$$\delta_i = \alpha_i + (-1)^{\bigoplus_{k \in DX} s_k \oplus r_k} \phi_i + r_i \pi + (\bigoplus_{k \in DZ} s_k \oplus r_k) \pi$$