A.2 R AND S-PLUS EXAMPLES

R is free software maintained and regularly updated by many volunteers. It is an open-source version using the S programming language, and many S-Plus functions also work in R. See http://www.r-project.org, at which site you can download R and find various documentation. Our discussion in this Appendix refers to R version 2.13.0.

Dr. Laura Thompson has prepared an excellent, detailed manual on the use of R and S-Plus to conduct the analyses shown in the second edition of *Categorical Data Analysis*. You can access this at

https://home.comcast.net/~lthompson221/Splusdiscrete2.pdf

A good introductory resource about R functions for various basic types of categorical data analyses is material prepared by Dr. Brett Presnell at the University of Florida. The sites

www.stat.ufl.edu/~presnell/Courses/sta4504-2000sp/R and in particular,

www.stat.ufl.edu/~presnell/Courses/sta4504-2000sp/R/R-CDA.pdf

have details for an introductory course on categorical data analysis with many of the examples from my books.

Another useful resource is the website of Dr. Chris Bilder

statistics.unl.edu/faculty/bilder/stat875

where the link to R has examples of the use of R for most chapters of my introductory text, An Introduction to Categorical Data Analysis. The link to Schedule at Bilder's website for Statistics 875 at the University of Nebraska has notes for a course on this topic following that text as well as R code and output imbedded within the notes. Thanks to Dr. Bilder for this outstanding resource.

Another good source of examples for Splus and R is Dr. Pat Altham's at Cambridge, UK,

www.statslab.cam.ac.uk/~pat

An upcoming excellent resource of the use of R for contingency table analysis is a soon-to-appear book by Dr. Maria Kateri. That text also provides functions for many methods not readily available in R.

Texts that contain examples of the use of R for various categorical data methods include *Statistical Modelling in R* by M. Aitkin, B. Francis, J. Hinde, and R. Darnell (Oxford 2009), *Modern Applied Statistics With S-PLUS*, 4th ed., by W. N. Venables and B. D. Ripley (Springer, 2010), *Analyzing Medical Data Using S-PLUS* by B. Everitt and S. Rabe-Hesketh (Springer, 2001), *Regression Modeling Strategies* by F. E. Harrell (Springer, 2001), and *Bayesian Computation with R* by J. Albert (Springer, 2009).

Chapter 1: Introduction

Univariate binomial and multinomial inference

The function dbinom can generate binomial probabilities, for example, dbinom(6, 10, 0.5) gives the probability of 6 successes in 10 trials with "probability of success" parameter $\pi = 0.50$. The function pbinom(6, 10, 0.5) would give the corresponding cumulative probability of 6 or fewer successes.

The function prop.test gives the Pearson (score) test and score confidence interval for a binomial proportion, for example, prop.test(6, 10, p=.5, correct=FALSE), where "correct=FALSE" turns off the continuity correction, which is the default. The function binom.test gives a small-sample binomial test, for example binom.test(8, 12, p=0.5, alternative = c("two.sided")) gives a two-sided test of H_0 : $\pi = 0.50$ with 8 successes in 12 trials.

The table function constructs contingency tables.

The function *chisq.test* can perform the Pearson chi-squared test of goodness-of-fit of a set of multinomial probabilities. For example, with 3 categories and hypothesized values (0.4, 0.3, 0.3) and observed counts (12, 8, 10),

The argument "simulate.p.value = TRUE" requests simulation of the exact small-sample test of goodness of fit, with B replicates. So, the second run above uses simulation of 10,000 multinomials with the hypothesized probabilities and finds the sample proportion of them having X^2 value at least as large as the observed value of 0.2222.

For special R functions for confidence intervals for a binomial parameter, see www.stat.ufl.edu/~aa/cda/R/one-sample/R1/index.html

The confidence intervals include the score (Wilson) CI, Blaker's exact CI, the small-sample Clopper-Pearson interval and its mid-P adaptation discussed in Section 16.6 of the textbook, and the Agresti–Coull CI and its add-4 special case.

Bayesian inference

See logitnorm.r-forge.r-project.org/ for utilities such as a quantile function for the logit-normal distribution.

The hpd function in the TeachingDemos library can construct HPD intervals from a posterior distribution. The package hdrcde is a more sophisticated package for such methods. For the informative analysis of the vegetarians example at the end of Section 1.6.4:

```
library("TeachingDemos")
y <- 0; n <- 25
a1 <- 3.6; a2 <- 41.4
a <- a1 + y; b <- a2 + n
h <- hpd(qbeta, shape1=a, shape2=b)</pre>
```

Chapters 2–3: Two-Way Contingency Tables

For creating mosaic plots in R, see www.datavis.ca and also the *mosaic* functions in the *vcd* and *vcdExtra* libraries; see Michael Friendly's tutorial at cran.us.r-project.org/web/packages/vcdExtra/vignettes/vcd-tutorial.pdf, which also is useful for basic descriptive and inferential statistics for contingency tables. To construct a mosaic plot for the data in Table 3.2, one can enter

```
> x<- c(9,8,27,8,47,236,23,39,88,49,179,706,28,48,89,19,104,293)
> data <- matrix(x, nrow=3,ncol=6, byrow=TRUE)
> dimnames(data) = list(Degree=c("< HS","HS","College"),Belief=c("1","2","3","4","5","6"))
> install.packages("vcdExtra")
> library("vcdExtra")
> StdResid <- c(-0.4,-2.2,-1.4,-1.5,-1.3,3.6,-2.5,-2.6,-3.3,1.8,0.0,3.4,3.1,4.7,4.8,-0.8,1.1,-6.7)
> StdResid <- matrix(StdResid,nrow=3,ncol=6,byrow=TRUE)
> mosaic(data,residuals = StdResid, gp=shading_Friendly)
```

Chi-squared and Fisher's exact test; Residuals

The function *chisq.test* also can perform the Pearson chi-squared test of independence in a two-way contingency table. For example, for Table 3.2 of the text, using also the *stdres* component for providing standardized residuals,

```
[1,] -0.368577 -2.227511 -1.418621 -1.481383 -1.3349600 3.590075 [2,] -2.504627 -2.635335 -3.346628 1.832792 0.0169276 3.382637 [3,] 3.051857 4.724326 4.839597 -0.792912 1.0794638 -6.665195
```

Likewise, replacing the stdres component by expected would generate the expected frequency estimates. As shown above, you can simulate the exact conditional distribution to estimate the P-value whenever the chi-squared asymptotic approximation is suspect.

Here is code to obtain the profile likelihood confidence interval for the odds ratio for Table 3.1 on seat-belt use and traffic accidents (using the fact that the log odds ratio is the parameter in a simple logistic model):

```
ratio is the parameter in a simple logistic model):
> yes <- c(54,25)
> n <- c(10379,51815)
> x < -c(1,0)
> fit <- glm(yes/n ~ x, weights=n, family=binomial(link=logit))</pre>
> summary(fit)
Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) -7.6361 0.2000 -38.17 <2e-16 ***
              2.3827
                          0.2421
                                    9.84
                                           <2e-16 ***
х
> confint(fit)
Waiting for profiling to be done...
                       97.5 %
                2.5 %
(Intercept) -8.055554 -7.268025
             1.919634 2.873473
> \exp(1.919634); \exp(2.873473)
[1] 6.818462
[1] 17.69838
   The function fisher.test performs Fisher's exact test. For example, for the tea
tasting data of Table 3.9 in the text,
> tea <- matrix(c(3,1,1,3),ncol=2,byrow=TRUE)</pre>
> fisher.test(tea)
Fisher's Exact Test for Count Data
data: tea
p-value = 0.4857
alternative hypothesis: true odds ratio is not equal to 1
95 percent confidence interval:
   0.2117329 621.9337505
sample estimates:
odds ratio
  6.408309
> fisher.test(tea,alternative="greater")
```

Fisher's Exact Test for Count Data

data: tea p-value = 0.2429

alternative hypothesis: true odds ratio is greater than 1

The P-value is the sum of probabilities of tables with the given margins that have probability no greater than the observed table. The output also shows the conditional ML estimate of the odds ratio (see Sec. 16.6.4) and a corresponding exact confidence interval based on noncentral hypergeometric probabilities. Use fisher.test(tea, alternative = "greater") for the one-sided test. For an $I \times J$ table called "table," using

```
> fisher.test(table, simulate.p.value=TRUE, B=10000)
```

generates Monte Carlo simulation with B replicates to estimate the exact P-value based on the exact conditional multiple hypergeometric distribution obtained by conditioning on all row and column marginal totals.

On page 10 of

www.stat.ufl.edu/~presnell/Courses/sta4504-2000sp/R/R-CDA.pdf

Brett Presnell shows a simple function for finding also the likelihood-ratio statistic G^2 .

Confidence intervals for association measures

For a 2×2 table, the function *prop.test* provides the Wald confidence interval for the difference of proportions, where one uses the option correct=FALSE to suppress the continuity correction.

For parameters comparing two binomial proportions such as the difference of proportions, relative risk, and odds ratio, a good general-purpose method for constructing confidence intervals is to invert the score test. Such intervals are not available in the standard software packages. See

```
www.stat.ufl.edu/~aa/cda/R/two-sample/R2/index.html
```

for R functions for confidence intervals comparing two proportions with independent samples (difference of proportions, relative risk, odds ratio). The site

```
www.stat.ufl.edu/~aa/cda/R/matched/R2_matched/index.html
```

has R functions for confidence intervals comparing two proportions with dependent samples. Most of these were written by my former graduate student, Yongyi Min, who also prepared the Bayesian intervals mentioned below. Please quote this site if you use one of these R functions for confidence intervals for association parameters. We believe these functions are dependable, but no guarantees or support are available, so use them at your own risk. Note that the score CI for the difference of proportions is based on the formula on p. 79 of the text based on the work of Mee (1984). The slightly different score interval suggested by Miettinen and Nurminen (1985) incorporates a bias correction factor in the variance of $(n_1 + n_2)/(n_1 + n_2 - 1)$ that can result in even better coverage properties according to an article by Newcombe and Nurminen (2011, Communications in Statistics, 40: 1271–1282). Bernhard Klingenberg has written an R function for both of these score intervals, with the Miettinen and Nurminen as the

default. For details, go to http://sites.williams.edu/bklingen. Here is Bernhard's code, with examples:

```
# from Bernhard Klingenberg
# returns score test statistic, p-value and restricted MLEs for diff
of prop p1 - p2:
score.test <- function(delta.null, y,n, alternative = "two.sided",</pre>
MN=TRUE) {
  N=sum(n)
  C=sum(y)
  L3=N
  L2=(n[1]+2*n[2])*delta.null-N-C
  L1=(n[2]*delta.null-N-2*y[2])*delta.null+C
  L0=y[2]*delta.null*(1-delta.null)
  c=L2^3/(3*L3)^3 - L1*L2/(6*L3^2) + L0/(2*L3)
  b=ifelse(c>=0,1,-1)*sqrt(L2^2/(3*L3)^2 - L1/(3*L3))
  d \leftarrow min(c/b^3,1)
  d \leftarrow max(d, -1)
  a=(3.14159265358979+acos(d))/3
  p2=2*b*cos(a)-L2/(3*L3)
 p2 = max(p2, 0)
 p2 = min(p2,1)
  p1=p2+delta.null
  p1 = max(p1, 0)
  p1 = min(p1,1)
  se0 \leftarrow sqrt(p1*(1 - p1)/n[1] + p2*(1 - p2)/n[2])
    if (!MN) z=(y[1]/n[1]-y[2]/n[2]-delta.null)/se0 #Mee
  else z=(y[1]/n[1]-y[2]/n[2]-delta.null)/(se0*N/(N-1)) #Mietinnen and
Nurminen
    if (se0 == 0){
  z = 0
  }
  pvalue <- switch(alternative,</pre>
                    "two.sided" = 1 - pchisq(z^2, df=1),
                    "less" = pnorm(z),
                    "greater" = pnorm(z, lower.tail = FALSE)
  return(list(test.stat = z, p.value = pvalue, p1.null = p1, p2.null =
p2))
}
#returns lower and upper score bounds for diff of prop p1 - p2:
score.int <- function(y,n,conflev=0.95, type="two.sided", MN=TRUE) {</pre>
  if (type=="two.sided") c=qnorm(1-(1-conflev)/2)^2 else
c=qnorm(conflev)^2
  delta1=(y[1]+1)/(n[1]+2) - (y[2]+1)/(n[2]+2) #starting point
  if (any(type=="lower",type=="two.sided")) {
    delta2 = -1
    while( abs(delta1-delta2)>10^(-6) ) {#Bisection for LB
      delta=(delta1+delta2)/2
```

```
z=score.test(delta,y,n, MN = MN)$test.stat^2
      if (z>c) delta2=delta else delta1=delta
   }
  }
  delta.LB=delta1
  delta1=(y[1]+1)/(n[1]+2) - (y[2]+1)/(n[2]+2) #starting point
  if (any(type=="upper",type=="two.sided")) {
    delta2=1;
    while( abs(delta1-delta2)>10^(-6) ) {#Bisection for UB
      delta=(delta1+delta2)/2
      z=score.test(delta,y,n, MN = MN)$test.stat^2
      if (z>c) delta2=delta else delta1=delta
   }
  }
  delta.UB=delta1
  return(switch(type,
                "lower"=delta.LB,
                "upper"=delta.UB,
                "two.sided"=cbind(delta.LB,delta.UB)
 ))
}
### Example:
> y <- c(10,5)
> n <- c(20,20)
> score.int(y,n)
        delta.LB delta.UB
[1,] -0.05793719 0.5161737
> score.int(y,n, MN=FALSE)
        delta.LB delta.UB
[1,] -0.05026568 0.5104669
> score.test(delta.null=0,y,n)
$test.stat
[1] 1.592168
$p.value
[1] 0.1113469
$p1.null
[1] 0.375
$p2.null
[1] 0.375
> score.test(delta.null=0,y,n, MN=FALSE)
$test.stat
[1] 1.632993
$p.value
[1] 0.1024704
$p1.null
[1] 0.375
$p2.null
[1] 0.375
```

For examples of using R to obtain $\min P$ confidence intervals for the odds ratio, see the link to Laura Thompson's manual at

https://home.comcast.net/~lthompson221/Splusdiscrete2.pdf.

Ralph Scherer at the Institute for Biometry in Hannover, Germany, has prepared a package *PropCIs* on CRAN incorporating many of these confidence interval functions for proportions and comparisons of proportions. It can be downloaded at

```
cran.r-project.org/web/packages/PropCIs/index.html
```

Fay (2010a) described an R package exact2x2 that constructs a small-sample confidence interval for the odds ratio by inverting the test using the P-value (mentioned in Section 16.6.1) that was suggested by Blaker (2000), which equals the minimum one-tail probability plus an attainable probability in the other tail that is as close as possible to, but not greater than, that one-tailed probability. See

```
journal.r-project.org/archive/2010-1/RJournal_2010-1_Fay.pdf
```

```
cran.r-project.org/web/packages/exact2x2/index.html
```

For example, for a 2×2 table called data, the command exact2x2(data, tsmethod = "blaker") provides an exact test using Blaker's P-value and the confidence interval based on inverting that test.

Euijung Ryu, a former PhD student of mine who is now at Mayo Clinic, has prepared R functions for various confidence intervals for the ordinal measure [P(Y1 > Y2) + (1/2)P(Y1 = Y2)] that is useful for comparing two multinomial distributions on an ordinal scale. See

```
www.stat.ufl.edu/~aa/cda/R/stochastic/ryu-stochastic-code.pdf
```

for the functions, including the Wald confidence interval as well as score, pseudoscore, and profile likelihood intervals that are computationally more complex and require using Joe Lang's mph.fit function (see below). Also, Euijung has prepared an R function for multiple comparisons of proportions with independent samples using simultaneous confidence intervals for the difference of proportions or the odds ratio, based on the Studentized-range inversion of score tests proposed by Agresti et al. (2008). See

```
www.stat.ufl.edu/~aa/cda/R/multcomp/ryu-simultaneous.pdf
```

Joseph Lang's mph.fit function just mentioned is a general purpose and very powerful function that can provide ML fitting of generalized loglinear models (Section 10.5.1) and other much more general "multinomial-Poisson homogeneous" models such as covered in Lang (2004, 2005). These include models that can be specified in terms of constraints of the form $h(\mu) = 0$, such as the marginal homogeneity model and the calf infection example in Section 1.5.6 of the text. For details, see

```
www.stat.uiowa.edu/~jblang/mph.fitting/index.htm
```

Joe has also prepared an R program, *ci.table*, for computing (among other things) score and likelihood-ratio-test-based (i.e., profile likelihood) intervals for contingency table parameters. See

www.stat.uiowa.edu/~jblang/ci.table.documentation/ci.table.examples.htm

Bayesian inference for two-way tables

Surveys of Bayesian inference using R were given by J. H. Park,

```
cran.r-project.org/web/views/Bayesian.html
and by Jim Albert,
```

```
bayes.bgsu.edu/bcwr
```

The latter is a website for the text $Bayesian\ Computation\ with\ R$ by Albert. It shows examples of some categorical data analyses, such as Bayesian inference for a 2×2 table, a Bayesian test of independence in a contingency table, and probit regression.

Yongyi Min has prepared some R functions for Bayesian confidence intervals for 2×2 tables using independent beta priors for two binomial parameters, for the difference of proportions, odds ratio, and relative risk. See

```
www.stat.ufl.edu/~aa/cda/R/bayes/index.html
```

These are evaluated and compared to score confidence intervals in Agresti and Min (2005).

Missing data

The ACD package can conduct some analyses of categorical data (e.g. loglinear models by ML, functions of count data using weighted least squares) when data are missing. See

```
cran.r-project.org/web/packages/ACD/ACD.pdf
```

Chapter 4: Generalized Linear Models

Generalized linear models can be fitted with the glm function:

```
{\tt stat.ethz.ch/R-manual/R-patched/library/stats/html/glm.html} \\ {\tt www.statmethods.net/advstats/glm.html}
```

That function can be used for such things as logistic regression, Poisson regression, and loglinear models.

Consider a binomial variate y based on n successes with explanatory variable x and a $N \times 2$ data matrix with columns consisting of the values of y and n-y. For example, for the logit link with the snoring data in Table 4.2 of the text, using scores (0, 2, 4, 5), showing also a residual analysis,

```
> snoring <- matrix(c(24,1355,35,603,21,192,30,224), ncol=2, byrow=TRUE)
> scores <- c(0,2,4,5)
> snoring.fit <- glm(snoring ~ scores, family=binomial(link=logit))
> summary(snoring.fit)

Call:
glm(formula = snoring ~ scores, family = binomial(link = logit))

Deviance Residuals:
    1    2    3    4
```

```
-0.8346
         1.2521
                 0.2758 -0.6845
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
0.39734
                      0.05001
                              7.945 1.94e-15 ***
scores
Signif. codes: 0 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 65.9045 on 3 degrees of freedom
Residual deviance: 2.8089
                         on 2 degrees of freedom
AIC: 27.061
Number of Fisher Scoring iterations: 4
> pearson <- summary.lm(snoring.fit)$residuals</pre>
                                              # Pearson residuals
> hat <- lm.influence(snoring.fit)$hat # hat or leverage values
> stand.resid <- pearson/sqrt(1 - hat) # standardized residuals
> cbind(scores, snoring, fitted(snoring.fit), pearson, stand.resid)
 scores
                             pearson stand.resid
      0 24 1355 0.02050742 -0.8131634 -1.6783847
1
      2 35 603 0.04429511 1.2968557
2
                                      1.5448873
      4 21 192 0.09305411 0.2781891
3
                                      0.3225535
4
      5 30
            224 0.13243885 -0.6736948 -1.1970179
```

For the identity link with data in the form of Bernoulli observations, use code such as

```
> fit <- glm(y ~ x, family=quasi(variance="mu(1-mu)"),start=c(0.5, 0))
> summary(fit, dispersion=1)
```

The fitting procedure will not converge if at some stage of the fitting process, probability estimates fall outside the permissible (0, 1) range.

The profile likelihood confidence interval is available with the *confint* function in R, which is applied to the model fit object. It is also available with the *profilelike.glm* function in the ProfileLikelihood library prepared by Leena Choi. See cran.r-project.org/web/packages/ProfileLikelihood/ProfileLikelihood.pdf.

The glm function can be used to fit Poisson loglinear models and counts and for rates. For negative binomial models, you can use the glm nh function in the MASS

```
rates. For negative binomial models, you can use the glm.nb function in the MASS library.
```

 $\verb|stat.ethz.ch/R-manual/R-patched/library/MASS/html/glm.nb.html|\\$

However, in the notation of Sec. 4.3.4, this function identifies the dispersion parameter (which it calls "theta") as k, not its reciprocal γ . Negative binomial regression can also be handled by Thomas Yee's VGAM package mentioned for Chapter 8 below and by the negbin function in the aod package:

cran.r-project.org/web/packages/aod/aod.pdf

To illustrate R for models for counts, for the data in Sec. 4.3 on numbers of satellites for a sample of horseshoe crabs (Note: The complete data set is in the Datasets link www.stat.ufl.edu/~aa/cda/data.html at this website),

```
> crabs <- read.table("crab.dat",header=T)</pre>
   color spine width satellites weight
      3
             3 28.3
                              8
                                  3050
 1
      4
             3 22.5
                              0
                                  1550
2
                              9
3
      2
            1 26.0
                                  2300
      4
                              0
 4
            3 24.8
                                  2100
5
       4
            3 26.0
                              4
                                  2600
6
             3 23.8
                                  2100
. . . .
              2 24.5
                                   2000
173
       3
                               0
> weight <- weight/1000 # weight in kilograms rather than grams
> fit <- glm(satellites ~ weight, family=poisson(link=log), data=crabs)
> summary(fit)
> library(MASS)
> fit.nb <- glm.nb(satell ~ weight, link=log)</pre>
> summary(fit.nb)
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
                        0.4048 -2.136 0.0327 *
(Intercept) -0.8647
weight2
              0.7603
                         0.1578 4.817 1.45e-06 ***
    Null deviance: 216.43 on 172 degrees of freedom
Residual deviance: 196.16 on 171 degrees of freedom
AIC: 754.64
              Theta: 0.931
          Std. Err.: 0.168
2 x log-likelihood: -748.644
```

The function *rstandard.glm* has a type argument that can be used to request standardized residuals. That is, you can type

```
> fit <- glm(... model formula, family, data, etc ...)
> rstandard(fit, type="pearson")
```

to get standardized Pearson residuals for a fitted GLM. Without the type argument, rstandard(fit) returns the standardized deviance residuals.

The *statmod* library at CRAN contains a function *glm.scoretest* that computes score test statistics for adding explanatory variables to a GLM.

Statistical Models in S by J. M. Chambers and T. J. Hastie (Wadsworth, Belmont, California, 1993, p. 227) showed the use of S-Plus in quasi-likelihood analyses using the quasi and make.family functions.

Following is an example of the analyses shown for the teratology data, including the quasi-likelihood approach:

```
# This borrows heavily from Laura Thompson's manual at
# https://home.comcast.net/~lthompson221/Splusdiscrete2.pdf
> rats <- read.table("teratology.dat", header = T)</pre>
> rats # Full data set of 58 litters at course website
  litter group n y
            1 10 1
1
       1
             1 11 4
2
       2
             1 12 9
3
       3
             4 6 0
57
      57
      58
             4 17 0
> rats$group <- as.factor(rats$group)</pre>
> fit.bin <- glm(y/n ~ group - 1, weights = n, data=rats, family=binomial)</pre>
> summary(fit.bin)
Coefficients:
                  # these are the sample logits
      Estimate Std. Error z value Pr(>|z|)
group1 1.1440 0.1292 8.855 < 2e-16 ***
                  0.3046 -7.153 8.51e-13 ***
group2 -2.1785
                  0.7196 -4.630 3.65e-06 ***
group3 -3.3322
                   0.4584 -6.514 7.33e-11 ***
group4 -2.9857
   Null deviance: 518.23 on 58 degrees of freedom
Residual deviance: 173.45 on 54 degrees of freedom
AIC: 252.92
> (pred <- unique(predict(fit.bin, type="response")))</pre>
[1] 0.75840979 0.10169492 0.03448276 0.04807692 # sample proportions
> (SE <- sqrt(pred*(1-pred)/tapply(rats$n,rats$group,sum)))</pre>
        1
             2
                            .3
0.02367106\ 0.02782406\ 0.02395891\ 0.02097744
                                                # SE's of proportions
> (X2 <- sum(resid(fit.bin, type="pearson")^2)) # Pearson stat.</pre>
[1] 154.707
> phi <- X2/(58 - 4)
                                          # estimate of phi for QL analysis
> phi
[1] 2.864945
> SE*sqrt(phi)
        1
                   2
                              3
0.04006599 0.04709542 0.04055320 0.03550674 # adjusted SE's for proportions
> fit.ql <- glm(y/n ~ group - 1, weights=n, data=rats, family=quasi(link=identity,
           variance="mu(1-mu)"),start=unique(predict(fit.bin,type="response")))
> summary(fit.ql) # This shows another way to get the QL results
```

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
                  0.04007 18.929
group1 0.75841
                                    <2e-16 ***
group2 0.10169
                  0.04710
                            2.159
                                    0.0353 *
group3 0.03448
                  0.04055
                           0.850
                                    0.3989
group4 0.04808
                  0.03551
                           1.354
                                    0.1814
```

(Dispersion parameter for quasi family taken to be 2.864945)

Chapters 5–7: Logistic Regression and Binary Response Analyses

Logistic Regression

Since logistic regression is a generalized linear model, it can be fitted with the glm function, as mentioned above.

If y is a binary variable (i.e., ungrouped binomial data with each n=1), the vector of y values (0 and 1) can be entered as the response variable. Following is an example with the horseshoe crab data as a data frame, declaring color to be a factor in order to set up indicator variables for it (which, by default, choose the first category as the baseline without its own indicator variable). (Note that the complete data set is in the Datasets link www.stat.ufl.edu/~aa/cda/data.html at this website.)

```
> crabs <- read.table("crabs.dat",header=TRUE)</pre>
> crabs
   color spine width satellites weight
      3
            3 28.3
                             8
                                 3050
 1
2
       4
            3 22.5
                                 1550
                              0
3
       2
            1 26.0
                                 2300
173
              2 24.5
                                   2000
> y <- ifelse(crabs$satellites > 0, 1, 0) # y = a binary indicator of satellites
> crabs$weight <- crabs$weight/1000 # weight in kilograms rather than grams
> fit <- glm(y ~ weight, family=binomial(link=logit), data=crabs)
> summary(fit)
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
(Intercept) -3.6947
                     0.8802 -4.198 2.70e-05 ***
             1.8151
                         0.3767
                                4.819 1.45e-06 ***
weight
    Null Deviance: 225.7585 on 172 degrees of freedom
Residual Deviance: 195.7371 on 171 degrees of freedom
AIC: 199.74
> crabs$color <- crabs$color - 1 # color now takes values 1,2,3,4
```

```
> crabs$color <- factor(crabs$color) # treat color as a factor
> fit2 <- glm(y ~ weight + color, family=binomial(link=logit), data=crabs)</pre>
> summary(fit2)
Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) -3.2572 1.1985 -2.718 0.00657 **
                         0.3888 4.354 1.34e-05 ***
weight
              1.6928
color2
              0.1448
                      0.7365 0.197 0.84410
             -0.1861
                          0.7750 -0.240 0.81019
color3
             -1.2694
                          0.8488 -1.495 0.13479
color4
(Dispersion Parameter for Binomial family taken to be 1 )
    Null Deviance: 225.7585 on 172 degrees of freedom
Residual Deviance: 188.5423 on 168 degrees of freedom
AIC: 198.54
   For grouped data, rather than defining the response as the set of success and failure
counts as was done in the Chapter 4 discussion above for the snoring data, one can
instead enter the response in the form y/n for y successes in n trials, entering the
number of trials as the weight. For example, again for the snoring data of Table 4.2,
> yes <- c(24,35,21,30)
> n <- c(1379,638,213,254)
> scores <- c(0,2,4,5)
> fit <- glm(yes/n ~ scores, weights=n, family=binomial(link=logit))</pre>
Coefficients:
(Intercept)
                  scores
    -3.8662
                  0.3973
Degrees of Freedom: 3 Total (i.e. Null); 2 Residual
Null Deviance:
Residual Deviance: 2.809
                                 AIC: 27.06
   For the AIDS and AZT use example:
> race <- c(1,1,0,0)
> azt <- c(1,0,1,0)
> symptoms < c(14,32,11,12)
> n <- c(107, 113,63,55)
> response <- matrix(c(symptoms, n-symptoms), ncol=2)</pre>
> fit <- glm(response ~ race + azt, family=binomial(link=logit))</pre>
```

> summary(fit)

Call:

```
glm(formula = response ~ race + azt, family = binomial(link = logit))
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
0.05548
                      0.28861
                               0.192 0.84755
azt
           -0.71946
                      0.27898 -2.579 0.00991 **
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 8.3499 on 3 degrees of freedom
Residual deviance: 1.3835 on 1 degrees of freedom
AIC: 24.86
Number of Fisher Scoring iterations: 4
   Hosmer-Lemeshow: One place I've seen a function for the Hosmer-Lemeshow test is
http://sas-and-r.blogspot.com/2010/09/example-87-hosmer-and-lemeshow-goodness.html
   The function rstandard can be used to request standardized residuals, after a
binary glm fit. For example, for the Berkeley admissions data shown on p. 63, the
model assuming no gender effect fits well except for the first department:
> data <- read.table("berkeley.dat",header=TRUE)</pre>
> data
  dept gender yes no
     A male 512 313
2
     A female 89 19
3
     B male 353 207
     B female 17
5
     C male 120 205
6
     C female 202 391
7
     D male 138 279
8
     D female 131 244
9
     E male 53 138
10
     E female 94 299
11
     F
         male 22 351
12
     F female 24 317
> attach(data)
> n <- yes + no
> fit <- glm(yes/n ~ factor(dept), weights=n, family=binomial)</pre>
> summary(fit)
Coefficients:
             Estimate Std. Error z value Pr(>|z|)
(Intercept)
             factor(dept)B -0.05059 0.10968 -0.461
                                          0.645
factor(dept)C -1.20915 0.09726 -12.432
                                          <2e-16 ***
```

<2e-16 ***

factor(dept)D -1.25833 0.10152 -12.395

```
factor(dept)E -1.68296
                          0.11733 -14.343
                                             <2e-16 ***
factor(dept)F -3.26911
                          0.16707 -19.567
                                             <2e-16 ***
    Null deviance: 877.056 on 11 degrees of freedom
Residual deviance: 21.736 on 6 degrees of freedom
AIC: 102.68
> rstandard(fit, type="pearson")
                    2 3
                                                      5
-4.1530728 \quad 4.1530728 \quad -0.5037077 \quad 0.5037077 \quad 0.8680662 \quad -0.8680662 \quad -0.5458732
                    9
                         10
                                          11
                                                     12
0.5458732 1.0005342 -1.0005342 -0.6197526 0.6197526
```

Big data: The R package glmnet can apparently fit logistic regression to data sets with very large numbers of variables or observations, and as mentioned below can use regularization methods such as the lasso:

cran.r-project.org/web/packages/glmnet/index.html

ROC curves

ROC curves can be constructed with the ROCR library. For example, for a probit model for the beetle mortality data of Section 7.1.4,

```
> dose < c(rep(1.691,59),rep(1.724,60),rep(1.755,62),rep(1.784,56),
+ rep(1.811,63),rep(1.837,59),rep(1.861,62),rep(1.884,60))
> y <- c(rep(1,6),rep(0,53),rep(1,13),rep(0,47),rep(1,18),rep(0,44),
+ rep(1,28),rep(0,28),rep(1,52),rep(0,11),rep(1,53),rep(0,6),
+ rep(1,61), rep(0,1), rep(1,60))
> fit.probit <- glm(y ~ dose, family=binomial(link=probit))</pre>
> summary(fit.probit)
            Estimate Std. Error z value Pr(>|z|)
(Intercept) -34.956
                          2.649 -13.20 <2e-16
              19.741
                          1.488 13.27
                                          <2e-16
dose
> library("ROCR") # to construct ROC curve
> pred <- prediction(fitted(fit.probit),y)</pre>
> perf <- performance(pred, "tpr", "fpr")</pre>
> plot(perf)
> performance(pred, "auc")
Slot "y.values":
[[1]]
[1] 0.9010852
                   # area under ROC curve
```

Cochran-Mantel-Haenszel test

The function mantelhaen.test can perform Cochran-Mantel-Haenszel tests for $I \times J \times K$ tables:

stat.ethz.ch/R-manual/R-patched/library/stats/html/mantelhaen.test.html For example, for the clinical trials data in Table 6.9,

```
> beitler <- c(11,10,25,27,16,22,4,10,14,7,5,12,2,1,14,16,6,0,11,12,1,0,10,10,1,1,4,8,4,6,2,1)
> beitler <- array(beitler, dim=c(2,2,8))
> mantelhaen.test(beitler, correct=FALSE)
```

Mantel-Haenszel chi-squared test without continuity correction

```
data: beitler
Mantel-Haenszel X-squared = 6.3841, df = 1, p-value = 0.01151
alternative hypothesis: true common odds ratio is not equal to 1
95 percent confidence interval:
    1.177590 3.869174
sample estimates:
common odds ratio
    2.134549
```

When I=2 and J=2, enter "correct=FALSE" so as not to use the continuity correction. In that case, the output also shows the Mantel-Haenszel estimate $\hat{\theta}_{MH}$ and the corresponding confidence interval for the common odds ratio. With the exact option,

```
> mantelhaen.test(beitler, correct=FALSE, exact=TRUE)
```

R provides the exact conditional test (Sec. 7.3.5) and the conditional ML estimate of the common odds ratio (Sec. 16.6.6). When I > 2 and/or J > 2, this function provides the generalized test that treats X and Y as nominal scale (i.e., df = (I-1)(J-1), given in equation (8.18) in the text).

Infinite estimates

Here is an example of the use of R for Table 6.11, in which center effect ML estimates for centers 1 and 3 are actually $-\infty$.

```
> data <- read.table("fungal.dat",header=TRUE)</pre>
> data
  center treatment y n
                105
      1
2
       1
                 0 0 9
3
       2
                1 1 13
4
       2
                 0 0 10
                 1 0 7
5
       3
       3
                 0 0 5
6
```

```
169
                0 2 8
9
       5
                1 5 14
10
       5
                 0 2 14
> attach(data)
> fit <- glm(y/n ~ treatment + factor(center), weights=n, family=binomial)
> summary(fit)
Coefficients:
                Estimate Std. Error z value Pr(>|z|)
(Intercept) -2.459e+01 2.330e+04 -0.001 0.9992 treatment 1.546e+00 7.017e-01 0.002 0.003
                1.546e+00 7.017e-01
                                      2.203 0.0276 *
treatment
factor(center)2 2.039e+01 2.330e+04 0.001 0.9993
factor(center)3 4.809e-03 3.172e+04 0.000 1.0000
factor(center)4 2.363e+01 2.330e+04 0.001
                                             0.9992
factor(center)5 2.257e+01 2.330e+04 0.001 0.9992
   Null deviance: 28.53202 on 9 degrees of freedom
Residual deviance: 0.50214 on 4 degrees of freedom
Number of Fisher Scoring iterations: 21
> fit2 <- glm(y/n ~ treatment + factor(center) -1, weights=n, family=binomial)
> summary(fit2)
Coefficients:
                Estimate Std. Error z value Pr(>|z|)
                1.5460 0.7017 2.203 0.027569 *
treatment
factor(center)1 -24.5922 23296.3959 -0.001 0.999158
factor(center)2 -4.2025 1.1891 -3.534 0.000409 ***
factor(center)3 -24.5874 21523.6453 -0.001 0.999089
factor(center)4 -0.9592 0.6548 -1.465 0.142956
factor(center)5 -2.0223 0.6700 -3.019 0.002540 **
    Null deviance: 73.07369 on 10 degrees of freedom
Residual deviance: 0.50214 on 4 degrees of freedom
Number of Fisher Scoring iterations: 21
```

Other binary response models

For binary data, alternative links are possible. For example, continuing with the horseshoe crab data from above,

Residual Deviance: 195.4621 on 171 degrees of freedom

For the complementary log-log link with the beetle data of Table 7.1, showing also the construction of standardized residuals (which can also be obtained by requesting rstandard(fit.cloglog, type="pearson")) and profile likelihood confidence intervals,

```
> beetles <- read.table("beetle.dat", header=T)
> beetles
   dose number killed
1 1.691
            59
2 1.724
            60
                   13
3 1.755
            62
                   18
                   28
4 1.784
            56
5 1.811
            63
                   52
                   53
6 1.837
            59
7 1.861
            62
                   61
8 1.884
            60
                   60
> binom.dat <- matrix(append(killed,number-killed),ncol=2)</pre>
> fit.cloglog <- glm(binom.dat ~ dose, family=binomial(link=cloglog),
    data=beetles)
> summary(fit.cloglog) # much better fit than logit
                Value Std. Error
                                   t value
(Intercept) -39.52250
                        3.232269 -12.22748
                        1.795086 12.26397
       dose 22.01488
    Null Deviance: 284.2024 on 7 degrees of freedom
Residual Deviance: 3.514334 on 6 degrees of freedom
> pearson.resid <- resid(fit.cloglog, type="pearson")
> std.resid <- pearson.resid/sqrt(1-lm.influence(fit.cloglog)$hat)
> cbind(dose, killed/number, fitted(fit.cloglog), pearson.resid, std.resid)
                             pearson.resid std.resid
   dose
1 1.691 0.1016949 0.09582195
                                 0.1532583 0.1772659
2 1.724 0.2166667 0.18802653
                                 0.5677671 0.6694966
3 1.755 0.2903226 0.33777217
                                -0.7899738 -0.9217717
4 1.784 0.5000000 0.54177644
                                -0.6274464 -0.7041154
5 1.811 0.8253968 0.75683967
                                 1.2684541 1.4855799
6 1.837 0.8983051 0.91843509
                                -0.5649292 -0.7021989
7 1.861 0.9838710 0.98575181
                                -0.1249636 -0.1489834
8 1.884 1.0000000 0.99913561
                                 0.2278334 0.2368981
> confint(fit.cloglog)
                2.5 %
                         97.5 %
(Intercept) -46.13984 -33.49923
             18.66945 25.68877
dose
```

Bayesian fitting

Jim Albert in $Bayesian\ Computation\ with\ R$ (Springer 2009, pp. 216-219) presented an R function, bayes.probit, for implementing his algorithm for fitting probit models with a Bayesian approach.

Penalized likelihood

The Copas smoothing method can be implemented with the R function *ksmooth*, with lambda=bandwidth. For example, for the kyphosis example of Sec. 7.4.3,

The *brglm* function in the MASS library can implement bias reduction using the Firth penalized likelihood approach for binary regression models, including models with logit, probit, and complementary log-log links:

```
cran.r-project.org/web/packages/brglm/index.html
```

The Firth penalized likelihood approach can also be done using the R package logistf. For example, for Table 6.11 analyzed above in the "infinite estimates" subsection:

```
> fit3 <- logistf(y/n ~ treatment + factor(center) -1, weights=n, family=binomial)
> summary(fit3)
logistf(formula = y/n ~ treatment + factor(center) - 1, weights = n,
    family = binomial)
```

Model fitted by Penalized ML

Confidence intervals and p-values by Profile Likelihood

Wald test = 26.05109 on 6 df, p = 0.000217816

```
coef se(coef) lower 0.95 upper 0.95
                                                                Chisa
                1.3678143 0.6436197 -3.125353 5.9101373 0.34269584
treatment
factor(center)1 -4.0036677 1.5193002 -8.998902 -1.6994870 17.89776479
factor(center)2 -3.6351503 1.0063781 -8.204822 -0.9953539 11.19907751
factor(center)3 -4.1707188 1.5811491 -9.187891 -1.6107831 14.20192563
factor(center)4 -0.8487087 0.6264638 -5.897048 4.2538020 0.03158963
factor(center)5 -1.8328467 0.6200202 -6.599538 2.9956561 0.00000000
               5.582773e-01
treatment
factor(center)1 2.330947e-05
factor(center)2 8.183801e-04
factor(center)3 1.642024e-04
factor(center)4 8.589313e-01
factor(center)5 1.000000e+00
Likelihood ratio test=40.72184 on 6 df, p=3.28493e-07, n=10
```

Covariance-Matrix:

```
[,1]
                     [,2]
                                [,3]
                                           [,4]
                                                      [,5]
                                                                 [,6]
[1,] 0.4142463 -0.2747484 -0.3377549 -0.3456519 -0.2304370 -0.2758511
[2,] -0.2747484 2.3082730 0.2240156 0.2292533 0.1528371 0.1829579
[3,] -0.3377549 0.2240156
                          1.0127969 0.2818266 0.1878864
[4,] -0.3456519
                0.2292533
                          0.2818266
                                      2.5000323
[5,] -0.2304370
               0.1528371 0.1878864 0.1922793 0.3924569
                                                           0.1534505
[6,] -0.2758511  0.1829579  0.2249146  0.2301733  0.1534505
                                                           0.3844251
```

Lasso for binary and count models is available in the R packages glmnet and $\mathit{glmpath}$:

```
cran.r-project.org/web/packages/glmnet/index.html
cran.r-project.org/web/packages/glmpath/index.html
```

The group lasso is available with the *grplasso* package:

cran.r-project.org/web/packages/grplasso/index.html

Generalized additive models

```
For a generalized additive model, R has a gam package:
```

```
cran.r-project.org/web/packages/gam/index.html
```

Thomas Yee's VGAM library can also handle GAMs:

```
\verb|www.stat.auckland.ac.nz/~yee/VGAM/doc/glmgam.pdf|
```

rss.acs.unt.edu/Rdoc/library/VGAM/html/vgam.html

For example, for the ungrouped horseshoe crab data,

```
> library("VGAM")
```

- > gam.fit <- vgam(y ~ s(weight), family=binomialff(link=logit), data=crabs)
- > plot(weight, fitted(gam.fit))

GAMs can also be fitted with the gam function in the mgcv library:

```
cran.r-project.org/web/packages/mgcv/mgcv.pdf
```

False discovery rate (FDR)

```
R packages for FDR are listed at strimmerlab.org/notes/fdr.html
```

Chapter 8: Multinomial Response Models

For baseline-category logit models, one can use the *multinom* function in the *nnet* library that has been provided by Venables and Ripley to do various calculations by neural nets (see, e.g., p. 230 of Venables and Ripley, 3rd ed.):

```
cran.r-project.org/web/packages/nnet/nnet.pdf
```

Statements have the form

```
> fit <- multinom(y ~ x + factor(z), weights=freq, data=gators)</pre>
```

The VGAM package

Especially useful for modeling multinomial responses is the VGAM package and vglm function developed by Thomas Yee at Auckland, New Zealand,

```
www.stat.auckland.ac.nz/~yee/VGAM
```

This package has functions that can also can fit a wide variety of models including multinomial logit models for nominal responses and cumulative logit models, adjacent-categories models, and continuation-ratio models for ordinal responses. For more details, see "The VGAM package for categorical data analysis," in *Journal of Statistical Software*, vol. 32, pp. 1-34 (2010), www.jstatsoft.org/v32/i10. See also www.stat.auckland.ac.nz/~yee/VGAM/doc/categorical.pdf for some basic examples of its multiple capabilities for modeling categorical data.

Following is an example of the use of vglm for fitting a baseline-category logit model to the alligator food choice data in Table 8.1 of the textbook. The data file has the five multinomial counts for the food choices identified as y1 through y5, with y1 being fish as in the text. The vglm function uses the final category as the baseline, so to use fish as the baseline, in the model statement we identify the response categories as $(y_2, y_3, y_4, y_5, y_1)$. By contrast, the multinom function in the nnet library picks the first category of the response variable as the baseline. The following also shows output using it. For both functions, a predictor identified as a factor in the model statement has its first category as the baseline, so the lake estimates shown here differ from those in the book, which used the last lake level as the baseline.

```
> alligators <- read.table("alligators.dat",header=TRUE)
> alligators
   lake gender size y1 y2 y3 y4 y5
              1
                          1
2
      1
              1
                   0
                      4
                          0
                             0
                                    2
3
      1
              0
                   1 16
                          3
                             2
                                 2
                                    3
              0
                   0
                       3
4
      1
                          0
                              1
5
      2
                       2
              1
                   1
                          2
                             0
                                 0
                                    1
6
      2
              1
                   0 13
                          7
                              6
                                 0
7
      2
              0
                       0
                              0
      2
                       3
8
              0
                   0
                          9
                              1
9
      3
              1
                       3
                          7
                   1
                                 0
                                    1
                              1
10
                   0
      3
                       8
                          6
                             6
              1
      3
              0
                       2
11
                   1
                             1
                                 1
      3
              0
                   0
12
                      0
                          1
                             0
                                 0
13
      4
              1
                   1 13 10
                             0
14
      4
              1
15
      4
              0
                   1
                       3
                          9
                             1
                                    1
16
      4
              0
                       8
                             0
                          1
                                 0
> library(VGAM)
> vglm(formula = cbind(y2,y3,y4,y5,y1) ~ size + factor(lake),
family=multinomial, data=alligators)
```

```
Coefficients:
  (Intercept):1
                   (Intercept):2
                                   (Intercept):3
                                                    (Intercept):4
                                                                            size:1
     -3.2073772
                      -2.0717560
                                      -1.3979592
                                                       -1.0780754
                                                                         1.4582046
                                          size:4 factor(lake)2:1 factor(lake)2:2
         size:2
                          size:3
     -0.3512628
                      -0.6306597
                                       0.3315503
                                                        2.5955779
                                                                         1.2160953
factor(lake)2:3 factor(lake)2:4 factor(lake)3:1 factor(lake)3:2 factor(lake)3:3
     -1.3483253
                      -0.8205431
                                       2.7803434
                                                        1.6924767
                                                                         0.3926492
factor(lake)3:4 factor(lake)4:1 factor(lake)4:2 factor(lake)4:3 factor(lake)4:4
      0.6901725
                       1.6583586
                                      -1.2427766
                                                       -0.6951176
                                                                       -0.8261962
Degrees of Freedom: 64 Total; 44 Residual
Residual Deviance: 52.47849
Log-likelihood: -74.42948
> library(nnet)
> fit2 <- multinom(cbind(y1,y2,y3,y4,y5) ~ size + factor(lake), data=alligators)</pre>
> summary(fit2)
Call:
multinom(formula = cbind(y1, y2, y3, y4, y5) ~ size + factor(lake),
    data = alligators)
Coefficients:
   (Intercept)
                      size factor(lake)2 factor(lake)3 factor(lake)4
y2
     -3.207394 1.4582267
                               2.5955898
                                             2.7803506
                                                            1.6583514
yЗ
     -2.071811 -0.3512070
                               1.2161555
                                             1.6925186
                                                           -1.2426769
     -1.397976 -0.6306179
                              -1.3482294
                                             0.3926516
                                                           -0.6951107
     -1.078137 0.3315861
                              -0.8204767
                                              0.6902170
                                                           -0.8261528
v5
Std. Errors:
                     size factor(lake)2 factor(lake)3 factor(lake)4
   (Intercept)
     0.6387317 0.3959455
                              0.6597077
                                            0.6712222
                                                           0.6128757
y2
yЗ
     0.7067258 0.5800273
                              0.7860141
                                            0.7804482
                                                           1.1854024
у4
     0.6085176 0.6424744
                              1.1634848
                                            0.7817677
                                                           0.7812585
     0.4709212 0.4482539
                              0.7296253
                                            0.5596752
                                                           0.5575414
```

Residual Deviance: 540.0803

AIC: 580.0803

The vglm function for ordinal models

The vglm function in the VGAM library can also fit a wide variety of ordinal models. Many examples of the use of vglm for various ordinal-response analyses are available at the website for my book, Analysis of Ordinal Categorical Data (2nd ed., 2010), www.stat.ufl.edu/~aa/ordinal/ord.html, and several of these are also shown below. For example, for the cumulative logit model fitted to the happiness data of Table 8.5 of the textbook, entering each multinomial observation as a set of indicators that indicates the response category, letting race = 0 for white and 1 for black, and letting traumatic be the number of traumatic events,

> happy <- read.table("happy.dat", header=TRUE)</pre>

```
> happy
  race traumatic y1 y2 y3
    0
            0 1 0 0
1
2
     Ω
               0 1 0 0
3
    0
              0 1 0 0
4
    0
              0 1 0 0
    0
              0 1 0 0
6
             0 1 0 0
7
     0
             0 1 0 0
8
               0 0 1 0
     0
               2 0 0 1
94
     1
95
     1
               3 0 1 0
96
     1
               3
                  0 1 0
     1
> library(VGAM)
> fit <- vglm(cbind(y1,y2,y3) ~ race + traumatic,</pre>
        family=cumulative(parallel=TRUE), data=happy)
> summary(fit)
Coefficients:
                Value Std. Error t value
(Intercept):1 -0.51812 0.33819 -1.5320
(Intercept):2 3.40060
                        0.56481 6.0208
             -2.03612
                        0.69113 -2.9461
race
                      0.18086 -2.2425
             -0.40558
traumatic
Names of linear predictors: logit(P[Y<=1]), logit(P[Y<=2])
Residual Deviance: 148.407 on 190 degrees of freedom
Log-likelihood: -74.2035 on 190 degrees of freedom
Number of Iterations: 5
> fit.inter <- vglm(cbind(y1,y2,y3) ~ race + traumatic + race*traumatic,</pre>
    family=cumulative(parallel=TRUE), data=happy)
> summary(fit.inter)
Coefficients:
                 Value Std. Error t value
(Intercept):1 -0.43927 0.34469 -1.2744
(Intercept):2
              3.52745
                         0.58737 6.0055
race
              -3.05662
                         1.20459 -2.5375
              -0.46905
                          0.19195 -2.4436
traumatic
race:traumatic 0.60850
                          0.60077 1.0129
Residual Deviance: 147.3575 on 189 degrees of freedom
Log-likelihood: -73.67872 on 189 degrees of freedom
Number of Iterations: 5
```

The parallel=TRUE option requests the proportional odds version of the model with the same effects for each cumulative logit. Then entering fitted(fit) would produce the

estimated probabilities for each category for each observation. Here, we also fitted the model with an interaction term, which does not provide a significantly better fit.

To use vglm to fit the cumulative logit model not having the proportional odds assumption, we take out the parallel=TRUE option. Then, we do a likelihood-ratio test to see if it gives a better fit:

```
> fit2 <- vglm(cbind(y1,y2,y3) ~ race + traumatic, family=cumulative,
         data=happy)
> summary(fit2)
Coefficients:
                 Value Std. Error t value
(Intercept):1 -0.56605 0.36618 -1.545821
(Intercept):2 3.48370 0.75950 4.586850
             -14.01877 322.84309 -0.043423
race:1
race:2
              -1.84673
                        0.76276 -2.421095
traumatic:1
              -0.34091
                          0.21245 -1.604644
traumatic:2
              -0.48356
                         0.27524 -1.756845
Residual Deviance: 146.9951 on 188 degrees of freedom
Log-likelihood: -73.49755 on 188 degrees of freedom
Number of Iterations: 14
```

> pchisq(deviance(fit)-deviance(fit2),df=df.residual(fit)-df.residual(fit2),lower.tail=FALSE)

Note that the ML effect estimate of race for the first logit is actually $-\infty$, reflecting the lack of any black subjects in the first happiness category.

For the same data, to fit the cumulative probit model with common effects for each probit, we use

```
fit.probit <- vglm(cbind(y1,y2,y3) ~ race + traumatic,
    family=cumulative(link=probit, parallel=TRUE), data=happy)
> summary(fit.probit)
```

Coefficients:

[1] 0.4936429

Residual Deviance: 148.1066 on 190 degrees of freedom Log-likelihood: -74.0533 on 190 degrees of freedom Number of Iterations: 5

To fit the adjacent-categories logit model to the same data, we use

```
> fit.acat <- vglm(cbind(y1,y2,y3) ~ race + traumatic,</pre>
```

```
family=acat(reverse=TRUE, parallel=TRUE), data=happy)
> summary(fit.acat)
Coefficients:
                 Value Std. Error t value
(Intercept):1 -0.49606 0.31805 -1.5597
(Intercept):2 3.02747 0.57392 5.2751
race
             -1.84230 0.64190 -2.8701
             -0.35701 0.16396 -2.1775
traumatic
Names of linear predictors: log(P[Y=1]/P[Y=2]), log(P[Y=2]/P[Y=3])
Residual Deviance: 148.1996 on 190 degrees of freedom
Log-likelihood: -74.09982 on 190 degrees of freedom
Number of Iterations: 5
   To fit the continuation-ratio logit model to the same data, one direction for forming
the sequential logits yields the results:
> fit.cratio <- vglm(cbind(y1,y2,y3) ~ race + traumatic,</pre>
       family=cratio(reverse=TRUE, parallel=TRUE), data=happy)
> summary(fit.cratio)
Coefficients:
                 Value Std. Error t value
(Intercept):1 -0.45530 0.32975 -1.3808
(Intercept):2 3.34108 0.56309 5.9335
              -2.02555 0.67683 -2.9927
race
              -0.38504 0.17368 -2.2170
traumatic
Names of linear predictors: logit(P[Y<2|Y<=2]), logit(P[Y<3|Y<=3])
Residual Deviance: 148.1571 on 190 degrees of freedom
Log-likelihood: -74.07856 on 190 degrees of freedom
```

The more common form of continuation-ratio logit is obtained by instead using RE-VERSE=FALSE in the model-fitting statement.

Other multinomial functions

Number of Iterations: 5

For the proportional odds version of cumulative logit models, you can alternatively use the *polr* function in the MASS library, with syntax shown next. However, the data file then needs the response as a factor vector, so we first put the data from the above examples in that form.

```
> library(MASS)
> response <- matrix(0,nrow=97,ncol=1)
> response <- ifelse(y1==1,1,0)
> response <- ifelse(y2==1,2,resp)</pre>
```

The *profilelike.polr* function in the ProfileLikelihood library can provide profile likelihood confidence intervals for the proportional odds version of the cumulative logit model. See

 $\verb|cran.r-project.org/web/packages/ProfileLikelihood/ProfileLikelihood.pdf|.$

The *ordinal* package at CRAN can fit cumulative link models. See www.cran.r-project.org/package=ordinal/. Apparently it can also fit models with random effects, using Gauss-Hermite quadrature or a Laplace approximation.

The MNP package can fit multinomial probit models using Bayesian methods. See imai.princeton.edu/research/files/MNPjss.pdf

Chapters 9–10: Loglinear Models

Since loglinear models are special cases of generalized linear models with Poisson random component and log link function, they can be fitted with the glm function. To illustrate this, the following code shows fitting the models (A,C,M) and (AC,AM,CM) for Table 9.3 for the high school survey about use of alcohol, cigarettes and marijuana. The code also shows forming Pearson and standardized residuals for the homogeneous association model, (AC,AM,CM). For factors, R sets the value equal to 0 at the first category rather than the last as in the text examples.

```
> drugs <- read.table("drugs.dat",header=TRUE)</pre>
> drugs
   a
       С
           m count
1 yes yes yes
               911
               538
2 yes yes no
3 yes no yes
                44
4 yes no no
               456
5 no yes yes
6 no yes no
                43
7 no no yes
                 2
               279
8 no no no
```

```
> indep <- glm(count ~ alc + cig + mar, family=poisson(link=log), data=drugs)</pre>
> summary(indep) % loglinear model (A, C, M)
Coefficients:
          Estimate Std. Error z value Pr(>|z|)
(Intercept) 6.29154 0.03667 171.558 < 2e-16 ***
          -1.78511 0.05976 -29.872 < 2e-16 ***
          -0.64931 0.04415 -14.707 < 2e-16 ***
cig2
          mar2
   Null deviance: 2851.5 on 7 degrees of freedom
Residual deviance: 1286.0 on 4 degrees of freedom
AIC: 1343.1
Number of Fisher Scoring iterations: 6
> homo.assoc <- update(indep, .~. + alc:cig + alc:mar + cig:mar)</pre>
> summary(homo.assoc) # loglinear model (AC, AM, CM)
Coefficients:
          Estimate Std. Error z value Pr(>|z|)
(Intercept) 6.81387 0.03313 205.699 < 2e-16 ***
                   0.45221 -12.225 < 2e-16 ***
alc2
          -5.52827
          -3.01575 0.15162 -19.891 < 2e-16 ***
cig2
         mar2
alc2:cig2 2.05453 0.17406 11.803 < 2e-16 ***
alc2:mar2 2.98601 0.46468 6.426 1.31e-10 ***
cig2:mar2 2.84789 0.16384 17.382 < 2e-16 ***
   Null deviance: 2851.46098 on 7 degrees of freedom
Residual deviance: 0.37399 on 1 degrees of freedom
AIC: 63.417
Number of Fisher Scoring iterations: 4
> pearson.resid <- resid(homo.assoc, type="pearson") # Pearson residuals
> sum(pearson.resid^2)  # Pearson goodness-of-fit statistic
[1] 0.4011006
> leverage <- lm.influence(homo.assoc)$hat # leverage values
> std.resid <- pearson/sqrt(1 - leverage) # standardized residuals
> std.resid <- rstandard(homo.assoc, type="pearson")</pre>
   # other way to get standardized residuals
> expected <- fitted(homo.assoc) # estimated expected frequencies
> cbind(count, expected, pearson.resid, std.resid)
 count expected pearson.resid std.resid
1 911 910.38317 0.02044342 0.6333249
2 538 538.61683 -0.02657821 -0.6333249
```

> alc <- factor(a); cig <- factor(c); mar <- factor(m)</pre>

```
3
    44 44.61683
                   -0.09234564 -0.6333249
    456 455.38317
4
                    0.02890528 0.6333249
5
     3
         3.61683
                   -0.32434086 -0.6333250
6
        42.38317
                    0.09474777 0.6333249
     43
7
     2
        1.38317
                    0.52447888 0.6333250
   279 279.61683
                   -0.03688791 -0.6333249
```

By the results of Sec. 9.5, we get the same results for the association between marijuana use and each of alcohol use and cigarette use if we treat the data as four binomials (instead of eight Poissons) and model the logit for marijuana use in terms of additive effects for alcohol use and cigarette use.

```
> drugs2 <- read.table("drugs_binomial.dat", header=TRUE)</pre>
> drugs2
    Α
        C M_yes M_no
1 yes
      yes
              911
                   538
                         1449
               44
                    456
                          500
2 yes
       no
3
      yes
                3
                    43
                           46
  no
  no
       no
                2
                    279
                          281
> attach(drugs2)
> alc <- factor(A); cig <- factor(C)</pre>
> fit.logistic <- glm(M_yes/n ~ alc + cig, weights=n,</pre>
                      family=binomial(link=logit))
> summary(fit.logistic)
Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept)
           -5.3090
                        0.4752 -11.172 < 2e-16
                                 6.426 1.31e-10
              2.9860
alcyes
                         0.4647
cigyes
              2.8479
                         0.1638 17.382 < 2e-16
    Null deviance: 843.82664 on 3 degrees of freedom
Residual deviance: 0.37399 on 1 degrees of freedom
```

The loglin function in the MASS library can fit loglinear models using iterative proportional fitting, reporting parameter estimates using constraints whereby they sum to zero (rather than a baseline equaling 0). The loglm function allows the models to be specified and fitted in a manner similar to using glm.

Association models

Following is an example for the linear-by-linear association model and the row effects and columns effects models (with scores 1, 2, 4, 5) fitted to Table 10.3 on premarital sex and teenage birth control.

```
> sexdata <- read.table("sex.dat", header=TRUE)
> attach(sexdata)
> uv <- premar*birth</pre>
```

```
> premar <- factor(premar); birth <- factor(birth)</pre>
> LL.fit <- glm(count ~ premar + birth + uv, family=poisson)
> summary(LL.fit)
Coefficients:
          Estimate Std. Error z value Pr(>|z|)
(Intercept) 4.10684 0.08951 45.881 < 2e-16 ***
          premar2
          -1.77002 0.16464 -10.751 < 2e-16 ***
premar3
          -1.75369
                   0.23432 -7.484 7.20e-14 ***
premar4
                   0.11952 -3.883 0.000103 ***
birth2
          -0.46411
                    0.16201 -4.472 7.74e-06 ***
birth3
          -0.72452
                    0.24910 -7.546 4.50e-14 ***
birth4
          -1.87966
           0.28584
                     0.02824 10.122 < 2e-16 ***
   Null deviance: 431.078 on 15 degrees of freedom
Residual deviance: 11.534 on 8 degrees of freedom
AIC: 118.21
Number of Fisher Scoring iterations: 4
> u <- c(1,1,1,1,2,2,2,2,4,4,4,4,5,5,5,5)
> v \leftarrow c(1,2,4,5,1,2,4,5,1,2,4,5,1,2,4,5)
> row.fit <- glm(count ~ premar + birth + u:birth, family=poisson)</pre>
> summary(row.fit)
Coefficients: (1 not defined because of singularities)
          Estimate Std. Error z value Pr(>|z|)
(Intercept) 4.98722 0.14624 34.102 < 2e-16 ***
          -0.65772
                   0.13124 -5.011 5.40e-07 ***
premar2
          premar3
          1.50195 0.17952 8.366 < 2e-16 ***
premar4
birth2
          -0.31939 0.19821 -1.611 0.107103
birth3
         -1.49032 0.23745 -6.276 3.47e-10 ***
birth4
birth1:u -0.59533 0.06555 -9.082 < 2e-16 ***
birth2:u -0.40543 0.06068 -6.681 2.37e-11 ***
birth3:u -0.12975
                     0.05634 -2.303 0.021276 *
birth4:u
                NA
                          NA
                                 NA
   Null deviance: 431.078 on 15 degrees of freedom
Residual deviance: 8.263 on 6 degrees of freedom
AIC: 118.94
Number of Fisher Scoring iterations: 4
> column.fit <- glm(count ~ premar + birth + premar:v, family=poisson)</pre>
> summary(column.fit)
Coefficients: (1 not defined because of singularities)
          Estimate Std. Error z value Pr(>|z|)
```

```
(Intercept) 1.40792
                      0.26947
                                5.225 1.74e-07 ***
                      0.29053 -2.357 0.018444 *
premar2
           -0.68466
           0.78235
                      0.22246
                               3.517 0.000437 ***
premar3
premar4
           2.11167
                      0.18958 11.138 < 2e-16 ***
           0.54590
                      0.11723
                               4.656 3.22e-06 ***
birth2
birth3
            1.59262
                      0.14787 10.770 < 2e-16 ***
birth4
            1.51018
                      0.16420
                               9.197 < 2e-16 ***
                                9.858 < 2e-16 ***
premar1:v
            0.58454
                      0.05930
            0.49554
                      0.07990
                                6.202 5.57e-10 ***
premar2:v
            0.20315
                      0.06538
                                3.107 0.001890 **
premar3:v
                                   NΑ
                                           NΑ
premar4:v
                 NA
                           NA
```

Null deviance: 431.0781 on 15 degrees of freedom Residual deviance: 7.5861 on 6 degrees of freedom

AIC: 118.26

Number of Fisher Scoring iterations: 4

Joseph Lang's mph.fit function can fit generalized loglinear models (Section 10.5.1) and other much more general "multinomial-Poisson homogeneous" models such as covered in Lang (2004, 2005):

www.stat.uiowa.edu/~jblang/mph.fitting/index.htm

Multiplicative models such as RC and stereotype

The gnm add-on package for R, developed by David Firth and Heather Turner at the Univ. of Warwick, can fit multiplicative models such as Goodman's RC association model for two-way contingency tables and Anderson's stereotype model for ordinal multinomial responses:

```
www2.warwick.ac.uk/fac/sci/statistics/staff/academic-research/firth/software
```

Thomas Yee's VGAM package mentioned for Chapter 8 above can also fit Goodman's RC association model and Anderson's stereotype model, as well as bivariate logistic and probit models for bivariate binary responses.

Greenacre and Nenadic have developed the ca package for simple, multiple, and joint correspondence analysis:

```
\label{lem:www.statmethods.net/advstats/ca.html} $$\operatorname{cran.r-project.org/web/packages/ca/ca.pdf}$$ The $ACD$ package can fit loglinear models when data are missing. See $$\operatorname{cran.r-project.org/web/packages/ACD/ACD.pdf}$$
```

Chapter 11: Models for Matched Pairs

Confidence interval for difference of proportions with matched pairs

For the score CI due to Tango (1998) and the adjusted Wald CI proposed by Agresti and Min (2005) that forms the ordinary Wald CI after adding 0.50 to each cell, see

```
www.stat.ufl.edu/~aa/cda/R/matched/R2_matched/index.html
```

McNemar test

The function *mcnemar.test* can conduct McNemar's test for matched pairs. For example, for Table 11.1,

where a continuity correction is made unless "correct=FALSE" is specified.

Bradley-Terry models

The Bradley-Terry model can be fitted using the glm function by treating it as a generalized linear model. It can also be fitted using specialized functions, such as with the brat function in Thomas Yee's VGAM library mentioned above:

```
rss.acs.unt.edu/Rdoc/library/VGAM/html/brat.html
or by Prof. David Firth as described at
www2.warwick.ac.uk/fac/sci/statistics/staff/academic-research/firth/software/bradleyterry
www.jstatsoft.org/v12/i01
```

Chapter 12: Clustered Categorical Responses: Marginal Models

GEE methods

Laura Thompson's manual at

```
\verb|https://home.comcast.net/~lthompson221/Splusdiscrete2.pdf|.
```

describes several packages for doing GEE analyses. For instance, in the following code we use the *gee* function in the *gee* library to analyze the opinions about abortion data analyzed in Sec. 13.3.2 with both marginal models and random effects models.

> abortion

	gender	response	question	case
1	1	1	1	1
2	1	1	2	1
3	1	1	3	1

```
1
                  1
                           1
                  1
6
         1
                  1
                           3
                                2
7
                  1
                           1
                                3
         1
8
         1
                 1
                           2
                                3
9
         1
                 1
                           3
                           1 1849
5545
                           2 1849
5546
         0
                  0
5547
                  0
                           3 1849
         0
                  0
                           1 1850
5548
         0
5549
                  0
                            2 1850
         0
                           3 1850
5550
         0
                  0
> z1 <- ifelse(abortion$question==1,1,0)
> z2 <- ifelse(abortion$question==2,1,0)
> z3 <- ifelse(abortion$question==3,1,0)</pre>
> library(gee)
> fit.gee <- gee(response ~ gender + z1 + z2, id=case, family=binomial,
            corstr="exchangeable", data=abortion)
> summary(fit.gee)
GEE: GENERALIZED LINEAR MODELS FOR DEPENDENT DATA
gee S-function, version 4.13 modified 98/01/27 (1998)
Model:
Link:
                            Logit
Variance to Mean Relation: Binomial
Correlation Structure:
                           Exchangeable
Coefficients:
               Estimate Naive S.E.
                                       Naive z Robust S.E.
(Intercept) -0.125325730 0.06782579 -1.84775925 0.06758212 -1.85442135
            0.003437873\ 0.08790630\ 0.03910838\ 0.08784072\ 0.03913758
gender
            0.149347107 0.02814374 5.30658404 0.02973865 5.02198729
z1
            0.052017986 0.02815145 1.84779075 0.02704703 1.92324179
z2
Working Correlation
                  [,2]
          [,1]
                              [,3]
[1,] 1.0000000 0.8173308 0.8173308
[2,] 0.8173308 1.0000000 0.8173308
[3,] 0.8173308 0.8173308 1.0000000
> fit.gee2 <- gee(response ~ gender + z1 + z2, id=case, family=binomial,
             corstr="independence", data=abortion)
> summary(fit.gee2)
```

Link: Logit
Variance to Mean Relation: Binomial
Correlation Structure: Independent

Coefficients:

```
Estimate Naive S.E. Naive z Robust S.E. Robust z (Intercept) -0.125407576 0.05562131 -2.25466795 0.06758236 -1.85562596 gender 0.003582051 0.05415761 0.06614123 0.08784012 0.04077921 z1 0.149347113 0.06584875 2.26803253 0.02973865 5.02198759 z2 0.052017989 0.06586692 0.78974374 0.02704704 1.92324166
```

Working Correlation

```
[,1] [,2] [,3]
[1,] 1 0 0
[2,] 0 1 0
[3,] 0 0 1
```

From the geepack library, the function geeglm performs fitting of clustered data using the GEE method. See

```
www.jstatsoft.org/v15/i02/paper
```

for details, including an example for a binary response. Possible working correlation structures include independence, exchangeable, autoregressive (ar1), and unstructured. In addition to the sandwich covariance matrix (which is the default), when the number of clusters is small one can find a jackknife estimator. Fitting statements have the form:

```
> geeglm(y ~ x1 + x2, family=binomial, id=subject, corst=''exchangeable'')
```

The library *repolr* has a function *repolr* for GEE methods with ordinal responses: cran.r-project.org/web/packages/repolr/repolr.pdf

Here is an example for the insomnia data of Table 12.3, using the independence working correlation structure (Thanks to Anestis Touloumis).

- > insomnia<-read.table("insomnia.dat",header=TRUE)</pre>
- > insomnia<-as.data.frame(insomnia)</pre>
- > insomnia

case	treat	occasion	${\tt outcome}$
1	1	0	1
1	1	1	1
2	1	0	1
2	1	1	1
3	1	0	1
3	1	1	1
4	1	0	1
4	1	1	1
5	1	0	1

. . .

```
239 0 0 4
239 0 1 4
```

- > library(repolr)
- > summary(fit\$gee)

Coefficients:

	Estimate	Naive S.E.	Naive z	Robust S.E.	Robust z
factor(cuts)1	-2.26708899	0.2027367	-11.1824294	0.2187606	-10.3633343
factor(cuts)2	-0.95146176	0.1784822	-5.3308499	0.1809172	-5.2591017
factor(cuts)3	0.35173977	0.1726860	2.0368745	0.1784232	1.9713794
treat	0.03361002	0.2368973	0.1418759	0.2384374	0.1409595
occasion	1.03807641	0.2375992	4.3690229	0.1675855	6.1943093
treat:occasion	0.70775891	0.3341759	2.1179234	0.2435197	2.9063728

ML for marginal models

Joseph Lang at the Univ. of Iowa has R and S-Plus functions such as *mph.fit* for ML fitting of marginal models (when the explanatory variables are categorical and not numerous) through the generalized loglinear model (10.10). This uses the constraint approach with Lagrange multipliers. The function *hmmm* at CRAN developed by R. Colombi, S. Giordano, M. Cazzaro, and J. Lang can fit hierarchical multinomial marginal models (Bergsma and Rudas 2002). The models can impose inequality constraints on the parameters. For details, see

cran.r-project.org/web/packages/hmmm/index.html

Chapters 13–14: Clustered Categorical Responses: Random Effects Models

Generalized linear mixed models

The function *lmer* (linear mixed effects in R) in the R package *Matrix* can be used to fit generalized linear mixed models. See the Gelman and Hill (2007) text, such as Sec. 12.4. See also the *lme4* package, described in

http://cran.r-project.org/web/packages/lme4/vignettes/Theory.pdf These use adaptive Gauss-Hermite quadrature.

The function glmm in the repeated library can fit generalized linear mixed models using Gauss–Hermite quadrature methods, for families including the binomial and Poisson:

```
rss.acs.unt.edu/Rdoc/library/repeated/html/glmm.html
```

The package glmmAK can also fit them, with a Bayesian approach with priors for the fixed effects parameters:

```
cran.r-project.org/web/packages/glmmAK/glmmAK.pdf
```

The function glmmML in the glmmML package can fit GLMMs with random intercepts

by adaptive Gauss–Hermite quadrature. For instance, in the following code we use it to analyze the opinions about abortion data analyzed in Sec. 13.3.2 with random effects models, employing Gauss-Hermite quadrature with 75 quadrature points and a starting value of 9 for the estimate of σ .

```
> abortion <- read.table("abortion.dat",header=TRUE)
     gender response question case
1
          1
                   1
2
                            2
          1
                   1
                                 1
3
                            3
                   1
          1
                                 1
                                 2
4
          1
                   1
                             1
5
                   1
                             2
                                 2
          1
                             3
6
. . .
          0
                   0
                             1 1850
5548
5549
                   0
                             2 1850
          Λ
                   0
5550
          0
                             3 1850
> z1 <- ifelse(abortion$question==1,1,0)
> z2 <- ifelse(abortion$question==2,1,0)
> z3 <- ifelse(abortion$question==3,1,0)
> library(glmmML)
> fit.glmm <- glmmML(response ~ gender + z1 + z2,</pre>
            cluster=abortion$case, family=binomial, data=abortion,
            method = "ghq", n.points=70, start.sigma=9)
> summary(fit.glmm)
                coef se(coef)
                                      z Pr(>|z|)
(Intercept) -0.61874
                       0.3777 -1.63839 1.01e-01
             0.01259
                       0.4888 0.02575 9.79e-01
gender
             0.83470
                       0.1601 5.21347 1.85e-07
z1
z2
             0.29240
                       0.1567 1.86622 6.20e-02
Scale parameter in mixing distribution: 8.736 gaussian
Std. Error:
                                          0.5421
        LR p-value for H_0: sigma = 0: 0
```

The function glmmPQL in the MASS library can fit GLMMs using penalized quasi-likelihood. The R package MCMCglmm can fit them with Markov Chain Monte Carlo methods:

```
cran.r-project.org/web/packages/MCMCglmm/vignettes/CourseNotes.pdf
```

For a text on GLMMs using R, see *Multivariate Generalized Linear Mixed Models* by D. M. Berridge and R. Crouchley, published 2011 by CRC Press. The emphasis is on multivariate models, using the Sabre software package in R.

Item response models

Dimitris Rizopoulos from Leuven, Belgium has prepared a package ltm for Item Response Theory analyses. This package can fit the Rasch model, the two-parameter

logistic model, Birnbaum's three-parameter model, the latent trait model with up to two latent variables, and Samejima's graded response model:

med.kuleuven.be/biostat/software/software.htm#LatentIRT

Latent class models

Steve Buyske at Rutgers has prepared a library for fitting latent class models with the EM algorithm:

www.stat.rutgers.edu/home/buyske/software.html

Beta-binomial and quasi-likelihood analyses

The following shows the beta-binomial and quasi-likelihood analyses of the teratology data presented in Sec. 14.3.4, continuing with the analyses shown above at the end of the R discussion for Chapter 4. Beta-binomial modeling is an option with the vglm function in the VGAM library (using Fisher scoring) and the betabin function in the aod library. It seems that vglm in VGAM uses Fisher scoring and hence reports SE values based on the expected information matrix, whereas betabin in aod uses the observed information matrix. Quasi-likelihood with the beta-binomial type variance is available with the quasibin function in the aod library. (In the following example, the random part of the statement specifies the same overdispersion for each group). For details about the aod package, see

```
cran.r-project.org/web/packages/aod/aod.pdf
```

Again, we borrow heavily from Laura Thompson's excellent manual.

```
> group <- rats$group
> library(VGAM) # We use Thomas Yee's VGAM library
> fit.bb <- vglm(cbind(y,n-y) ~ group, betabinomial(zero=2,irho=.2),
  # two parameters, mu and rho, and zero=2 specifies 0 covariates for 2nd
  # parameter (rho); irho is the initial guess for rho in beta-bin variance.
> summary(fit.bb) # fit of beta-binomial model
Coefficients:
                Value Std. Error t value
(Intercept):1 1.3458
                        0.24412 5.5130
(Intercept):2 -1.1458
                        0.32408 -3.5355 # This is logit(rho)
             -3.1144
                        0.51818 -6.0103
group2
              -3.8681
                        0.86285 -4.4830
group3
             -3.9225
                        0.68351 -5.7387
group4
Names of linear predictors: logit(mu), logit(rho)
Log-likelihood: -93.45675 on 111 degrees of freedom
> logit(-1.1458, inverse=T)
                               # This is a function in VGAM
[1] 0.2412571
                         # The estimate of rho in beta-bin variance
```

```
> install.packages("aod")  # another way to fit beta-binomial models
> library(aod)
> betabin(cbind(y,n-y) ~ group, random=~1,data=rats)
Beta-binomial model
betabin(formula = cbind(y, n - y) ~ group, random = ~1, data = rats)
Fixed-effect coefficients:
             Estimate Std. Error z value Pr(> |z|)
(Intercept) 1.346e+00 2.481e-01 5.425e+00 5.799e-08
           -3.115e+00 5.020e-01 -6.205e+00 5.485e-10
group2
           -3.869e+00 8.088e-01 -4.784e+00 1.722e-06
group3
group4
           -3.924e+00 6.682e-01 -5.872e+00 4.293e-09
Overdispersion coefficients:
                Estimate Std. Error z value Pr(> z)
phi.(Intercept) 2.412e-01 6.036e-02 3.996e+00 3.222e-05
> quasibin(cbind(y,n-y) ~ group, data=rats) # QL with beta-bin variance
Quasi-likelihood generalized linear model
quasibin(formula = cbind(y, n - y) ~ group, data = rats)
Fixed-effect coefficients:
           Estimate Std. Error z value Pr(>|z|)
(Intercept) 1.2124 0.2233 5.4294 < 1e-4
                      0.5626 -5.9893
group2
            -3.3696
                                        < 1e-4
                                        4e-04
            -4.5853 1.3028 -3.5197
group3
           -4.2502 0.8484 -5.0097 < 1e-4
group4
Overdispersion parameter:
  phi
0.1923
Pearson's chi-squared goodness-of-fit statistic = 54.0007
```

Negative binomial and other count models

As shown above in the Chapter 4 description for R, the glm.nb function in the MASS library is a modification of the glm function to handle negative binomial regression models:

```
stat.ethz.ch/R-manual/R-patched/library/MASS/html/glm.nb.html
```

The negbin function in the aod package can also handle negative binomial regression:

```
cran.r-project.org/web/packages/aod/aod.pdf
```

Thomas Yee's VGAM package can also fit zero-inflated Poisson models and negative binomial models.

Chapter 15: Non-Model-Based Classification and Clustering

Discriminant analysis

In the MASS library there is a lda function for linear discriminant analysis and a qda function for quadratic discriminant analysis:

```
stat.ethz.ch/R-manual/R-patched/library/MASS/html/lda.html
stat.ethz.ch/R-manual/R-patched/library/MASS/html/qda.html
```

Classification trees

In the tree library,

```
cran.r-project.org/web/packages/tree/tree.pdf
```

there is a tree function for binary recursive partitioning, and a prune.tree function for pruning them.

See also the *rpart* package and its *rpart* function for recursive partitioning to construct classification trees and *prune* function for pruning them:

```
cran.r-project.org/web/packages/rpart/index.html
```

For example, for the horseshoe crab data with width and quantitative color as predictors,

```
> library(tree)
> attach(crabs)
> fit <- rpart(y ~ color + width, method="class")</pre>
> plot(fit)
> text(fit)
> printcp(fit)
Classification tree:
rpart(formula = y ~ color + width, method = "class")
Variables actually used in tree construction:
[1] color width
Root node error: 62/173 = 0.35838
n= 173
              CP nsplit rel error xerror

      2 0.080645
      1
      0.83871
      1.03226
      0.102421

      3 0.064516
      2
      0.75806
      0.96774
      0.100972

      4 0.048387
      3
      0.69355
      0.93548
      0.100149

      5 0.016129
      4
      0.64516
      0.85484
      0.097794

      6 0.010000
      6
      0.61290
      0.82258
      0.096728

> plotcp(fit)
```

```
> summary(fit)
> plot(fit, uniform=TRUE,
    main="Classification Tree for Crabs")
> pfit2 <- prune(fit, cp= 0.02)
> plot(pfit2, uniform=TRUE,
    main="Pruned Classification Tree for Crabs")
plot(pfit2, uniform=TRUE,
+ main="Pruned Classification Tree for Crabs")
> text(pfit2, use.n=TRUE, all=TRUE, cex=.8)
> post(pfit2, file = "ptree2.ps",
    title = "Pruned Classification Tree for Crabs")
post(pfit2, file = "ptree2.ps",
+ title = "Pruned Classification Tree for Crabs")
```

Cluster analysis

The dist function in R computes distances to be used in a cluster analysis:

```
stat.ethz.ch/R-manual/R-patched/library/stats/html/dist.html
```

The *method="binary"* option invokes the Jaccard-type dissimilarity distance discussed in the text. The *method="manhattan"* option invokes L1-norm distance, which for binary data is the total number of variables that do not match. The *hclust* function can perform basic hierarchical cluster analysis, using inputted distances:

```
stat.ethz.ch/R-manual/R-patched/library/stats/html/hclust.html
```

For example, for the text example on election clustering using only the states in Table 15.5, with the manhattan distance and the average linkage method for summarizing dissimilarities between clusters,

```
> x <- read.table("election.dat", header=F)
> x
  V1 V2 V3 V4 V5 V6 V7 V8 V9
   0 0 0 0 1 0 0 0
      0
         0 1 1 1
4
            0 1
5
      0
         0
            1
               1
                  1
6
   Ω
      Λ
         1
            1
               1
                  1
      1
         1
            1
               1
                  1
8
   0
      0
         0
            1
               1
                  0
         0
            1
10
                  1
      0
         0
            1
               1
                  0
  0
      Ω
         Ω
            0
               Ω
                  0 0 0
      0 0 0 0 0 0 1
13 0
14 0 0 0 0 0 0 0 0
> distances <- dist(x,method="manhattan")</pre>
> states <- c("AZ", "CA", "CO", "FL", "IL", "MA", "MN",
             "MO", "NM", "NY", "OH", "TX", "VA", "WY")
> democlust <- hclust(distances, "average")</pre>
```

```
> postscript(file="dendrogram-election.ps")
```

Chapter 16: Large- and Small-Sample Theory for Multinomial Models

See the discussion for Chapters 1-3 above for information about special R functions for small-sample confidence intervals for association measures in contingency tables.

Alessandra Brazzale has prepared the hoa package for higher-order asymptotic analyses, including approximate conditional analysis for logistic and loglinear models:

cran.r-project.org/web/packages/cond/vignettes/Rnews-paper.pdf
www.isib.cnr.it/~brazzale/lib.html

> plot(democlust, labels=states)

> graphics.off()