

$$1. R_a = \frac{12}{2} = 6 \Omega.$$

$$1ii) V_e = 12 - \frac{2}{3}(6) \\ = 8V$$

$$V_e = k_t \omega$$

$$k_t = 0.01909.$$

$$T_e = k_t I_a$$

$$= 0.0127$$

$$= 12.7 \text{ mNm}.$$

$$4. V_e = 120 - 50(0.1)$$

$$= 115V.$$

$$V_e = k_e \omega$$

$$k_e = 1.05.$$

$$V_{emf} = 120 - 90(0.1)$$

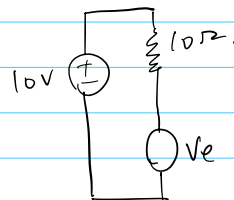
$$= 111V.$$

$$\omega = \frac{111}{1.05}$$

$$= 105.6 \text{ rad/s}$$

$$\approx 1009 \text{ RPM}.$$

$$3. k_t = 0.05 \text{ Nm/A}.$$



$$\omega = 0. \quad V_e = 0. \\ \omega \uparrow \quad V_e \uparrow.$$

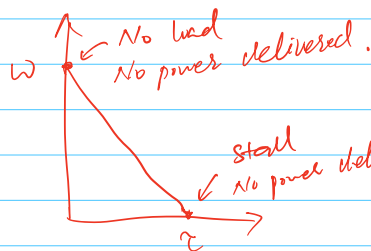
$$5. 230 - 200(0.2) = 190V.$$

$$k_e = 1.51$$

$$T_e = k_t I_a$$

$$= 302.$$

$$P_{dep} = 302 \omega.$$

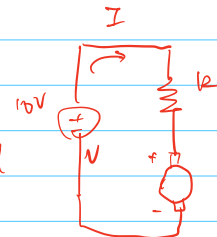


$$k_e \omega = V - IR$$

$$\omega = \frac{V}{k_e} - \frac{\tau}{k_t k_e}$$

$$\omega = \frac{V}{k_e} - \frac{R}{k_t k_e} \tau.$$

$$11 \quad R \text{ m})$$



$$E = V - IR$$

$$\tau = k_t I$$

$$E = k_e \omega$$

$$\text{Power} = \tau \omega = \tau \left(\frac{V}{k_e} - \frac{k_t k_e}{k_t + k_e} \tau \right)$$

$$= \frac{V}{k_e} \tau - \frac{k_t}{k_t + k_e} \tau^2$$

for max mechanical power.

$$\frac{dP}{d\tau} = 0$$

$$\frac{V}{k_e} - \frac{2k_t}{k_t + k_e} \tau = 0$$

$$\frac{V}{k_e} = \frac{2k_t}{k_t + k_e} \tau$$

$$V = \frac{2k_t}{k_t + k_e} \tau$$

$$\tau = \frac{V k_t}{2k_e}$$

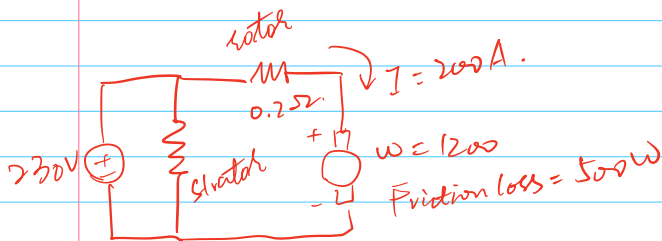
$$= \frac{10(0.05)}{2(10)}$$

$$= 0.025 \text{ Nm}$$

$$\omega = 100$$

$$\text{Power} = \tau \omega$$

5. Shunt-connected.



$$E = 230 - IR = 190 \text{ V}$$

$$\text{Electrical Power developed} = EI$$

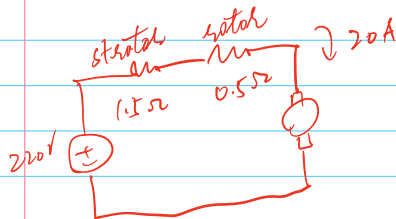
$$= 190(200) = 38000 \text{ W}$$

$$\text{Mechanical power developed}$$

$$= 38000 - 500 = 37500 \text{ W}$$

$$\tau = \frac{P}{\omega} = \frac{37500}{\frac{1200}{60} \text{ rev/s}} = 298.4 \text{ Nm}$$

6. Series Connected DC motor.



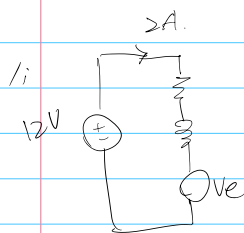
$$E = 182 \text{ V}$$

$$P = EI$$

$$= 3600 \text{ W}$$

$$P_{\text{out}} = 3450$$

$$\eta = 78.4\%$$



$$R = 6 \Omega$$

$$V_e = 12 - 6\left(\frac{2}{3}\right)$$

$$V_e = 8 \text{ V}$$

$$V_e = k_e \cdot \omega$$

$$k_e = 0.0190$$

$$T_e = k_t \cdot I_a$$

$$= 12.7 \text{ mNm}$$

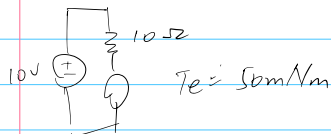
$$2. \quad V_e = k_e \cdot \omega$$

$$= 0.0190 \cdot 200 \frac{2000}{60}$$

$$= 4 \text{ V}$$

$$\frac{12 - 4}{6} = 1.33 \text{ A} = \frac{4}{3} \text{ A}$$

3.



$$V_e = V - I_a R$$

$$k_e \omega = V - \frac{T_e}{k_t} R$$

$$\omega = \frac{V}{k_e} - \frac{T_e}{k_t k_e} R$$

$$P = T_e \omega$$

$$= T_e \left(\frac{V}{k_e} - \frac{T_e}{k_t k_e} R \right)$$

$$= \frac{V}{k_e} T_e - \frac{R}{k_t k_e} T_e^2$$

$$\frac{dP}{dT_e} = \frac{V}{k_e} - \frac{2R}{k_t k_e} T_e = 0$$

$$\frac{V}{k_e} = \frac{2R}{k_t k_e} T_e$$

$$T_e = \frac{V k_t}{2R}$$

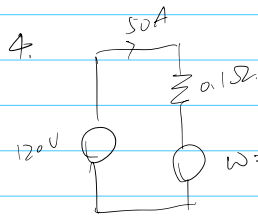
$$= \frac{10 (10 \times 10^{-3})}{2 (10)}$$

$$= 0.025 \text{ Nm}$$

torque at maximum power.

$$\omega = \frac{V}{k_e} - \frac{T_e}{k_t k_e} R$$

$$P = T_e \cdot \omega$$



$$V_e = k_e \cdot \omega$$

$$(120 - 50 \times 0.1) = k_e \cdot 2\pi \frac{1045}{60}$$

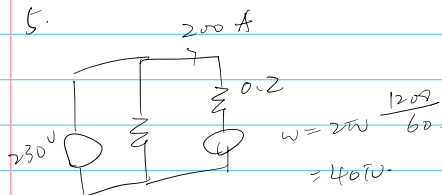
$$k_e = 1.05$$

$$V_e = k_e \cdot \omega$$

$$\omega = \frac{(120 - 30(0.1))}{1.05}$$

$$= 105.6$$

$$= 105.6 \text{ RPM.}$$



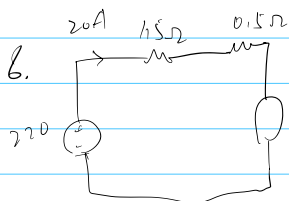
$$\text{Electrical Power} = [230 - 200(0.2)](200)$$

$$= 38000$$

$$\text{Mechanical Power} = 38000 - 500$$

$$T_e = \frac{P_m}{\omega}$$

$$= 298.4 \text{ Nm.}$$



$$V_e = 220 - 20(2)$$

$$= 180 \text{ V.}$$

$$V_e = k_e \cdot \omega$$

$$180 = k_e \cdot 2\pi \frac{1200}{60}$$

$$k_e = 1.43$$

$$T_e = k_t \cdot I_a$$

$$= 1.43(20)$$

$$= 28.64 \text{ Nm.}$$

$$P_{\text{dev}} = T_e \cdot \omega$$

$$= 3600 \text{ W.}$$

$$P_{\text{out}} = 3600 - 150$$

$$= 3450 \text{ Watt.}$$

$$\frac{3450}{220 \times 20} \times 100\% = 78.4\%$$

