

# Elements of Macroeconomics

Week 6

## 11 Short-Term: The Aggregate Expenditure Model

The aggregate expenditure model is about business cycle fluctuation in the short run. This means prices are fixed (Keynesianism). It derives mechanics how a recession and a boom can occur given the difference between planned and actual investment/inventory. Additionally, it highlights how government intervention can help.

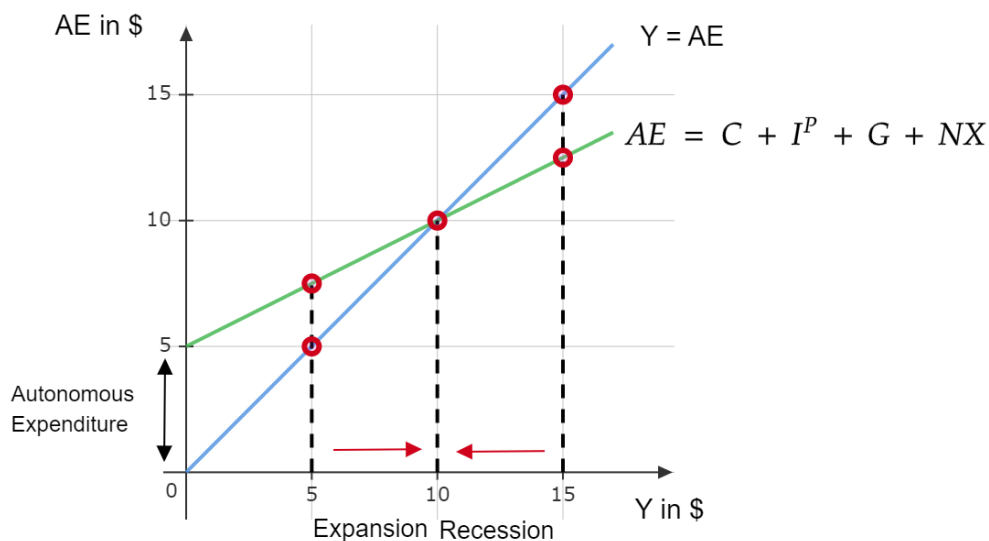
Equations we need:

$$Y = \bar{c} + bY + \overbrace{I^P + I^U}^{I^A} + G + NX \quad (1)$$

$$AE = \bar{c} + bY + I^P + G + NX \quad (2)$$

Where:

- $Y$  = Real GDP
- $AE$  = Real aggregate expenditure
- $\bar{c}$  = autonomous consumption
- $b$  = MPC
- $I^P$  = Planned investment
- $I^U$  = Unplanned investment
- $I^A$  = Actual investment
- $G$  = Government spending
- $NX$  = Net Exports



Four things to Note!

1.  $Y$  is how much is produced vs  $AE$  is how much is sold/bought (*expenditure*)

→  $AE$  does NOT include unplanned investment,  $Y$  does

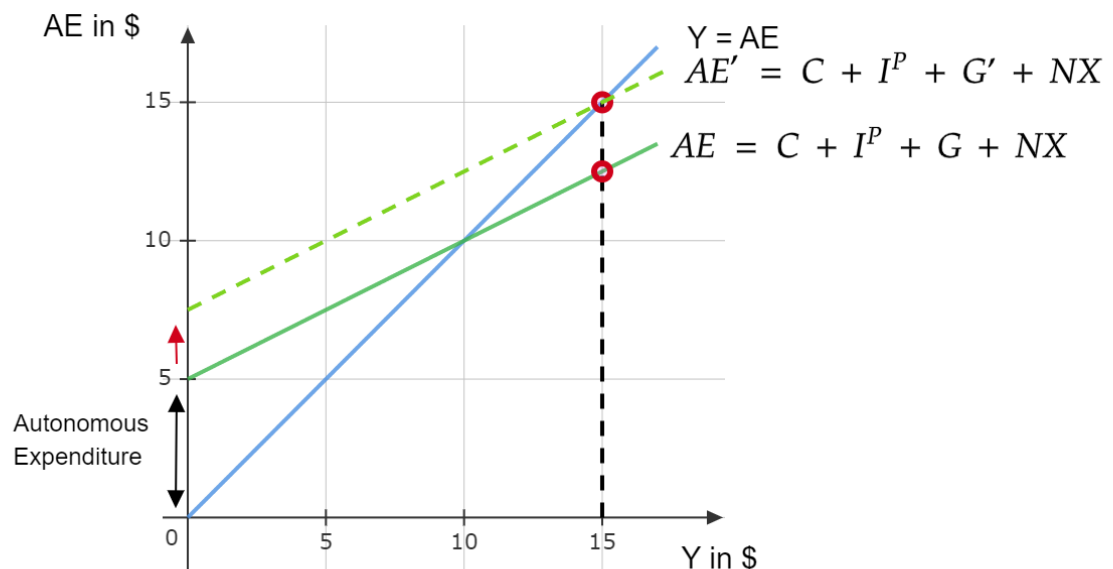
2. When  $I^U$  is positive, produce less in the next cycle; when negative, produce more

3. Movement vs Shift vs Rotation:

- $Y$  increases or decreases, changing  $bY$ , and there is a **MOVEMENT** (not a shift) in the  $AE$  curve
- **autonomous spending** changes  $(\bar{C}, I, G, NX)$  the **ENTIRE  $AE$  CURVE SHIFTS** up/down to adjust
- $b$  increases leads to a **ROTATION**

4. We can change the equilibrium by shifting the curve

- A new equilibrium is created based on where the new  $AE$  curve intersects with the  $Y=AE$  line
- In the first graph below, there is a recessionary gap because  $AE$  is below  $Y$ . Since it takes time for firms to adjust, the government may want to step in by increasing government spending.
- This increase in  $G$  shifts the  $AE$  curve up, creating a new equilibrium at which  $AE = Y$



## 11.1 Equilibrium

Let us derive the equilibrium:

$$Y = AE \quad (3)$$

$$Y = C + I^P + G + NX \quad (4)$$

$$Y = \bar{c} + MPC * Y + I^P + G + NX \quad (5)$$

$$Y - MPC * Y = \bar{c} + I^P + G + NX \quad (6)$$

$$Y(1 - MPC) = \bar{c} + I^P + G + NX \quad (7)$$

$$Y = \left( \bar{c} + I^P + G + NX \right) \frac{1}{(1 - MPC)} \quad (8)$$

Now, let us plug in some numbers:

$$C = 2,000 + 0.65Y$$

$$I^P = 3,500$$

$$G = 2000$$

$$NX = -500$$

Result: We should get:  $Y^* = 20.000$ .

## 11.2 Multiplier

Now, let's focus on the consequences on  $Y$  when Fiscal policy changes.

### 1. Government spending

Let's fix all autonomous expenditure and assume  $G$  increases by  $\Delta G$

$$Y = (\bar{c} + \bar{I}^P + \bar{G} + \Delta G + \bar{N}X) \frac{1}{(1 - MPC)}$$

Subtracting this from equation 8 gets us:

$$\Delta Y = \frac{\Delta G}{(1 - MPC)}$$

**Bottom line:**  $Y$  increases not only by the additional amount of government spending, but by even more! *Why?*

### 2. Reducing Taxes

Now, let's assume the government does not increase  $G$ , but lowers taxes by  $\Delta T$ . The consumption equation changes!

$$C = \bar{c} + MPC * (Y - T)$$

Redoing the same steps as above:

$$\begin{aligned} Y &= \bar{c} + MPC * (Y - T) + \bar{I}^P + G + \bar{N}X \\ Y - MPC * Y &= \bar{c} - MPC * T + \bar{I}^P + G + \bar{N}X \\ Y(1 - MPC) &= \bar{c} - MPC * T + \bar{I}^P + G + \bar{N}X \\ Y &= (\bar{c} - MPC * T + \bar{I}^P + G + \bar{N}X) \frac{1}{(1 - MPC)} \end{aligned}$$

So far so good, let's reduce taxes by  $\Delta T$ :

$$Y = (\bar{c} - MPC * \bar{T} - MPC * \Delta T + \bar{I}^P + \bar{G} + \bar{N}X) \frac{1}{(1 - MPC)}$$

and take the difference:

$$\Delta Y = \frac{MPC * \Delta T}{(1 - MPC)}$$

**Bottom line:**  $Y$  increases by more than the tax cut IF  $MPC > 0.5$ . But strictly less than increasing government spending. *Why?*

### 3. Balanced budget:

But wait, where does the government get the money from? Either it increases its debt or increases taxes. The first case was the former. Now let's look at the balanced budget, eg. government spending increases by increasing taxes:  $\Delta G = \Delta T$

$$Y = (\bar{c} - MPC * \bar{T} - MPC * \Delta T + \bar{I}^P + \bar{G} + \Delta G + \bar{N}X) \frac{1}{(1 - MPC)}$$

Taking the difference leads to:

$$\Delta Y = \frac{\Delta G}{(1 - MPC)} - \frac{MPC * \Delta T}{(1 - MPC)} = \Delta G$$

**Bottom line:** in this model, the government can increase output by spending more and increasing taxes!!