

EWF User Manual

Contents

1	Release notes	1
1.1	Release 0.1	1
2	Installing Dependencies	2
2.1	Installing the g++ compiler	2
2.1.1	On Windows	2
2.1.2	On Mac	2
2.1.3	On Linux	2
2.2	Installing the boost library	3
2.2.1	On Windows and Linux	3
2.2.2	On MacOS	3
2.3	Installing python and pip	3
2.4	Installing CMake	3
2.5	Installing the pybind11 module in python	3
3	Installing EWF	3
4	Calling EWF in python	4
4.1	DiffusionRunner	4
4.2	BridgeDiffusionRunner	5
4.3	DiffusionDensityCalculator	5
4.4	BridgeDiffusionDensityCalculator	6
5	Parameter configuration	6
6	Example python scripts	7
7	Bugs, queries, suggestions, comments	7

1 Release notes

1. Initial release version 1.0, 28th December 2022
2. Release version 1.1, 26th March 2024

1.1 Release 0.1

We have patched up some bugs in the previous version, overhauled the user interface, simplified installation and included python bindings such that EWF can now be called from within python. We strongly encourage using EWF from within a python environment, and provide four ready-made functions which allow for the simulation of samples from both the diffusion and bridge diffusion, as well as the pointwise evaluation of the transition density for the neutral case. Users can further expose any C++ functionality present in EWF to python through the file `EWF_pybind.cpp`.

Using EWF from command line as in the initial release has been deprecated and is no longer possible.

2 Installing Dependencies

EWF requires the following components to be run

1. `g++` compiler
2. `boost` library
3. `python` together with `pip`
4. `CMake`
5. `pybind11`

The following instructions are meant to illustrate how to install the above, and are functional as of the 26th March 2024. Please note that new releases of the above software might require different installation procedures to the ones below, and thus there is no guarantee that these instructions are up to date nor correct for your specific platform!

2.1 Installing the `g++` compiler

2.1.1 On Windows

If `g++` is not present on your distribution (you can check this by typing `g++ -v` in Command Prompt, which will return all the information regarding the installed `g++` compiler together with its location if `g++` is present, otherwise an error will be returned):

1. Download the latest MinGW (`mingw-get-setup.exe`) from <https://osdn.net/projects/mingw/releases/>
2. Follow the installation prompts, note down where MinGW is installed (typically this would be `C:\MinGW`) and in the package selection menu choose the option `mingw32-gcc-g++-bin`. From the “Installation” drop down menu click on “Apply Changes”
3. Once installation is complete, go to System Properties and under the Advanced tab click on “Environment Variables”. Click on the Path field and edit it to include the location where the MinGW bin file was installed to (under a typical installation this would be `C:\MinGW\bin`)

To ensure that `g++` was installed as necessary, re-run `g++ -v` within Command Prompt which should now print out the location and further information regarding the compiler you installed.

NB: If you already have Microsoft Visual Studio Code installed on your platform, then we would suggest using the default compiler `MVSC` rather than installing any other compiler, as `pip` defaults to using `MVSC` if the latter is present!

2.1.2 On Mac

If `g++` is not present on your platform (you can check this by running `g++ -dumpversion | cut -f1 -d` within terminal), download the latest version of Xcode from the Mac App Store (this might take a while!) and install following the prompts. To check that `g++` was installed as necessary, re-run `g++ -dumpversion | cut -f1 -d` within terminal.

2.1.3 On Linux

If `g++` is absent from your distribution (within terminal type `g++ --version`), then from terminal run `sudo apt update` followed by `sudo apt install build-essential`. To check that installation was successful, re-run `g++ --version` in terminal. This should work on most Linux distributions, but if it does not please search online for an installation procedure for your specific distribution!

2.2 Installing the boost library

2.2.1 On Windows and Linux

From <https://www.boost.org/users/download/> download the latest version of `boost` (please note that EWF was written using `boost` version 1.84.0 and thus we cannot ensure that certain features are not superseded or deprecated in more up to date version of `boost` - if the latest version produces error on compiling, please download and install version 1.84.0). Once downloaded, extract the files to your desired location on your platform.

2.2.2 On MacOS

Download “HomeBrew” from `brew.sh` (installation instruction provided on webpage), and in terminal run `brew install boost` for the latest version of `boost`.

2.3 Installing python and pip

On Windows/Mac OS: Download the latest version of python from <https://www.python.org/downloads/> and run the installer.

On Linux: Run `sudo apt install python` in terminal.

NB: If you have a recent version of python, then `pip` is probably already present on your platform. If not, you can run `python3 get-pip.py` on Windows/Mac OS, or `sudo apt install python3-pip`.

2.4 Installing CMake

On Linux/Windows: Run `pip install cmake` in terminal/Command Prompt.

On MacOS: Run `brew install cmake` in terminal.

2.5 Installing the pybind11 module in python

On Linux/Windows: Run `pip install pybind11` in terminal/Command Prompt.

On Mac: Run `brew install pybind11` in terminal.

3 Installing EWF

NB: if using Windows, please ensure that your `PATH` variable (part of your environment variables) is pointing at the directories containing `g++`, `boost`, `python`, `pip`, `pybind11` and `CMake`. You can find out where `pybind11` and `CMake` are by running `python3 -v` and entering `import PACKAGE_NAME`.

To install EWF, run the following in terminal

```
$ mkdir build
$ cd build
$ cmake ..
$ cmake --build .
$ cd ..
$ pip install .
```

Provided all steps are followed and no errors are thrown, then you can test that EWF was run correctly by running the provided test cases found in the `examples` directory, which should print some information to terminal, and create two texts files together with a `png` file.

NB: To run the example script, you will need to have `numpy` and `matplotlib` installed in `python` (simply run `pip install PACKAGE` in terminal).

4 Calling EWF in python

To call EWF from within python, simply add `import EWF_pybind` at the start of your python script. This allows you to invoke the following four functions:

1. `DiffusionRunner` - which allows you to generate draws from the law of a Wright–Fisher diffusion
2. `BridgeDiffusionRunner` - which allows you to generate draws from the law of a Wright–Fisher diffusion bridge
3. `DiffusionDensityCalculator` - which allows you to evaluate the transition density of a Wright–Fisher diffusion
4. `BridgeDiffusionDensityCalculator` - which allows you to evaluate the transition density of a Wright–Fisher diffusion bridge

Detailed explanation of the above functions can be found below, whilst example scripts for running both simulation and pointwise evaluation of the transition densities for both diffusion and bridge diffusion cases can be found in the `example` directory.

NB: All four functions return `void`, and all relevant output is to be found in the corresponding output file (the name of which is provided as input by the user)!

4.1 DiffusionRunner

Generate `nSim` draws from the law $WF_{\sigma, \theta}^{(x)}$ sampled at time `endT`.

Parameters:

- `nSim` (*int*) - the number of simulated points desired
- `x` (*float*) - the starting point for the diffusion
- `startT` (*float*) - the starting time (in diffusion time units!) for the diffusion
- `endT` (*float*) - the desired sampling time (in diffusion time units!) for the diffusion
- `Absorption` (*bool*) - boolean dictating whether diffusion is conditioned on non-absorption at the boundary. This quantity is only relevant in cases when the mutation rate is zero at a boundary, and in particular is ignored if the mutation rate is strictly positive.
- `Filename` (*string*) - specifies the name of the file where the user desires to save their output
- `diffusion.threshold` (*float*, optional) - threshold below which Gaussian approximations are used. Unless specified, default is `diffusion.threshold = 0.1`

Returns: Resulting `nSim` draws are printed to file in `Filename`

4.2 BridgeDiffusionRunner

Generate `nSim` draws from the law $\mathbb{WF}_{\sigma, \theta}^{(t, x, z)}$ sampled at time `sampleT`.

Parameters:

- `nSim` (*int*) - the number of simulated points desired
- `x` (*float*) - the starting point for the diffusion bridge
- `z` (*float*) - the ending point for the diffusion bridge
- `startT` (*float*) - the starting time (in diffusion time units!) for the diffusion bridge
- `endT` (*float*) - the ending time (in diffusion time units!) for the diffusion bridge
- `sampleT` - the sampling time (in diffusion time units!) for the diffusion bridge
- `Absorption` (*bool*) - boolean dictating whether diffusion is conditioned on non-absorption at the boundary. This quantity is only relevant in cases when the mutation rate is zero at a boundary, and in particular is ignored if the mutation rate is strictly positive.
- `Filename` (*string*) - specifies the name of the file where the user desires to save their output
- `diffusion_threshold` (*float*, optional) - time threshold below which Gaussian approximations are used. Unless specified, default is `diffusion_threshold = 0.1`.
- `bridge_threshold` (*float*, optional) - time threshold below which a diffusion approximation and linear interpolation are used. Unless specified, default is `diffusion_threshold = 0.04`.

Returns: Resulting `nSim` draws are printed to file in `Filename`

4.3 DiffusionDensityCalculator

Compute the transition density for a *neutral* Wright–Fisher diffusion by appropriately truncating the infinite sums. Running on a non-neutral Wright–Fisher diffusion is not supported and will throw an error!

Parameters:

- `x` (*float*) - the starting point for the diffusion
- `startT` (*float*) - the starting time (in diffusion time units!) for the diffusion
- `endT` (*float*) - the desired sampling time (in diffusion time units!) for the diffusion
- `Absorption` (*bool*) - boolean dictating whether diffusion is conditioned on non-absorption at the boundary. This quantity is only relevant in cases when the mutation rate is zero at a boundary, and in particular is ignored if the mutation rate is strictly positive.
- `Filename` (*string*) - specifies the name of the file where the user desires to save their output
- `diffusion_threshold` (*float*, optional) - threshold below which Gaussian approximations are used. Unless specified, default is `diffusion_threshold = 0.1`

Returns: Resulting transition density evaluations are printed to file in `Filename`

4.4 BridgeDiffusionDensityCalculator

Compute the transition density for a *neutral* Wright–Fisher diffusion bridge by appropriately truncating the infinite sums. Running on a non-neutral Wright–Fisher diffusion is not supported and will throw an error!

Parameters:

- **x** (*float*) - the starting point for the diffusion bridge
- **z** (*float*) - the ending point for the diffusion bridge
- **startT** (*float*) - the starting time (in diffusion time units!) for the diffusion bridge
- **endT** (*float*) - the ending time (in diffusion time units!) for the diffusion bridge
- **sampleT** - the sampling time (in diffusion time units!) for the diffusion bridge
- **Absorption** (*bool*) - boolean dictating whether diffusion is conditioned on non-absorption at the boundary. This quantity is only relevant in cases when the mutation rate is zero at a boundary, and in particular is ignored if the mutation rate is strictly positive.
- **Filename** (*string*) - specifies the name of the file where the user desires to save their output
- **diffusion_threshold** (*float*, optional) - time threshold below which Gaussian approximations are used. Unless specified, default is `diffusion_threshold = 0.1`.
- **bridge_threshold** (*float*, optional) - time threshold below which a diffusion approximation and linear interpolation are used. Unless specified, default is `diffusion_threshold = 0.04`.

Returns: Resulting transition density evaluations are printed to file in **Filename**

5 Parameter configuration

Recall that EWF returns paths distributed according to the law of a diffusion or diffusion bridge satisfying the following stochastic differential equation

$$dX_t = \frac{1}{2} [\sigma X_t(1 - X_t)\eta(X_t) - \theta_2 X_t + \theta_1(1 - X_t)] dt + \sqrt{X_t(1 - X_t)} dW_t \quad (1)$$

for $t \geq 0$ with $X_0 \in [0, 1]$, where $\eta(x)$ is a finite degree polynomial in x , i.e. $\eta(x) = \sum_{i=1}^n a_i x^i$ for $n \in \mathbb{N}$. Such a formulation allows for a wide class of non-neutral regimes including the case of:

1. Genic selection - here $\eta(x)$ is set to be the constant function 1, such that the contribution from selection to the drift component in (1) becomes $\sigma X_t(1 - X_t)$ and σ is the only free parameter.
2. Diploid selection - here $\eta(x)$ is typically formulated as $\eta(x) = h + x(1 - 2h)$ with the free parameter $h \in \mathbb{R}$ determining the relative fitness of the heterozygotes and commonly termed the dominance parameter or degree of dominance. Thus in this case selection contributes a factor of $\sigma X_t(1 - X_t)(h + X_t(1 - 2h))$ to the drift in (1), where we now have 2 free parameters σ and h .

In the general case where $\eta(x)$ is a polynomial with degree $n \in \mathbb{N}$, the selection contribution becomes $\sigma X_t(1 - X_t) \sum_{i=1}^n a_i x^i$ and we now have $n + 1$ free parameters: σ and $\{a_i\}_{i=1}^n$.

The presence or absence of the mutation parameter $\theta = (\theta_1, \theta_2)$ dictates whether the boundary points $\{0, 1\}$ are absorbing or entrance/reflecting. Furthermore, whenever $\theta_1, \theta_2 > 0$, the corresponding boundary is reflecting and attainable if $\theta_i < \frac{1}{2}$ or entrance (and therefore unattainable) if $\theta_i \geq \frac{1}{2}$.

6 Example python scripts

In the examples directory there are two python scripts detailing how to use EWF from within python. After setting the desired Wright–Fisher diffusion parameters, the corresponding class is instantiated, and the simulator is invoked to generate 10,000 draws from the law of the diffusion. Subsequently the neutral transition density is estimated through the transition density calculator function, with the resulting estimate for the transition density being plotted on top of the histogram obtained from the previously simulated draws.

We point out that any further function users might wish to expose from the EWF C++ codebase to python can be included in the `EWF_python_bindings.cpp` file, but users must re-run `run.sh` for the implemented changes to be reflected in the EWF python module.

To run the example scripts, please ensure your python has the `numpy` and `matplotlib` packages installed.

7 Bugs, queries, suggestions, comments

If you spot any bugs, or have any queries, suggestions or comments please do not hesitate to get in touch on Jaromir.Sant@gmail.com!