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## ALICE

### Analysis & Learning Iterative Consecutive Executions

Helga Ingimundardóttir

University of Iceland

June 30, 2016



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## Motivation:

- ★ The general goal is to train optimisation algorithms, for an arbitrary problem domain, using data.

## Contribution:

- ★ The main contribution of this thesis is towards a better understanding of how this training data should be constructed.

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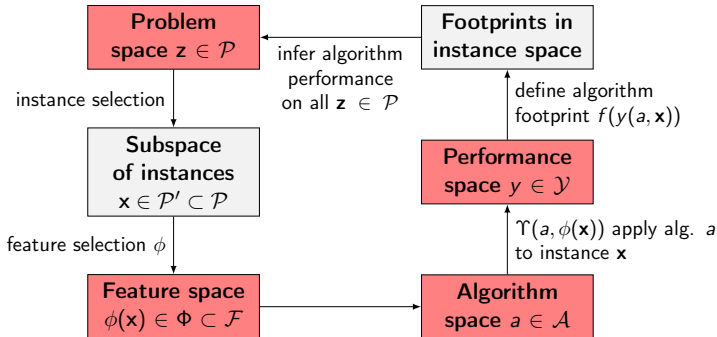
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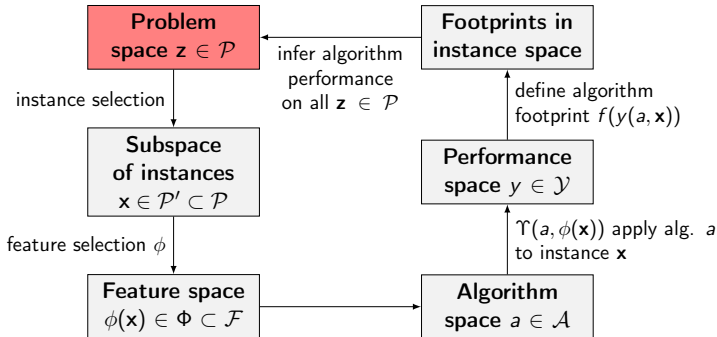
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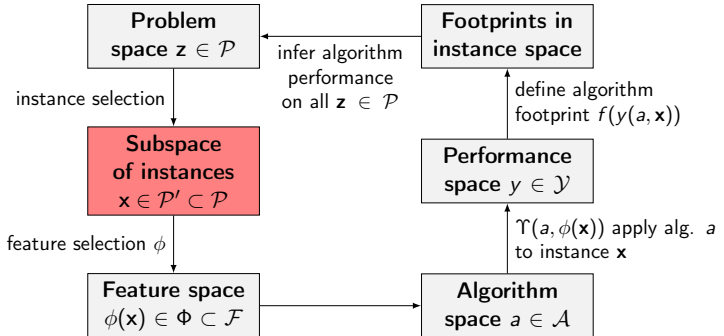
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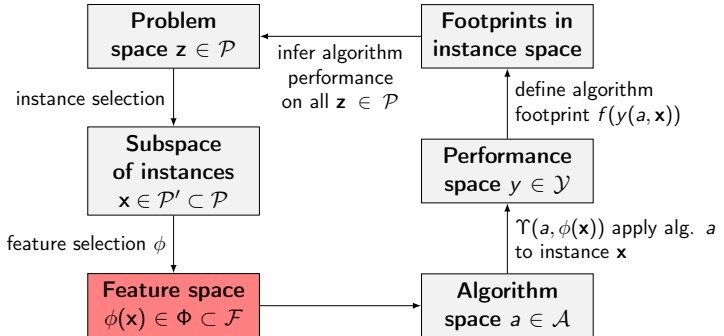
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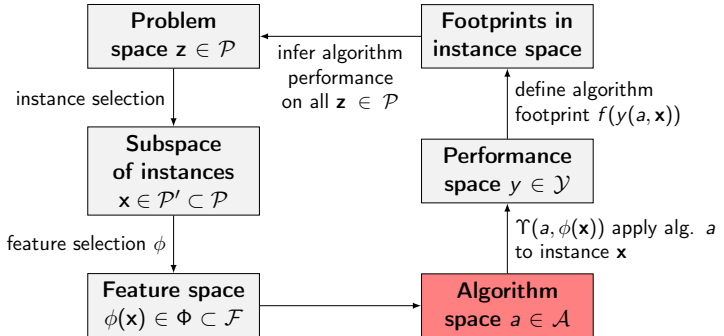
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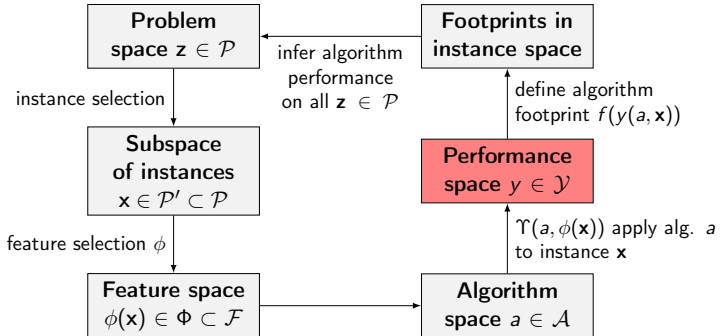
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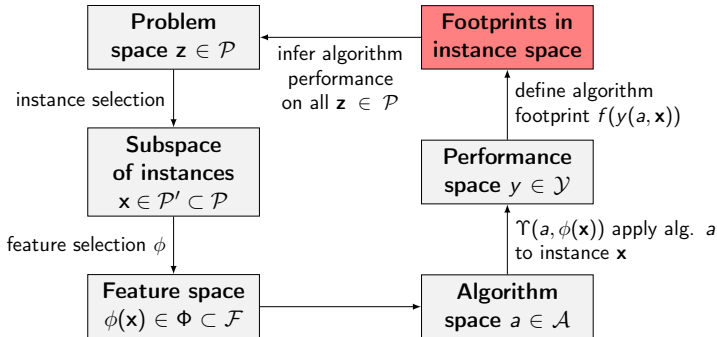
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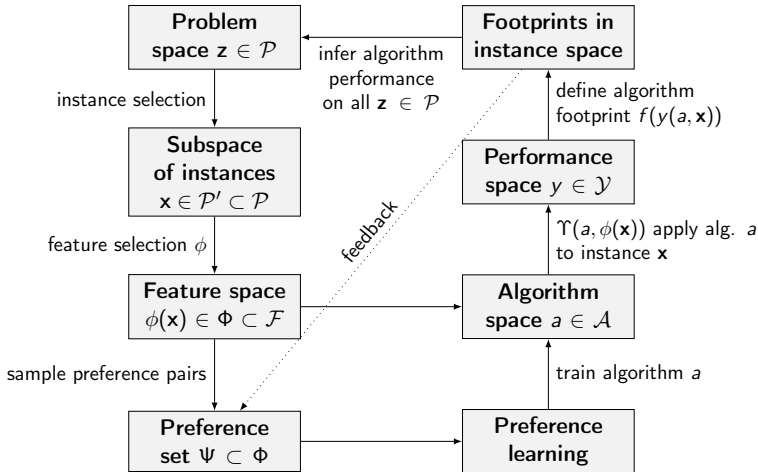
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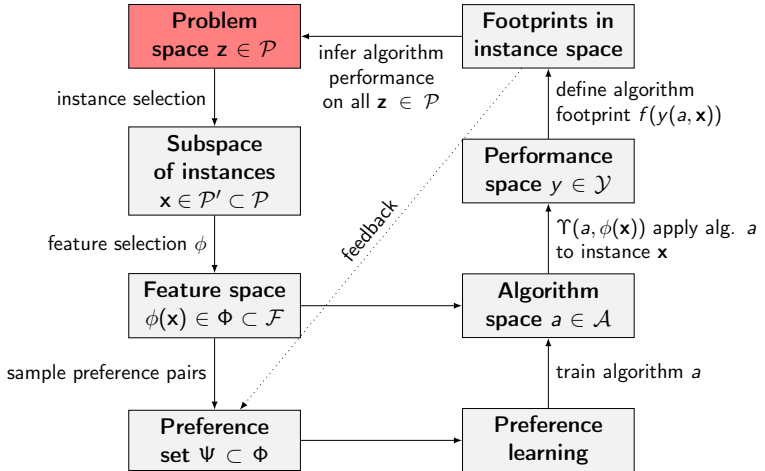
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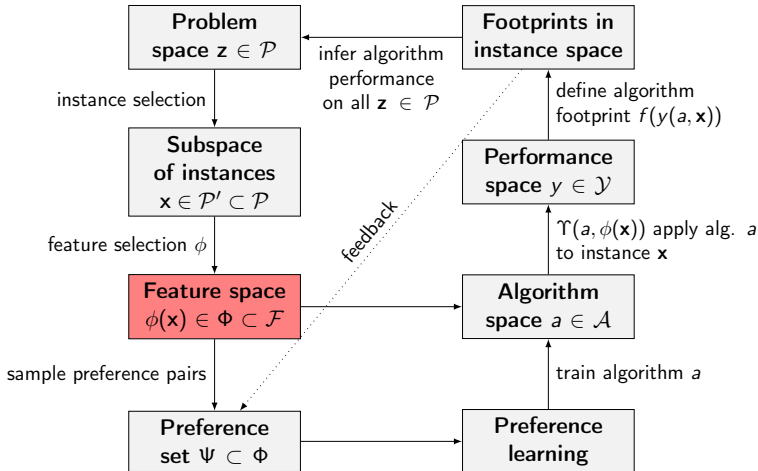
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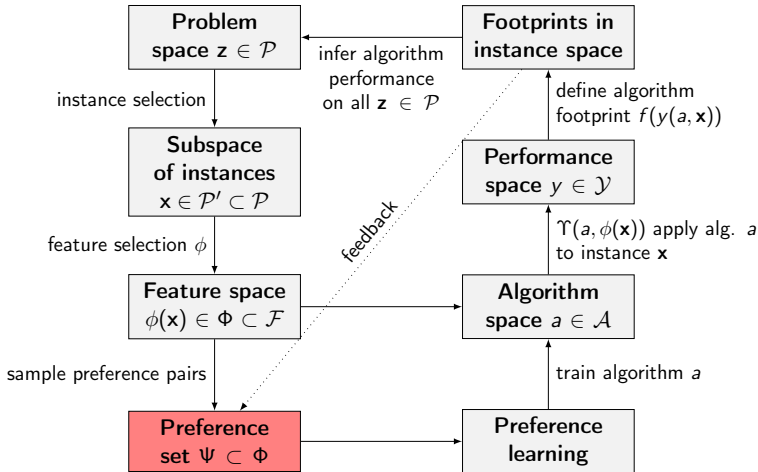
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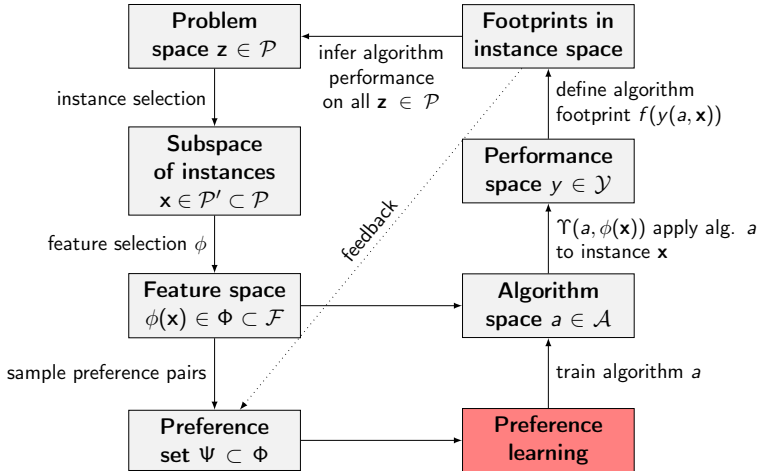
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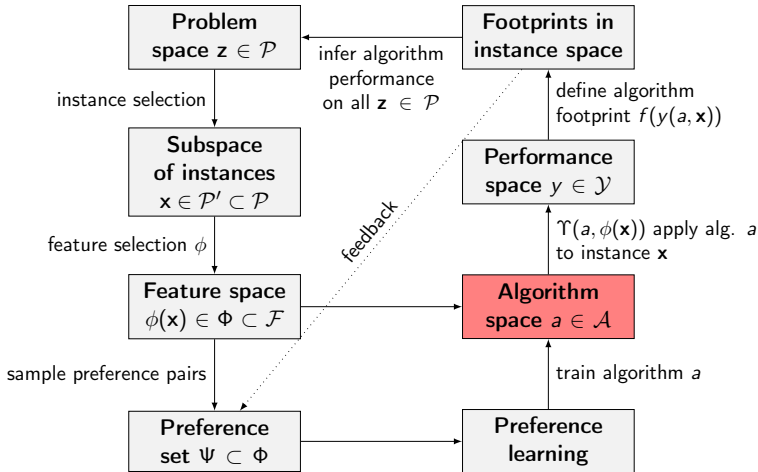
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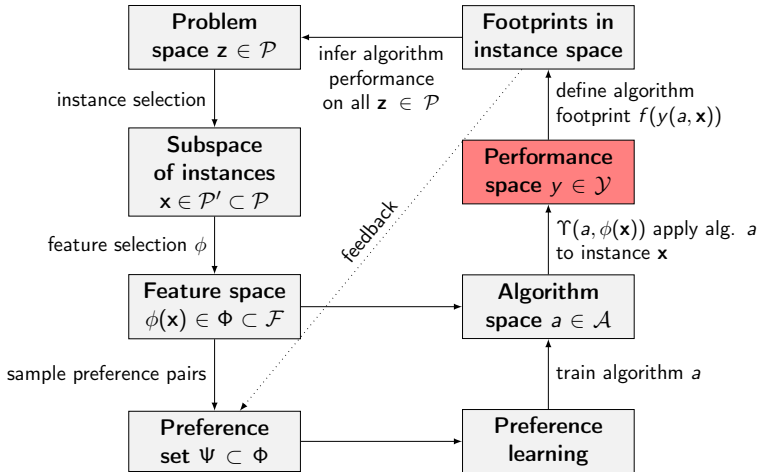
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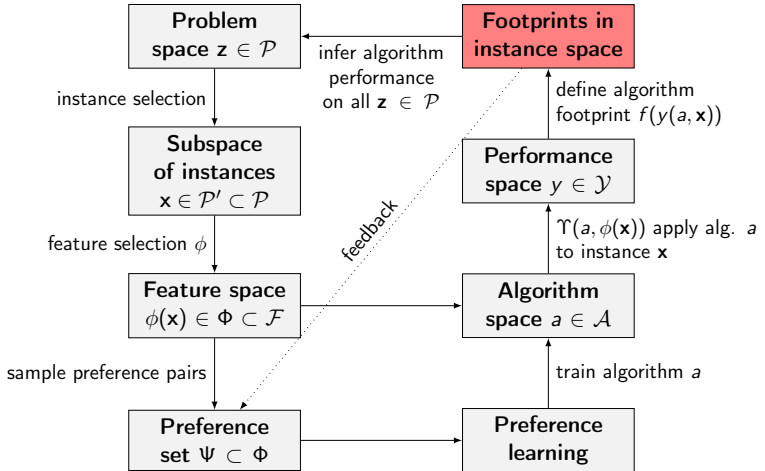
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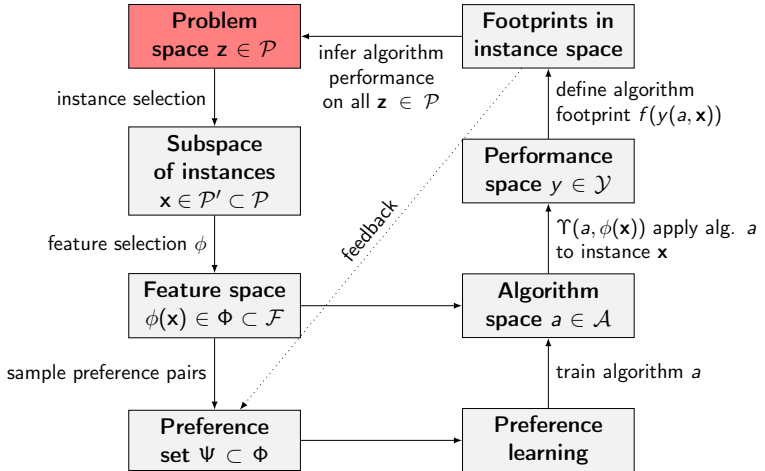
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The attending guests: They all have to:

$J_1$ ) Alice

$J_2$ ) March Hare

$J_3$ ) Dormouse

$J_4$ ) Mad Hatter.

$M_1$ ) have wine or pour tea

$M_2$ ) spread butter

$M_3$ ) get a haircut

$M_4$ ) check the time of the broken watch

$M_5$ ) say what they mean.

This can be considered as is a typical  $4 \times 5$  job-shop, where:

- ★ our guests are the jobs
- ★ their tasks are the machines
- ★ objective is to minimise  $C_{\max}$  (when Alice can leave).



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- |                    |   |
|--------------------|---|
| $J_1)$ Alice       | $M_1)$ have wine or pour tea              |
| $J_2)$ March Hare  | $M_2)$ spread butter                      |
| $J_3)$ Dormouse    | $M_3)$ get a haircut                      |
| $J_4)$ Mad Hatter. | $M_4)$ check the time of the broken watch |
|                    | $M_5)$ say what they mean.                |

This can be considered as is a typical  $4 \times 5$  job-shop, where:

- ★ our guests are the jobs
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# Mad Hatter tea-party ( $k$ -solutions)

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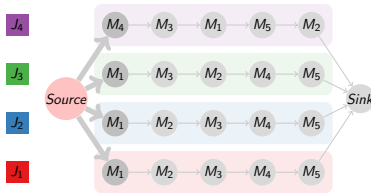
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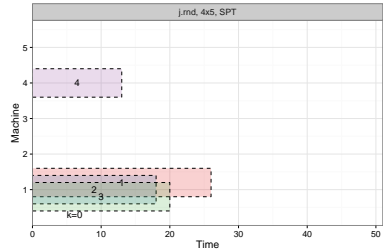
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Start:  $k = 0$



**Figure:** Disjunctive graph



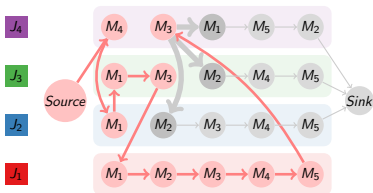
**Figure:** Gantt chart

# Mad Hatter tea-party ( $k$ -solutions)

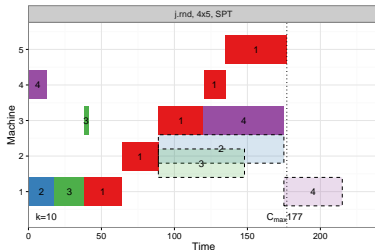
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Midway:  $k = 10$



**Figure:** Disjunctive graph



**Figure:** Gantt chart

# Mad Hatter tea-party ( $k$ -solutions)

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Finish:  $k = 20$

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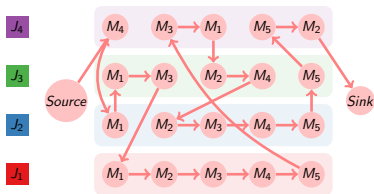
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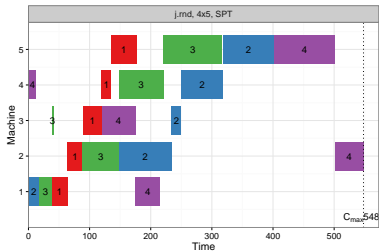
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**Figure:** Disjunctive graph



**Figure:** Gantt chart

# Mad Hatter tea-party ( $K$ -solutions)

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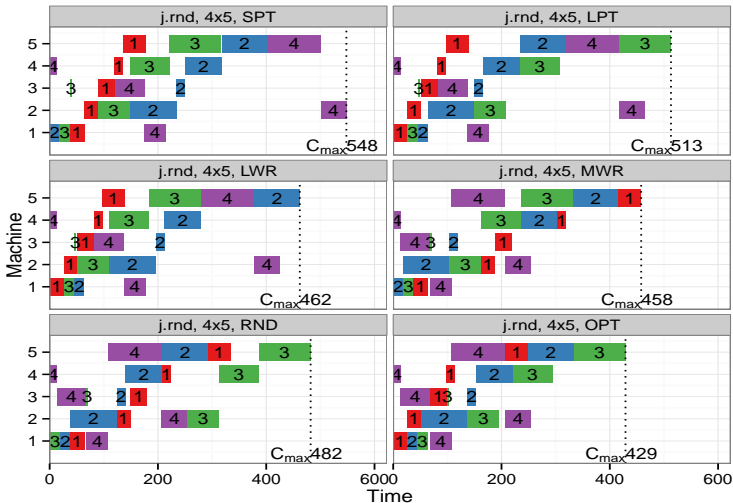
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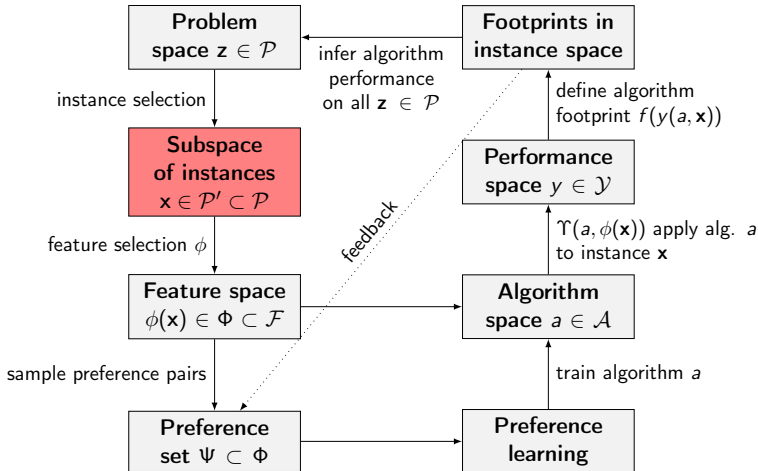
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# Problem instance generators

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	name	size ( $n \times m$ )	$N_{\text{train}}$	$N_{\text{test}}$	note
JSP	$\mathcal{P}_{j.\text{rnd}}^{6 \times 5}$	$6 \times 5$	500	500	random
	$\mathcal{P}_{j.\text{rndn}}^{6 \times 5}$	$6 \times 5$	500	500	random-narrow
	$\mathcal{P}_{j.\text{rnd}, J_1}^{6 \times 5}$	$6 \times 5$	500	500	random with job variation
	$\mathcal{P}_{j.\text{rnd}, M_1}^{6 \times 5}$	$6 \times 5$	500	500	random with machine variation
	$\mathcal{P}_{j.\text{rnd}}^{10 \times 10}$	$10 \times 10$	300	200	random
	$\mathcal{P}_{j.\text{rndn}}^{10 \times 10}$	$10 \times 10$	300	200	random-narrow
	$\mathcal{P}_{j.\text{rnd}, J_1}^{10 \times 10}$	$10 \times 10$	300	200	random with job variation
	$\mathcal{P}_{j.\text{rnd}, M_1}^{10 \times 10}$	$10 \times 10$	300	200	random with machine variation
	$\mathcal{P}_{\text{JSP.ORLIB}}$	various	–	82	various
FSP	$\mathcal{P}_{f.\text{rnd}}^{6 \times 5}$	$6 \times 5$	500	500	random
	$\mathcal{P}_{f.\text{rndn}}^{6 \times 5}$	$6 \times 5$	500	500	random-narrow
	$\mathcal{P}_{f.\text{jc}}^{6 \times 5}$	$6 \times 5$	500	500	job-correlated
	$\mathcal{P}_{f.\text{mc}}^{6 \times 5}$	$6 \times 5$	500	500	machine-correlated
	$\mathcal{P}_{f.\text{mxc}}^{6 \times 5}$	$6 \times 5$	500	500	mixed-correlation
	$\mathcal{P}_{f.\text{rnd}}^{10 \times 10}$	$10 \times 10$	300	200	random
	$\mathcal{P}_{\text{FPS.ORLIB}}$	various	–	31	various

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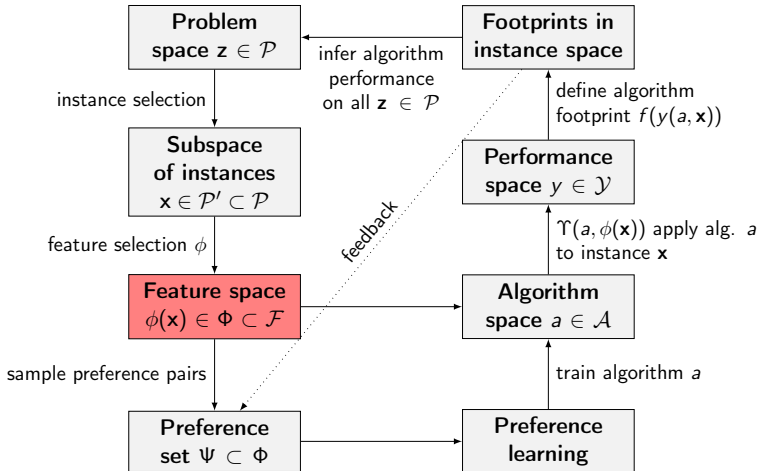
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job	$\phi_1$	job processing time
	$\phi_2$	job start-time
	$\phi_3$	job end-time
	$\phi_4$	job arrival time
	$\phi_5$	time job had to wait
	$\phi_6$	total processing time for job
	$\phi_7$	total work remaining for job
	$\phi_8$	number of assigned operations for job
machine	$\phi_9$	when machine is next free
	$\phi_{10}$	total processing time for machine
	$\phi_{11}$	total work remaining for machine
	$\phi_{12}$	number of assigned operations for machine
	$\phi_{13}$	change in idle time by assignment
	$\phi_{14}$	total idle time for machine
	$\phi_{15}$	total idle time for all machines
	$\phi_{16}$	current makespan
final makespan	$\phi_{17}$	final makespan using SPT
	$\phi_{18}$	final makespan using LPT
	$\phi_{19}$	final makespan using LWR
	$\phi_{20}$	final makespan using MWR
	$\phi_{\text{RND}}$	final makespans using 100 random rollouts
	$\phi_{21}$	mean for $\phi_{\text{RND}}$
	$\phi_{22}$	standard deviation for $\phi_{\text{RND}}$
	$\phi_{23}$	minimum value for $\phi_{\text{RND}}$
	$\phi_{24}$	maximum value for $\phi_{\text{RND}}$

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# Trajectory strategies for $\phi$

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Conclusions

Following the **policy**:

- ★  $(\phi^{\text{OPT}})$  expert  $\pi_*$ .
- ★  $(\phi^{\text{SPT}})$  shortest processing time (SPT).
- ★  $(\phi^{\text{LPT}})$  longest processing time (LPT).
- ★  $(\phi^{\text{LWR}})$  least work remaining (LWR).
- ★  $(\phi^{\text{MWR}})$  most work remaining (MWR).
- ★  $(\phi^{\text{RND}})$  random policy (RND).
- ★  $(\phi^{\text{ES.}\rho})$  the policy obtained by optimising with CMA-ES.
- ★  $(\phi^{\text{ALL}})$  union of all of the above.

# Trajectory strategies for $\phi$

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- ★  $(\Phi^{\text{LWR}})$  least work remaining (LWR).
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- ★  $(\Phi^{\text{RND}})$  random policy (RND).
- ★  $(\Phi^{\text{ES}.\rho})$  the policy obtained by optimising with CMA-ES.
- ★  $(\Phi^{\text{ALL}})$  union of all of the above.

# Trajectory strategies for $\Phi$

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Following the **policy**:

- ★  $(\Phi^{\text{OPT}})$  expert  $\pi_*$ .
- ★  $(\Phi^{\text{SPT}})$  shortest processing time (SPT).
- ★  $(\Phi^{\text{LPT}})$  longest processing time (LPT).
- ★  $(\Phi^{\text{LWR}})$  least work remaining (LWR).
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$(6 \times 5, N_{train} = 500)$

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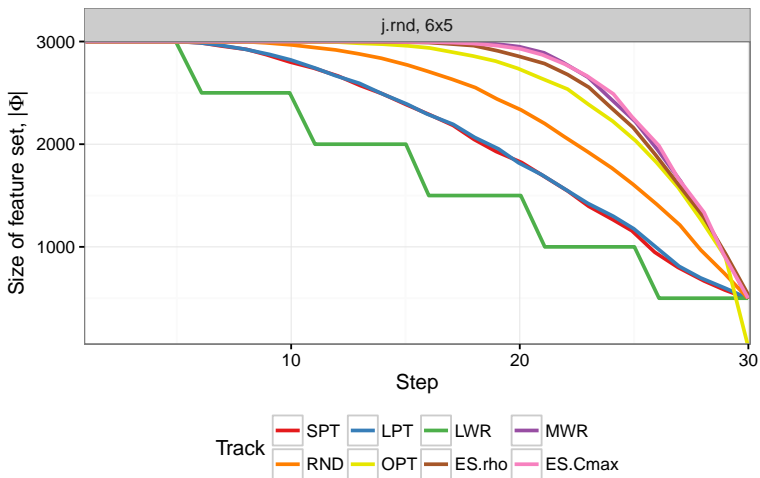
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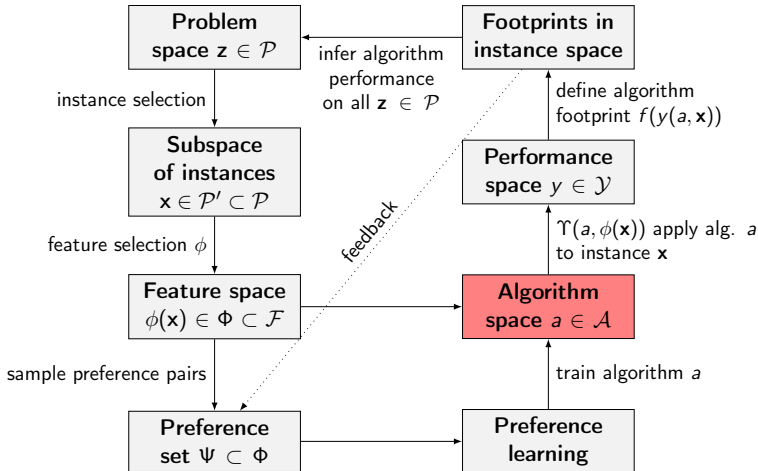
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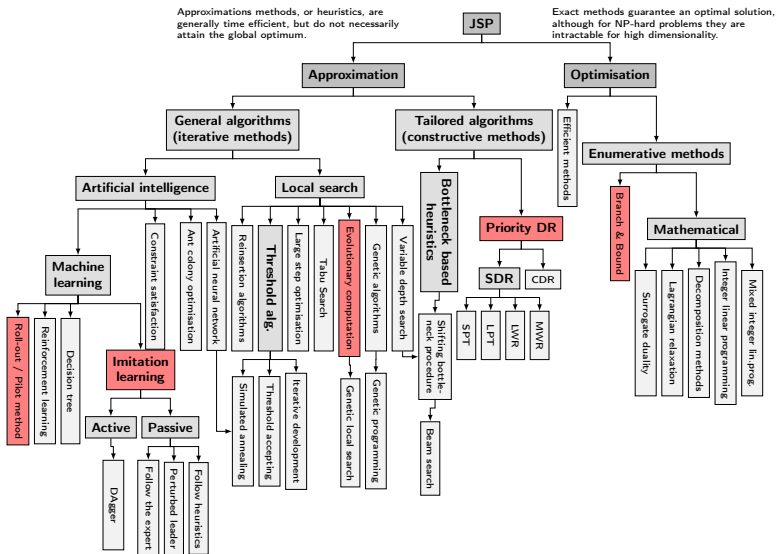
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# Various Methods for Solving JSP

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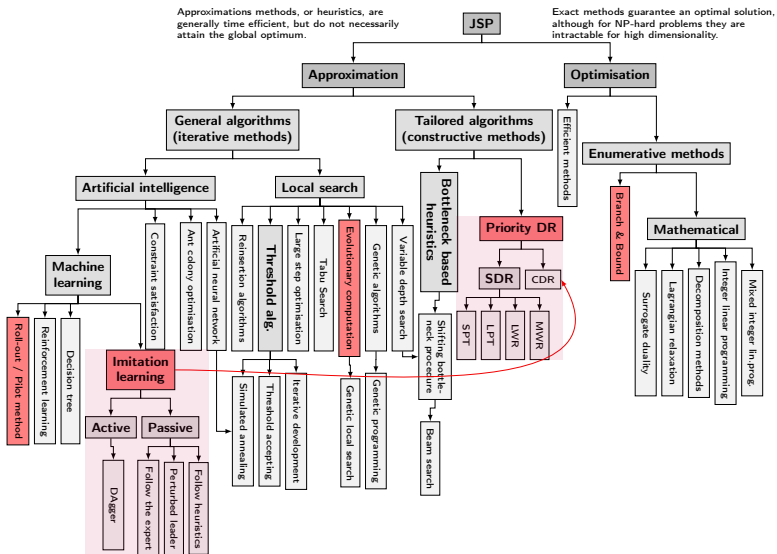
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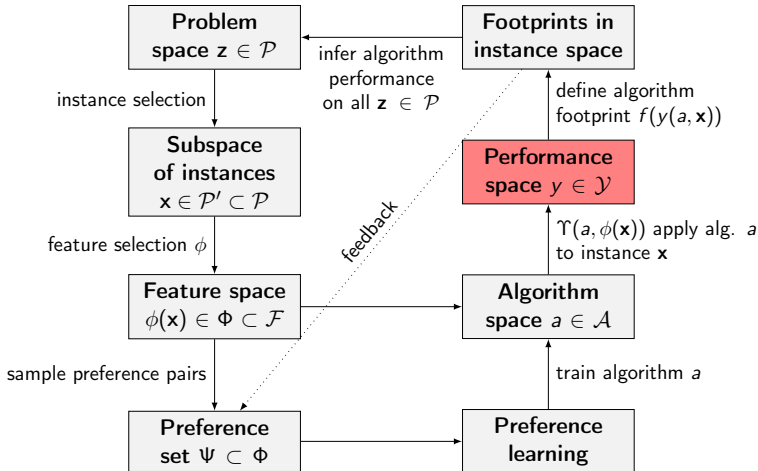
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Performance of policy  $\pi$  compared with its optimal makespan, found using an expert policy,  $\pi_*$ , is the following loss function:

$$\rho = \frac{C_{\max}^{\pi} - C_{\max}^{\pi_*}}{C_{\max}^{\pi_*}} \cdot 100\%$$

The goal is to minimise this discrepancy between **predicted** value and **true** outcome.

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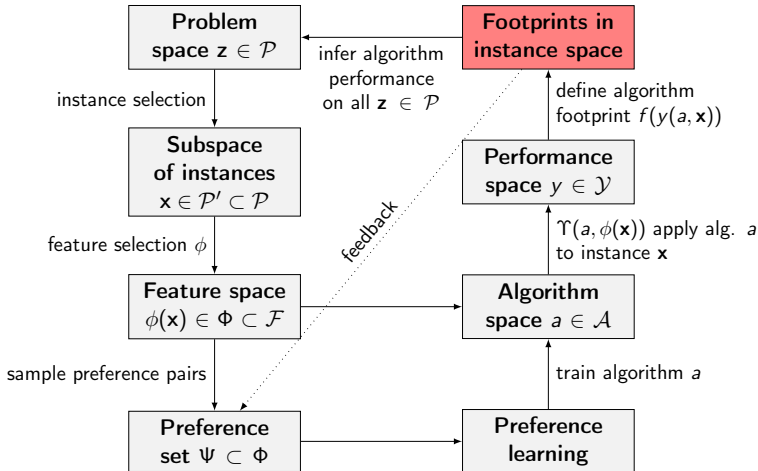
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# Deviation from optimality, $\rho$

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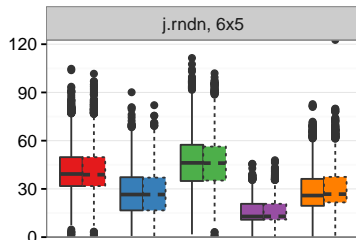
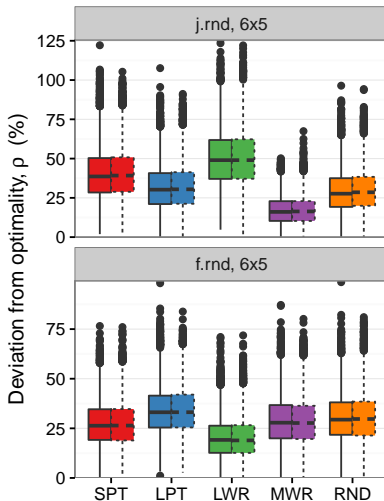
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Simple dispatching rule

- Shortest Processing Time
- Longest Processing Time
- Least Work Remaining
- Most Work Remaining
- Random dispatches

Data set



# Deviation from optimality, $\rho$

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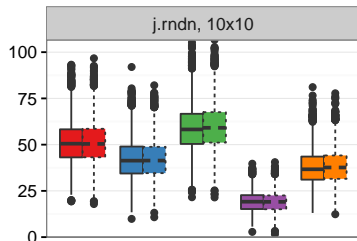
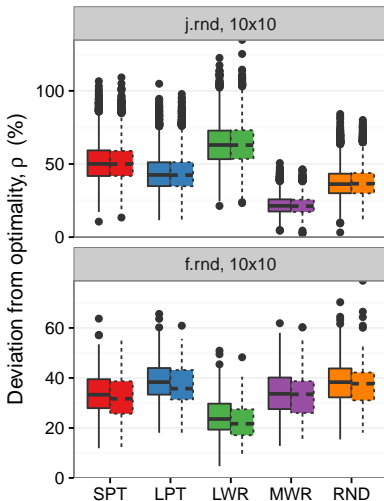
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## Simple dispatching rule

- Shortest Processing Time
- Longest Processing Time
- Least Work Remaining
- Most Work Remaining
- Random dispatches

## Data set

- train
- test

# Making optimal decisions, $\xi_{\pi}^{\star}$

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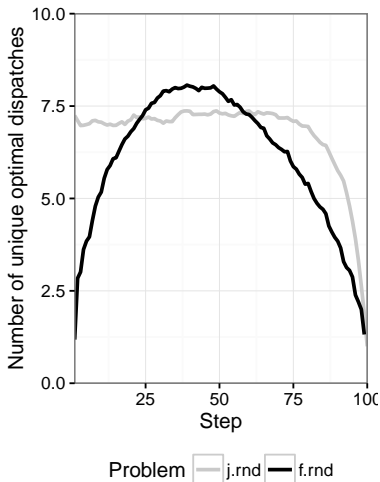
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# Making optimal decisions, $\xi_{\pi}^{\star}$

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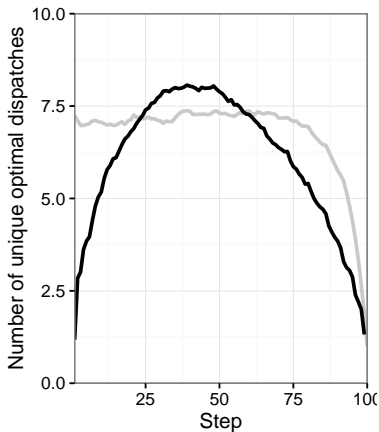
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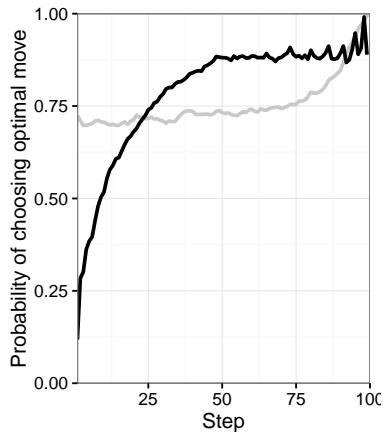
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Problem    j.rnd    f.rnd



Problem    j.rnd    f.rnd

# Probability of SDR being optimal, $\xi_{\langle \text{SDR} \rangle}^*$

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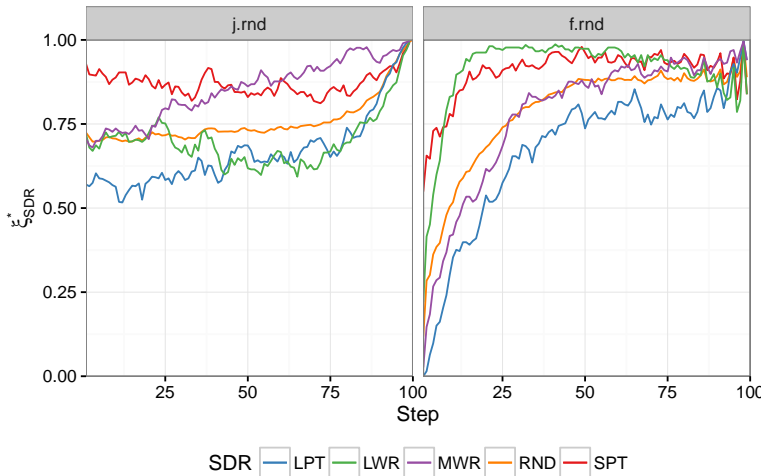
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# Blended dispatching rule

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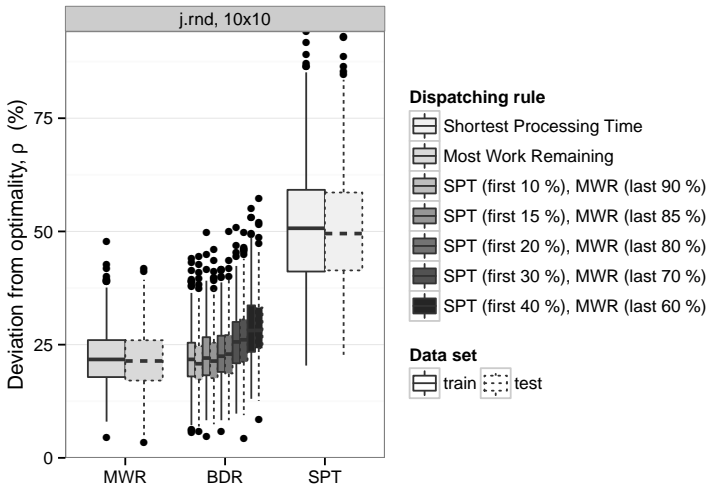
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# Impact of suboptimal decision, $\{\zeta_{\min}^*, \zeta_{\max}^*\}$

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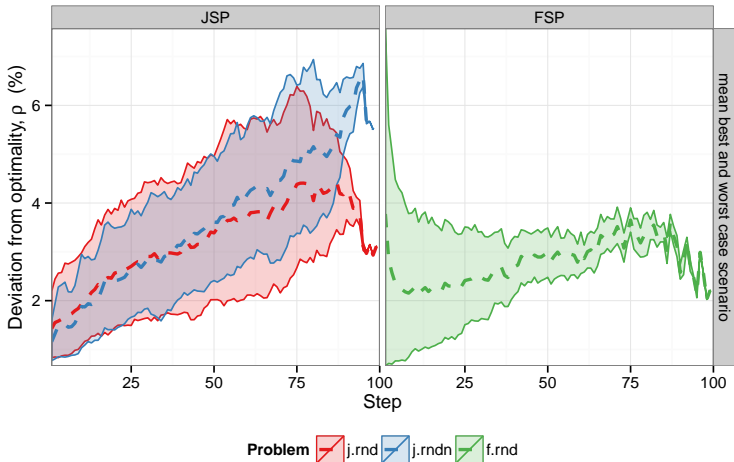
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# Probability of SDR being optimal, $\xi_{\langle \text{SDR} \rangle}$

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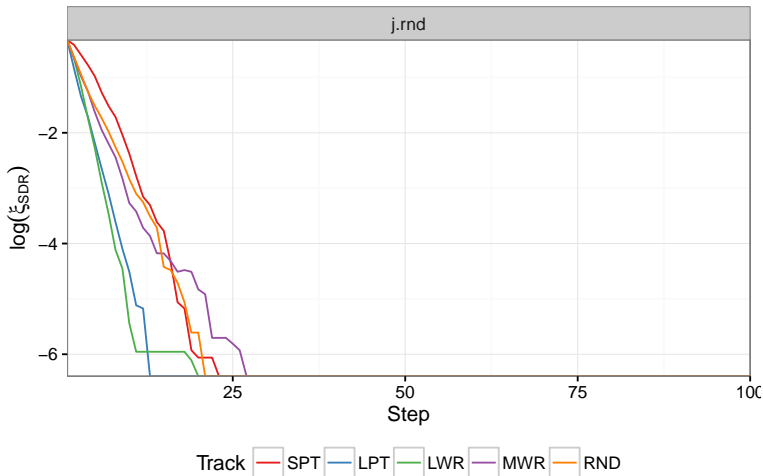
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# Impact of suboptimal decision, $\{\zeta_{\min}^{\pi}, \zeta_{\max}^{\pi}\}$

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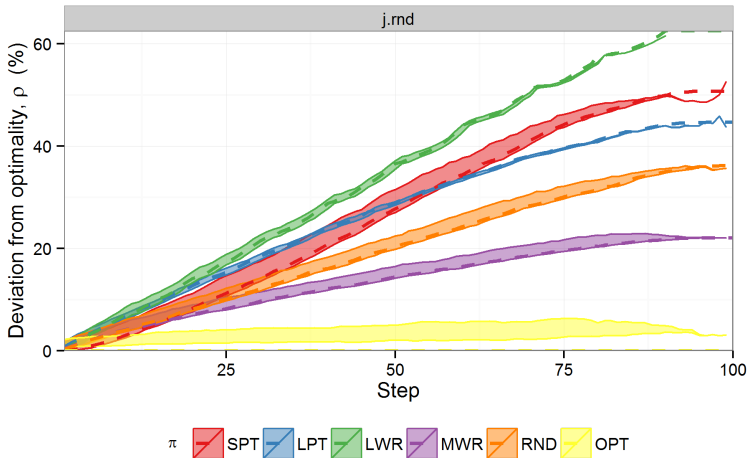
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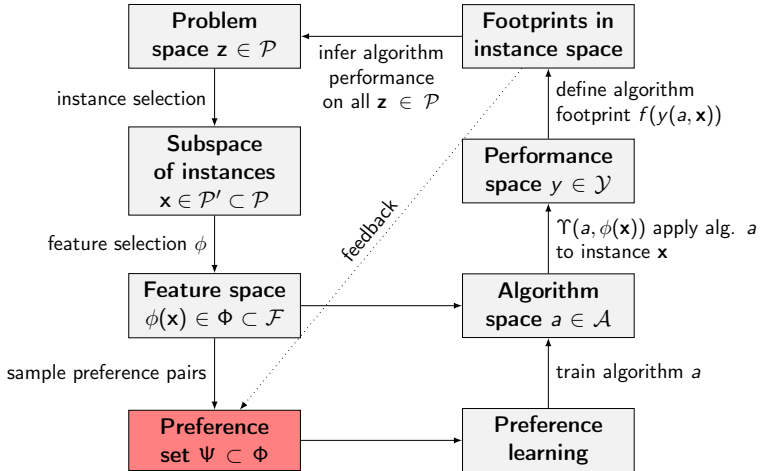
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ALICE framework for creating dispatching rules:

- ★ **Linear classification** to identify good dispatches, from worse ones.
- ★ Generate feature set,  $\Phi \subset \mathcal{F}$ , both from
  - ★ optimal solutions,  $\phi^o$
  - ★ suboptimal solutions,  $\phi^s$by exploring various trajectories within the feature-space (where  $\phi^o, \phi^s \in \mathcal{F}$ ).
- ★ Sample  $\Phi$  to create training set  $\Psi$  with rank pairs:
  - ★ optimal decision,  $(z^o, y_o) = (\phi^o - \phi^s, +1)$
  - ★ suboptimal decision,  $(z^s, y_s) = (\phi^s - \phi^o, -1)$using different ranking schemes (where  $z^o, z^s \in \Psi$ )
- ★ Sample  $\Psi$  using stepwise bias for time independent policy.

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# Sampled size of $|\Phi(k)|$

$(6 \times 5, N_{train} = 500)$

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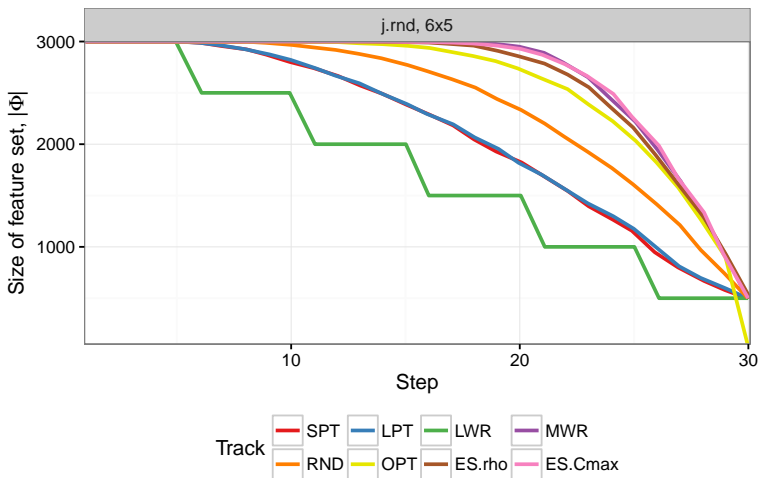
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# Sampled size of $|\Psi(k)|$ ( $6 \times 5$ , $N_{train} = 500$ )

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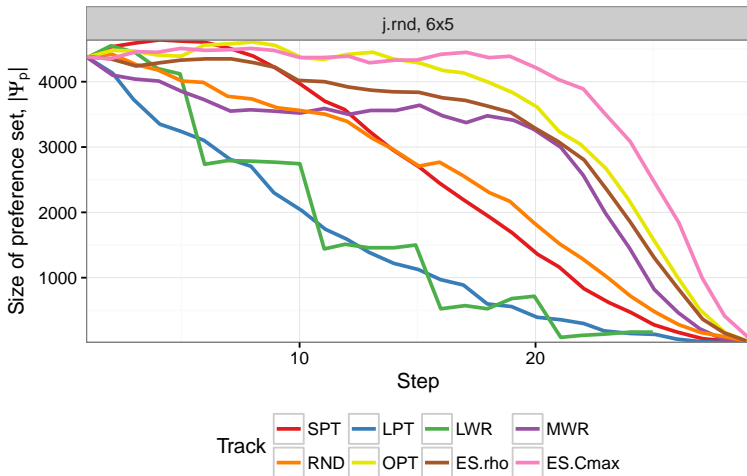
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# Stepwise bias strategies

( $6 \times 5$ ,  $N_{train} = 500$ )

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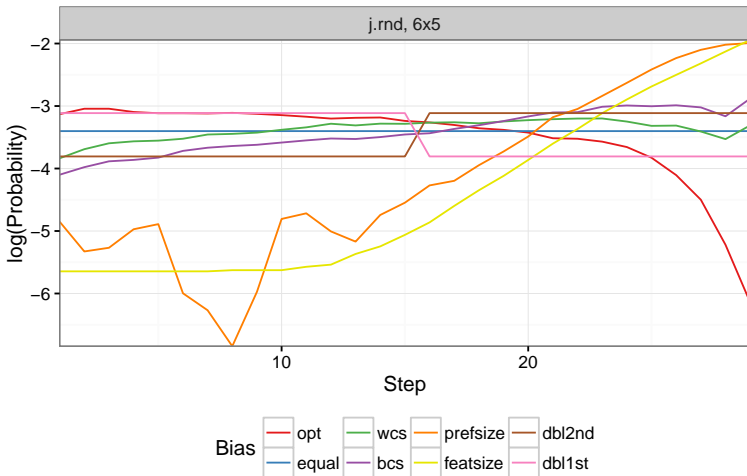
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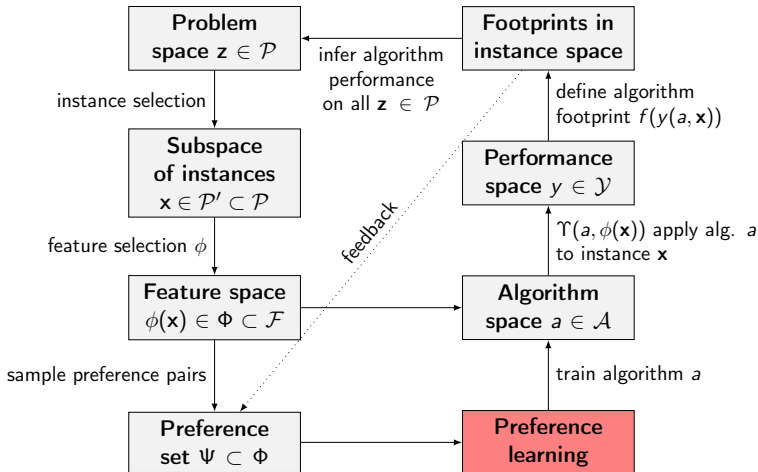
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Preference learning:

- ★ Mapping of points to ranks:  $\{h(\cdot) : \Phi \mapsto Y\}$  where

$$\phi_o \succ \phi_s \iff h(\phi_o) > h(\phi_s)$$

- ★ The preference is defined by a linear function:

$$h(\phi) = \langle w_i \cdot \phi \rangle$$

optimised w.r.t.  $w$  based on training data  $\Psi$

- ★ Note: Limitations in approximation function to capture the complex dynamics incorporated in optimal trajectories.



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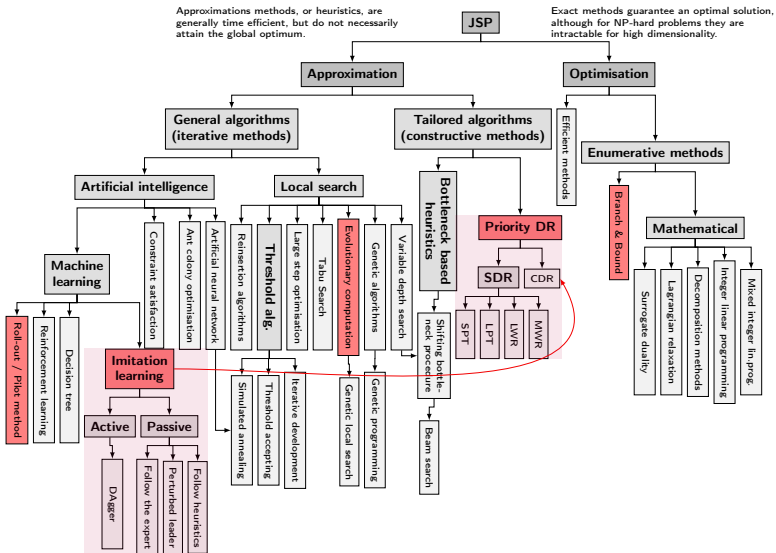
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Passive imitation learning (single pass):

- ★ Prediction with expert advice,  $\pi_\star$
- ★ Follow the perturbed leader ( $\text{OPT}_\epsilon$ )
- ★ Follow a heuristic (e.g. SDRs).



# Passive imitation learning

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# Passive imitation learning

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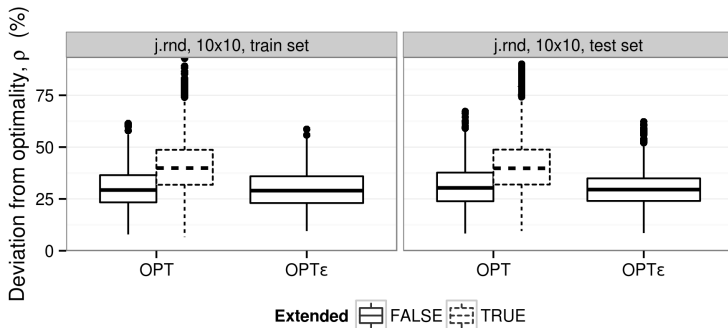
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Conclusions

Passive imitation learning (single pass):

- ★ Prediction with expert advice,  $\pi_*$
- ★ Follow the perturbed leader ( $\text{OPT}_\epsilon$ )
- ★ Follow a heuristic (e.g. SDRs).





# Active imitation learning

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Active imitation learning (**iterative**):

★ Dataset Aggregation (DAgger)

$$\pi_i = \beta_i \pi_\star + (1 - \beta_i) \hat{\pi}_{i-1}$$

where  $\hat{\pi}_{i-1}$  is the previous learned model, and  $\hat{\pi}_i$  learns on aggregated dataset of all previous iterations.



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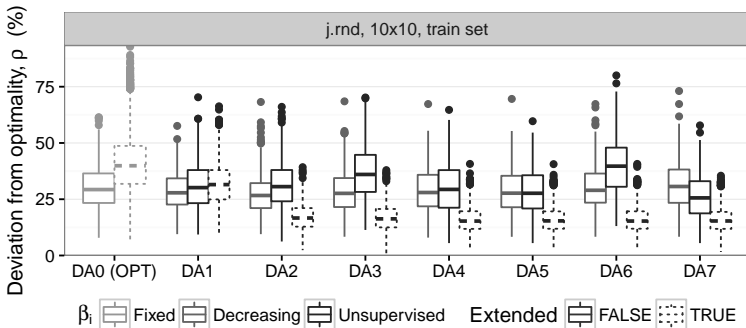
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# Deviation from optimality, $\rho$

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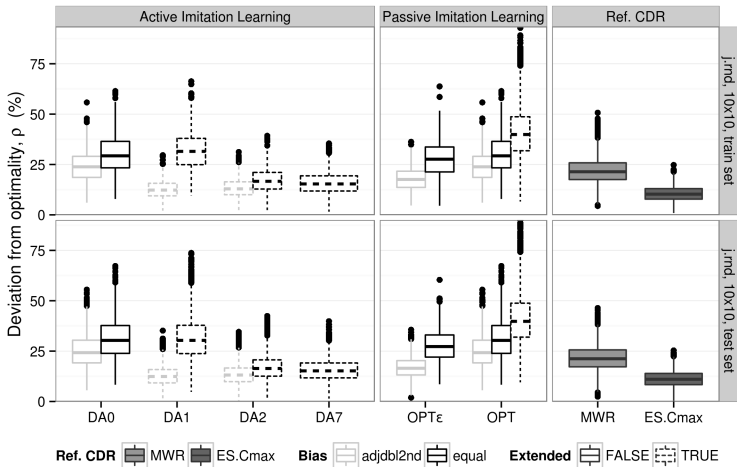
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# Framework for Algorithm Learning

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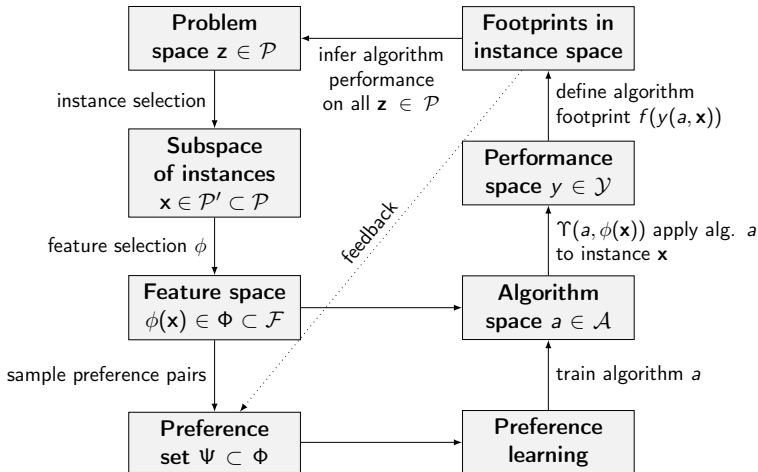
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The thesis introduced a framework for learning (**linear**) composite priority dispatching rule – using **job-shop** as a case-study – with the following guidelines:

- ★ For a given problem domain, use a suitable problem generator to train and test on.
- ★ Define features to grasp the essence of visited  $k$ -solutions
- ★ Success is highly dependent on the preference pairs introduced to the system:

- ★  $\Psi_p$  reduces the preference set without loss of performance.
- ★ Stepwise bias is needed to balance time dependent  $\Psi_p$  in order to create time independent models.

It is non intuitive how to go about collecting training data.



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It is **non intuitive** how to go about **collecting** training data.

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Continued from prev. slide:

- ★ Learning **optimal** trajectories predominant in literature. Study showed  $\Phi^{\text{OPT}}$  can result in **insufficient** knowledge.
- ★ Following sub-optimal deterministic policies, yet labelling with an optimal solver, improves the guiding policy.
- ★ Active update procedure using DAgger ensures sample states the learned model is likely to encounter is integrated to  $\Psi_p^{\text{DAI}}$ .
- ★ Instead of reusing same problem instances, extend the training set with new instances for quicker convergence of DAgger.
- ★ In sequential decision making, all future observations are dependent on previous operations.



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# Acknowledgements

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**Funding:** University of Iceland's  
Research Fund.

**Doctoral committee:**

- ★ Prof. Tómas Philip Rúnarsson,  
University of Iceland (advisor).
- ★ Prof. Gunnar Stefánsson,  
University of Iceland.
- ★ Prof. Michèle Sebag,  
Université Paris-Sud.





# Thank you for your attention

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## Questions?

Helga Ingimundardóttir  
hei2@hi.is

Supplementary material:

- ★ Shiny application
- ★ Github.

