

$$\delta = (-1)^{\oplus_1} \in D_X \otimes \phi + (-1)^{\oplus_2} \in D_Z \otimes \pi$$