

Custom score 1

Number of blank cells in the board. This is the simplest heuristic we can get after relaxing constraints on the original problem.

Custom score 2

Difference of legal moves of current player and opponent player along with hashing of heuristic score for the game state

Custom score 3

Sum of legal moves of both players. This is another relaxation of heuristic of custom score 1 taking only legal moves.

Playing Matches

Match #	Opponent	AB_Improved		AB_Custom		AB_Custom_2		AB_Custom_3	
		Won	Lost	Won	Lost	Won	Lost	Won	Lost
6	4	7	3	7	3	8	2		
6	4	7	3	6	4	8	2		
5	5	8	2	9	1	6	4		
6	4	8	2	8	2	7	3		
5	5	8	2	6	4	7	3		
5	5	7	3	8	2	8	2		
4	6	6	4	8	2	7	3		
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Win Rate:		52.9%		72.9%		74.3%		72.9%	

As we can see on hashing custom 2 gave better results as it could go to deeper depth in the same time then if we were not using hashing. Custom1 and custom 3 are more general heuristic and could lead to wrong path thereby a slightly less winning percentage.