
Structure factor for a ternary electrolyte mixture

> restart:

> with(LinearAlgebra):

> m:=Vector([1,2,3]); # Molecular masses

$$n := \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \tag{1}$$

> w:=Vector([0.2, 0.35, 0.45]); # Mass fractions

$$w := \begin{bmatrix} 0.2 \\ 0.35 \\ 0.45 \end{bmatrix}$$
 (2)

> Rho:=3; # Total density

$$P := 3 \tag{3}$$

> rho:=Rho*w; # Partial densities

$$\rho := \begin{bmatrix} 0.6000000000000000 \\ 1.050000000000000 \\ 1.350000000000000 \end{bmatrix}$$

$$(4)$$

> rhobar:=Vector([2.0,3.0,3.85714]); # For lowMach

$$rhobar := \begin{bmatrix} 2.0 \\ 3.0 \\ 3.85714 \end{bmatrix}$$
 (5)

For EOS we need inverses of rho_bar's:

> rhobar_inv:=map(x->1/x, rhobar);

$$rhobar_inv := \begin{bmatrix} 0.5000000000 \\ 0.3333333333 \\ 0.2592594513 \end{bmatrix}$$
 (6)

Charged species test case

> z_:=Vector(3,[2,1,z3]):

> z3:=solve(Transpose(z_).w=0, z3);

$$z3 := -1.666666667$$
 (7)

> z_; # Charges per mass

For ideal mixtures we have an explicit form for structure factor

1. No charges ideal mixture:

> S_w_id:=(IdentityMatrix(3)-w.Transpose(Vector(3,1))).
DiagonalMatrix(Vector(3,i->w[i]*m[i])).Transpose(IdentityMatrix (3)-w.Transpose(Vector(3,1)))/Rho;

$$S_{_w_id} := \begin{bmatrix} 0.070000000000000 & -0.017500000000000 & -0.0525000000000000 \\ -0.017500000000000 & 0.161875000000000 & -0.144375000000000 \\ -0.052500000000000 & -0.144375000000000 & 0.196875000000000 \end{bmatrix}$$

$$(9)$$

And structure factor for total density rho:

> S_rho_z_id:=Rho^4*Transpose(rhobar_inv).S_w_id.rhobar_inv;
$$S_rho_z_id := 0.349999274044588082$$
 (10)

2. No charges non-ideal mixture

This was computed earlier for 2015 paper (see Amit.mw)

$$S_{_W} := \begin{bmatrix} 0.05541976620 & -0.0002417640633 & -0.05517800210 \\ -0.0002417640633 & 0.09323259833 & -0.09299083420 \\ -0.05517800210 & -0.09299083420 & 0.1481688363 \end{bmatrix}$$
 (11)

$$S_rho := 0.300902667950801506$$
 (12)

2. With charges ideal mixture:

> S_w_z_id:=S_w_id - S_w_id.z_.Transpose(z_).S_w_id / (Transpose (z_).S_w_id.z_); # In the presence of charges

$$S_{_w_z_id} := \begin{bmatrix} 0.0448000000013440 & -0.0615999999997480 & 0.0167999999984040 \\ -0.0615999999997480 & 0.0846999999967660 & -0.0230999999970180 \\ 0.0167999999984040 & -0.0230999999970180 & 0.00629999999861403 \end{bmatrix}$$

$$(13)$$

> Transpose(z_).S_w_z_id.z_; # Confirm charge neutral 1.68268177185363 10⁻¹⁶ (14)

Structure factor for total density rho:

> S_rho_z_id:=Rho^4*Transpose(rhobar_inv).S_w_z_id.rhobar_inv;
$$S_rho_z_id := 0.0700000726432194603$$
 (15)

3. With charges non-ideal mixture

> S_w_z:=S_w - S_w.z_.Transpose(z_).S_w / (Transpose(z_).S_w.z_); #
In the presence of charges

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0.0261818181798331 \quad -0.0359999999900849 \quad 0.00981818182672957
             -0.0359999999878882 \quad 0.0495000000082877
                                                    -0.0134999999784314
                                                                             (16)
             0.00981818181588683 -0.0134999999868089 0.00368181821587624
> Transpose(z_).S_w_z.z_; # Confirm charge neutral
                           6.02315760988784 \ 10^{-11}
                                                                             (17)
Structure factor for total density rho:
> S_rho_z:=Rho^4*Transpose(rhobar_inv).S_w_z.rhobar_inv;
                       S \ rho \ z := 0.0409091341858012422
                                                                             (18)
Testing stuff--UNFINISHED
> #P1:=(IdentityMatrix(3)-w.Transpose(Vector(3,1)));
> #P2:=(IdentityMatrix(3)-S_w_id.z_.Transpose(z_)/(Transpose(z_).
  S_w_id.z_));
> #P1.P2-P2.P1; # Confirm these commute
> #S_w_z:=P2.P1.DiagonalMatrix(Vector(3,i->w[i]*m[i]/Rho)).
Transpose(P1).Transpose(P2);
```