RNA-seq: Differential expression

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STAT/BIOF/GSAT 540 2015
Lecture

Outline

- Look more closely at real data
- Motivation for new differential expression methods
- Weighted regression approach ('limma-voom')
- Methods specific for count data (EdgeR and DESeq)

Properties of data sets

Study	PMID	Species	Samples	UniqueAlignedReads	ReadsPerSample	Notes
bodymap	22496456	human	19	2,197,622,796	115,664,358	Illumina Human BodyMap 2.0 tissue comparison
modencodefly	21179090	fly	30	2,278,788,557	75,959,619	developmental time course
modencodeworm	19181841	worm	46	1,451,119,823	31,546,083	developmental time course
yang	20363980	mouse	1	27,883,862	27,883,862	hybrid cell line, X always inactive
trapnell	20436464	mouse	4	111,376,152	27,844,038	time course
mortazavi	18516045	mouse	3	61,732,881	20,577,627	tissue comparison
cheung	20856902	human	41	834,584,950	20,355,730	HapMap - CEU
hammer	20452967	rat	8	158,178,477	19,772,310	experimental vs. control at 2 time points
bottomly	21455293	mouse	21	343,445,340	16,354,540	2 inbred mouse strains
montgomery+pickrell	20220756	human	60	886,468,054	14,774,468	HapMap - CEU+YRI
wang	18978772	human	22	223,929,919	10,178,633	tissue comparison
gilad	20009012	human	6	41,356,738	6,892,790	liver; males and femlaes
core	19056941	human	2	8,670,342	4,335,171	lung fibroblasts
katz.mouse	21057496	mouse	4	14,368,471	3,592,118	control vs. CUG-BP1 knockdown myoblasts
nagalakshmi	18451266	yeast	4	7,688,602	1,922,151	priming technique comparison
sultan	18599741	human	4	6,573,643	1,643,411	cell type comparison

Modified from http://bowtie-bio.sourceforge.net/recount/

Case study: The gilad data set

Letter

Sex-specific and lineage-specific alternative splicing in primates

Ran Blekhman, 1,4,5 John C. Marioni, 1,4,5 Paul Zumbo, 2 Matthew Stephens, 1,3,5 and Yoav Gilad 1,5

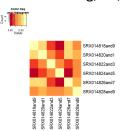
¹Department of Human Genetics, University of Chicago, Chicago, Illinois 60637, USA; ²Keck Biotechnology Laboratory, New Haven, Connecticut 06511, USA; ²Department of Statistics, University of Chicago, Chicago, Illinois 60637, USA
Genome Res. 2010 Feb;20(2):180-9

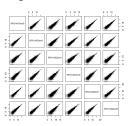
- Six human liver samples (3M 3F)
- Illumina GAII, two lanes per sample. 32bp?
- 13,000 genes detected according to authors
- 627 genes reported as "sexually dimorphic" in H.s.

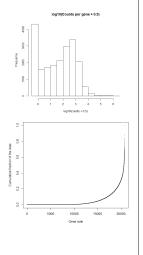
What I got via their supplement table 1: 20689 x 6 matrix with Ensembl gene IDs. (different version available through bowtie web site)

Gilad data set, cont'd

- Total read count: 20,679,864 (2.8 4.3 million per sample, mean=3.4 million)
- 4314 genes have 0 counts (total in 6 samples)
- 7599 have less than 10 counts total
- 196 genes have over 10000
 - ightarrow 11,527,345 counts for those genes (56%) Albumin (12%); complement, Jun, fibrinogen, serpins, APOs
- After some filtering, 10,720 genes.

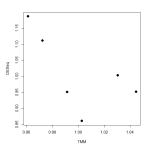






Scale factors for the Gilad data set

lib.size	ТММ	DESeq	TMM, unfilt.	DESeq, unfilt.
2096011	1.031	1.002	0.99	1.00
2072827	0.991	0.951	0.92	0.95
1968729	1.045	0.951	1.15	0.963
1862868	1.003	0.866	1.02	0.858
2673491	0.961	1.18	0.92	1.185
2476156	0.972	1.11	0.99	1.115



Differential expression: Why we might need new methods

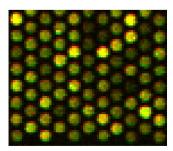
- Goal: accurate p-values for our hypothesis tests
- Properties relied upon for inference from *t* statistics shouldn't hold for count data.
- Perhaps most important: Heteroscedasticity
 - Strong mean-variance relationship *expected* with count data.

One challenge: Most evaluations are based on simulations. There are no widely used/accepted gold standards.

Properties of expression data: counts

Microarray

- Signal is fundamentally counts (deep down)
- But values are averaged across pixels and counts are high.
- Never really have zero: background ensures that values are not too small and thus "continuous"



http://www.genomics.agilent.com

Sequencing

- Unit of measurement is the read; no such thing as 0.1 read.
- · Counts of reads start at 0
- As counts get high, the distinction should diminish





NOTE: We are focused on the distribution of expression values for a gene across technical or biological replicates For this discussion we care less about comparing two genes within a sample.

Statistics of counts

- Say RNA for gene g is present "in the cell" at 1 out of 1,000,000 molecules.
 - Abundance a = 1/1,000,000 (1e-6)
- If we randomly pick $R_{lib}=1,000,000$ molecules ("reads"), how many gene g RNAs will we see? (R_g)

 $E(R_q | R_{lib}) = ?$. But could get 0 or 5 "by chance".

```
ightarrow R_g \sim Binomial(R_{lib}, a)
Approximately: R_g \sim Poisson~(R_{lib}*a)
As R_{lib}*a gets large, approx: R_g \sim Normal(R_{lib}*a, R_{lib}*a)
```

In all cases, variance is an increasing function of the mean

Options for doing differential expression on counts

Summary of the problem: Count data is expected to violate both normality and equal variance assumptions.

Possibilities for coping:

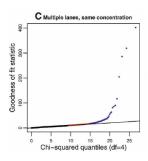
- Use a non-parametric test (e.g. SAM-seq based on Wilcoxon; larger sample sizes needed, will not discuss further)
- Make adjustments and use standard methodology
- Use a model specific for count data

 $Some\ material\ from\ Mark\ Robinson\ (http://www.fgcz.ch/education/StatMethods Expression/03_Count_data_analysis.pdf)$

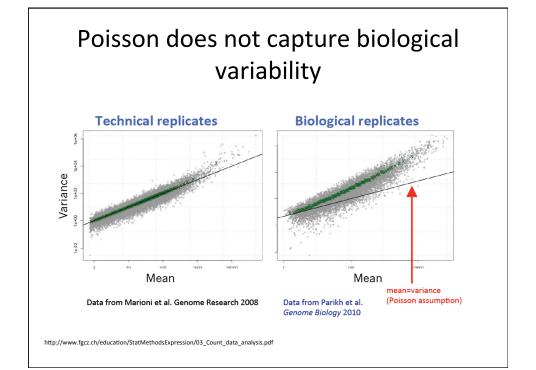
Poisson is appropriate for tech rep

(Marioni et al.)

- Looked for "systematic differences between results for the same sample, sequenced at the same concentration in different lanes, over and above those expected from sampling error"
- Differences reasonably well explained by Poisson statistics, but does not account for biological variation (back to this later)



http://genome.cshlp.org/content/18/9/1509.long



Impact of heteroscedasticity

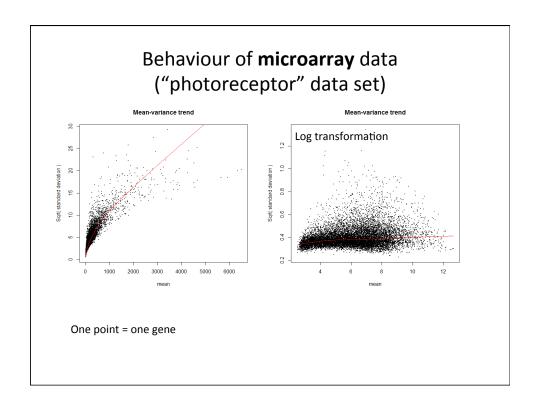
- OLS: assume all errors have same variance
- If not true: higher variance regions get more weight in minimization of error than they should (since they are less precise)

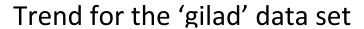
Standard errors of betas will be poor estimates Recall: $t = \hat{\beta}/\hat{\sigma}$

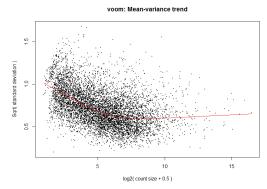
... So p-values will also be wrong; In case of positive relationship, too small.

Transformation can help

- log, square root, ...
- For microarray data, taking logs is often deemed sufficient (but see "VSN" and other methods)
- None of these seem to adequately remove the trends in RNA-seq data

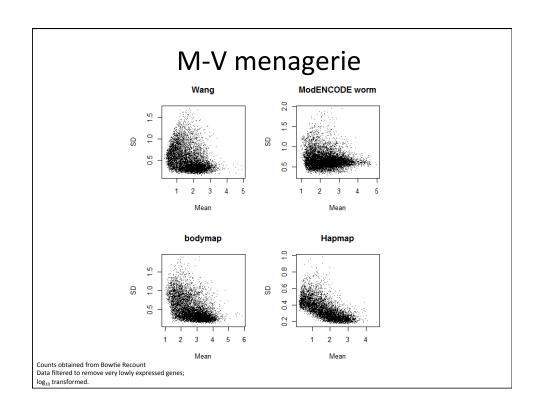


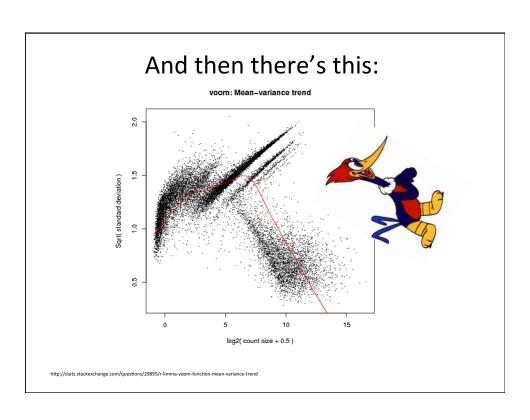




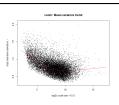
Typical for RNA-seq: Mean-variance relation is steepest for low log expression. Thus impact on inference is largest at low expression levels.

Law et al. (*Genome Biology* 2014, **15**:R29 2014) explain this: biological variability dominates at higher counts, technical (sampling) variability at lower counts.





Voom



Transformation approach to allow use of limma.

Key idea: Modeling the mean-variance relation is more important than getting the probability distribution exactly right.

Genome Biology 2014, 15:R29

Voom

"Voom is an acronym for 'mean-variance modelling at the observational level" $\!\!\!\!$

- 1. Fit your linear model to the data (log₂-transformed cpm)
- 2. Take the residuals. Their sqrt-stdev (quarter-root variance) per gene usually has a reasonable relationship with the mean; That is, consider $\hat{\mu} \sim \sqrt{sd}(\varepsilon)$
- 3. Fit a lowess smoother to this relationship (red line in plots)
- 4. Use the lowess to estimate the variance for each (fitted): get weights $w_i = 1/\text{lowessfit}(\widehat{c_i})^4$

where \widehat{C}_i is the \log_2 -transformed fitted cpm and lowessfit() provides the predicted sqrt-stdev.

Intuition: points where we are less sure of the actual value (higher variance) get lower weight in the analysis.

Getting observation-level estimates of variance

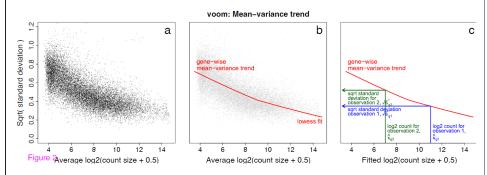


Figure 2 Voom mean-variance modeling. Panel (a), gene-wise square-root residual standard deviations are plotted against average log-count. Panel (b), a functional relationship between genewise means and variances is given by a robust lowess fit to the points. Panel (c), the mean-variance trend enables each observation to map to a square-root standard deviation value using its fitted value for log-count.

Genome Biology 2014, 15:R29

Weighted regression

R & Limma already supported weighted regression, so what it is?

Usual normal equations are

$$\hat{\beta} = (X^T X)^{-1} X^T y$$

Modified to use weights:

$$\hat{\beta} = (X^T W X)^{-1} X^T W y$$

Where W is a diagonal matrix

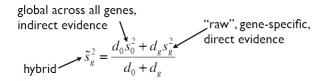
Intuition: In minimizing the residual, we want to "care less" about data points which are less precise.

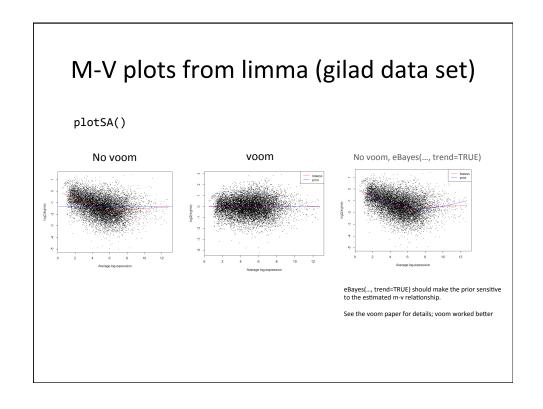
$$argmin(\hat{\beta}) \sum_{i}^{n} w_{i} (X_{i}^{T} \hat{\beta} - y_{i})^{2}$$

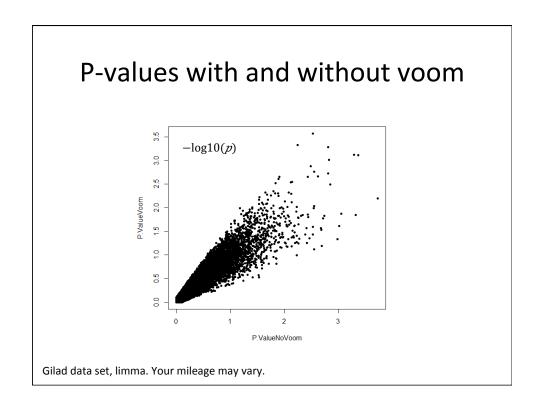
Thus the weights are expressed in terms of 1/variance. Hard part is estimating the variance (we end up treating it as "known") But if values are right, assumptions of linear least squares are restored.

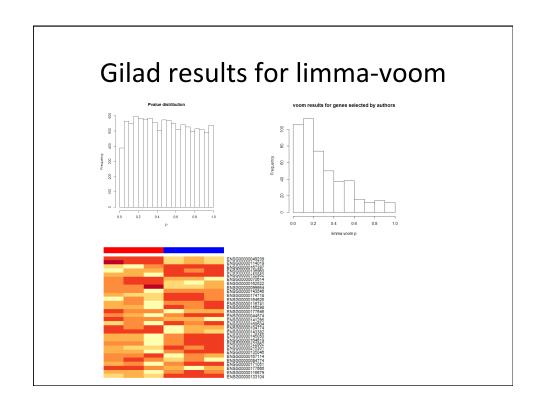
More about voom approach

- It does not modify the data. It only modifies the results of the lmFit call: the β values
- Residual standard error estimates are now (hopefully) better
- limma will further squeeze those:









Using a model specific for counts

- Implementation: EdgeR, DESeq, baySeq, others
- Some groups used a Poisson model, but field moved to using negative binomial in a generalized linear model framework
- Originally approaches developed with SAGE in mind: small sample sizes, low "library size"

(>1 million tags would be very unusual. 50-100k typical).

More recently influenced by RNA-seq data.

EdgeR and DESeq

- Use negative binomial distribution.
- In addition, both try to address the meanvariance trend in special ways. How they do this is the main difference.
 - Both use NB + GLMs (and offer simpler method if you have a one-way layout)
 - Both use m-v trends to help moderate dispersion estimates
- At best generate estimates of variance for each gene; voom does this for each observation.
- Caution: peer-reviewed explanations may be out of date (esp. for DESeq), look at user manuals!

Negative binomial distribution

- A gamma mixture of Poisson distributions
 - Count sampling distribution = Poisson
 - Biological sampling means from gamma
 - i.e., distribution of replicates
- "Overdispersed Poisson"
- Has an extra parameter to estimate compared to Poisson: the dispersion.
- Key problem: Estimating the dispersion from small data sets is tricky.

Modeling using negative binomial dist.

$$\sigma^2_i = \mu_i (1 + \mu_i \phi_i)$$

where ϕ_i is the dispersion for gene i. With ϕ =0, get Poisson.

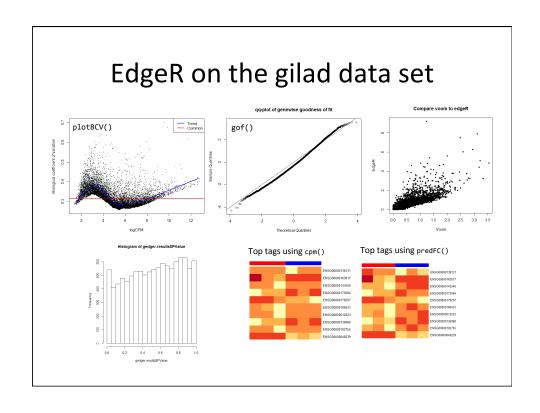
Could estimate directly from the data for gene \emph{i} , but hard to trust data from small samples

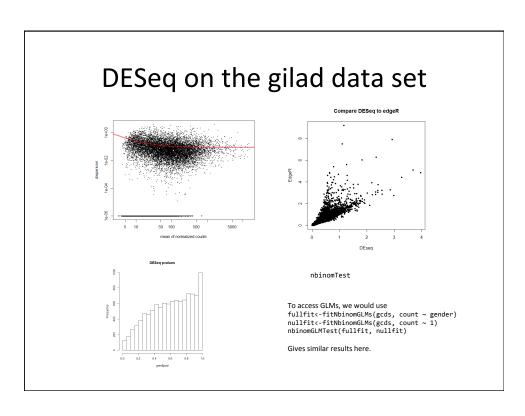
Another option is to make ϕ a parametric function of the mean (e.g. quadratic). But popular methods use more flexible approach:

 $\mathbf{edgeR:}\ \phi \ \text{is gene-specific but moderated towards a trend}.$

estimateGLMTrendedDisp — fits the trend (bin and fit spline) followed by estimateGLMTagwiseDisp — squeezes towards the trend Early versions of edgeR used a common estimate and then squeezing

DESeq: ϕ also gene-specific: use trended value unless direct estimate is higher for gene (but offers many other options including ones that make it more like edgeR; see help for estimateDispersions)





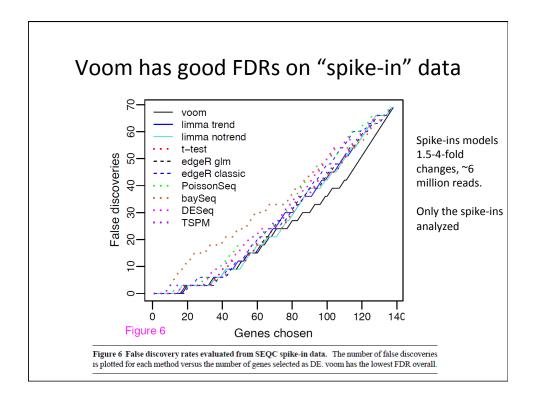
Summary of the differences between edgeR and DESeq

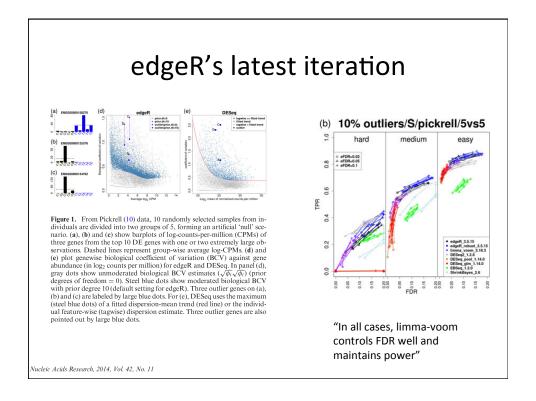
- Dispersion estimation
 - "edgeR uses moderated dispersion (towards trend)"
 - "DESeq use maximum of fitted trend and genewise" (conservative) DESEq2 tries to fix this
 - "edgeR is somewhat sensitive to outliers, but DESeq suffers somewhat in power" - edgeR-robust tries to fix outlier sensitivity.
- Normalization
 - TMM -weighted trimmed mean of M-value
 - DESeq sample--wise median ratio

Also, GLM features of DESeq are more limited than edgeR. Only provides p-values and some fit statistics; no 'toptable' and no easy facilities for accessing specific contrasts. So for complex designs edgeR is easier.

Quotes from http://www.fgcz.ch/education/StatMethodsExpression/ 03_Count_data_analysis.pdf

Voom does well in simulations 10 0.04 10 0.04 10 0.04 10 0.05 10 0.04 10 0.05





How do we choose a method?

- · There is no great gold standard to use. Simulations somewhat unsatisfying, spike-ins not completely realistic
- EdgeR and DESeq are very similar in design; latest versions may fix many of the issues they had last year.
- **Limma-voom** has emerged as a sound choice
 - Performs as well or better than NB (see paper for explanations why)
 - Flexible, fast
 - Familiar to limma users
- * None of the methods discussed deal specially with splice variants: See cuffdiff and DEXSeq, limma::diffSplice or quantify at transcript (or exon) level and proceed as usual.

Selected bibliography

Robinson and Smyth, 2008 Biostatistics 9:321-332. Introduces NB model, common dispersion estimate; qCML libSizes, exact test for diff ex. from NB.

Zhou et al., 2014 Nucleic Acids Research - doi: 10.1093/nar/gku310 - Describes edgeR-robust

*Robinson and Oshlack 2010 Genome Biology 11:R25. Library space concept and TMM normalization.

Oshlack et al. 2010 Genome Biology 11:220 Useful review, but already out of date.

Bullard et al. 2010 BMC Bioinformatics 11:94. Evaluation of Fisher's test, Poisson GLM and t-test. Proposes "gold standard" based on MAQC data.

Auer and Doerge 2010 Genetics 185:405-416. Proposes Poisson GLM with overdispersion.

*Anders and Huber 2010 Genome Biology 11:R106. Introduces DESeq, trended dispersion estimate, normalization method; and a diff ex method for one-way layouts. Love et al. 2014 Genome Biology http://genomebiology.com/2014/15/12/550/abstract Describes DESeq2

Blekhman et al. 2010 Genome Research 20(2):180-9. "Sex-specific and lineage-specific alternative splicing in primates" Source of the 'gilad' data set.

Mardis 2011 Nature 470: 198-203 - Good review of sequencing technology but probably already out of date. Di et al. Stat. Appl. in Genetics Mol. Bio. 2011 vol10. Introduction is a useful review of statistical approaches

McCarthy et al., 2012 NAR: Extension of edgeR to GLM; Decomposition of TCV and BCV; adds trended dispersion.

Lund et al. Stat. Appl. in Genetics Mol. Bio. 2012 11:5. McCarthy and Smyth are coauthors on this paper that shows that EdgeR and DESeq do not give accurate p-values. Proposes another NB method using quasi-likelihood to address the problems.

* Law et al. Voom: precision weights unlock linear model analysis tools for RNA-seq read Counts Genome Biology 2014, 15:R29. Paper from Smyth formally describing Voom and evaluation of its performance.

DESeg. EdgeR and limma user manuals

Drzecy, zugera niu minima des minima in "Mark Robinson lecture sildes: <u>http://www.fecz.ch/education/StatMothodsExpression.</u> lectures 3 and 4 – very useful! Davis McCarthy 2009 Thesis Bloconductor forums