

Data structures and algorithms

Tutorial 12

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Outline

1 Heap

- Definition
- Back to tree definitions
- Heap property
- Heap operation
- Complexity of the heap operations
- Mapping a heap into an array

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1 Heap

■ Definition

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What is a heap?

- A Heap is used to implement a priority queue
- A heap stores data in left-justified balanced binary tree

Outline

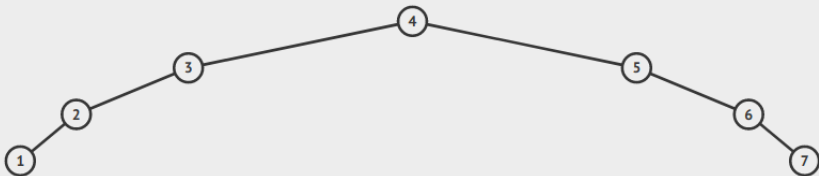
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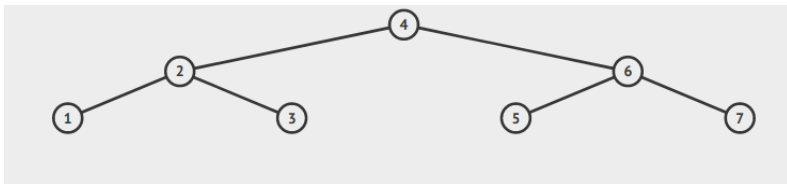
A binary tree is balanced if:

- Both sub-trees are balanced and the height of the two sub-trees differ by at most one.
(Equivalently)
- All the nodes at depths 0 through $n-2$ have two children.

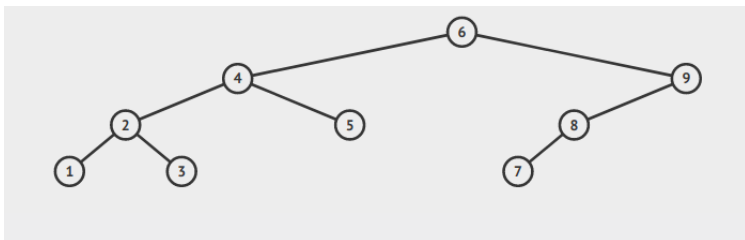
Is this a balanced tree?



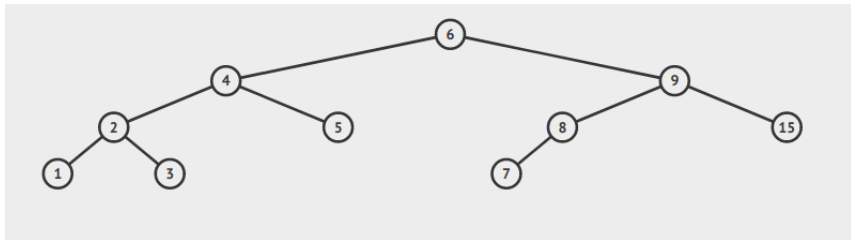
Is this a balanced tree?



Is this a balanced tree?



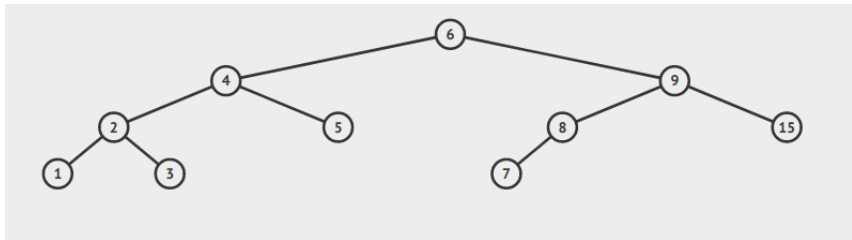
Is this a balanced tree?



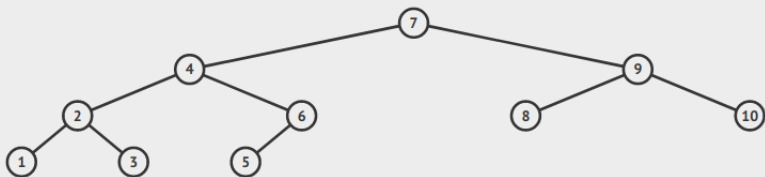
A binary tree is balanced and left-justified if:

- The tree is balanced.
- Leaves are filled in a left to right fashion.

Is this a left-justified balanced binary tree?



Is this a left-justified balanced binary tree?

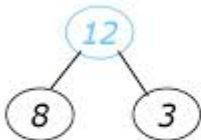


Outline

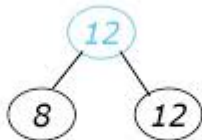
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- **Heap property**
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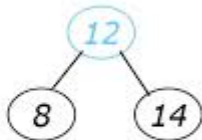
Each and every node in the heap should satisfy the heap property:
The value in the node is as large as or larger than the values in its children.



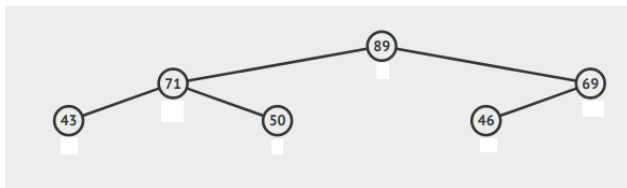
*Blue node has
heap property*



*Blue node has
heap property*



*Blue node does not
have heap property*



Important note: The tree satisfying the heap property isn't a Binary Search Tree!

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Operations that a heap should support are:

- Insert a new element to the heap.
- Get the maximum value.
- Delete the maximum value.

How to do the following operations:

- Insert a new value 100
- Insert a new value 75



How to do the insertion?

- Add the new value as the last leaf.
- Compare it to its parent.
 - If the new value is larger than the parent, swap them and compare it to the new parent (Perform sift-up recursively).
 - else, DONE.

How to delete the top of the tree (the root/ the maximum value)?

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- Insert a new element to the heap: $O(\log(n))$
- Get the maximum value: $O(1)$
- Delete the maximum value: $O(\log(n))$

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- Heap visualization: <https://visualgo.net/en/heap>
- How to do heap sorting?

Feedback form: <https://forms.gle/BZ76rh8hfth3Pxfu5>