Biplot

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BIPLOT

Se cargan las librerías necesesarias:

Se carga la matriz de datos:

```
vinos <- read_excel("/cloud/project/Estadística Multivariada/vinos.xls")
BD<-as.data.frame(vinos)[,-1]</pre>
```

Exploracion de matriz

```
#Dimensión de la matriz.
dim(BD)
## [1] 45 21
colnames(BD)
    [1] "a o"
                    "denomina" "grupo"
                                          "grado"
                                                      "avol"
                                                                 "atot"
##
                               "folin"
   [7] "acfi"
                   "ph"
                                                                 "procian"
                                          "somers"
                                                      "srv"
## [13] "acrg"
                   "acse"
                               "achplc"
                                          "ic"
                                                      "ic2"
                                                                 "tono"
## [19] "iim"
                               "vla"
                    "eq1"
str(BD)
## 'data.frame':
                    45 obs. of 21 variables:
##
    $ a o
                    1 1 1 1 1 1 1 1 1 1 ...
              : num
    $ denomina: num
                     1 1 1 1 1 1 1 1 1 1 ...
##
   $ grupo
                     1 1 1 1 1 1 1 1 1 1 ...
              : num
    $ grado
                     12.8 12.8 12.5 11.9 12.5 12.1 12.2 12.6 13 12.4 ...
              : num
                     1.2 0.75 1 0.7 0.95 0.5 0.8 0.4 0.4 0.35 ...
##
   $ avol
              : num
   $ atot
                     6.7 6.9 7.2 7.7 7.7 5.8 5.9 5.4 4.6 5.5 ...
              : num
                     5.2 6 6 6.8 6.3 5.2 4.9 4.9 4.1 5 ...
##
    $ acfi
              : num
                     3.7 3.5 3.6 3.3 3.6 3.2 3.4 3.3 3.6 3.3 ...
##
    $ ph
              : num
##
    $ folin
                     2827 1818 1459 2054 2930 ...
              : num
                     50.8 37.8 35.1 32.1 49.6 30.6 35.6 30.6 41.7 30 ...
    $ somers
              : num
##
    $ srv
                     811 968 866 978 1128 ...
              : num
##
    $ procian : num
                     3794 1736 2306 3420 3158 ...
##
                     386 144 225 204 214 167 252 315 293 152 ...
    $ acrg
              : num
##
    $ acse
              : num
                     287 141 132 110 148 95 160 124 170 67 ...
##
    $ achplc
              : num
                     181 69 78 84 75 74 101 101 137 56 ...
##
    $ ic
              : num
                     7.81 4.88 5.52 4.64 6.99 3.98 7.6 6.15 6.6 5.49 ...
                     8.95 5.55 6.35 5.15 7.87 4.36 8.84 7.11 7.85 6.23 ...
##
    $ ic2
##
   $ tono
                     0.72 0.755 0.456 0.675 0.672 0.716 0.716 0.74 0.93 0.75 ...
              : num
```

```
## $ iim : num 18.4 23.6 36.8 36.4 34.2 38.1 28.5 27.7 21.6 30.3 ...

## $ eq1 : num 0.489 0.48 0.598 0.42 0.45 0.434 0.501 0.566 0.557 0.689 ...

## $ vla : num 0.21 0.56 0.38 0.29 0.36 0.3 0.24 0.4 0.28 0.26 ...

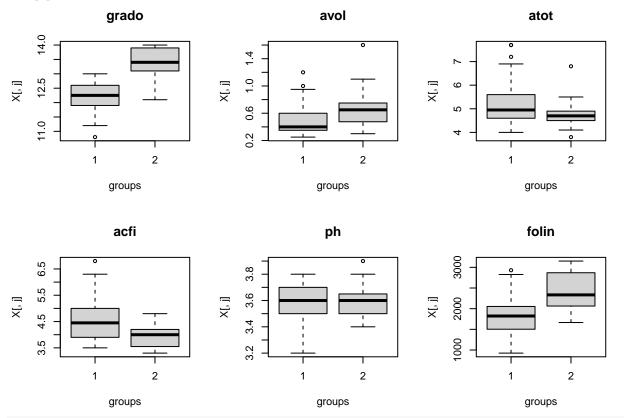
BD$denomina = as.factor(BD$denomina)

BD$grupo = as.factor(BD$grupo)
```

Gráficos de exploración

BX1<-BoxPlotPanel(BD[,4:9], nrows=2, groups=BD\$denomina)

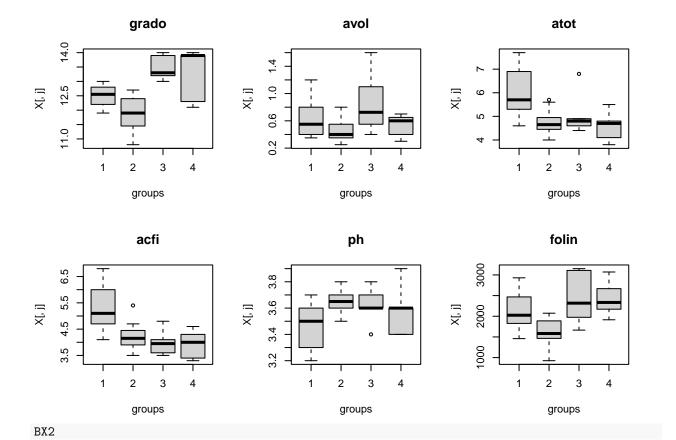
[1] 2



BX1

\$mfrow
[1] 2 3
BX2<-BoxPlotPanel(BD[,4:9], nrows=2, groups=BD\$grupo)</pre>

[1] 2



\$mfrow

[1] 2 3

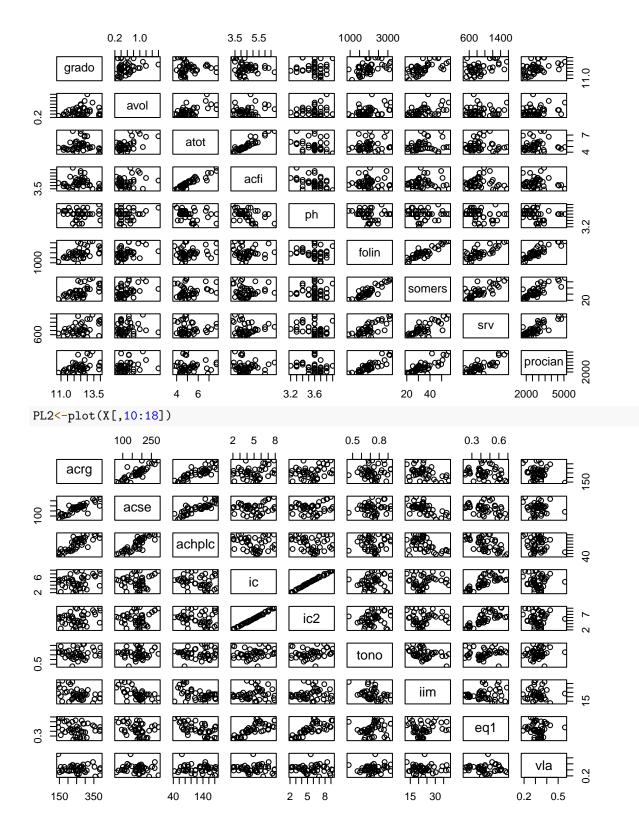
Filtrado de variables

1.- Selección de variables numéricas

X<-BD[,4:21]

2.- Generación del scatter plot

PL1<-plot(X[,1:9])



Reducción de la dimensionalidad

1.- ACP

```
acpvino<-PCA.Analysis(X,Scaling = 5)</pre>
summary(acpvino)
   ###### Principal Components Analysis ######
##
## Transformation of the raw data:
## [1] "Standardize columns"
##
##
   Eigenvalues & Explained Variance (Inertia)
        Eigenvalue Exp. Var Cummulative
##
## [1,] 277.12688
                    34.991
                                 34.991
## [2,]
        199.36534
                     25.172
                                 60.163
## [3,]
         85.42317
                    10.786
                                 70.949
##
##
   STRUCTURE OF THE PRINCIPAL COMPONENTS
##
##
           Dim 1 Dim 2 Dim 3
          -0.676 -0.142 0.188
## grado
## avol
          -0.450 0.204 -0.519
          -0.225 0.738 -0.526
## atot
          -0.063 0.797 -0.397
## acfi
## ph
           0.191 -0.593 -0.193
## folin
         -0.910 -0.094 -0.072
## somers -0.920 -0.154 -0.090
          -0.798 -0.088 0.277
## srv
## procian -0.873 -0.102 0.036
## acrg
          -0.301 -0.726 -0.441
## acse
          -0.213 -0.856 -0.372
## achplc
          0.119 -0.830 -0.355
          -0.926 0.117 -0.074
## ic
## ic2
          -0.932 0.095 -0.048
          -0.351 -0.290 0.612
## tono
## iim
           0.021 0.810 -0.179
## eq1
          -0.688 0.416 0.255
## vla
           0.006 0.071 0.368
```

2.- Contenido del objeto acpvino

names(acpvino)

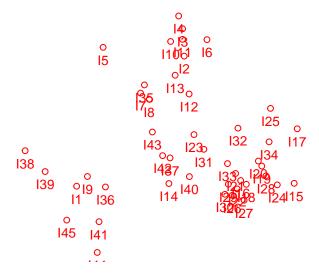
```
[1] "Title"
                                   "Type"
                                                             "call"
##
   [4] "Non_Scaled_Data"
                                   "alpha"
                                                             "Dimension"
   [7] "Means"
                                   "Medians"
                                                             "Deviations"
                                   "Maxima"
                                                             "P25"
## [10] "Minima"
                                                             "Initial_Transformation"
## [13] "P75"
                                   "GMean"
## [16] "Scaled_Data"
                                   "nrows"
                                                             "ncols"
                                                             "dim"
## [19] "nrowsSup"
                                   "ncolsSup"
## [22] "EigenValues"
                                   "Inertia"
                                                             "CumInertia"
## [25] "EV"
                                   "Structure"
                                                             "RowCoordinates"
## [28] "ColCoordinates"
                                   "RowContributions"
                                                             "ColContributions"
## [31] "Scale_Factor"
                                   "ClusterType"
                                                             "Clusters"
```

[34] "ClusterColors" "ClusterNames"

3.- Generación del gráfico sin caja

acp1<-plot(acpvino, ShowBox=FALSE)</pre>

Principal Components Analysis (Dim 1 (35 %)- 2 (25.2 %))



Screeplot con barras

acp2<-princomp(X, cor=TRUE, score=TRUE)
plot(acp2)</pre>

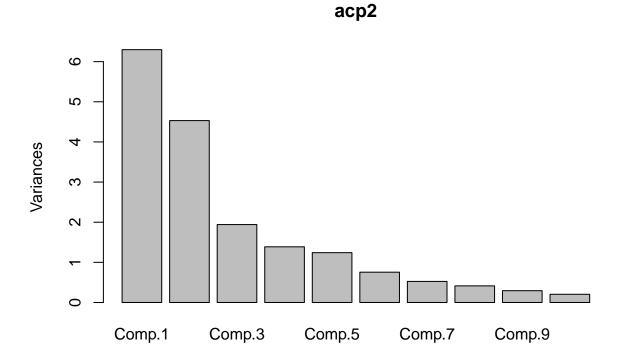
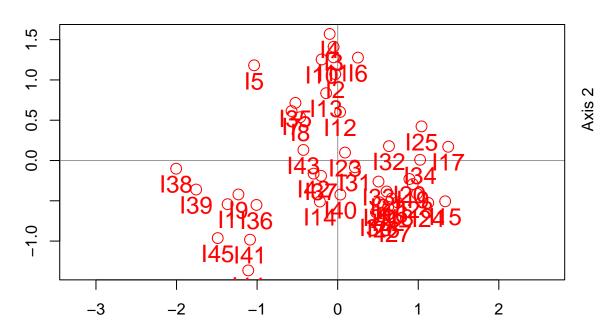


Gráfico circular de correlación

Principa

Principal Components Analysis (Dim 1 (35 %)-2 (25.2 %))



Agregar grupos al biplot definido por usuario

Grafico con poligonos

CexInd= tamaño de los argumentos

Principal Components Analysis (Dim 1 (35 %)-2 (25.2 %))

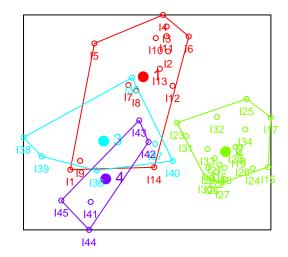


Gráfico con elipses

```
acp5<-plot(acpvino1, PlotClus=TRUE, ClustCenters=TRUE,
    margin=0.05, CexInd=0.7, TypeClus="el",
    ShowBox=F)</pre>
```

Principal Components Analysis (Dim 1 (35 %)-2 (25.2 %))

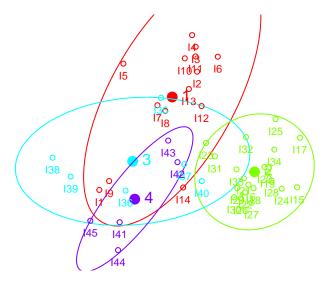
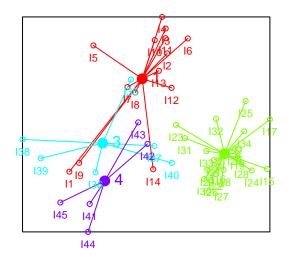


Gráfico con estrellas

```
acp6<-plot(acpvino1, PlotClus=TRUE, ClustCenters=TRUE,
    margin=0.05, CexInd=0.7, TypeClus="st",
    ShowBox=TRUE)</pre>
```

Principal Components Analysis (Dim 1 (35 %)-2 (25.2 %))



Aplicacion del Biplot

Predeterminado JK

```
bipvino<-PCA.Biplot(X, Scaling = 5)
summary(bipvino)</pre>
```

```
###### Biplot for Principal Components Analysis ######
##
## Call
## PCA.Biplot(X = X, Scaling = 5)
## Type of coordinates:
## Transformation of the raw data:
## [1] "Standardize columns"
## Type of Biplot
## [1] "PCA"
##
##
   Eigenvalues & Explained Variance (Inertia)
        Eigenvalue Exp. Var Cummulative
##
## [1,]
        277.12688
                     34.991
                                 34.991
        199.36534
  [2,]
                                 60.163
                     25.172
  [3,]
         85.42317
                     10.786
                                 70.949
##
##
##
   RELATIVE CONTRIBUTIONS OF THE FACTOR TO THE ELEMENT
##
##
   Row Contributions
##
##
       Dim 1 Dim 2 Dim 3
## I1 42.04 6.63 44.06
## I2
       0.03 32.75 2.51
## I3
       0.07 57.27 18.53
## I4
       0.28 70.89 8.84
## I5 29.69 38.53 12.87
       2.64 67.95 1.86
## 16
## I7 23.63 27.17 9.95
```

```
## I8 15.06 20.09 8.55
## I9 60.32 7.05 10.79
## I10 1.55 61.24 11.60
## I11 0.12 74.78 12.48
## I12 0.09 35.48 28.14
## I13 1.68 57.21 29.79
## I14 2.95 15.65 39.81
## I15 64.41 9.27 3.81
## I16 35.26 17.46 4.85
## I17 63.73 0.99 14.28
## I18 51.05 25.08 0.12
## I19 75.88 7.45 9.01
## I20 77.10 5.13 0.77
## I21 24.48 9.79 18.31
## I22 30.80 25.95 0.05
## I23 2.08 2.45 0.20
## I24 71.22 15.56 0.82
## I25 72.83 12.08 2.23
## I26 32.34 43.51 1.52
## I27 35.29 35.58 11.66
## I28 63.06 11.10 3.65
## I29 16.99 16.98 27.32
## I30 17.97 32.85 0.25
## I31 9.13 1.41 35.53
## I32 55.95 4.40 3.60
## I33 28.58 7.60 26.59
## I34 67.06 0.00 4.97
## I35 7.12 13.24 1.64
## I36 41.97 12.56 27.66
## I37 4.81 4.11 20.46
## I38 83.21 0.21 0.95
## I39 88.41 3.71 2.38
## I40 0.08 13.31 0.69
## I41 42.39 34.59 1.36
## I42 9.24 2.75 29.92
## I43 23.86 2.26 7.75
## I44 29.74 44.90 6.03
## I45 56.52 23.65 1.05
##
## Column Contributions
##
          Dim 1 Dim 2 Dim 3
          45.71 2.02 3.54
## grado
## avol
          20.23 4.14 26.96
## atot
           5.06 54.44 27.69
## acfi
           0.40 63.45 15.73
           3.63 35.20 3.72
## ph
          82.89 0.89 0.52
## folin
## somers 84.58 2.36 0.81
## srv
          63.74 0.78 7.65
## procian 76.19 1.04 0.13
## acrg
           9.08 52.64 19.41
           4.54 73.25 13.87
## acse
## achplc 1.41 68.84 12.61
## ic
          85.75 1.37 0.54
```

```
86.89 0.91 0.23
## ic2
## tono
           12.30 8.43 37.44
           0.04 65.55 3.20
## iim
## eq1
           47.38 17.28 6.51
## vla
            0.00 0.51 13.58
##
##
##
##
    Qualities of representation of the rows (Cummulative contributions)
##
       Dim 1 Dim 2 Dim 3
## I1 42.04 48.67 92.73
        0.03 32.78 35.29
## I2
## I3
        0.07 57.34 75.87
## I4
        0.28 71.17 80.01
## I5
      29.69 68.22 81.09
## 16
        2.64 70.59 72.45
## I7
       23.63 50.80 60.75
## I8 15.06 35.15 43.70
## I9 60.32 67.37 78.16
## I10 1.55 62.79 74.39
## I11 0.12 74.90 87.38
## I12 0.09 35.57 63.71
## I13 1.68 58.89 88.68
## I14 2.95 18.60 58.41
## I15 64.41 73.68 77.49
## I16 35.26 52.72 57.57
## I17 63.73 64.72 79.00
## I18 51.05 76.13 76.25
## I19 75.88 83.33 92.34
## I20 77.10 82.23 83.00
## I21 24.48 34.27 52.58
## I22 30.80 56.75 56.80
## I23  2.08  4.53  4.73
## I24 71.22 86.78 87.60
## I25 72.83 84.91 87.14
## I26 32.34 75.85 77.37
## 127 35.29 70.87 82.53
## I28 63.06 74.16 77.81
## I29 16.99 33.97 61.29
## I30 17.97 50.82 51.07
## I31 9.13 10.54 46.07
## I32 55.95 60.35 63.95
## I33 28.58 36.18 62.77
## 134 67.06 67.06 72.03
## I35 7.12 20.36 22.00
## I36 41.97 54.53 82.19
## I37
      4.81 8.92 29.38
## I38 83.21 83.42 84.37
## I39 88.41 92.12 94.50
## I40 0.08 13.39 14.08
## I41 42.39 76.98 78.34
## I42 9.24 11.99 41.91
## I43 23.86 26.12 33.87
## 144 29.74 74.64 80.67
```

```
## I45 56.52 80.17 81.22
##
##
##
   Qualities of representation of the columns (Cummulative contributions)
##
##
           Dim 1 Dim 2 Dim 3
## grado
           45.71 47.73 51.27
           20.23 24.37 51.33
## avol
## atot
           5.06 59.50 87.19
## acfi
           0.40 63.85 79.58
## ph
            3.63 38.83 42.55
           82.89 83.78 84.30
## folin
## somers 84.58 86.94 87.75
## srv
           63.74 64.52 72.17
## procian 76.19 77.23 77.36
## acrg
            9.08 61.72 81.13
## acse
            4.54 77.79 91.66
## achplc 1.41 70.25 82.86
           85.75 87.12 87.66
## ic
## ic2
           86.89 87.80 88.03
## tono
           12.30 20.73 58.17
## iim
           0.04 65.59 68.79
           47.38 64.66 71.17
## eq1
## vla
            0.00 0.51 14.09
```

Valores propios

bipvino\$EigenValues

```
## [1] 277.12687550 199.36534193 85.42316719 61.02361652 54.61472549

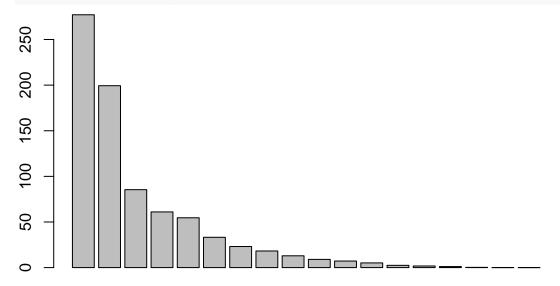
## [6] 33.21950770 23.10087611 18.20271969 12.93567822 8.99721387

## [11] 7.17039349 5.14634483 2.46693118 1.76863760 1.12884586

## [16] 0.26153511 0.02966717 0.01792254
```

Screeplot

SC<-barplot(bipvino\$EigenValues)</pre>



Vectores propios

bipvino\$EV

```
[,1]
                            [,2]
                                        [,3]
##
   [1,] -0.269400471 -0.06678758 0.13502664
  [2,] -0.179235894  0.09563188 -0.37266607
## [3,] -0.089642289 0.34663991 -0.37767939
## [4,] -0.025075364 0.37420670 -0.28461188
## [5,] 0.075921760 -0.27872944 -0.13842752
## [6,] -0.362771201 -0.04421297 -0.05176113
## [7,] -0.366464498 -0.07220257 -0.06472232
## [8,] -0.318130606 -0.04157401 0.19854164
   [9,] -0.347804576 -0.04785685 0.02584725
## [10,] -0.120049408 -0.34086254 -0.31617278
## [11,] -0.084888000 -0.40207820 -0.26728099
## [12,] 0.047378644 -0.38977456 -0.25488092
## [13,] -0.368971746  0.05491570 -0.05287232
## [14,] -0.371435455   0.04476039 -0.03421019
## [15,] -0.139772430 -0.13640832 0.43913353
## [16,] 0.008178563 0.38035721 -0.12838425
## [17,] -0.274261123 0.19527349 0.18313281
## [18,] 0.002361018 0.03345360 0.26444673
```

Tabla de inercias

Eje	Valor Propio	Inercia	Inercia acumulada
Eje 1	277.1268755	34.991	34.991
Eje 2	199.3653419	25.172	60.163
Eje 3	85.4231672	10.786	70.949
Eje 4	61.0236165	7.705	78.654
Eje 5	54.6147255	6.896	85.550
Eje 6	33.2195077	4.194	89.744
Eje 7	23.1008761	2.917	92.661
Eje 8	18.2027197	2.298	94.959
Eje 9	12.9356782	1.633	96.592
Eje 10	8.9972139	1.136	97.728
Eje 11	7.1703935	0.905	98.633
Eje 12	5.1463448	0.650	99.283
Eje 13	2.4669312	0.311	99.594
Eje 14	1.7686376	0.223	99.817
Eje 15	1.1288459	0.143	99.960
Eje 16	0.2615351	0.033	99.993
Eje 17	0.0296672	0.004	99.997
Eje 18	0.0179225	0.002	99.999

Tabla contribución de columnas

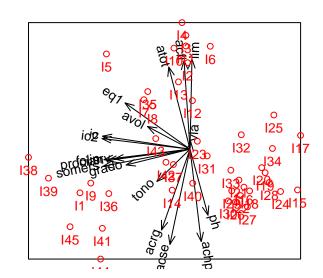
kable(bipvino\$ColContributions)

	Dim 1	Dim 2	Dim 3
grado	45.71	2.02	3.54
avol	20.23	4.14	26.96
atot	5.06	54.44	27.69
acfi	0.40	63.45	15.73
ph	3.63	35.20	3.72
folin	82.89	0.89	0.52
somers	84.58	2.36	0.81
srv	63.74	0.78	7.65
procian	76.19	1.04	0.13
acrg	9.08	52.64	19.41
acse	4.54	73.25	13.87
achplc	1.41	68.84	12.61
ic	85.75	1.37	0.54
ic2	86.89	0.91	0.23
tono	12.30	8.43	37.44
$_{ m iim}$	0.04	65.55	3.20
eq1	47.38	17.28	6.51
vla	0.00	0.51	13.58

Gráficos Biplot

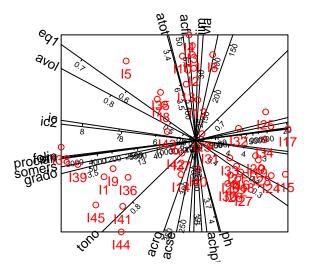
plot(bipvino, ShowBox=TRUE)

PCA Biplot (Dim 1 (35 %)- 2 (25.2 %))



• Prolongación de vectores linea recta

PCA Biplot (Dim 1 (35 %)- 2 (25.2 %))



• Prolongación de vectores con flechas y linea punteada

PCA Biplot (Dim 1 (35 %)- 2 (25.2 %))

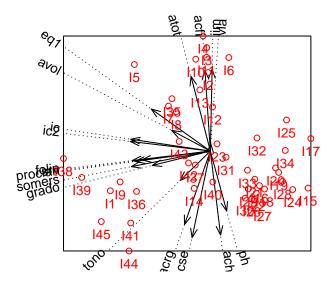
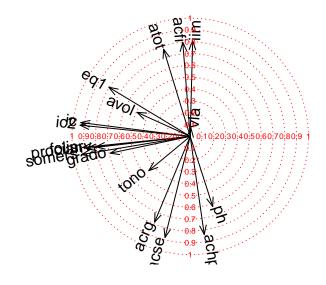


Gráfico circular correlaciones

GC<-CorrelationCircle(bipvino)</pre>

PCA Biplot – Correlation Circle

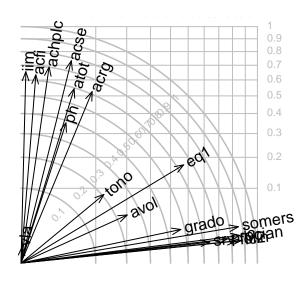


Axis 1

Gráfico contribuciones de los vectores

ColContributionPlot(bipvino, AddSigns2Labs = FALSE)

PCA Biplot – Contribution Plot

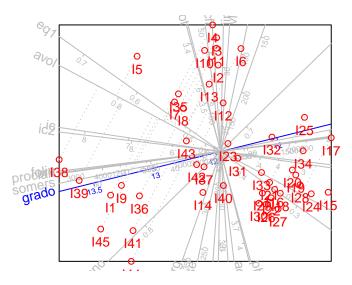


√xis 2

Axis 1

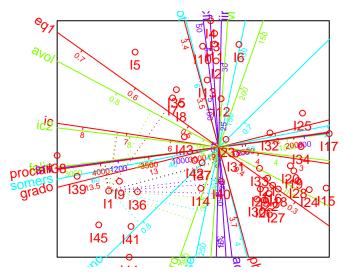
• Proyección individuos sobre una variable donde dp= selecciona la variable

PCA Biplot (Dim 1 (35 %)- 2 (25.2 %))



• Proyección de ind sobre todas las variables con PredPoints= individuo

PCA Biplot (Dim 1 (35 %)- 2 (25.2 %))

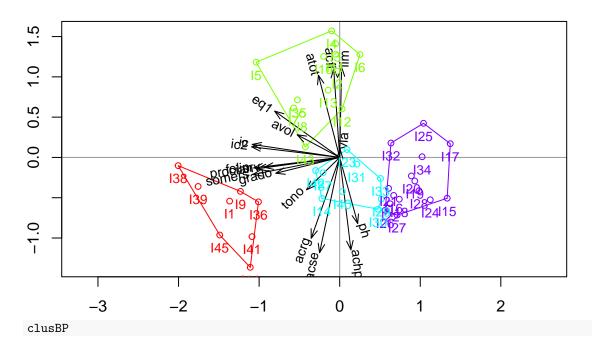


- Cluster Jerárquico con datos originales con el metodo ward.D

• Cluster aplicado al biplot

clusBP<-plot(bipvino, PlotClus=TRUE, ShowAxis=TRUE)</pre>

PCA Biplot (Dim 1 (35 %)- 2 (25.2 %))



NULL