AMAT 362—Work Sheet 21

Dr. Justin M. Curry

Due: April 25, 2022. Worth 15 points.

	Name:
1.	(3 points) Suppose X and Y are independent and uniformly distributed on $[0,1]$. (a) (1 point) Find the PDF of $X+Y$
	(b) (1 point) What's the probability $P(X + Y \le 1)$?
	(c) (1 point) Find the PDF of $X - Y$.

- 2. (3 points) Suppose again that X and Y are independent and uniformly distributed on [0,1].
 - (a) (1 point) Find $P(X^2 + Y^2 \le 1)$

(b) (1 point) Find $P(X^2 + Y^2 \le 1) \mid X + Y \ge 1$)

(c) (1 point) Find $P(Y \le X^2)$.

3. (2 points) Two people try to meet at a certain place between 5pm and 5:30pm. Suppose each person arrives independently and uniformly at random in this window in time and then waits 5 minutes to see if the other person is there. What's the probability of them meeting?

4. (7 points) Suppose (X,Y) is uniformly distributed over the region $\{(x,y) \mid 0 < x < y < 1\}$

(a) (2 points) Compute the PDF of Y-X.

- (b) (1 point) Are X and Y independent?
- (c) (1 point) Find E(Y X).
- (d) (3 points) Find the *covariance* of X and Y.