

# Evolutionary learning of weighted linear composite dispatching rules for scheduling

Case study for JSP and PFSP

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# Motivation

## General Goal

General goal is how to search for *good* solutions for an arbitrary problem domain.

Automate the design of optimization algorithms.

Use of randomly sampled problem instances and their corresponding optimal vs. suboptimal solutions.



# Case Study: JSP and PFSP

## Abstract

Framework for creating dispatching rules for JSP and PFSP.

**Linear classification** to identify good dispatches from worse ones.

**Robust** for higher dimensions.

**Keywords:** Scheduling • Composite dispatching rules • JSP • PFSP  
• Evolutionary Search • Performance Measures • Scalability



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# Job Shop Scheduling (1)

## JSP

Simple job shop scheduling problem is where  $n$  jobs are scheduled on a set of  $m$  machines, subject to constraints:

- each job must follow a predefined machine order,
- that a machine can handle at most one job at a time.

**Objective:** schedule the jobs so as to minimize the maximum completion time, i.e., makespan,  $C_{\max}$ .

## PFSP

Permutation flow shop scheduling is the same as JSP except the predefined machine order is homogeneous for all jobs.

# Job Shop Scheduling (2)

## Problem space distributions used in experimental studies

|      | name  | size           | $N_{\text{train}}$ | $N_{\text{test}}$ | note           |
|------|---|----------------|--------------------|-------------------|----------------|
| PFSP | $\mathcal{P}_{f, \text{rnd}}^{6 \times 5}$    | $6 \times 5$   | 500                | —                 | random         |
|      | $\mathcal{P}_{f, \text{rndn}}^{6 \times 5}$   | $6 \times 5$   | 500                | —                 | random-narrow  |
|      | $\mathcal{P}_{f, \text{jc}}^{6 \times 5}$     | $6 \times 5$   | 500                | —                 | job-correlated |
|      | $\mathcal{P}_{f, \text{rnd}}^{10 \times 10}$  | $10 \times 10$ | —                  | 500               | random         |
|      | $\mathcal{P}_{f, \text{rndn}}^{10 \times 10}$ | $10 \times 10$ | —                  | 500               | random-narrow  |
|      | $\mathcal{P}_{f, \text{jc}}^{10 \times 10}$   | $10 \times 10$ | —                  | 500               | job-correlated |
|      |   |                |                    |                   |                |
| JSP  | $\mathcal{P}_{j, \text{rnd}}^{6 \times 5}$    | $6 \times 5$   | 500                | —                 | random         |
|      | $\mathcal{P}_{j, \text{rndn}}^{6 \times 5}$   | $6 \times 5$   | 500                | —                 | random-narrow  |
|      | $\mathcal{P}_{j, \text{rnd}}^{10 \times 10}$  | $10 \times 10$ | —                  | 500               | random         |
|      | $\mathcal{P}_{j, \text{rndn}}^{10 \times 10}$ | $10 \times 10$ | —                  | 500               | random-narrow  |
|      |   |                |                    |                   |                |



# Job Shop Scheduling (3)

## Dispatching rules (DR) for constructing JSSP

Starts with an empty schedule and adds on one job at a time.

When a machine is free the DR inspects the waiting/available jobs and selects the job with the **highest priority**.

Complete schedule consists of  $\ell = n \times m$  sequential dispatches.

At each dispatch  $k$  features  $\phi(k)$  for the temporal schedule are calculated.

Performance of DR is compared with its optimal makespan, as percentage relative deviation from optimality:  $\rho = \frac{C_{\max}^{DR} - C_{\max}^{opt}}{C_{\max}^{opt}} \cdot 100\%$

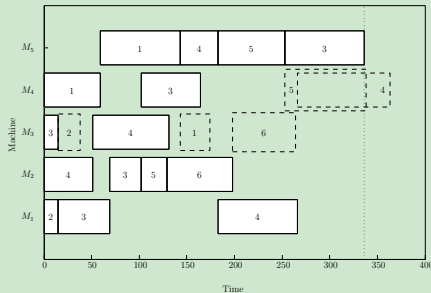
# Job Shop Scheduling (4)

## Features for JSSP

| $\phi$      | Feature description  |
|-------------|--|
| $\phi_1$    | processing time for job on machine                               |
| $\phi_2$    | start-time   |
| $\phi_3$    | end-time   |
| $\phi_4$    | when machine is next free  |
| $\phi_5$    | current makespan   |
| $\phi_6$    | work remaining   |
| $\phi_7$    | most work remaining  |
| $\phi_8$    | slack time for this particular machine                           |
| $\phi_9$    | slack time for all machines                                      |
| $\phi_{10}$ | slack time weighted w.r.t. number of operations already assigned |
| $\phi_{11}$ | time job had to wait   |
| $\phi_{12}$ | size of slot created by assignment                               |
| $\phi_{13}$ | total processing time for job                                    |

# Job Shop Scheduling

## Example



A schedule being built at step  $k = 16$ . The dashed boxes represent five different possible jobs that could be scheduled next using a DR.



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# Evolutionary search

Instead of using logistic regression for to find the weights  $\mathbf{w}$  for linear preference function:

$$h(\phi) = \sum_{i=1}^d w_i \phi = \langle \mathbf{w} \cdot \phi \rangle.$$

a widely-used evolutionary algorithm, Covariance Matrix Adaptation Evolution Strategy (**CMA-ES**), is applied directly on the desired objective function. For this study both, a) expected relative error,  $\mathbb{E}[\rho]$ ; and b) final makespan,  $\mathbb{E}[C_{\max}]$ , will be considered.

**Benefit** No need to collect training data beforehand.

**Drawback** Computationally expensive to evaluate  $\mathbb{E}[\cdot]$



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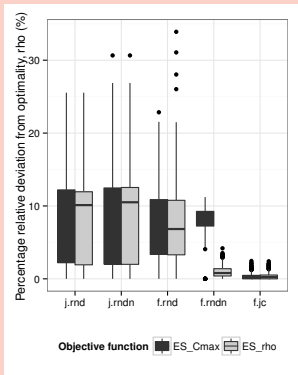
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# Experiments (1)

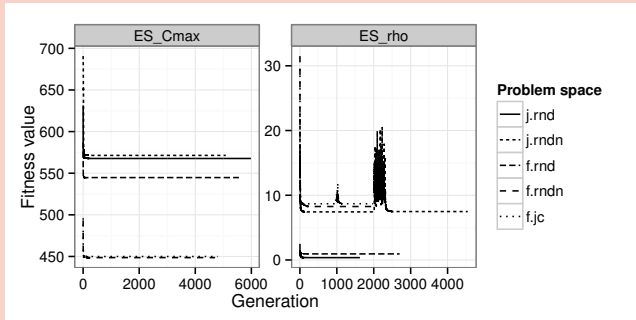
## Fitness for optimising with CMA-ES



Box-plot of training data for percentage relative deviation from optimality,  $\rho$ , when implementing the final weights obtained from CMA-ES optimisation, using both obj. functions,  $\mathbb{E}[C_{\max}]$  and  $\mathbb{E}[\rho]$ .

## Experiments (2)

### Fitness for optimising with CMA-ES

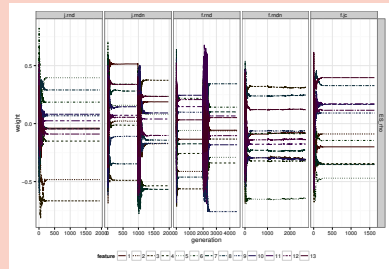
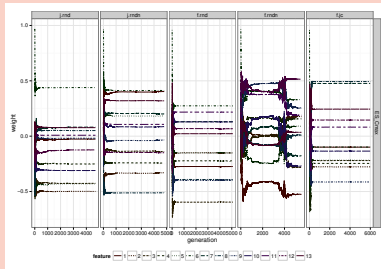


Fitness for minimising w.r.t.  $C_{\max}$  and  $\rho$ , per generation of CMA-ES.



# Experiments (3)

## Evolution of weights of features



Evolution of weights of **FEATURES** at each generation of the CMA-ES optimisation, for minimisation w.r.t.  $C_{\max}$  (left) and  $\rho$  (right).



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# Summary and conclusions (1)

Introduced a framework for learning linear composite dispatch rules for scheduling.

The approach finds linear weights by **direct optimisation with CMA-ES**.

The method significantly outperforms SDRs from the literature, and authors' previous work which were based on preference learning.

## Summary and conclusions (2)

### CMA-ES optimisation

#### Benefits:

Does not rely on optimal solutions – although if known, they can help getting out of local minima.

Scalable – model based on  $6 \times 5$  successfully applied to  $10 \times 10$ .

#### Drawbacks:

Computationally expensive.

Limited to linear preference function  $h(\cdot)$



## Summary and conclusions (3)

### Future work

Facilitate evolutionary search by use of surrogate models which indirectly estimate mean expected error w.r.t. current population without loss in performance

Thank you for your attention



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Questions?

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