Evolutionary learning of linear composite dispatching rules for scheduling

Helga Ingimundardottir and Thomas Philip Runarsson

bine several relatively simple dispatching rules such that they may benefit each other for a given problem space. Generally, this is done in an ad-hoc fashion, requiring expert knowledge from heuristics designers, or extensive exploration of suitable combinations of heuristics. The approach here is to automate that selection by translating

Abstract A prevalent approach to solving job shop scheduling problems is to com-

binations of heuristics. The approach here is to automate that selection by translating dispatching rules into measurable features and optimising what their contribution should be via evolutionary search. The framework is straight forward and easy to implement and shows promising results. Various data distributions are investigated

for both job shop and flow shop problems, as is scalability for higher dimensions. Moreover, the study shows that the choice of objective function for evolutionary search is worth investigating. Since the optimisation is based on minimising the expected mean of the fitness function over a large set of problem instances which can

vary within the set, then normalising the objective function can stabilise the optimi-

1 Job shop scheduling

sation process away from local minima.

The job-shop scheduling problem (JSP) deals with the allocation of tasks of competing resources where the goal is to optimise a single or multiple objectives – in particular minimising a schedule's maximum completion time, i.e., the makespan,

by applying dispatching rules (DR), e.g., choosing a task corresponding to longest or shortest processing time, most or least successors, or ranked positional weight,

denoted C_{max} . Due to difficulty in solving this problem, heuristics are generally applied. Perhaps the simplest approach to generating good feasible solutions for JSP is

Helga Ingimundardottir Industrial Eng., Mechanical Eng. and Computer Science, University of Iceland, e-mail: hei2@hi.is Thomas Philip Runarsson

Industrial Eng., Mechanical Eng. and Computer Science, University of Iceland, e-mail: tpr@hi.is

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[8]. The classical dispatching rules are continually used in research; a summary of over 100 classical DRs for JSP can be found in [16]. However, careful combinations of such simple rules, i.e., composite dispatching rules (CDRs) can perform significantly better [12]. As a consequence, a linear composite of dispatching rules for JSP

was presented in [10]. There the goal was to learn a set of weights, w via ordinal

 $h(\mathbf{x}_j) = \langle \mathbf{w} \cdot \boldsymbol{\phi}(\mathbf{x}_j) \rangle,$

yields the preference estimate for dispatching job j that corresponds to post-decision state \mathbf{x}_i , where $\phi(\mathbf{x}_i)$ denotes the feature mapping (cf. Section 4). In short, Eq. (1) is

regression such that

i.e., sum of processing times of its predecessors. Ties are broken in an arbitrary fashion or by another heuristic rule. Combining dispatching rules for JSP is promising, however, there is a large number of rules to choose from, thus its combinations rely on expert knowledge or extensive trial-and-error process to choose a suitable DR [21]. Hence given the diversity within the JSP paradigm, there is no "one-rulefits-all" for all problem instances (or shop constraints), however single priority dispatching rules (SDR) based on job processing attributes have proven to be effective

a simple linear combination of features found using a classifier which is trained by giving more weight to instances that are preferred w.r.t. optimality in a supervised learning fashion. As a result, the job dispatched is the following,

$$j^* = \arg\max_{j} \left\{ h(\mathbf{x}_j) \right\}.$$

(1)

(2)

A more popular approach in recent JSP literature is applying genetic algorithms

evaluated, and even for low dimensional JSP, it can quickly become computationally infeasible. GAs can be used directly on schedules [3, 4, 22, 13, 1], however, then

encoding schemes for representing the schedules [3], in addition, special care must be taken when applying cross-over and mutation operators in order for schedules

to still remain feasible. Moreover, in case of JSP, GAs are not adapt for fine-tuning

around optima. Luckily a subsequent local search can mediate the optimisation [4].

The most predominant approach in hyper-heuristics, a framework of creating new heuristics from a set of predefined heuristics, is genetic programming [2]. Dispatching rules based genetic algorithms (DRGA) [23, 5, 15] are a special case of

genetic programming [14], where GAs are applied indirectly to JSP via dispatching

rules, i.e., where a solution is no longer a proper schedule but a representation of a schedule via applying certain DRs consecutively. There are two main viewpoints on how to approach scheduling problems, a) lo-

cal level by building schedules for one problem instance at a time; and b) global level by building schedules for all problem instances at once. For local level construction a simple construction heuristic is applied. The schedule's features are collected at

each dispatch iteration from which a learning model will inspect the feature set to discriminate which operations are preferred to others via ordinal regression. The fo-

cus is essentially on creating a meaningful preference set composed of features and

work consists of four fundamental components, namely, Problem space or instance space set of problem instances; Feature space \mathscr{F} , measurable properties of the instances in \mathcal{P} ;

In order to formulate the relationship between problem structure and heuristic efficiency, one can utilise Rice's framework for algorithm selection [18]. The frame-

their ranks as the learning algorithm is only run once to find suitable operators for the value function. This is the approach taken in [10]. Expanding on that work, this study will explore a global level construction viewpoint where there is no feature set collected beforehand since the learning model is optimised directly via evolutionary search. This involves numerous costly value function evaluations. In fact it involves an indirect method of evaluation whether one learning model is preferable

set of all algorithms under inspection; Performance space \mathcal{Y} , the outcome for \mathscr{P} using an algorithm from \mathscr{A} .

to another, w.r.t. which one yields a better expected mean.

For a given problem instance $\mathbf{x} \in \mathscr{P}$ with k features $\phi(\mathbf{x}) = \{\phi_1(\mathbf{x}), ..., \phi_k(\mathbf{x})\} \in \mathscr{F}$

and using algorithm $a \in \mathscr{A}$ the performance is $y = Y(a, \phi(\mathbf{x})) \in \mathscr{Y}$, where Y:

data structure; c) algorithm space \mathscr{A} is simply the scheduling policies under consideration and discussed in Section 5; d) performance space is based on the resulting C_{max} . Different fitness measures are investigated in Section 5.1; and e) mapping Y is the step-by-step scheduling process.

 $\mathscr{A} \times \mathscr{F} \mapsto \mathscr{Y}$ is the mapping for algorithm and feature space onto the performance space. [19, 20, 11] formulate JSP in the following manner: a) problem space \mathscr{P} is defined as the union of N problem instances consisting of processing time and ordering matrices given in Section 3; b) feature space \mathcal{F} , which is outlined in Section 4. Note, these are not the only possible set of features, however, they are built on the work by [10, 19] and deemed successful in capturing the essence of a JSP

In the context of Rice's framework, and returning to the aforementioned approaches to scheduling problems, then the objective is to maximise its expected heuristic performance, i.e.,

a) Local level

2 Outline

Algorithm space \mathscr{A} ,

$$\max_{\mathscr{P}' \subset \mathscr{P}} \mathbb{E}[Y(a, \phi(\mathbf{x}))]$$
 (3)

where $\mathbf{x} \in \mathscr{P}'$ and algorithm a is obtained via ordinal regression based on the

feature space \mathscr{F} , i.e., $\mathscr{F}|_{\mathscr{P}'} \mapsto \mathscr{A}$, such as the approach taken in [10], and will be used as a benchmark for the following,

where training data $\mathbf{x} \in \mathscr{P}$ is guided by its algorithm a, i.e., $\mathscr{A} \mapsto \mathscr{P}$. This will

be the focus of this study.

Note that the mappings $\phi : \mathcal{P} \mapsto \mathcal{F}$ and $Y : \mathcal{A} \mapsto \mathcal{Y}$ are the same for both

 $\max \mathbb{E}[Y(a, \phi(\mathbf{x}))]$

(4)

paradigms.

The paper concludes in Section 6 with discussion and conclusions.

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For this study synthetic JSP and its subclass, permutation flow shop problem

3 Problem space

b) Global level

(PFSP), the scheduling task considered here is where n jobs are scheduled on a set of m machines, i.e., problem size $n \times m$, subject to the constraint that each job must follow a predefined machine order and that a machine can handle at most one job set a time. The pair (i, a) refers to the operation of disputching job, i on machine m

at a time. The pair (j,a) refers to the operation of dispatching job j on machine a. As a result, a total of $\ell = n \cdot m$ sequential operations need to be made for a complete schedule.

The objective is to schedule the jobs so as to minimize the maximum completion

times, $C_{\rm max}$, also known as the makespan. For a mathematical formulation of JSP the reader is recommended [10].

There are two fundamental types of problem classes: non-structured versus struc-

There are two fundamental types of problem classes: non-structured versus structured. Firstly there are the "conventional" structured problem classes, where problem instances are generated stochastically by fixing the number of jobs and machines, as well as processing times are i.i.d. and sampled from a discrete uniform

distribution from the interval $I = [u_1, u_2]$, i.e., $p \sim \mathcal{U}(u_1, u_2)$. Two different process-

ing time distributions are explored, namely $\mathcal{P}_{j.rnd}$ where I = [1,99] and $\mathcal{P}_{j.rndn}$ where I = [45,55], referred to as random and random-narrow, respectively. The machine order is a random permutation of all of the machines in the job-shop.

Analogous to $\mathcal{P}_{j.rnd}$ and $\mathcal{P}_{j.rndn}$ the problem classes $\mathcal{P}_{f.rnd}$ and $\mathcal{P}_{f.rndn}$, respectively, correspond to the structured PFSP problem classes, however with a homogeneous machine order permutation. Secondly, there are structured problem

homogeneous machine order permutation. Secondly, there are structured problem classes of PFSP which are modelled after real-world flow-shop manufacturing namely job-correlated $\mathcal{P}_{f,jc}$ where job processing times are dependent on job index and independent of machine index. Problem instances for PFSP are generated using [24] problem generator¹.

For each JSP and PFSP class N_{train} and N_{test} instances were generated for training

For each JSP and PFSP class N_{train} and N_{test} instances were generated for training and testing, respectively. Values for N are given in Table 1. Note, difficult problem instances are not filtered out beforehand, such as the approach in [24].

Both code, written in C++, and problem instances used in their experiments can be found at: http://www.cs.colostate.edu/sched/generator/

Table 1 Problem space distributions used in Section 5. Note, problem instances are synthetic and each problem space is i.i.d. and '-' denotes not available.

name	size	$N_{ m train}$	$N_{\rm test}$	note				
Permutation flow shop problem (PFSP)								
$\mathscr{P}_{f.rnd}^{6 imes 5}$	6×5	500	_	random				
$\mathscr{P}_{f.rndn}^{6 \times 5}$	6 × 5	500	_	random-narrow				
$\mathscr{P}_{f.jc}^{6 imes 5}$	6×5	500	-	job-correlated				
$\mathcal{P}_{f.rnd}^{10\times10}$	10×10	-	500	random				
$\mathcal{P}_{f.rndn}^{10\times10}$	10×10	-	500	random-narrow				
$\mathcal{P}_{f.jc}^{10\times10}$	10×10	-	500	job-correlated				
Job shop problem (JSP)								
€6×5 j.rnd	6×5	500	_	random				
$\mathcal{P}_{j.rndn}^{6\times5}$	6 × 5	500	_	random-narrow				
$\mathcal{P}_{j.rnd}^{10\times10}$	10×10	-	500	random				
$\mathcal{P}_{j.rndn}^{10\times10}$	10×10	_	500	random-narrow				

4 Feature space

When building a complete JSP schedule, a job is placed at the earliest available time slot for its next machine while still fulfilling constraints that each machine can handle at most one job at a time, and jobs need to have finished their previous ma-

handle at most one job at a time, and jobs need to have finished their previous machines according to its machine order. Unfinished jobs are dispatched one at a time according to some heuristic. After each dispatch the schedule's current features are

updated. Features are used to grasp the essence of the current state of the schedule. As seen in Table 2, temporal scheduling features applied in this study are given for each possible post-decision state. An example of a schedule being built is given in Fig. 1, where there are a total of five possible jobs that could be chosen to be

dispatched by some dispatching rule. These features would serve as the input for Eq. (1).

It's noted that some of the features directly correspond to a SDR commonly used in practice. For example, if the weights \mathbf{w} in Eq. (1) were all zero, save for $w_6 = 1$,

in practice. For example, if the weights **w** in Eq. (1) were all zero, save for $w_6 = 1$, then Eq. (2) yields the job with the highest ϕ_6 value, i.e., equivalent to dispatching rule most work remaining (MWR).

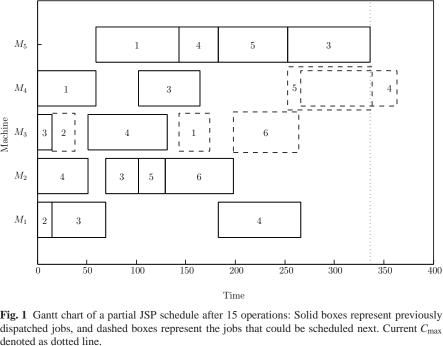
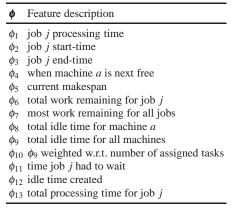


Table 2 Feature space \mathscr{F} for \mathscr{P} given the resulting temporal schedule after dispatching an operation (j,a).



5 Experimental study

stances the performance measure is the following, $C_{\max}^{\text{model}} - C_{\max}^{opt}$

The optimum makespan² is denoted C_{\max}^{opt} , and the makespan obtained from the heuristic model by C_{\max}^{model} . Since the optimal makespan varies between problem in-

$$\rho := \frac{C_{\text{max}}^{\text{model}} - C_{\text{max}}^{opt}}{C_{\text{max}}^{\text{opt}}} \cdot 100\%$$
 (5)

which indicates the percentage relative deviation from optimality. Throughout a Kolmogorov-Smirnov test with $\alpha = 0.05$ is applied to determine statistical signifi-

Inspired by DRGA, the approach taken in this study is to optimise the weights win Eq. (1) directly via evolutionary search such as covariance matrix adaptation evolution strategy (CMA-ES) [7]. This has been proven to be a very efficient numerical optimisation technique.

Using standard set-up of parameters of the CMA-ES optimisation, the runtime was limited to 288 hours on a cluster for each training set given in Section 3 and in

every case the optimisation reached its maximum walltime.

5.1 Performance measures

cance between methodologies.

Generally, evolutionary search only needs to minimise the expected fitness value. However, the approach in [10] was to use the known optimum to correctly label

which operations' features were optimal when compared to other possible operations. Therefore, it would be of interest to inspect if there is any performance edge

gained by incorporating optimal labelling in evolutionary search. Therefore, two objective functions will be considered, namely,

$$ES_{C_{\max}} := \min \mathbb{E}[C_{\max}] \tag{6}$$

$$ES_{\rho} := \min \mathbb{E}[\rho] \tag{7}$$
 Main statistics of the experimental run are given in Table 3 and depicted in Fig. 3

for both approaches. In addition, evolving decision variables, here weights **w** for Eq. (1), are depicted in Fig. 4.

In order to compare the two objective functions, the best weights reported were

used for Eq. (1) on the corresponding training data. Its box-plot of percentage relative deviation from optimality, defined by Eq. (5), is depicted in Fig. 2 and Table 4 present its main statistics; mean, median, standard deviation, minimum and maximum values.

² Optimum values are obtained by using a commercial software package [6].

Fig. 4(a) suggest. For other problem spaces, Eq. (6) gave slightly better results than Eq. (7). However, there was no statistical difference between adopting either objective function. Therefore, minimisation of expectation of ρ , is preferred over simply using the unscaled resulting makespan.

In the case of $\mathcal{P}_{f.rndn}$, Eq. (6) gave a considerably worse results, since the optimisation got trapped in a local minima, as the erratic evolution of the weights in

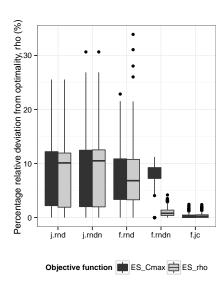


Fig. 2 Box-plot of training data for percentage relative deviation from optimality, defined by Eq. (5), when implementing the final weights obtained from CMA-ES optimisation, using both objective functions from Eqs. (6) and (7), left and right, respectively.

5.2 Problem difficulty

is depicted in Fig. 3. Note, all problem spaces reached their allotted computational time without converging. In fact $\mathcal{P}_{f.rnd}$ and $\mathcal{P}_{j.rndn}$ needed restarting during the optimisation process. Furthermore, the evolution of the decision variables **w** are depicted in Fig. 4. As one can see, the relative contribution for each weight clearly

The evolution of fitness per generation from the CMA-ES optimisation of Eq. (7)

differs between problem spaces. Note, that in the case of $\mathcal{P}_{j.rndn}$ (cf. Fig. 4(b)), CMA-ES restarts around generation 1,000 and quickly converges back to its previous fitness. However, lateral relation of weights has completely changed, implying that there are many optimal combinations of weights to be used. This can be expected due to the fact some features in Table 2 are a linear combination of others, e.g. $\phi_3 = \phi_1 + \phi_2$.

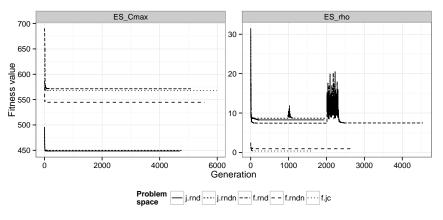


Fig. 3 Fitness for optimising (w.r.t. Eqs. (6) and (7) above and below, receptively), per generation of the CMA-ES optimisation.Table 3 Final results for CMA-ES optimisation; total number of generations and function evalua-

tions and its resulting fitness value for both performance measures considered.

(a) w.r.t. Eq. (6)	(b) w.r.t. Eq. (7)				
\mathscr{P} #gen #eval ES $_{C_{\max}}$	\mathscr{P} #gen #eval ES_{ρ}				
j.rnd 4707 51788 448.612	j.rnd 1944 21395 8.258				
j.rndn 4802 52833 449.942	j.rndn 1974 21725 8.691				
f.rnd 5088 55979 571.394	f.rnd 4546 50006 7.479				
f.rndn 5557 61138 544.764	f.rndn 2701 29722 0.938				
f.jc 5984 65835 567.688	f.jc 1625 17886 0.361				

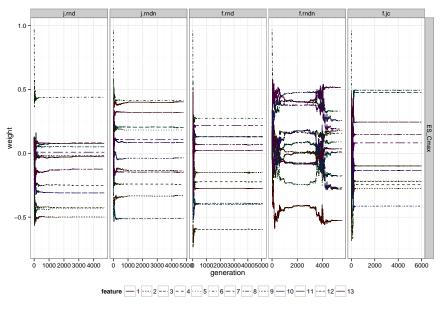
5.3 Scalability

As a benchmark, the linear ordinal regression model (PREF) from [10] was created. Using the weights obtained from optimising Eq. (7) and applying them on their

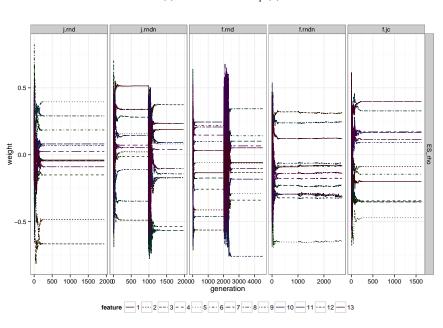
 6×5 training data. Their main statistics of Eq. (5) are reported in Table 4 for all training sets described in Table 1. Moreover, the best SDR from which the features in Table 2 were inspired by, are also reported for comparison, i.e., most work remaining (MWR) for all JSP problem spaces, and least work remaining (LWR) for all PFSP

problem spaces. To explore the scalability of the learning models, a similar comparison to Section 5.2 is made for applying the learning models on their corresponding 10×10

tion 5.2 is made for applying the learning models on their corresponding 10×10 testing data. Results are reported in Table 5. Note, that only resulting C_{max} is reported as the optimum makespan is not known and Eq. (5) is not applicable.



(a) minimise w.r.t. Eq. (6)



(b) minimise w.r.t. Eq. (7)

Fig. 4 Evolution of weights of features (given in Table 2) at each generation of the CMA-ES optimisation. Note, weights are normalised such that $\|\mathbf{w}\| = 1$.

Table 4 Main statistics of percentage relative deviation from optimality, ρ , defined by Eq. (5) for various models, using corresponding 6×5 training data.

 $a \times a6 \times 5$

() 786×5

	(a)	$\mathscr{P}_{j.rr}^{6\times}$	nd					(b)	$\mathscr{P}_{j.rr}^{6\times}$	o ıdn		
model	mean	med	sd	min	max		model	mean	med	sd	min	max
$\mathrm{ES}_{C_{\mathrm{max}}}$	8.54	10	6	0	26		$ES_{C_{max}}$	8.68	11	6	0	31
ES_{ρ}	8.26	10	6	0	26		ES_{ρ}	8.69	11	6	0	31
PREF	10.18	11	7	0	30		PREF	10.00	11	6	0	31
MWR	16.48	16	9	0	45		MWR	14.02	13	8	0	37
	(c)	$\mathscr{P}_{f.r.}^{6 imes}$	5 nd					(d)	$\mathscr{P}_{f.r.}^{6 imes}$	5 ndn		
model	mean	med	sd	min	max		model	mean	med	sd	min	max
$\mathrm{ES}_{C_{\mathrm{max}}}$	7.44	7	5	0	23		$\mathrm{ES}_{C_{\mathrm{max}}}$	8.09	8	2	0	11
	7.48	7	5	0	34		ES_{ρ}		1	1	0	4
PREF	9.87	9	7	0	38		PREF		2	1	0	7
LWR	20.05	19	10	0	71		LWR	2.25	2	1	0	7
(e) $\mathscr{P}_{f,jc}^{6\times5}$												
model mean med sd min max												
		I	$\mathrm{ES}_{\mathcal{C}}$	max	0.33		0 0	0 2				
		I	ES_{ρ}		0.36	(0 0	0 2				
			PRÍ		1.08		1 1	0 5				
		I	W	R	1.13		1 1	0 6				

6 Discussion and conclusions

distributions, continuing the preliminary experiments in [10], or w.r.t. the job ordering permutations – i.e., homogeneous machine order for PFSP versus heterogeneous machine order for JSP. From the results based on 6×5 training data given in Table 4, it's obvious that CMA-ES optimisation substantially outperforms the previous PREF methods from [10] for all problem spaces considered. Furthermore, the results hold when testing on 10×10 (cf. Table 5), suggesting the method is indeed scalable to higher dimensions.

Data distributions considered in this study either varied w.r.t. the processing time

search is worth investigating. There was no statistical difference from minimising the fitness function directly and its normalisation w.r.t. true optimum (cf. Eqs. (6) and (7)), save for $\mathcal{P}_{f.rndn}$. Implying, even though ES doesn't rely on optimal solutions, there are some problem spaces where it can be of great benefit. This is due to the fact that the problem instances can vary greatly within the same problem space [11]. Thus normalising the objective function would help the evolutionary search to deviate from giving too much weight for problematic problem instances.

Moreover, the study showed that the choice of objective function for evolutionary

Table 5 Main statistics of C_{max} for various models, using corresponding 10×10 test data.

(b) @10×10

(a) @10×10

(a) $\mathscr{P}_{j.rnd}$	(b) $\mathcal{S}_{j.rndn}^{100000}$					
model mean med sd min max	model mean med sd min max					
ES _{C_{max}} 922.51 914 73 741 1173 ES _ρ 931.37 931 71 735 1167 PREF 1011.38 1004 82 809 1281 MWR 997.01 992 81 800 1273	ES _{C_{max}} 855.85 857 50 719 1010 ES _ρ 855.91 856 51 719 1020 PREF 899.94 898 56 769 1130 MWR 897.39 898 56 765 1088					
(c) $\mathscr{P}_{f.rnd}^{10\times10}$	(d) $\mathscr{P}_{f.rndn}^{10\times10}$					
model mean med sd min max	model mean med sd min max					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	ES _{Cmax} 1065.48 1059 32 992 1222 ES _p 980.11 980 8 957 1006 PREF 987.49 988 9 958 1011 LWR 986.94 987 9 959 1010					
(e) $\mathscr{P}_{f,ic}^{10\times 10}$						

(e) $\mathscr{P}_{f.jc}^{ion}$

model	mean	med	sd	mın	max
$\mathrm{ES}_{C_{\mathrm{max}}}$	1135.44	1134	286	582	1681
	1135.47				
PREF	1136.02	1135	286	582	1685
LWR	1136.49	1141	287	581	1690

The main drawback of using evolutionary search for learning optimal weights for Eq. (1) is how computationally expensive it is to evaluate the mean expected fit-

ness. Even for a low problem dimension 6-job 5-machine JSP, each optimisation run reached their walltime of 288 hours without converging. Now, 6×5 JSP requires 30 sequential operations where at each time step there are up to 6 jobs to choose from – i.e., its complexity is $\mathcal{O}(n^{n \cdot m})$ making it computationally infeasible to apply this framework for higher dimensions as is. However, evolutionary search only requires the rank of the candidates and therefore it is appropriate to retain a sufficiently accurate surrogate for the value function during evolution in order to reduce the number of costly true value function evaluations, such as the approach in [9]. This could reduce the computational cost of the evolutionary search considerably, making it feasible to conduct the experiments from Section 5 for problems of higher dimen-

sions, e.g. with these adjustments it is possible to train on 10×10 and test on for example 14×14 to verify whether scalability holds for even higher dimensions.

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