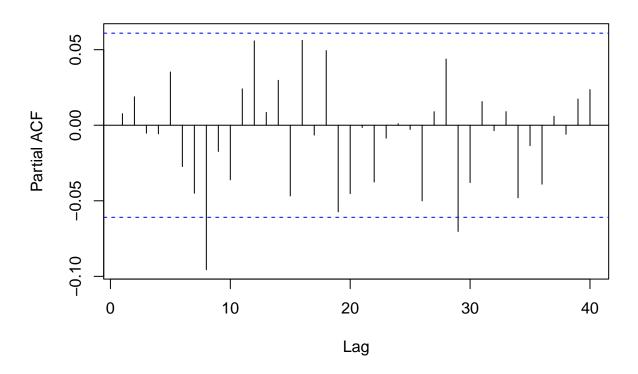
spec.pgram(logR)



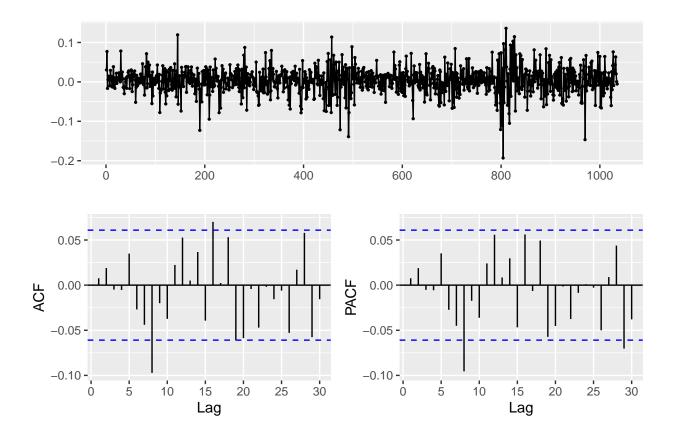
acf(logR, lag.max = 40)



pacf(logR, lag.max = 40)



logR %>% ggtsdisplay(main="")



##The PACF shown below is suggestive of an AR(18) model. So an initial candidate model is an ##ARIMA(18 ##We fit an ARIMA(18,1,0) model along with variations including ARIMA(4,1,0), ARIMA(2,1,0), ARIMA(3,1,1 #the Augmented Dickey-Fuller test, the Phillips-Perron unit root test and the KPSS test for stationarity ndiffs(logR)

For AR models, the ACF will dampen exponentially and the PACF plot will be used to identify the orde

[1] 0

```
adf.test(logR); pp.test(logR); kpss.test(logR)
## Warning in adf.test(logR): p-value smaller than printed p-value
```

```
##
## Augmented Dickey-Fuller Test
##
## data: logR
## Dickey-Fuller = -10.745, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
## Warning in pp.test(logR): p-value smaller than printed p-value
```

```
## Phillips-Perron Unit Root Test
##
## data: logR
## Dickey-Fuller Z(alpha) = -1034, Truncation lag parameter = 7, p-value =
## 0.01
## alternative hypothesis: stationary

## Warning in kpss.test(logR): p-value greater than printed p-value

##
## KPSS Test for Level Stationarity
##
## data: logR
## KPSS Level = 0.061001, Truncation lag parameter = 7, p-value = 0.1

# The null hypothesis is rejected for ADF and Unit Root test
# For KPSS test, the null hypothesis of stationarity around a trend is not rejected since the p-value i
# Hence we can conclude that the series is stationary
```

Fit ARIMA Model

##

```
#AIC Table
aicc_table = function(dataset,P,Q){
  table = matrix(NA,(P+1),(Q+1))
  for (p in 0:P){
    for (q in 0:Q){
     table[p+1,q+1] = Arima(dataset,order=c(p,0,q))$aicc
    }
} dimnames(table) = list(paste("<b> AR",0:P,"</b>",sep=""),paste("MA",0:Q,sep=""))
  table
}
logR_aicc_table = aicc_table(logR,10,10)
require(knitr)
```

Loading required package: knitr

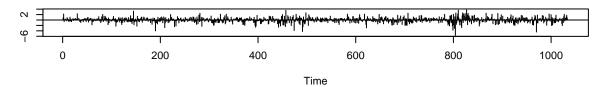
```
kable(logR_aicc_table,digits=2)
```

	MA0	MA1	MA2	MA3	MA4	MA5	MA6	MA7	MA8	MA9	MA10
AR0	-	-	-	-	-	-	-	-	-	-	_
	4099.30	4097.35	4095.72	4093.74	4091.76	4091.23	4089.73	4089.85	4096.92	4095.16	4093.96
AR1	-	-	-	-	-	-	-	-	-	-	-
	4097.35	4095.44	4093.55	4094.70	4092.66	4089.49	4093.36	4093.90	4095.36	4093.33	4091.07
AR2	-	-	-	-	-	-	-	-	-	-	-
	4095.71	4093.69	4095.40	4093.82	4091.85	4095.50	4094.58	4096.60	4093.44	4091.40	4098.53

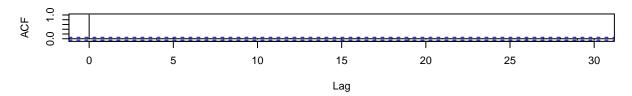
```
MA0
                      MA1
                                MA2
                                         MA3
                                                   MA4
                                                            MA5
                                                                     MA6
                                                                               MA7
                                                                                        MA8
                                                                                                  MA9 MA10
AR3
            4093.72 \ 4091.69 \ 4093.83 \ 4091.80 \ 4090.13 \ 4094.33 \ 4095.87 \ 4093.83 \ 4091.72 \ 4092.28 \ 4096.59
AR4
            4091.73 \ \ 4089.70 \ \ 4091.86 \ \ 4089.67 \ \ 4098.30 \ \ 4092.10 \ \ \ 4093.98 \ \ \ 4091.80 \ \ \ 4101.61 \ \ \ 4100.88 \ \ \ 4094.49
AR5
            4090.99 \ 4089.73 \ 4093.15 \ 4092.17 \ 4096.96 \ 4090.75 \ 4088.76 \ 4090.16 \ 4099.71 \ 4099.60 \ 4097.21
AR6
            4089.73 \ 4093.18 \ 4098.45 \ 4092.84 \ 4094.79 \ 4096.63 \ 4099.09 \ 4103.85 \ 4099.00 \ 4097.48 \ 4093.56
AR7
            4089.82 \ 4093.53 \ 4096.64 \ 4094.86 \ 4092.80 \ 4090.66 \ 4102.78 \ 4097.10 \ 4097.24 \ 4098.91 \ 4099.36
AR8
            4097.35 4095.89 4094.01 4093.76 4103.38 4101.33 4099.72 4100.38 4099.50 4098.42 4100.91
AR9
            4095.63 4093.85 4092.05 4093.68 4101.52 4100.37 4098.85 4095.32 4099.06 4102.62 4097.72
AR10
            4094.98 \ 4093.06 \ 4099.93 \ 4097.98 \ 4095.99 \ 4099.54 \ 4102.89 \ 4100.81 \ 4100.32 \ 4098.70 \ 4096.10
```

```
## The lowest one is at AR6 & MA7, so try ARIMA(6,0,7)
##The AIC works as such: Some models, such as ARIMA(3,1,3), may offer better fit than ARIMA(2,1,3), but
m1.logR=Arima(logR, order=c(6,0,7))
summary(m1.logR)
## Series: logR
## ARIMA(6,0,7) with non-zero mean
## Coefficients:
##
            ar1
                   ar2
                            ar3
                                    ar4
                                            ar5
                                                     ar6
                                                              ma1
                                                                       ma2
##
         1.0872 0.294 -1.3250 0.1632 1.0986
                                                -0.9002
                                                         -1.0847
                                                                   -0.2847
                                                                            1.3117
        0.0556 0.035
                        0.0583 0.0451 0.0435
                                                  0.0596
                                                           0.0638
                                                                    0.0512 0.0647
## s.e.
##
            ma4
                     ma5
                              ma6
                                      ma7
         -0.1360
                 -1.1039 0.8562 0.0081 0.0033
                  0.0503 0.0805 0.0340 0.0010
## s.e.
         0.0681
## sigma^2 estimated as 0.001092: log likelihood=2067.16
                                BIC=-4030.19
## AIC=-4104.32
                 AICc=-4103.85
## Training set error measures:
                        ME
                                  RMSE
                                             MAE MPE MAPE
                                                                 MASE
## Training set 0.000122528 0.03282064 0.02393867 -Inf Inf 0.6861385 0.0005626716
#non-seasonal
tsdiag(m1.logR,gof=15,omit.initial=FALSE)
```

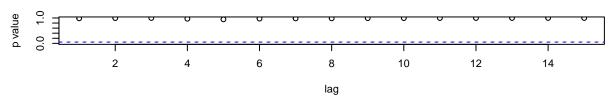
Standardized Residuals



ACF of Residuals

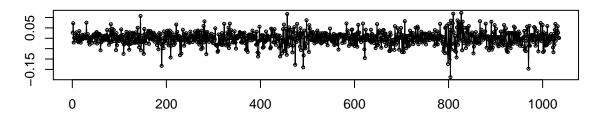


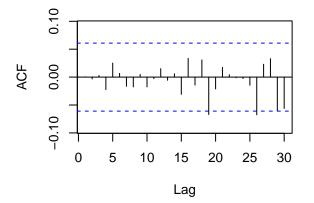
p values for Ljung-Box statistic

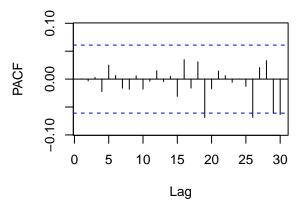


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m1.logR\$residuals







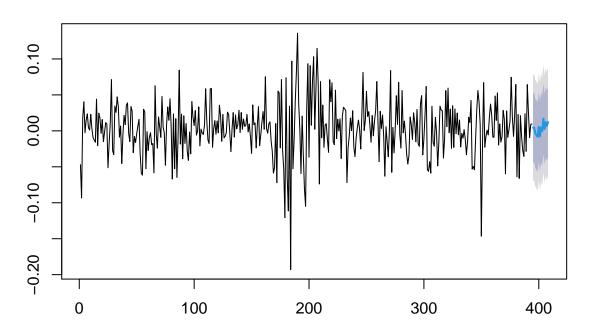
From acf: no significant autocorrelation - hence white noise series

Further Exploration - 14 Days

```
## Here we choose training data : testing data = .95 : .05

logR1 <- logR[(0.6*length(logR)): length(logR)]
logR_train <- logR1[1:((0.95)*length(logR1))]
logR_test <- logR1[(0.95*length(logR1)):length(logR1)]
arima_train <- Arima(logR_train, order = c(6,0,7))
pred <- predict(arima_train, n.ahead = (length(logR1)-(0.95*length(logR1)) + 1))$pred
forecast <- forecast(arima_train, h = 14)
plot(forecast)</pre>
```

Forecasts from ARIMA(6,0,7) with non-zero mean



```
##The heavy gray bar and light gray bar separately represent the 99% and 95% confidence interval for th
accuracy(pred,logR_test)
##
                     ME
                              RMSE
                                          MAE
                                                    MPE
                                                            MAPE
## Test set 0.007828905 0.03397488 0.02654998 51.98492 170.5449
### I chose logR[(0.43*length(logR)): length(logR)] this portion to be the dataset which can return a r
### MAE and RMSE are two of the most common metrices to measure accuracy for continuous variable
### Still need to be interpreted: which metric should we use?
### ( FYI RMSE is used by the sample I referred)
##Trying to convert log-returns to actual prices
## Add new dates
addDate = function(lastDate, num){
  dayList <- vector(mode = "list")</pre>
 dayList[1] = format(lastDate, "%Y-%m-%d")
```

for (n in 1:num){
 if (n == 1) {

}

else {

newDate = as.Date(paste(dayList[n])) + 1

```
newDate = as.Date.numeric(as.numeric(dayList[n])) + 1
}
if (weekdays(newDate) == "Saturday") {
    dayList[n+1] = newDate + 2
}
else if (weekdays(newDate) == "Sunday") {
    dayList[n+1] = newDate + 1
}
else {
    dayList[n+1] = newDate
}
as.Date.numeric(as.numeric(dayList[2:length(dayList)]))
}
```

```
## Find actual prices
actPrice = function(lastPrice, logReturns){
  pList <- vector(mode = "list", length = length(logReturns) + 1)
  pList[1] = as.numeric(lastPrice)

for (n in 1:length(logReturns)){
   newP = exp(log(as.numeric(pList[n])) + as.numeric(logReturns[n]))
   pList[n+1] = newP
  }
  pList[2:length(pList)]
}</pre>
```

```
lastAdj = SHOP$SHOP.Adjusted[length(SHOP$SHOP.Adjusted)]
lastMax =SHOP$SHOP.High[length(SHOP$SHOP.Adjusted)]
lastMin = SHOP$SHOP.Low[length(SHOP$SHOP.Adjusted)]
pList_Adj = actPrice(lastAdj, forecast$mean )
pList_Max = actPrice(lastMax, forecast$upper[,1] ) #here we chose Hi 80%
pList_Min = actPrice(lastMin, forecast$lower[,1] ) # and Lo 80%
SHOP_prices <- SHOP
SHOP prices$SHOP.Close = NULL
SHOP_prices$SHOP.Open = NULL
SHOP_prices$SHOP.Volume = NULL
lastDate = index(adj_prices)[length(adj_prices)]
days_pred = addDate(lastDate, 14)
df_ini <- data.frame(Date = days_pred,</pre>
                 Name = rep(c("SHOP.High", "SHOP.Low", "SHOP.Adjusted"), each = 14),
                  X = rnorm(42)
zdf <- read.zoo(file = df_ini,split = "Name")</pre>
new_prices = rbind(SHOP_prices, zdf)
new_prices$SHOP.Adjusted[535:548] <- as.numeric(pList_Adj)</pre>
new_prices$SHOP.High[535:548] <- as.numeric(pList_Max)</pre>
new_prices$SHOP.Low[535:548] <- as.numeric(pList_Min)</pre>
```

tail(new_prices)

```
##
              SHOP. High SHOP. Low SHOP. Adjusted
## 2021-02-25 2265.856 918.0984
                                      1445.738
## 2021-02-26 2420.310 889.2368
                                      1470.527
## 2021-03-01 2548.530 849.0346
                                      1474.472
## 2021-03-02 2708.930 818.1074
                                      1492.220
## 2021-03-03 2864.771 784.1955
                                      1502.401
## 2021-03-04 3046.376 755.8448
                                      1521.027
fig <- plot(new_prices['2020-12/2021-03'], col = c('palegreen3', 'salmon', 'orange'),
            main = "Upcoming 7 Days Price Range Prediction for SHOP")
addLegend("topleft",
              legend.names=c("Max. Price", "Min. Price", "Adj. Price"),
```

col=c('palegreen3','salmon','orange'),

lty=c(1,1,1),
lwd=c(2,2,2),
bg="white")

Upcoming 7 Days Price Range Prediction fo 08HOP-01 / 2021-03-04

