

Prof. Dr. Florian Künzner

Technical University of Applied Sciences Rosenheim, Computer Science

Start: 8:01

CA 2 – Data representation

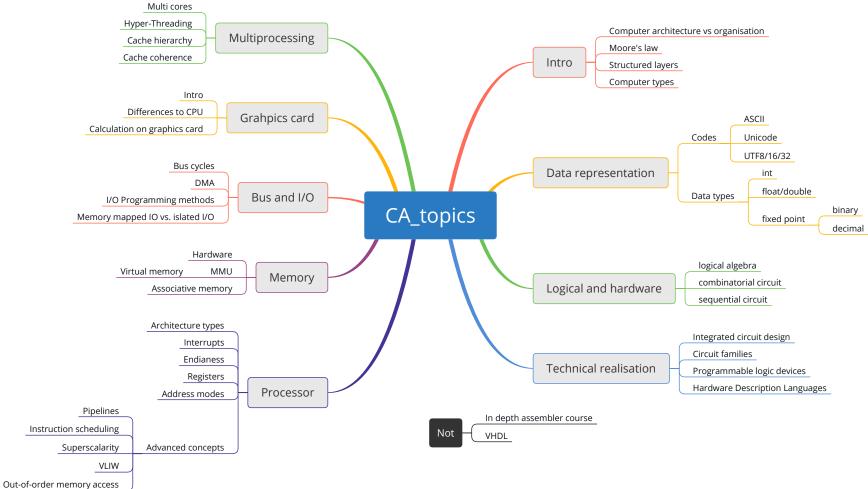
The lecture is based on the work and the documents of Prof. Dr. Theodor Tempelmeier

Computer Science

Goal



Goal





Goal



Technische

CA::Data representation

- Important basics
- ASCII
- Unicode and UTF
- Data types: Numbers



Important basics - numeral systems

How much do you still know* about numeral systems?

low

current knowledge

high

^{*}Use a **stamp** for your estimate.

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Important basics









Which numeral systems do you know?

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Important basics

Numeral systems

■ DEC: 0, 1, ..., 9;

BIN: 0, 1;

■ HEX: 0. 1. 9. A. B. F: e.g.: 0x123

Conversion between:

■ HEX <-> DEC

BIN <-> HEX

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Important basics

Numeral systems

■ DEC: 0, 1, ..., 9;

BIN: 0, 1;

_ _ _ ,

e.g.: 291

e.g.: 100100011

e.g.: 0x123

Conversion between:

HEX <-> DEC

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- HEX <-> DEC
- BTN <-> HEX

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e.g.: 100100011

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DIN. 0, 1,

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Conversion between:

■ HEX <-> DEC

■ BIN <-> HEX

0000

1001 1010 1011

1100

1101

1111

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Important basics - hints

DEC	\rightarrow
0	→
\wedge	- /
•	
:	
g	
V P	
$\Lambda\Lambda$	
12	
13	
14	
15	



Important basics - short exercise 1/2

Convert HEX: OxCOFE to BIN.

1100 0000 1111 1110

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Important basics - short exercise 2/2

Convert BIN: 1100 0000 1101 1110 to HEX.











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Questions?

All right? \Rightarrow

V

Question? \Rightarrow

*

and use chat

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Binary system

Why is the binary (dual) system used in computer science?

Binary system for digits and characters

- Technically easy to realise (0/1)
- Well understood theoretical basis
 - Boolean algebra
 - Formal logic

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Subtraction is reduced to addition

Idea: Complementation and addition of the complement

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Subtraction is reduced to addition

Idea: Complementation and addition of the complement

```
1 11: -> 01011

2 6: -> 00110

3 complement of 6: 11001

4 + 1

5 -----

6 11010

7 addition of 11 + (-6):

8 11: 01011

9 -6: 11010

10 X00101 =
```

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Subtraction is reduced to addition

Idea: Complementation and addition of the complement

```
1 11: -> 01011
2 6: -> 00110
3 complement of 6: 11001
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9 -6: 11010
```

Computer Science



Subtraction is reduced to addition

Idea: Complementation and addition of the complement

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Subtraction is reduced to addition

Idea: Complementation and addition of the complement

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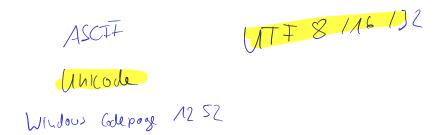
10 ------

11 X00101 => 5
```

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Codes



Which codes for characters do you know?

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ASCII (American Standard Code for Information Interchange)

<u>Dec</u>	H	x Oct	Char	,	Dec	Нх	Oct	Html	Chr	Dec	Нх	Oct	Html	Chr	Dec	Нх	Oct	Html Ch	<u>1r</u>
0	0	000	NUL	(null)	32	20	040		Space	64	40	100	۵#64;	0	96	60	140	`	8
1	1	001	SOH	(start of heading)	33	21	041	¢#33;	1	65	41	101	A ;	A	97	61	141	@#97;	a
2				(start of text)	34	22	042	a#34;	**	66	42	102	B	В	98	62	142	b	b
3	3	003	ETX	(end of text)	35	23	043	a#35;	#	67	43	103	a#67;	С	99	63	143	6#99;	C
4	4	004	EOT	(end of transmission)	36	24	044	4#36;	ş	68	44	104	4#68;	D	100	64	144	@#100;	d
5	5	005	ENQ	(enquiry)	37	25	045	6#37;	*	69	45	105	4#69;	E	101	65	145	e	e
6	6	006	ACK	(acknowledge)	38	26	046	6#38;	6	70	46	106	a#70;	F	102	66	146	6#102;	f
7	- 7	007	BEL	(bell)	39	27	047	4#39;	1	71	47	107	@#71;	G	103	67	147	a#103;	g
8	8	010	BS	(backspace)	40	28	050	¢#40;	(72	48	110	6#72;	H	104	68	150	a#104;	h
9	9	011	TAB	(horizontal tab)	41	29	051	@#41;)	73	49	111	6#73;	I	105	69	151	i	i
10	A	012	LF	(NL line feed, new line)	42	2A	052	6#42;	*				a#74;					@#106;	
11	В	013	VT	(vertical tab)	43	2B	053	a#43;	+	75	4B	113	G#75;	K	107	6B	153	a#107;	k
12	С	014	FF	(NP form feed, new page)				a#44;		76	40	114	a#76;	L	108	6C	154	@#108;	1
13	D	015	CR	(carriage return)	45	2D	055	a#45;	F 1	77	4D	115	G#77;	M	109	6D	155	@#109;	m
14	E	016	SO	(shift out)	46	2E	056	a#46;	-	78	4E	116	a#78;	N	110	6E	156	@#110;	n
15	F	017	SI	(shift in)	47	2F	057	6#47;	/	79	4F	117	a#79;	0	111	6F	157	o	0
16	10	020	DLE	(data link escape)	48	30	060	a#48;	0				4#80;					@#112;	
17	11	021	DC1	(device control 1)	49	31	061	a#49;	1	81	51	121	Q	Q	113	71	161	q	q
18	12	022	DC2	(device control 2)	50	32	062	a#50;	2	82	52	122	4#82;	R	114	72	162	@#114;	r
19	13	023	DC3	(device control 3)	51	33	063	3	3	83	53	123	4#83;	S	115	73	163	s	8
20	14	024	DC4	(device control 4)				a#52;		84	54	124	a#84;	Т	116	74	164	@#116;	t
21	15	025	NAK	(negative acknowledge)	53	35	065	4#53;	5	85	55	125	6#85 ;	U	117	75	165	u	u
22	16	026	SYN	(synchronous idle)				¢#54;		86	56	126	4#86 ;	٧	118	76	166	@#118;	V
23	17	027	ETB	(end of trans. block)	55	37	067	<u>@</u> #55;	7	87	57	127	a#87;	W	119	77	167	@#119;	\mathbf{w}
24	18	030	CAN	(cancel)	56	38	070	4#56;	8	88	58	130	6#88;	Х				@#120;	
25	19	031	EM	(end of medium)	57	39	071	<u>6#57;</u>	9	89	59	131	6#89 ;	Y	121	79	171	@#121;	Y
26	1A	032	SUB	(substitute)	58	ЗА	072	4#58;	:	90	5A	132	a#90;	Z	122	7A	172	@#122;	Z
27	1B	033	ESC	(escape)	59	ЗВ	073	<u>@</u> #59;	3	91	5B	133	@#91;	[123	7B	173	@#123;	-{
28	10	034	FS	(file separator)	60	3С	074	4#60;	<	92	5C	134	@#92;	A.	124	7C	174	@#124;	
29	1D	035	GS	(group separator)	61	ЗD	075	=	=	93	5D	135	@#93;]	125	7D	175	}	}
30	1E	036	RS	(record separator)	62	ЗE	076	>	>	94	5E	136	a#94;					4#126;	
31	1F	037	US	(unit separator)				4#63;	2	95	5F	137	@#95;	_	127	7F	177		DEI
. 1/			C C	0001		$\sim \Lambda$	\cap I	D - 1		Land 1			_		-				

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Extended ASCII codes

128	Ç	144	É	160	á	176		192	L	208	Ш	224	α	240	=
129	ü	145	æ	161	í	177	•••••	193	Т.	209	₹	225	ß	241	±
130	é	146	Æ	162	ó	178		194	т	210	π	226	Γ	242	≥
131	â	147	ô	163	ú	179	1	195	F	211	Ш	227	π	243	≤
132	ä	148	ö	164	ñ	180	4	196	- (212	F	228	Σ	244	ſ
133	à	149	ò	165	Ñ	181	4	197	+	213	F	229	σ	245	J
134	å	150	û	166	•	182	1	198	F	214	П	230	μ	246	÷
135	ç	151	ù	167	•	183	П	199	╟	215	#	231	τ	247	æ
136	ê	152	Ÿ	168	3	184	7	200	L	216	+	232	Φ	248	۰
137	ë	153	Ö	169	-	185	4	201	F	217	J	233	•	249	
138	è	154	Ü	170	4	186		202	<u>JL</u>	218	Г	234	Ω	250	
139	ï	155	¢	171	1/2	187	ล	203	ī	219		235	δ	251	V
140	î	156	£	172	1/4	188	ī	204	ŀ	220		236	00	252	n
141	ì	157	¥	173	i	189	Ш	205	=	221	1	237	ф	253	2
142	Ä	158	R.	174	«	190	4	206	#	222	1	238	ε	254	
143	Å	159	f	175	»	191	7	207	<u>_</u>	223	•	239	\Diamond	255	

Source: www.LookupTables.com

[source: asciitable.com]



ASCII

ASCII - American Standard Code for Information Interchange

Any problems with ASCII?



- International standard (ISO 10646)
- For every character one code
- In the long term: A digital code is defined for each meaningful character or text element of all known cultures, countries/languages, and character systems.
- Is constantly extended
- http://www.unicode.org



Unicode

International standard (ISO 10646)

Binary system

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Unicode

Character range:

first code U+00 0000 last code U+10 FFFF

Character sets Name Unit

Calculation #chars first

ast

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Unicode

Character range:

first code U+00 0000 last code U+10 FFFF

Character sets Name Unit

UCS-2 16 Bit

 2^{16}

Calculation #chars first

65536

U+0000

last

U+FFFF

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Unicode

Character range:

first code U+00 0000 last code U+10 FFFF

Characte	r sots
Characte	1 3613

Calculation #chars first last Unit Name 2^{16} UCS-2 16 Bit U+0000 65536 U+FFFF UCS-4 17 Planes $17 * 2^{16}$ 1114112 U+00 0000 U+10 FFFF

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Unicode

Character range:

first code U+00 0000 last code U+10 FFFF

Character sets

Name Unit		n #chars	first	last
UCS-2 16 Bit	2^{16}	65536	U+0000	U+FFFF
UCS-4 17 Plan	nes $17 * 2^{16}$	1114112	U+00 000	00 U+10 FFFF

Examples:

Unicode Full number Character

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Unicode

Character range:

first code U+00 0000

last code U+10 FFFF

Character sets

Name Unit Calculation #chars first last

 2^{16} UCS-2 16 Bit U+0000 65536 U+FFFF

UCS-4 17 Planes $17 * 2^{16}$ 1114112 U+00 0000 U+10 FFFF

Examples:

Unicode Full number Character

00 0041 U+0041

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Unicode

Character range:

first code U+00 0000

last code U+10 FFFF

Character sets

Name Unit Calculation #chars first last

UCS-2 16 Bit 2¹⁶ 65536 U+0000 U+FFFF

UCS-4 17 Planes $17 * 2^{16}$ 1114112 U+00 0000 U+10 FFFF

Examples:

Unicode Full number Character

U+0041 00 0041

U+1F600 01 F600



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Unicode 10.0 - Planes

Plane 0 00 0000-00 FFFF BMP Basic Multilungual Plane	Plane 1 01 0000-01 FFFF SMP Supplementary Multilungual Plane	Plane 2 02 0000-02 FFFF SIP Supplementary Ideographic Plane	Plane 3 03 0000-03 FFFF unassigned	Plane 4 04 0000-04 FFFF unassigned
Plane 5 05 0000-05 FFFF unassigned	Plane 6 06 0000-06 FFFF unassigned	Plane 7 07 0000-07 FFFF unassigned	Plane 8 08 0000-08 FFFF unassigned	Plane 9 09 0000-09 FFFF unassigned
Plane 10 OA 0000-0A FFFF unassigned	Plane 11 OB 0000-0B FFFF unassigned	Plane 12 oc 0000-oc FFFF unassigned	Plane 13 OD 0000-0D FFFF unassigned	Plane 14 OE 0000-0E FFFF SSP Supplementary Special-purpose Plane
Plane 15 OF 0000-OF FFFF SPUA-A Supplementary Private Use Area planes	Plane 16 10 0000-10 FFFF SPUA-A Supplementary Private Use Area planes			





Unicode

Enter unicode characters

OS Program

Keyboard shortcut

More shortcuts: wikipedia.org

*must be enabled as input source

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Unicode

Enter unicode characters

OS Program

Linux Terminal, xed, LibreOffice

Keyboard shortcut

CTRL+SHIFT+U + HEX Number

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^{*}must be enabled as input source

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Unicode

Enter unicode characters

OS Program Keyboard shortcut
Linux Terminal, xed, LibreOffice CTRL+SHIFT+U + HEX Number
Windows Microsoft Word, Excel, WordPad HEX Number + ALT+C

More shortcuts: wikipedia.org

^{*}must be enabled as input source

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Unicode

Enter unicode characters

OS	Program	Key	board
Linux	Terminal, xed, LibreOffice	CTRI	L+SHI
Windows	Microsoft Word, Excel, WordPad	HEX	Numb
macOS*	Console, Text	ALT	+ HE

More shortcuts: wikipedia.org

Keyboard shortcut

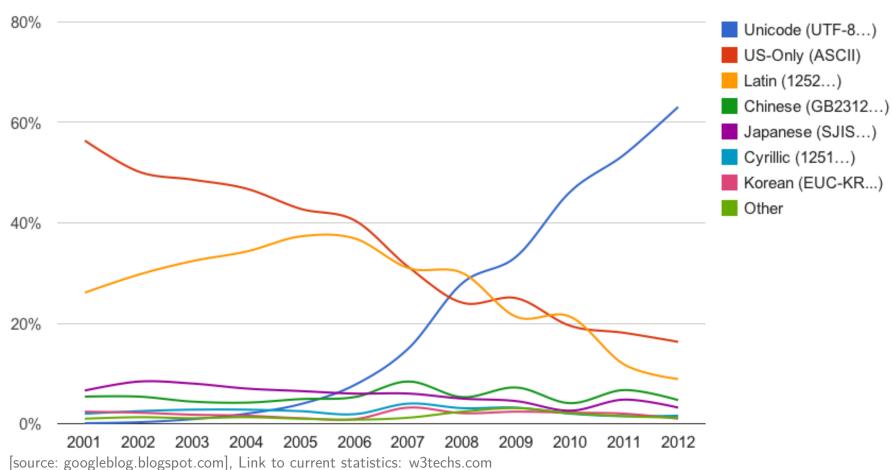
CTRL+SHIFT+U + HEX Number
HEX Number + ALT+C ((() ord)
ALT + HEX Number → ALT+×

^{*}must be enabled as input source

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Unicode usage



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Questions?

All right? \Rightarrow

V

Question? \Rightarrow

*

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Character set vs. character encoding?

Unicode vs UTF

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Character set vs. character encoding?

Unicode vs UTF

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UTF - Unicode Transformation Format

UTF maps all unicode code points to a unique sequence of bytes.

Used for

- Store information into files, databases, ...
- Transfer data (websites, e-mail, ...)

Choice depends on

- Storage space
- Source code compatibility
- Interoperability with other systems
- Runtime for encoding/decoding

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UTF - Unicode Transformation Format

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UTF - Unicode Transformation Format

Overview of UTF encodings

Encoding Bits Length

Common use

UTF-8 8-bit Variable length: 1 to 4 bytes Internet, Linux

16-bit Variable length: 2 or 4 bytes Qt, Java, Tcl UTF-16

UTF-32 32-bit Fixed length: 4 bytes

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UTF-8

UTF-8 length

Number	Bits for					
of bytes	code point		Unicode rai	nge	Comment	
1	7		0 - 00	007F	Compatible with ASCII	Plan 6
2	11		80 - 00	O7FF)
3	16		800 - 00	FFFF)
4	21	1	0000 - 10	FFFF	} F	1(au 1 - 16

UTF-8 encoding details

Unicode range					
			007F		
			O7FF		

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UTF-8

UTF-8 length

	Bits for code point		Unicod	e rai	nge	Comment
	_				0	
1	7		0 -	00	007F	Compatible with ASCII
2	11		80 -	00	O7FF	
3	16		800 -	00	FFFF	
4	21	1	0000 -	10	FFFF	

UTF-8 encoding details

	Unicode range			Byte 1	Byte 2	Byte 3	Byte 4
	0 -	00	007F	0xxxxxxx			
	80 -	00	O7FF	110xxxxx	10xxxxxx		
	800 -	00	FFFF	1110xxxx	10xxxxxx	10xxxxxx	
1	0000 -	10	FFFF	11110xxx	10xxxxxx	10xxxxxx	10xxxxxx

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UTF-8 - example

Encode the "ü" into UTF-8!

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UTF-8 - example

Encode the "ü" into UTF-8!

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UTF-8 - example

Encode the "ü" into UTF-8!

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Summary

UTF-8 - example

Encode the "ü" into UTF-8!

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Question? \Rightarrow

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UTF-16

UTF-16 length

Number Bits for of bytes code point

16

20

Unicode range

0 - 00 FFFF

01 0000 - 10 FFFF subtraction required:

Comment

U+XXXXXXX - 0x10000

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UTF-16

UTF-16 length

Number Bits for of bytes code point Unicode range Comment

2 16 0 - 00 FFFF

4 20 01 0000 - 10 FFFF subtraction required:
U+XXXXXXX - 0x10000

UTF-16 encoding details

Unicode range Byte 1 Byte 2 Byte 3 Byte 4

0 - 00 FFFF xxxxxxxxx xxxxxxxx

High surrogate Low surrogate

01 0000 - 10 FFFF 110110xx xxxxxxxx 110111xx xxxxxxxx

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UTF-16 - example

Encode the "(U+1F600) into UTF-16!

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UTF-16 - example

Encode the "—" (U+1F600) into UTF-16!

```
1 4 byte variant and therefore correction required:
```

```
2 \text{ } 0x1F600 - 0x10000 = 0xF600
```

```
4 F 6 0 0
5 1111 0110 0000 0000
```

```
7 In UTF-16
```

8 High surrogate Low surrogate 9 11011000 00111101 11011110 00000000

10 D 8 3 D D E 0

-> 0xD83DDE00

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UTF-16 - example

Encode the "—" (U+1F600) into UTF-16!

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UTF-16 - example

Encode the "—" (U+1F600) into UTF-16!

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Questions?

All right? \Rightarrow



Question? \Rightarrow



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UTF-32

UTF-32 length

Number Bits for

of bytes code point Unicode range Comment

4 21 00 0000 - 10 FFFF directly representable

UTF-32 encoding details

Unicode range Byte 1 Byte 2 Byte 3 Byte 4

0 - 10 FFFF 0000000 000xxxxx xxxxxxxx xxxxxxx

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UTF-32

UTF-32 length

Number Bits for

of bytes code point Unicode range Comment

4 21 00 0000 - 10 FFFF directly representable

UTF-32 encoding details

Unicode range Byte 1 Byte 2 Byte 3 Byte 4

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UTF-32 - example

Encode the "—" (U+1F600) into UTF-32!

```
2 0x1F600

3

4 1 F 6 0 0

5 0001 1111 0110 0000 0000

6

7 In UTF-32:
8 00000000 0000001 11110110 00000000
9 0 0 1 F 6 0 0
```

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UTF-32 - example

Encode the "—" (U+1F600) into UTF-32!

- only the 4 byte variant exists
- 2 0x1F600

```
4 1 F 6 0 0
```

- 5 0001 1111 0110 0000 0000
- 7 In UTF-32
- 8 00000000 00000001 11110110 00000000
- 9 0 0 0 1 F 6 0 0

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UTF-32 - example

Encode the "—" (U+1F600) into UTF-32!

```
1 Only the 4 byte variant exists
```

2 0x1F600

4 1 F 6 0 0

5 0001 1111 0110 0000 0000

7 In UTF-32

8 00000000 00000001 11110110 00000000

8 00000000 00000001 11110110 00000000

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UTF-32 - example

Encode the "—" (U+1F600) into UTF-32!

-> 0x0001F600

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Questions?

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Question? \Rightarrow

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Numbers

Type

Integer

Floating point – binary float, double, ...

Floating point – decimal decimal32, decimal64, ...

Fixed point – binary Fixed point – decimal Common data type

unsigned int, int, ...

Often not well integrated Mostly in software Often not well integrated Mostly in software

Realisation

Hardware: ALU

Hardware: FPU

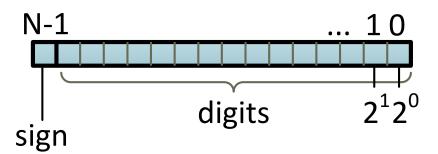
Mostly in software

Computer Science



Integer (signed)

Example: short int



Positive number: The weight for position i is 2^i

Negative number: The sign is interpreted as -2^N

Example short int: Minimum: -32768; Maximum: 32767

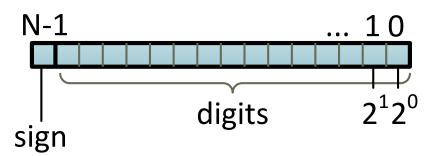
imits: http://www.cplusplus.com/reference/climits

Computer Science



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Floating point – binary

Usually scientific numbers with mantissa and exponent.

Requires hardware support (FPU - floating point unit).

Format: $x = m \cdot B^e$ (m = mantissa, B = basis, and e = exponent)

Examples:

C: float x;

Ada: x: float

Computer Science



Floating point – binary

Floating point binary formats are defined in the IEEE Standard for Floating-Point Arithmetic (IEEE 754).

			Number		
	Name	Common name	of bits	Characteristic	Mantissa
	binary16	Half precision	16	5 bits; $c = e + 15$	10 bits
float	binary32	Single precision	32	8 bits; $c = e + 127$	23 bits
double	binary64	Double precision	64	11 bits; $c = e + 1023$	52 bits
Long	binary128	Quadruple precision	128	15 bits; $c = e + 16383$	112 bits
(Coes)	binary256	Octuple precision	256	19 bits; $c = e + 262143$	236 bits

IEEE 754 on Wikipedia: https://en.wikipedia.org/wiki/IEEE_754



Floating point – binary

Example: float (single precision)



Exponent $-126, \ldots, +127$ Exponent is represented via the characteristic

Characteristic c = e + 127

Mantissa $1 \le m < B$ Is normalised in the binary system

1.MMM...M

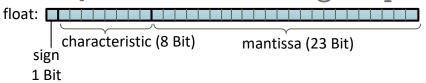
Advantage: 1 doesn't have to be saved

Computer Science



Floating point – binary

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Computer Science



Floating point – binary

Convert the decimal number 1.75 into the binary32 (float) representation.

Computer Science



Floating point – binary

Convert the decimal number 1.75 into the binary32 (float) representation.

```
1.75 -> binary:
2 01.11000...0 -> it has already the required form
                   of 1.MMM...M (=> e=0)
```

Computer Science



Floating point – binary

Convert the decimal number 1.75 into the binary32 (float) representation.

Computer Science



Floating point – binary

Convert the decimal number 1.75 into the binary32 (float) representation.

Prof. Dr. Florian Künzner, SoSe 2021

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Floating point – binary

Convert the decimal number 1.75 into the binary32 (float) representation.

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Floating point – binary

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Floating point – binary

Nr.	Code	different	equal
1	36.2 != 36.2		

Computer Science



Floating point – binary

Nr.	Code	different	equal
1	36.2 != 36.2		
2	0.362 * 100.0 != 36.2		

Computer Science



Floating point – binary

Nr.	Code	different	equal
1	36.2 != 36.2		
2	0.362 * 100.0 != 36.2		
3	0.362 * (100.0 / 100.0) != 0.362		

Computer Science



Summary

Floating point – binary

Nr.	Code	different	equal
1	36.2 != 36.2		
2	0.362 * 100.0 != 36.2		
3	0.362 * (100.0 / 100.0) != 0.362		
4	(0.362 * 100.0) / 100.0 != 0.362		

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Questions?

All right? \Rightarrow

Question? \Rightarrow

and use chat

speak after I ask you to

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Floating point – decimal

Floating point decimal formats are defined in the IEEE Standard for Floating-Point Arithmetic (IEEE 754).

Format: $x = (-1)^{\text{signbit}} \times 10^{\text{exponentbits}_2 - 101_{10}} \times \text{truesignificand}_{10}$

Number of

	decimal digits	Exponent min.	Exponent max.
decimal32			
decimal64			
decimal128			

IEEE 754 on Wikipedia: https://en.wikipedia.org/wiki/IEEE 754

- Possible in gnu C with _Decimal32, _Decimal64, and _Decimal128
- Example C: _Decimal32 x = 0.1df;
- Possible in gnu C++ with decimal32, decimal64, and decimal128
- Example C++: std::decimal::decimal32 x(0.1);

More details on the format (on Wikipedia): https://en.wikipedia.org/wiki/Decimal32_floating-point_format_

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decimal64	16	-383	+384

decimal128 34 -6143 +6144

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/ Jana: Big Deciral

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Questions?

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4

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Fixed point

Fixed point numbers have a fixed imaginary point that is not moved.

Usage:

- Areas where rounding errors must be avoided (e.g. commercial applications)
- If no floating point hardware (FPU) is available (e.g. in embedded systems)
- Devices use the numbers in this format anyway (e.g. analog/digital converter)

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Two variants:

Type Usage

Binary fixed point technical

Decimal fixed point economical