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HONOURS THESIS

A cellular automata approach to model informal settlement growth

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“The main problems in life can only be solved when you know what works, what doesn’t and why”

Charlie Munger, American investor and billionaire

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Abstract

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Abstract will come here in the future.

Acknowledgements

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CA	Cellular Automata
UN	United Nations
StatsSA	Statistics South Africa

Dedicated to John Horton Conway (1937-2020)

Chapter 1

Introduction

1.1 Project description

The process of urbanisation has been a double edged sword whereby many a people have benefited from it while a lot more have not. The issue of informal settlements is one that covers areas such socio-economic, governance, climate, politics, healthcare, and resource management to name a few.

One of the few approaches to tackle these issues is through good modelling, and understanding the growth of such informal settlements.

This project will employ a cellular automata technique, specifically John Conway's 'Game of Life' to model informal settlement growth in South Africa.

1.2 Problem description and background

From the 1950s to the early 2000s the rate of urbanisation has increased 20%, however the amount of people living in inadequate housing, informal settlements, and slums globally is still about 1 billion.[13]

According to the United Nations (UN) the definition of an informal settlement is a dwelling with a lack of security, sanitation, water, living area, and housing durability.[6]

The UN also has a list of 17 Sustainable Development Goals of which number 11 is to create 'Sustainable Cities and Communities'. These goals are such that if even a few can be achieved the other will become easier to achieve as well. Discuss Informal settlement framework(what, where, when, how of informal settlements)

Cellular Automata (abbreviated as CA) is a discrete computational model which is studied in automata theory. The basic components of such a model is a grid which contains cells. Each cell can have a finite number of states it

can take on. An initial state at time ($t = 0$) is assigned to the grid as a whole. For each time interval thereafter the cells change their states according to a predefined set of rules.[11]

Conway's *Game of Life* also known as *Life* was created by the British Mathematician John H Conway in the 1970s and first appeared in the *Scientific American* magazine.[5]

The states the cells in Life can take on are either alive or dead. The rules that govern the states of Life are as follows:

1. Due to under-population a cell will die if it has less than 2 neighbours¹.
2. If a cell has 3 or 2 neighbours it will remain alive in the next cycle.
3. If a cell has more than 3 neighbours it will die.
4. If a dead cell is surrounded by 3 alive cells it will become alive in the next cycle.

Using such a set of rules this project will embark on creating a model that will accurately predict informal settlement growth in South Africa.

Some limitations have been noted in using CA to model urban growth. These include creating trade-offs between flexibility and simplicity for the transitional rules. At the same time other opportunities in CA models also present themselves for study such as calibration, stochastic components, and cell types.[10]

1.3 Aims and objectives

1.3.1 Aims

- Create a sound mathematical and statistical model
- Apply model to Life to predict growth of informal settlements

1.3.2 Objectives

- Conduct the relevant literature reviews
- Get access to relevant maps needed regarding informal settlements

¹These are cell which are alive and are located around the current cell

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- If above step fails, create own maps
 - Create an application that allows a map to be added and a grid to be placed for simulating Life.
 - Create a mathematical and statistical model to provide an initial state
 - Apply initial state to the map
 - Iterate and monitor growth output
 - Calculate accuracy of model by comparing maps from different time periods

Chapter 2

Literature Review

2.1 Cellular Automata and Game of Life

Cellular Automata can be modelled in a number of dimensions including anything from one, two, three, four, or more dimensions.[1] In this project the focus will be on the two dimensional approach using a n -dimensional lattice (will be referred to as a grid). The grid can be of infinite size, however will be limited to a finite space i.e. a predetermined set of cells superimposed over a map of an informal settlement.

An individual square in the grid (which will be referred to as a cell) can have upto eight neighbours. This is shown in the diagram below.

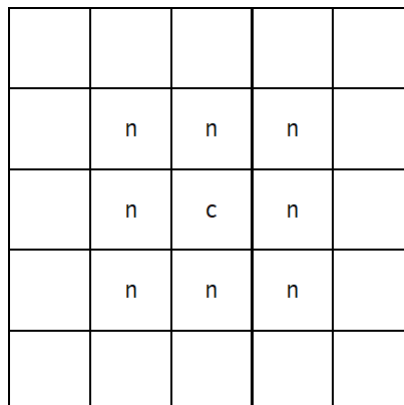


FIGURE 2.1: A cell 'c' and its neighbours 'n'

Source: Own Creation (2021)

A cell can have two discrete states for any given discrete time unit (referred to as generation). These states can be 'alive' or 'dead'. A cell is shown to be alive by having it *shaded* and if it is dead it is left blank.[1] This is shown in the figure below.

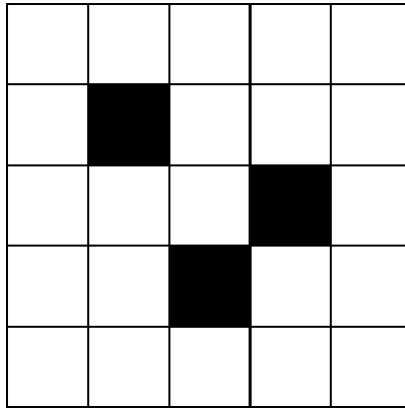
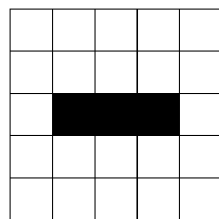
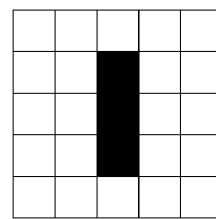


FIGURE 2.2: A grid showing alive and dead cells

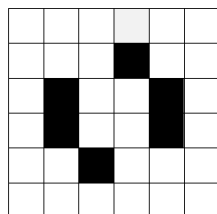
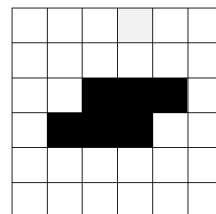
Source: Own Creation (2021)

As shown in Figure 2.1 a cell can have either lateral or diagonal neighbours. The rules of *Life* were discussed briefly above in Section 1.2. A graphical representation of these is shown below.

(A) Generation $t = 0$ (B) Generation $t = 1$ FIGURE 2.3: A simple 2 generation iteration of *Life*

Source: Own Creation (2021)

Another slightly more advanced setup of *Life* is shown below.

(A) Generation $t = 0$ (B) Generation $t = 1$ FIGURE 2.4: An advanced 2 generation iteration of *Life*

Source: Own Creation (2021)

In a seminal paper by Stephen Wolfram, four classes of CA were proposed according to their behaviour given an initial random condition .[12] These four classes are as follows:

- Class 1 - After a finite number of generations a unique homogeneous state is reached i.e. all cells become the same eventually.
- Class 2 - Simple structures are generated which are either periodic, or stable (also called persistent).
- Class 3 - An aperiodic (or chaotic) patterns emerge which carry on indefinitely.
- Class 4 - Capable of universal computations i.e. can exhibit complex behaviour.

Due to the nature of the rules of *Life* certain patterns emerge. This is thanks to the cycles of repeated states which evolve over certain number of generations. These patterns include still-lives, period two (or *blinkers*), gliders, oscillators, glider guns, and puffer trains.[1]

The applications of CA and, or *Life* have sparked a number of research papers in fields such as physics, music, complexity, and computation.

Examples in physics include, interaction between a complex system and electromagnetic radiation [2], an implementation of *Life* with quantum features.[4]

Implementations in music include the development of CAMUS (Cellular Automata Music).[8]

In the fields of complexity, and computation a vast array of work has been done therefore a few examples include; Universal Computer-Constructor in CA [7], and creation of a Turing Machine in *Life*. [9]

2.2 Informal settlements

Informal settlements are housing dwellings that are part of urban districts or neighbourhoods that arise and develop without oversight or control from the state. They are synonymous with 'slums' or 'squatters', though are not the same. They form an integral element of urban sustainability whereby developing cities can not develop without them. The connotations with 'informal', 'slums', and 'squatter' have always been seen in a negative light. This is not seen as beneficial as the growth of urbanisation is highly intertwined with

informal settlements.[3]

Across the globe informal settlements are known colloquially by their own variety of terms. [13] In this project the umbrella term informal settlement will be utilised.

The process of informal settlements growth can be grouped into three categories namely:[3]

- *settling* - simply settling down on what is usually unclaimed land
- *inserting* - usually into urban areas that are abandoned, or uninhabited
- *attaching* - informal settlements that grow out of existing urban settlements

In morphological terms, informal settlements can be classified into eight different types. This refers to the urban conditions rather than the process mentioned above, however it is not to say that the two are mutually exclusive. The types are not mutually exclusive from each other either. The types are as follows:[3]

- Districts -
- Waterfronts -
- Escarpments -
- Easements -
- Sidewalks -
- Adherences -
- Backstages -
- Enclosures -

Bibliography

- [1] A. Adamatzky. *Game of Life Cellular Automata*. Springer London, 2010. ISBN: 9781849962179. URL: <https://books.google.co.za/books?id=5iz6C0zzWKcC>.
- [2] Claudio Conti. “The Enlightened Game of Life”. In: *Game of Life Cellular Automata* (Oct. 2008). DOI: [10.1007/978-1-84996-217-9_22](https://doi.org/10.1007/978-1-84996-217-9_22).
- [3] Kim Dovey and Ross King. “Forms of informality: Morphology and visibility of informal settlements”. In: *Built Environment* 37.1 (2011), pp. 11–29.
- [4] Adrian Flitney and Derek Abbott. “Towards a Quantum Game of Life”. In: Jan. 2010, pp. 465–486. ISBN: 978-1-84996-216-2. DOI: [10.1007/978-1-84996-217-9_23](https://doi.org/10.1007/978-1-84996-217-9_23).
- [5] Martin Gardner. “MATHEMATICAL GAMES”. In: *Scientific American* 223.4 (1970), pp. 120–123. ISSN: 00368733, 19467087. URL: <http://www.jstor.org/stable/24927642>.
- [6] *Goal 11: Make cities and human settlements inclusive, safe, resilient and sustainable - SDG Indicators*. URL: <https://unstats.un.org/sdgs/report/2016/goal-11/>.
- [7] Adam Goucher. “Universal Computation and Construction in GoL Cellular Automata”. In: *Game of Life Cellular Automata*, ISBN 978-1-84996-216-2. Springer-Verlag London Limited, 2010, p. 505 (Jan. 2010). DOI: [10.1007/978-1-84996-217-9_25](https://doi.org/10.1007/978-1-84996-217-9_25).
- [8] Eduardo Miranda and Alexis Kirke. “Game of Life Music”. In: *Game of Life Cellular Automata*, ISBN 978-1-84996-216-2. Springer-Verlag London Limited, 2010, p. 489 (Jan. 2010). DOI: [10.1007/978-1-84996-217-9_24](https://doi.org/10.1007/978-1-84996-217-9_24).
- [9] Paul Rendell. “A Simple Universal Turing Machine for the Game of Life Turing Machine”. In: *J. Cellular Automata* 6 (Jan. 2011), pp. 323–340. DOI: [10.1007/978-1-84996-217-9_26](https://doi.org/10.1007/978-1-84996-217-9_26).

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- [10] Inés Santé et al. "Cellular automata models for the simulation of real-world urban processes: A review and analysis." In: *Landscape and Urban Planning* 96.2 (2010), pp. 108 –122. ISSN: 0169-2046.
- [11] Tommaso Toffoli and Norman Margolus. *Cellular automata machines : a new environment for modeling*. Cambridge, Mass: MIT Press, 1987. ISBN: 9780262200608.
- [12] Stephen Wolfram. "Universality and complexity in cellular automata". In: *Physica D: Nonlinear Phenomena* 10.1-2 (1984), pp. 1–35. DOI: [10.1016/0167-2789\(84\)90245-8](https://doi.org/10.1016/0167-2789(84)90245-8).
- [13] *World Cities Report 2016 Urbanization and Development: Emerging Futures*. United Nations Pubn, July 2016. 260 pp. ISBN: 9211327083.