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Analysis & Learning Iterative Consecutive Executions

Helga Ingimundardóttir

University of Iceland

June 30, 2016



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Motivation:

- ★ The general goal is to train optimisation algorithms using data.

Contribution:

- ★ The main contribution of this thesis is towards a better understanding of how this training data should be constructed.



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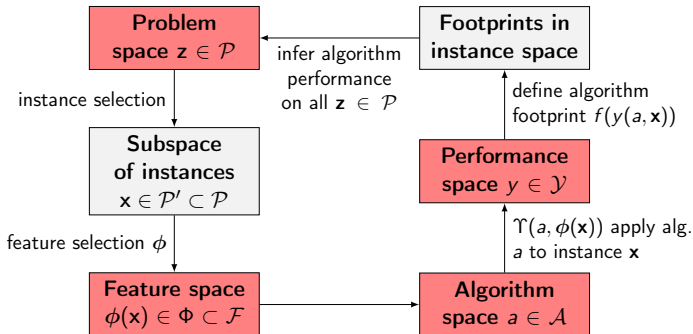
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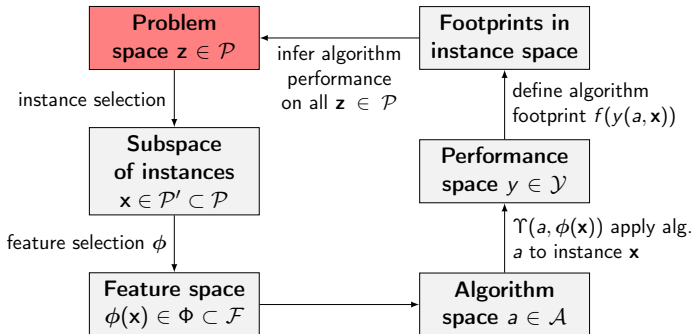
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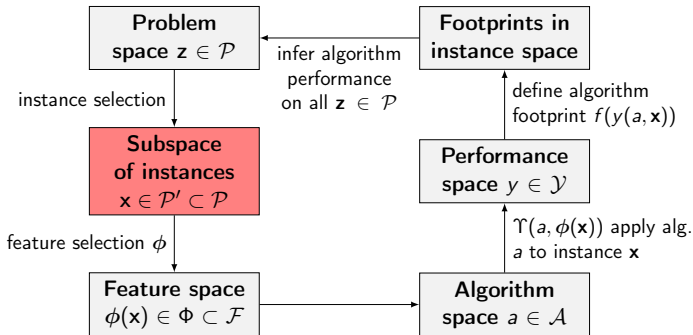
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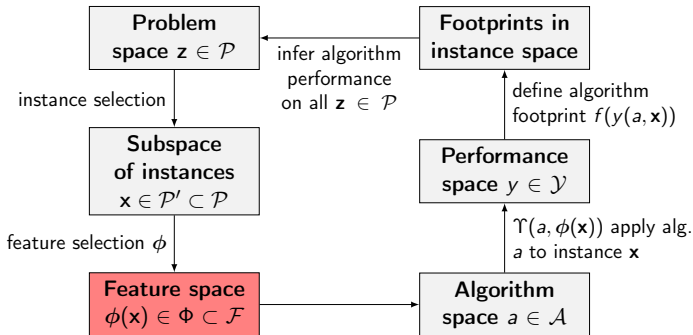
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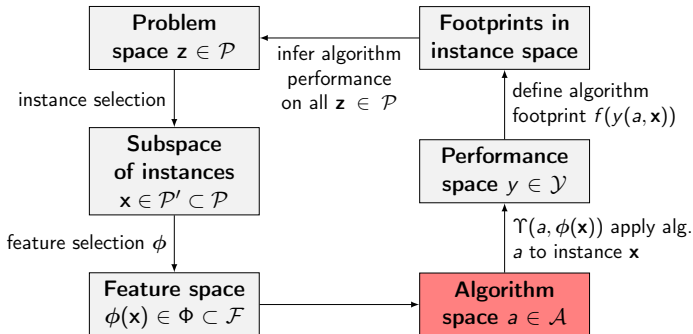
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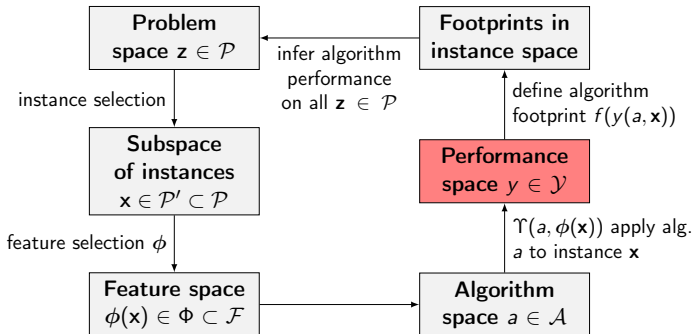
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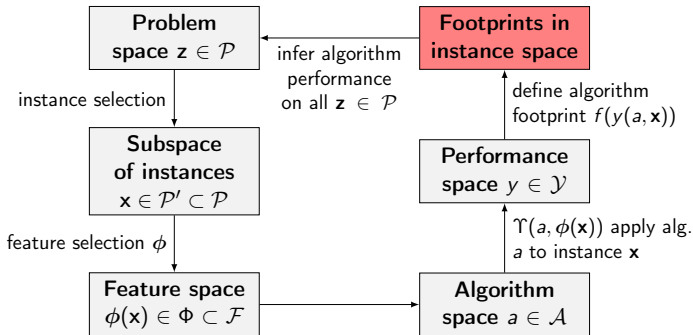
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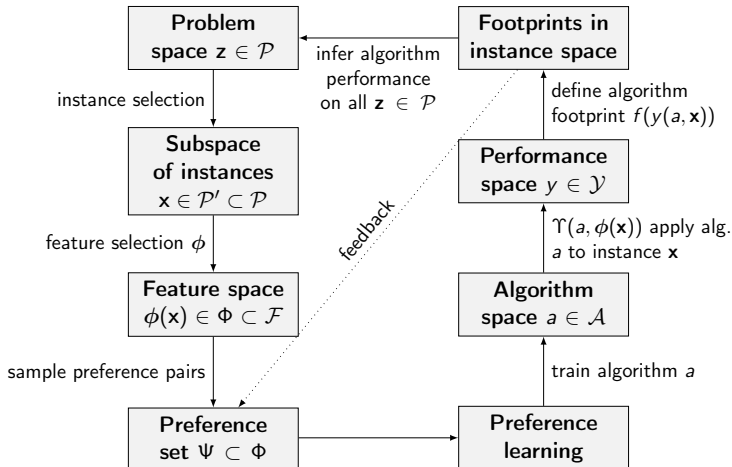
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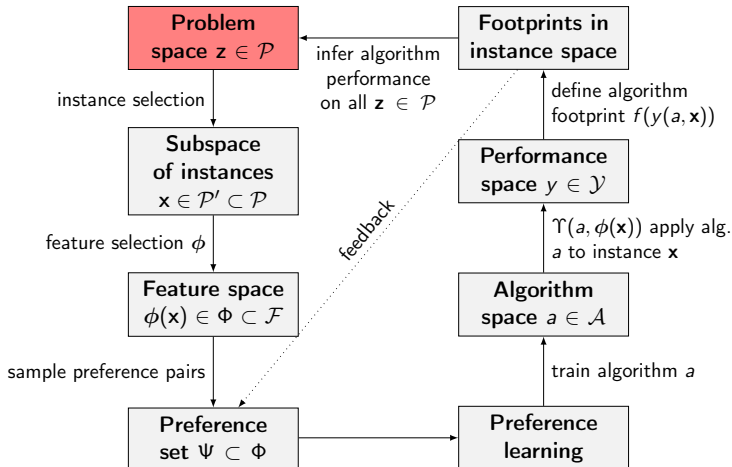
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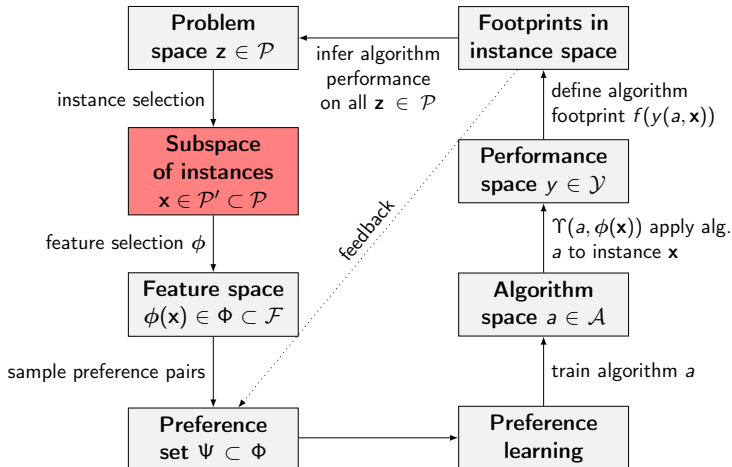
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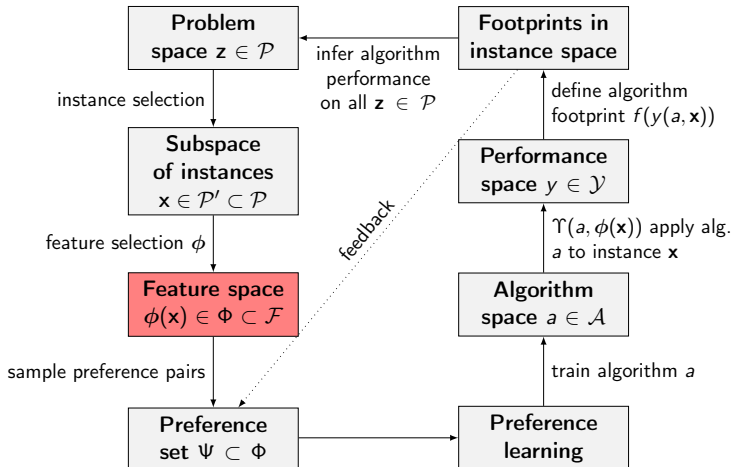
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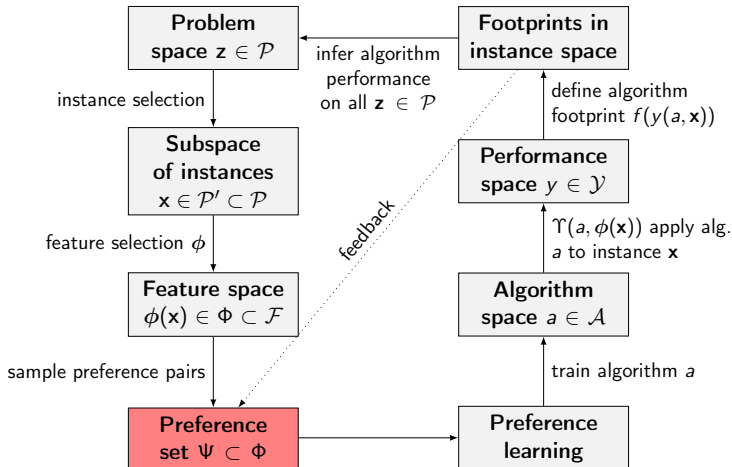
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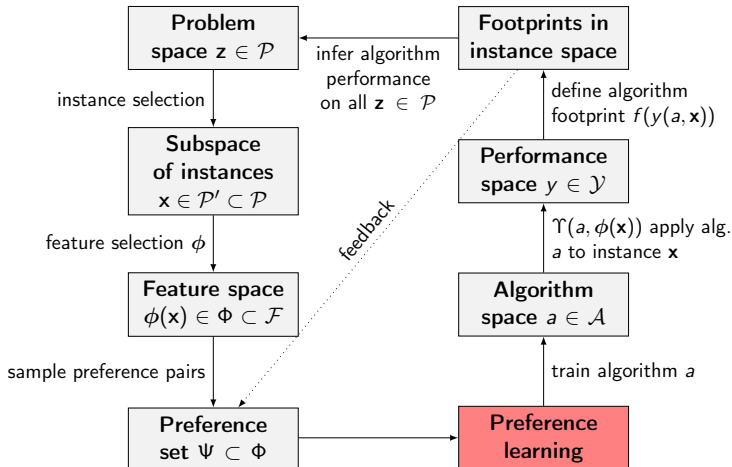
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Framework for Algorithm Learning

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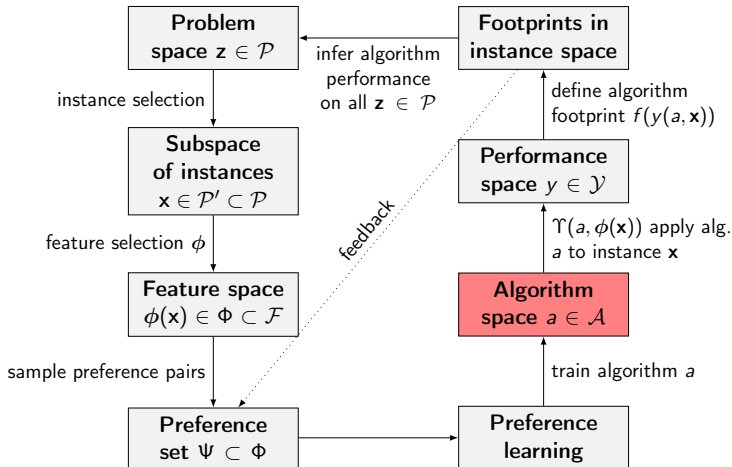
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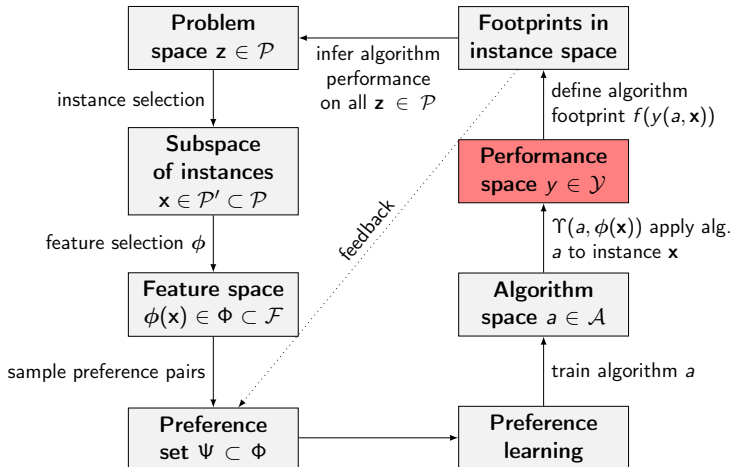
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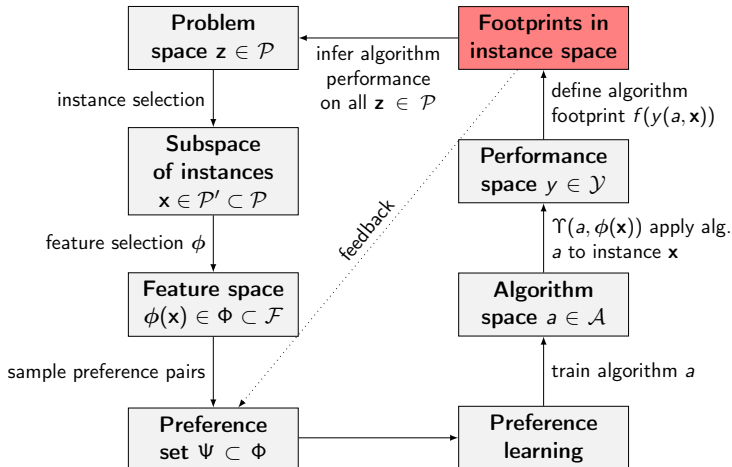
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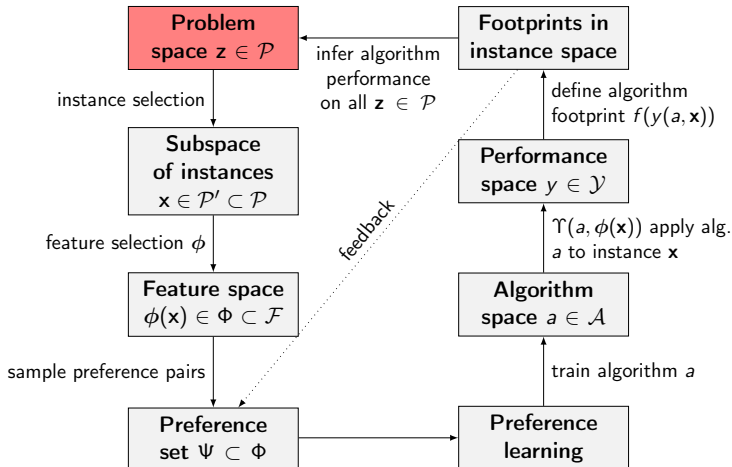
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The attending guests: They all have to:

J_1) Alice

M_1) have wine or pour tea

J_2) March Hare

M_2) spread butter

J_3) Dormouse

M_3) get a haircut

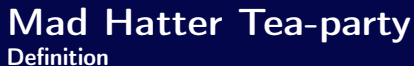
J_4) Mad Hatter.

M_4) check the time of the broken watch

M_5) say what they mean.

This can be considered as a typical 4×5 job-shop, where:

- ★ our guests are the jobs
- ★ their tasks are the machines
- ★ objective is to minimise C_{\max} (when Alice can leave).



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Start: $k = 0$

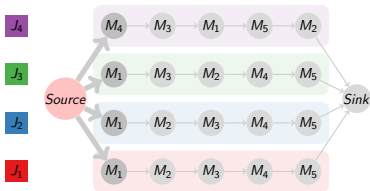


Figure: Disjunctive graph

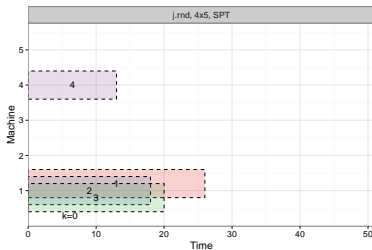


Figure: Gantt chart

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Midway: $k = 10$

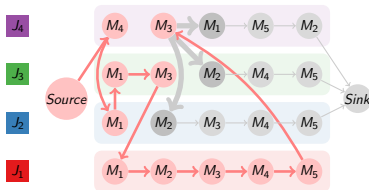


Figure: Disjunctive graph

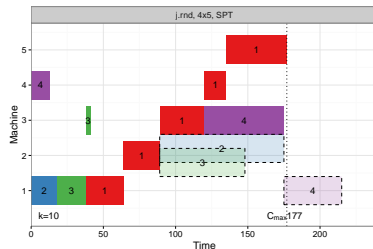


Figure: Gantt chart

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Finish: $k = 20$

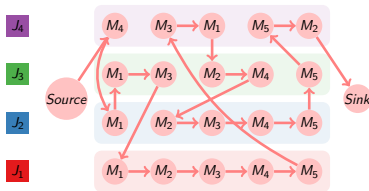


Figure: Disjunctive graph

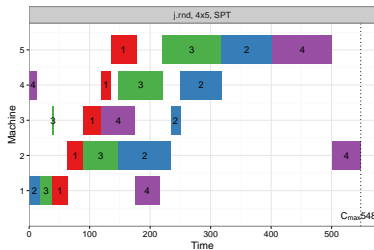


Figure: Gantt chart

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K -solutions

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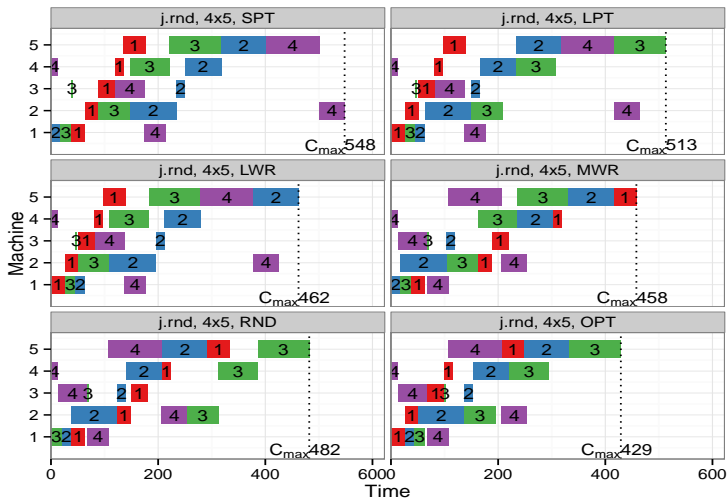
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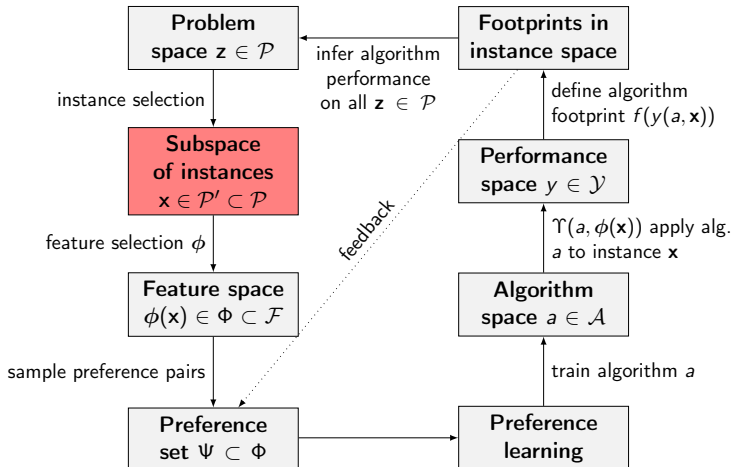
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Problem Instance Generators

Based on Watson et al. (2002)

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	name	size ($n \times m$)	N_{train}	N_{test}	note
JSP	$\mathcal{P}_{j.\text{rnd}}^{6 \times 5}$	6×5	500	500	random
	$\mathcal{P}_{j.\text{rndn}}^{6 \times 5}$	6×5	500	500	random-narrow
	$\mathcal{P}_{j.\text{rnd}, J_1}^{6 \times 5}$	6×5	500	500	random with job variation
	$\mathcal{P}_{j.\text{rnd}, M_1}^{6 \times 5}$	6×5	500	500	random with machine variation
	$\mathcal{P}_{j.\text{rnd}}^{10 \times 10}$	10×10	300	200	random
	$\mathcal{P}_{j.\text{rndn}}^{10 \times 10}$	10×10	300	200	random-narrow
	$\mathcal{P}_{j.\text{rnd}, J_1}^{10 \times 10}$	10×10	300	200	random with job variation
	$\mathcal{P}_{j.\text{rnd}, M_1}^{10 \times 10}$	10×10	300	200	random with machine variation
	$\mathcal{P}_{\text{JSP}, \text{ORLIB}}$	various	–	82	various
FSP	$\mathcal{P}_{f.\text{rnd}}^{6 \times 5}$	6×5	500	500	random
	$\mathcal{P}_{f.\text{rndn}}^{6 \times 5}$	6×5	500	500	random-narrow
	$\mathcal{P}_{f.\text{jc}}^{6 \times 5}$	6×5	500	500	job-correlated
	$\mathcal{P}_{f.\text{mc}}^{6 \times 5}$	6×5	500	500	machine-correlated
	$\mathcal{P}_{f.\text{mxc}}^{6 \times 5}$	6×5	500	500	mixed-correlation
	$\mathcal{P}_{f.\text{rnd}}^{10 \times 10}$	10×10	300	200	random
	$\mathcal{P}_{\text{FPS}, \text{ORLIB}}$	various	–	31	various

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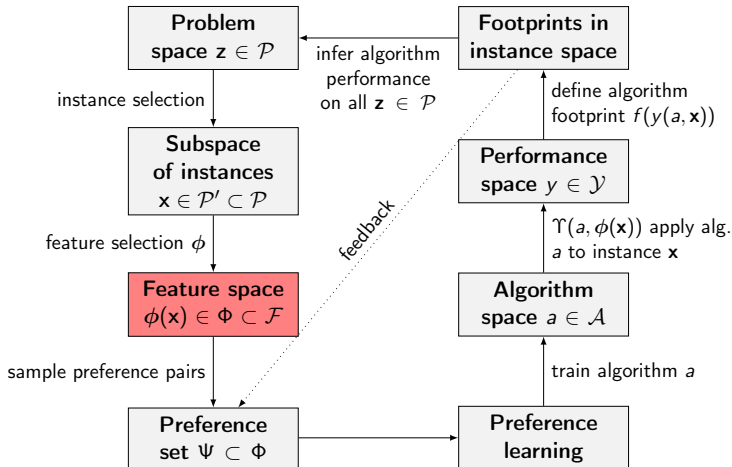
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job	ϕ_1	job processing time
	ϕ_2	job start-time
	ϕ_3	job end-time
	ϕ_4	job arrival time
	ϕ_5	time job had to wait
	ϕ_6	total processing time for job
	ϕ_7	total work remaining for job
	ϕ_8	number of assigned operations for job
machine	ϕ_9	when machine is next free
	ϕ_{10}	total processing time for machine
	ϕ_{11}	total work remaining for machine
	ϕ_{12}	number of assigned operations for machine
	ϕ_{13}	change in idle time by assignment
	ϕ_{14}	total idle time for machine
	ϕ_{15}	total idle time for all machines
	ϕ_{16}	current makespan
final makespan	ϕ_{17}	final makespan using SPT
	ϕ_{18}	final makespan using LPT
	ϕ_{19}	final makespan using LWR
	ϕ_{20}	final makespan using MWR
	ϕ_{RND}	final makespans using 100 random rollouts
	ϕ_{21}	mean for ϕ_{RND}
	ϕ_{22}	standard deviation for ϕ_{RND}
	ϕ_{23}	minimum value for ϕ_{RND}
	ϕ_{24}	maximum value for ϕ_{RND}

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Trajectory Strategies for ϕ

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Following the **policy**:

- ★ (ϕ^{OPT}) expert π_* .
- ★ (ϕ^{SPT}) shortest processing time (SPT).
- ★ (ϕ^{LPT}) longest processing time (LPT).
- ★ (ϕ^{LWR}) least work remaining (LWR).
- ★ (ϕ^{MWR}) most work remaining (MWR).
- ★ (ϕ^{RND}) random policy (RND).
- ★ $(\phi^{\text{ES}, \rho})$ the policy obtained by optimising with CMA-ES.
- ★ (ϕ^{ALL}) union of all of the above.

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- ★ (ϕ^{OPT}) expert π_* .
- ★ (ϕ^{SPT}) shortest processing time (SPT).
- ★ (ϕ^{LPT}) longest processing time (LPT).
- ★ (ϕ^{LWR}) least work remaining (LWR).
- ★ (ϕ^{MWR}) most work remaining (MWR).
- ★ (ϕ^{RND}) random policy (RND).
- ★ $(\phi^{\text{ES}, \rho})$ the policy obtained by optimising with CMA-ES.
- ★ (ϕ^{ALL}) union of all of the above.

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Sampled Size of $|\Phi(k)|$

$6 \times 5, N_{train} = 500$

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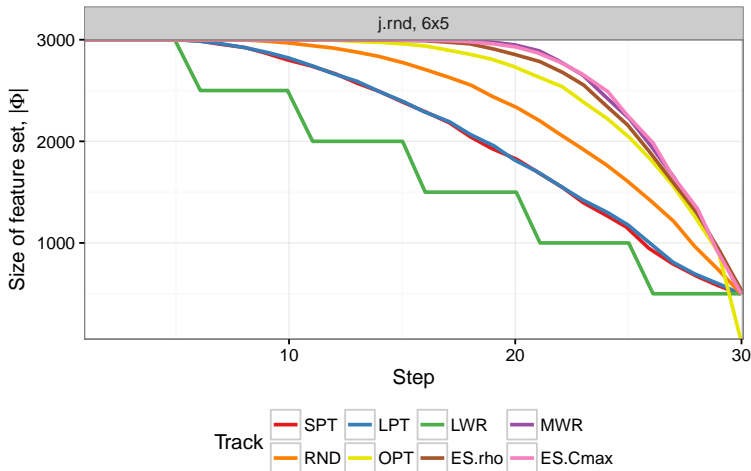
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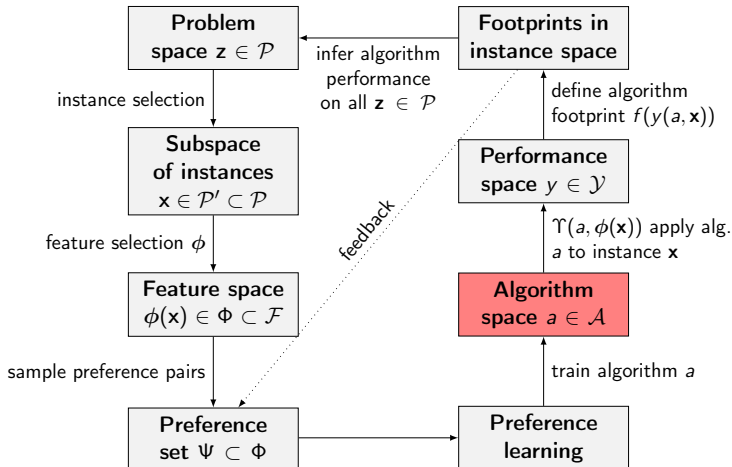
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Various Methods for Solving JSP

Based on Jain and Meeran (1999)

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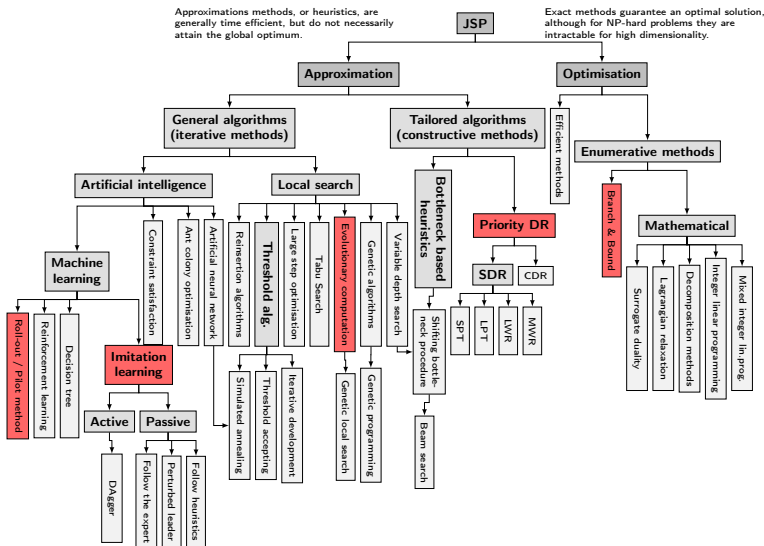
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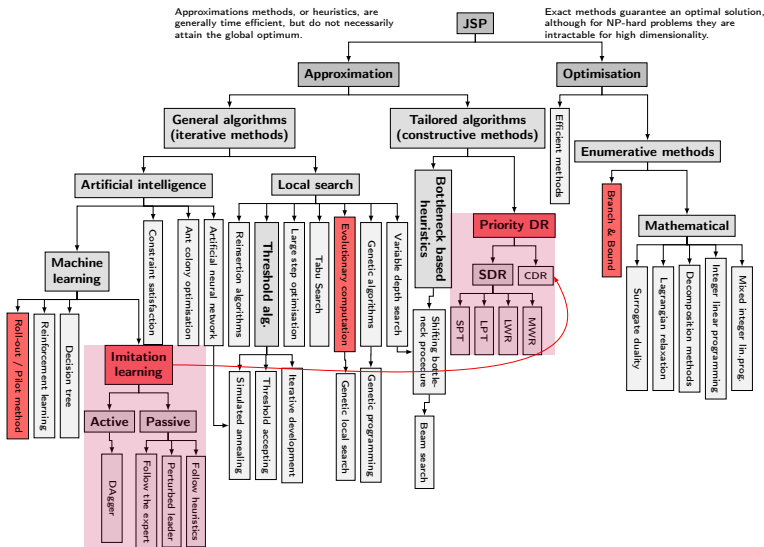
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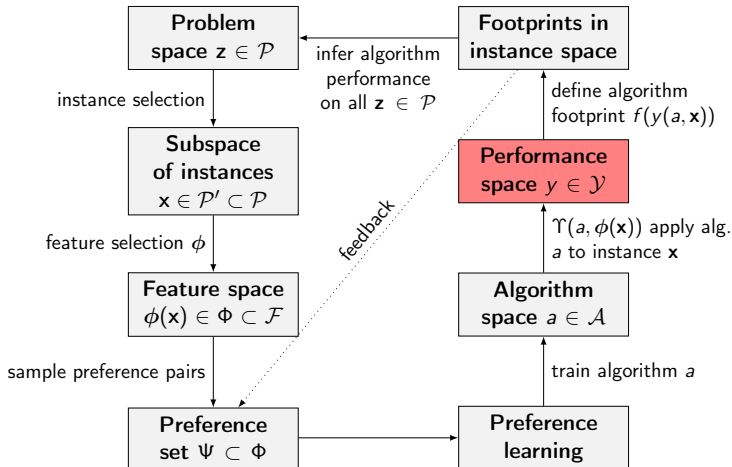
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Performance of policy π compared with its optimal makespan, found using an expert policy, π_* , is the following loss function:

$$\rho = \frac{C_{\max}^{\pi} - C_{\max}^{\pi_*}}{C_{\max}^{\pi_*}} \cdot 100\%$$

The goal is to minimise this discrepancy between **predicted** value and **true** outcome.

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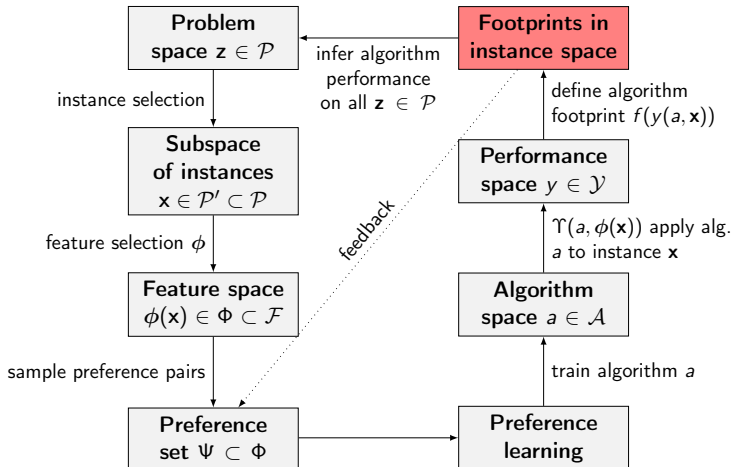
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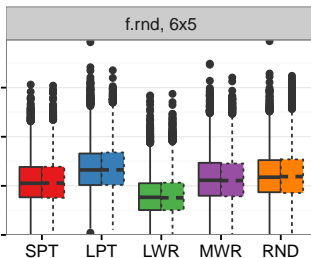
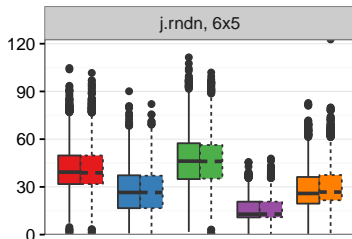
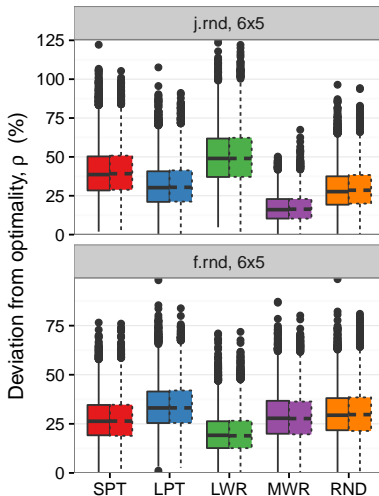
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Simple dispatching rule

- Shortest Processing Time
- Longest Processing Time
- Least Work Remaining
- Most Work Remaining
- Random dispatches

Data set



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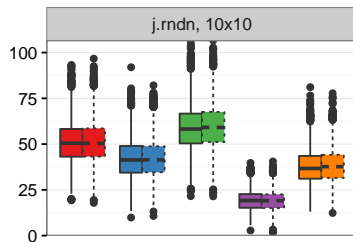
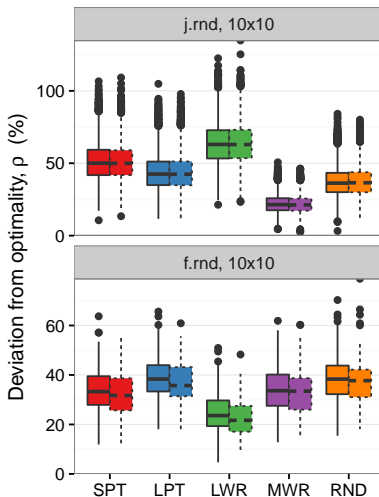
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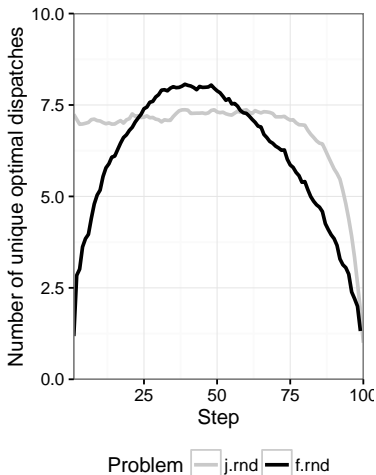
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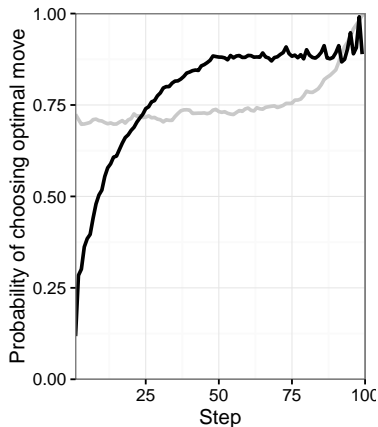
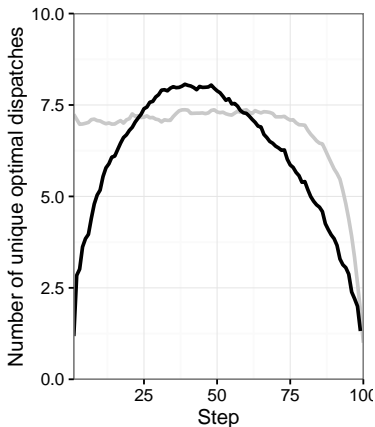
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Probability of SDR Being Optimal

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$$\xi_{(\text{SDR})}^*$$

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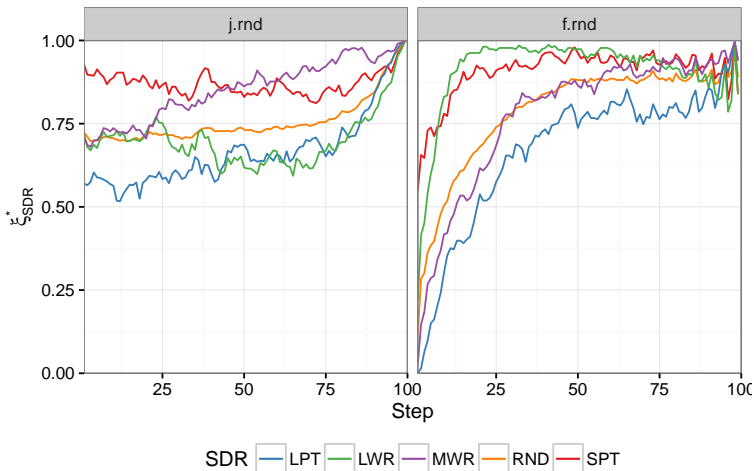
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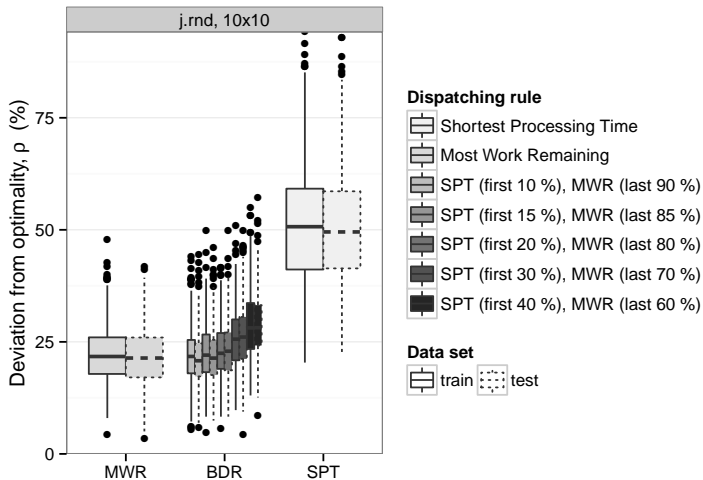
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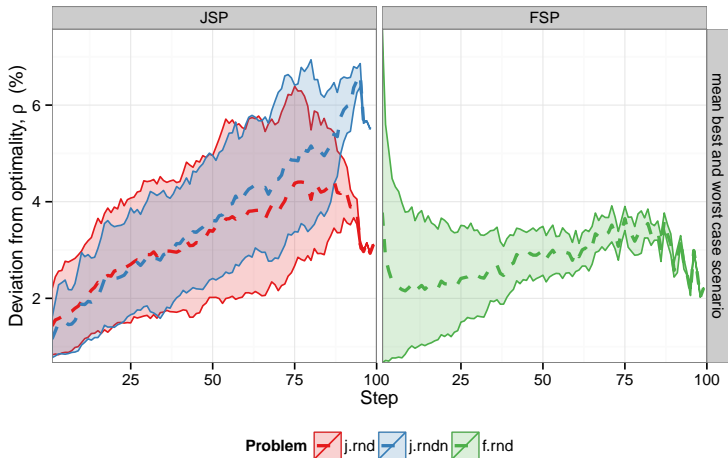
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Probability of SDR Being Optimal

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ξ_{SDR}

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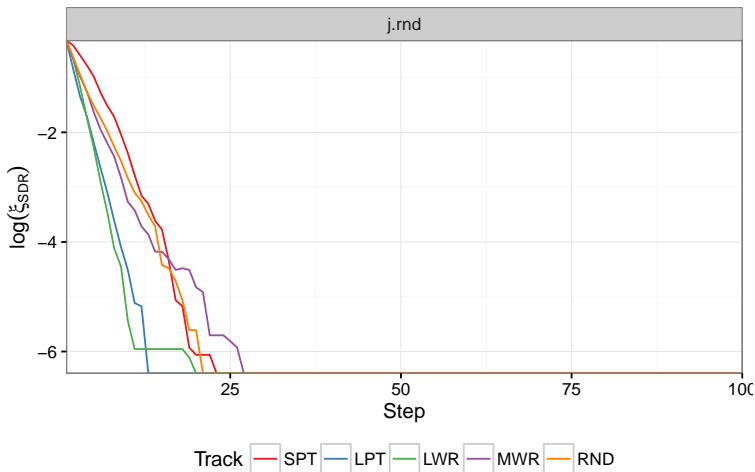
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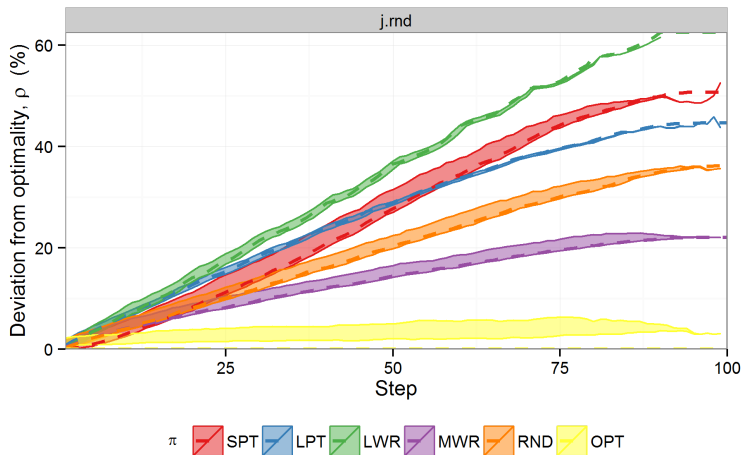
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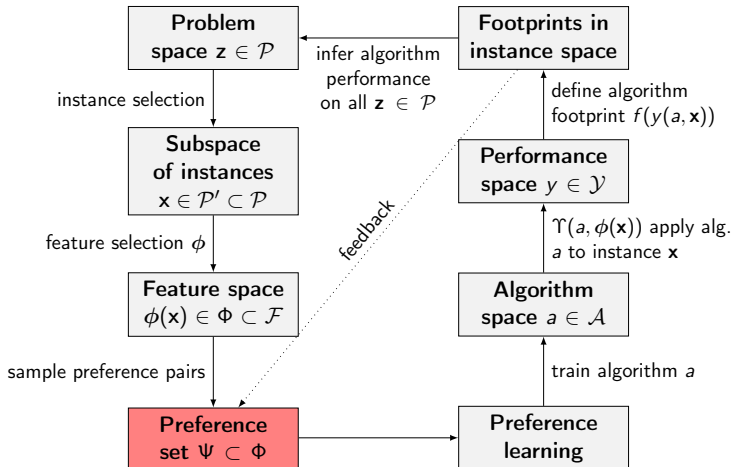
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ALICE framework for creating dispatching rules:

- ★ **Linear classification** to identify good dispatches, from worse ones.
- ★ Generate feature set, $\Phi \subset \mathcal{F}$, both from
 - ★ optimal solutions, ϕ^o
 - ★ suboptimal solutions, ϕ^sby exploring various trajectories within the feature-space (where $\phi^o, \phi^s \in \mathcal{F}$).
- ★ Sample Φ to create training set Ψ with rank pairs:
 - ★ optimal decision, $(z^o, y_o) = (\phi^o - \phi^s, +1)$
 - ★ suboptimal decision, $(z^s, y_s) = (\phi^s - \phi^o, -1)$using different ranking schemes (where $z^o, z^s \in \Psi$)
- ★ Sample Ψ using stepwise bias for time independent policy.

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Sampled Size of $|\Phi(k)|$

$6 \times 5, N_{train} = 500$

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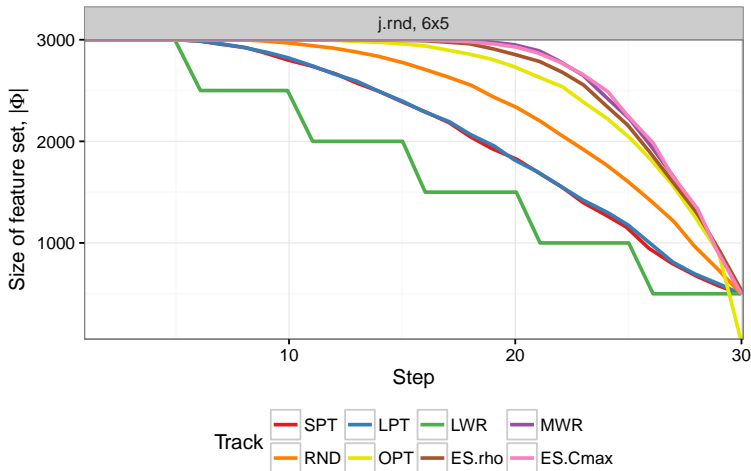
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Sampled Size of $|\Psi(k)|$

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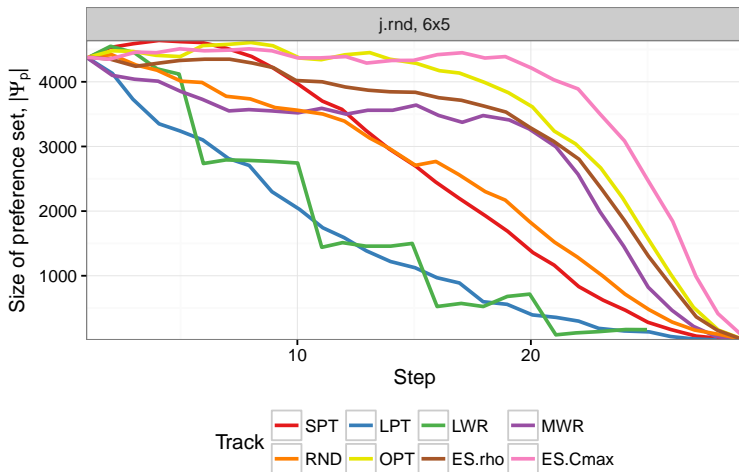
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Stepwise Bias Strategies

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$6 \times 5, N_{train} = 500$

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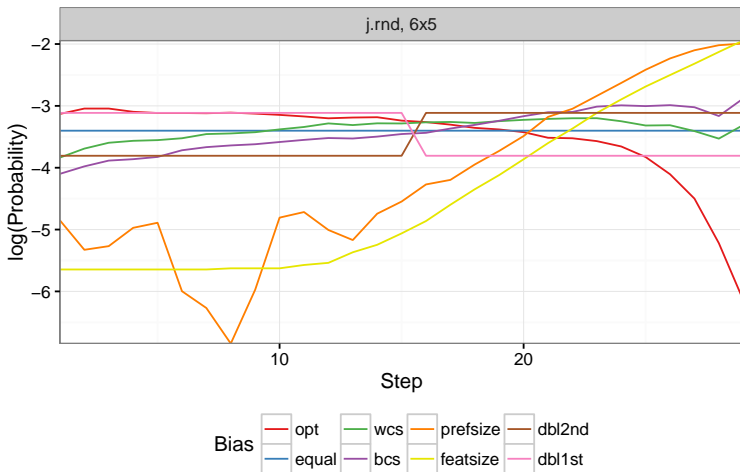
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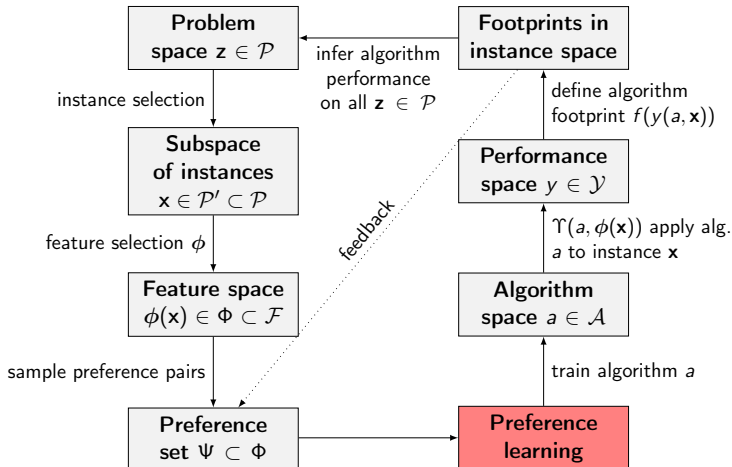
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Preference learning:

- ★ Mapping of points to ranks: $\{h(\cdot) : \Phi \mapsto Y\}$ where

$$\phi_o \succ \phi_s \iff h(\phi_o) > h(\phi_s)$$

- ★ The preference is defined by a linear function:

$$h(\phi) = \langle \mathbf{w} \cdot \phi \rangle$$

optimised w.r.t. \mathbf{w} based on training data Ψ

- ★ Note: Limitations in approximation function to capture the complex dynamics incorporated in optimal trajectories.

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Various Methods for Solving JSP

Based on Jain and Meeran (1999)

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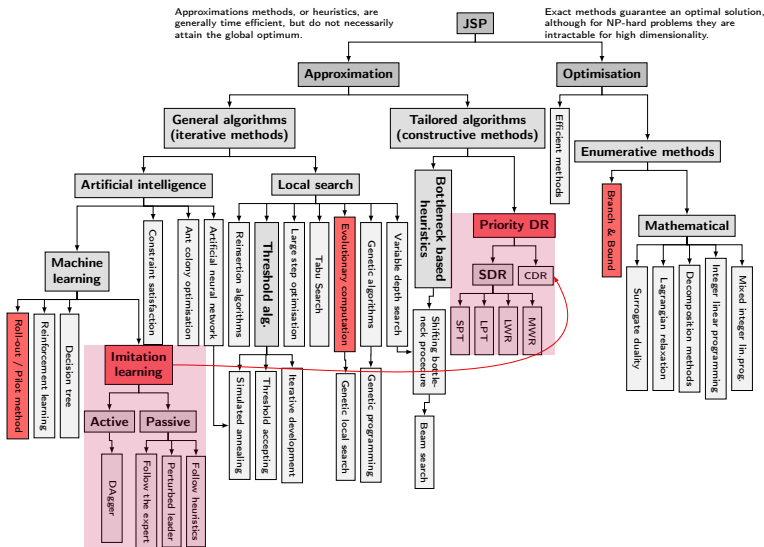
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Passive imitation learning (**single** pass)

- ★ Prediction with expert advice, π_\star
- ★ Follow the perturbed leader (OPT_ϵ)
- ★ Follow a heuristic (e.g. SDRs).



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Passive Imitation Learning

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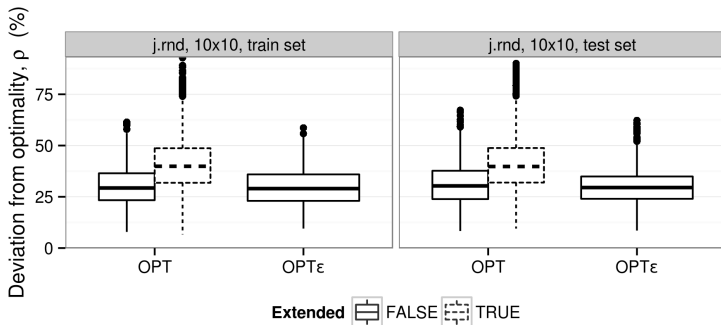
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Active imitation learning (**iterative**):

★ Dataset Aggregation (DAgger)

$$\pi_i = \beta_i \pi_\star + (1 - \beta_i) \hat{\pi}_{i-1}$$

where $\hat{\pi}_{i-1}$ is the previous learned model, and $\hat{\pi}_i$ learns on aggregated dataset of all previous iterations.

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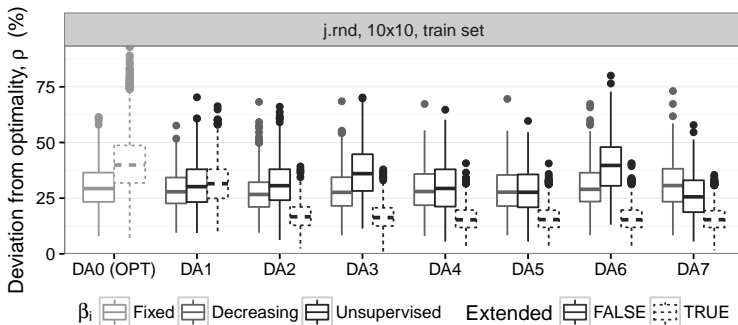
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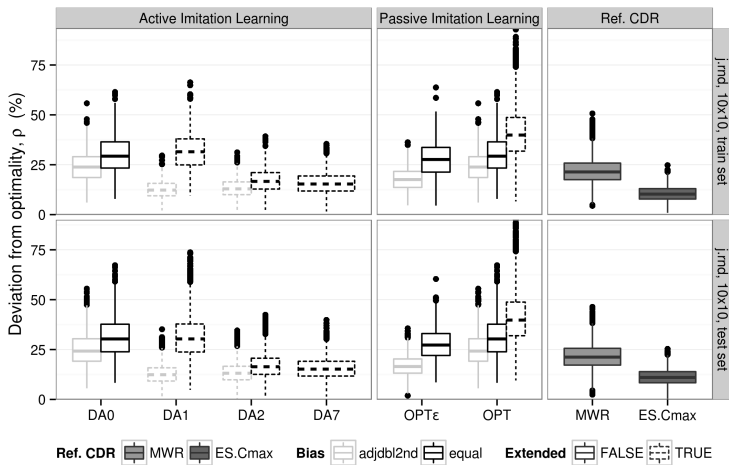
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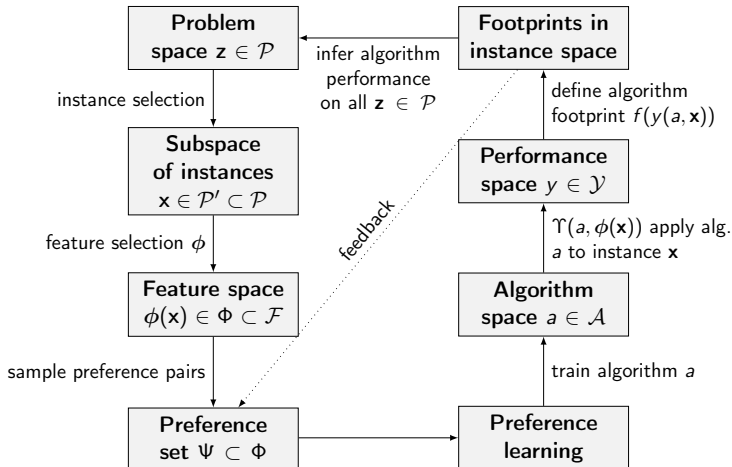
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The thesis introduces a framework for learning (**linear**) composite priority dispatching rule – using **job-shop** as a case-study – with the following guidelines

- ★ For a given problem domain, use a suitable problem generator to train and test on.
- ★ Define features to grasp the essence of visited k -solutions
- ★ Success is highly dependent on the preference pairs introduced to the system:
 - ★ Ψ_p reduces the preference set without loss of performance.
 - ★ Stepwise bias is needed to balance time dependent Ψ_p in order to create time independent models.

It is non intuitive how to go about collecting training data.

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The thesis introduces a framework for learning (linear) composite priority dispatching rule – using job-shop as a case-study – with the following guidelines:

- ★ For a given problem domain, use a suitable problem **generator** to **train** and **test** on.
 - ★ Define features to grasp the essence of visited k -solutions
 - ★ Success is highly dependent on the preference pairs introduced to the system:
 - ★ Ψ_p reduces the preference set without loss of performance.
 - ★ Stepwise bias is needed to balance time dependent Ψ_p in order to create time independent models.
- It is non intuitive how to go about collecting training data.

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Continued from prev. slide:

- ★ Learning **optimal** trajectories predominant in literature. Study showed Φ^{OPT} can result in **insufficient** knowledge.
- ★ Following sub-optimal deterministic policies, yet labelling with an optimal solver, improves the guiding policy.
- ★ Active update procedure using DAgger ensures sample states the learned model is likely to encounter is integrated to Ψ_p^{DAI} .
- ★ Instead of reusing the same problem instances, extend the training set with new instances for quicker convergence of DAgger.
- ★ In sequential decision making, all future observations are dependent on previous operations.

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- ★ Active update procedure using **Dagger** ensures sample states the **learned model is likely to encounter** is integrated to $\Psi_p^{\text{DA}i}$.
- ★ Instead of reusing the same problem instances, extend the training set with new instances for quicker convergence of Dagger.
- ★ In sequential decision making, all future observations are dependent on previous operations.

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Funding: University of Iceland's Research Fund.

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Illustrations: Sir John Tenniel (1820–1914)

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Supplementary material:

- ★ Shiny application
- ★ Github.

