

### Time-Complexity notation

$O = 0 \leq f(n) \leq cg(n), o = 0 \leq f(n) < cg(n)$

$\Omega = 0 \leq cg(n) \leq f(n), \omega = 0 < cg(n) \leq f(n)$

### Master Method

Case 1:  $F(n) = O(n^{\log_b a - \epsilon})$  then,  $T(n) = \Theta(n^{\log_b a})$

Case 2:  $F(n) = O(n^{\log_b a} \log^k(n))$  then,  $T(n) = \Theta(n^{\log_b a} \log^{k+1}(n))$

Case 3:  $F(n) = O(n^{\log_b a + \epsilon})$  then,  $T(n) = \Theta(n^{\log_b a})$

**Red-Black:** Search=Insertion=Deletion=Color Changes  $O(\log n)$ , Rotations  $O(1)$

### Heaps

Top Down  $O(n \log n)$ , Bottom Up  $O(n)$

Heapification:  $O(n)$ , Update=Extract-Minimum:  $O(\log n)$ , Minimum-Index=Get-Minimum=Get-Key:  $O(1)$

### Sorting

Bucket Sort:  $O(n + m)$ , space  $O(m)$

Radix Sort:  $O(kn)$

Counting Sort:  $O(n)$

Insertion Sort: Data Movement  $O(n^2)$ , Comparisons  $O(n \log n)$ .

Selection Sort: Data Movement  $O(n)$ , Comparisons  $O(n^2)$ .

Merge Sort:  $O(n \log n)$

Quick Sort:  $O(n^2)$

**Union Find** union:  $O(1)$ , find:  $O(\log n)$

**Huffman Codes:**  $O(n \log n)$

**Selection:**  $O(n)$

**String Matching:**  $O(n + m)$

### Graphs

**DFS and BFS:** list  $O(|V| + |E|)$ , Matrix  $O(V^2)$

**Bellman-Fort:**  $O(|V||E|)$ , works for everything but negative cycles.

**Acyclic:**  $O(|V| + |E|)$ , doesn't have cycles, works with negative weights has to sorted in a topological order.

**Dijkstra:** Binary heap  $O((|V| + |E|) \log |V|)$ , delete  $O(|V| \log |V|)$ , update  $O(|E| \log |V|)$

Fibonacci heap  $O(|V| \log(|V|) + |E|)$ , delete  $O(|V| \log |V|)$ , update  $O(|E|)$

No heap  $O(|V|^2)$ , delete  $O(|V||V|)$ , update  $O(|E|)$

**Prims:**  $O((|V| + |E|) \log |V|)$ , delete  $O(|V| \log |V|)$ , update  $O(|E| \log |V|)$

**Kruskal:**  $O((|V| + |E|) \log |V|)$ , heap operations  $O((|V| + |E|) \log |V|)$ , union find  $O(|E| \log |V|)$

**Floyd-Warshall:**  $O(|V|^3)$ , no negative cycle  $O(|V|^2|E|)$ , no negative weights  $O(|V|^2 \log(|V|) + |V||E|)$

### Max Flow:

**Ford-Fulkerson:**  $O(|E||f|)$

**Edmonds-Krap:**  $O(|V||E|^2)$

### P, NP, NPC

P = Polynomial Time Solvable, Nondeterministic Polynomial Time Solvable.

$O(n^k)$ , as long as k is a constant then, the problem is P.

A problem is called NP-Hard if every problem is reducible to that problem.

A problem is called NO-Complete if the problem belong to NP, and it is an NP-Hard problem.

### Counting-Sort(A, B, k)

**for** i=0 **to** k **do** C[i]=0

**for** j=1 **to** n **do** C[A[j]0] += 1

**for** i=1 **to** k **do** C[i] += C[i-1]

### Compute-Next(P, m)

next[1]=0, q=0

**for** i = 2 **to** m **do**

**while** q>0 **and** P[i]!=P[q+1] **do** q = next(q)

**if** P[i]==P[q+1] **then** q++

next[i]=q;

### String-Matching(T, n, P, m) $O(n)$

i  $\leftarrow$  1, q  $\leftarrow$  0

**while** i  $\leq$  n **do**

**if** T[i] = P[q + 1] **then** i  $\leftarrow$  i + 1, q  $\leftarrow$  q + 1

**else**

**if** q = 0 **then** i  $\leftarrow$  i + 1

**else** q = next [q]

**if** q = m **then**

print "pattern found at position" i - m

q = next [q]

### Bellman-Ford(G, w, s)

Initialize-Single-Source(G, s)

**for** i=1 **to** V - 1 **do**

**for** each edge (u, v) that belongs to E **do**

Relax(u, v, w)

**for** each edge (u, v) that belongs to E **do**

**if** d[v]>d[u]+w(u, v) **then return** False