## LR Parsing Example

Computer Science 426

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## Grammar

| goal                  | $\rightarrow$                       | expr   |
|-----------------------|-------------------------------------|--|
| expr                  | $\rightarrow$                       | term - expr  |
|                       |                                     | term   |
| $\operatorname{term}$ | $\stackrel{\cdot}{\longrightarrow}$ | factor * term  |
|                       |                                     | factor   |
| factor                | $\rightarrow$                       | id   |
|                       | expr                                | $\begin{array}{ccc} \exp r & \rightarrow & \\ &   \\ \operatorname{term} & \rightarrow & \\   &   \end{array}$ |

## **Action and Goto Tables**

|       | ACTION |    |    | GOTO |      |      |        |
|-------|--------|----|----|------|------|------|--------|
|       | id     | -  | *  | eof  | expr | term | factor |
| $S_0$ | s4     | _  | _  | _    | 1    | 2    | 3      |
| $S_1$ | _      | _  | _  | acc  |      | _    | _      |
| $S_2$ | —      | s5 | _  | r3   |      |      |        |
| $S_3$ | —      | r5 | s6 | r5   |      |      |        |
| $S_4$ | —      | r6 | r6 | r6   |      |      | _      |
| $S_5$ | s4     |    | —  |      | 7    | 2    | 3      |
| $S_6$ | s4     |    |    |      |      | 8    | 3      |
| $S_7$ |        |    |    | r2   |      |      |        |
| $S_8$ | —      | r4 |    | r4   | _    | _    |        |

## Algorithm

```
push '$'
\operatorname{\mathtt{push}}\ s_0
token \( \to \text_token()
repeat forever
    \texttt{s} \; \leftarrow \; \texttt{top of stack}
    if ACTION[s,token] = "reduce\ A \to \beta" then
        pop 2 * |\beta| symbols
        \texttt{s} \; \leftarrow \; \texttt{top of stack}
                                      /* not a pop() */
        \operatorname{push} A
        push GOTO[s,A]
    else if ACTION[s,token] = "shift s_i" then
        push token
        push s_i
        \texttt{token} \leftarrow \texttt{next\_token()}
    else if ACTION[s, token] = "accept" and
              token = eof then
        report success
    else report a syntax error
```

| Stack | Input | Action |
|-------|-------|--------|
| $s_0$ |       |        |
|       |       |        |
|       |       |        |
|       |       |        |
|       |       |        |
|       |       |        |
|       |       |        |
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|       |       |        |