Bernoulli Distribution

27 March 2023 16:06

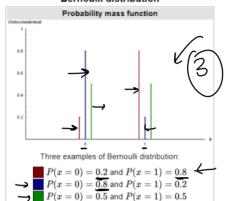
p-> Prob of succes >(

Bernoulli distribution is a probability distribution that models a binary outcome, where the outcome can be either success (represented by the value 1) or failure (represented by the value 0). The Bernoulli distribution is named after the Swiss mathematician Jacob Bernoulli, who first introduced it in the late 1600s.

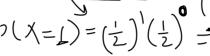
The Bernoulli distribution is characterized by a single parameter, which is the probability of success, denoted by p. The probability mass function (PMF) of the Bernoulli distribution is:

| pmf = P(x=x) = | px (1-p) -x <





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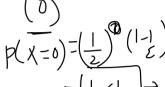
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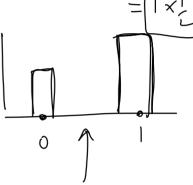
 $\left(\frac{1}{6}\right)$ $\left(\frac{5}{8}\right)$

experiment

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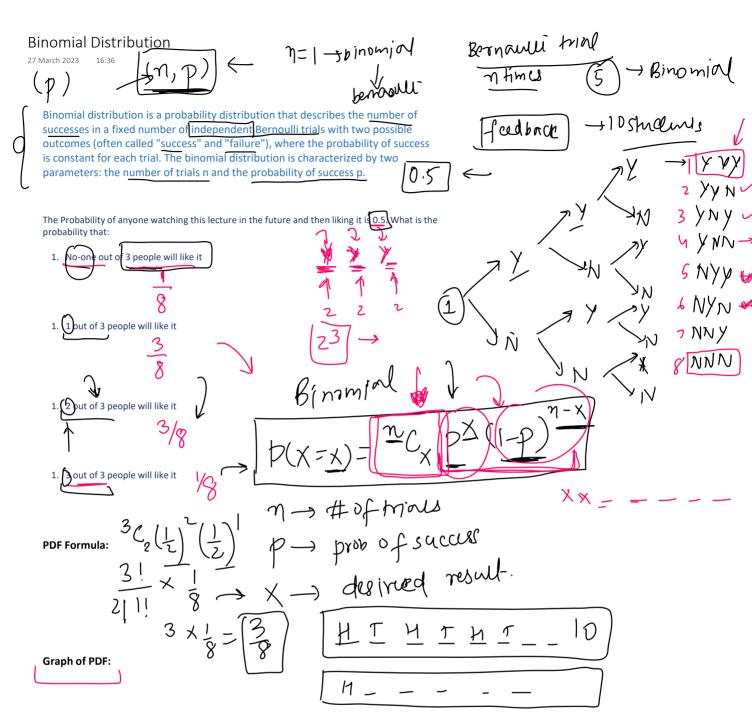
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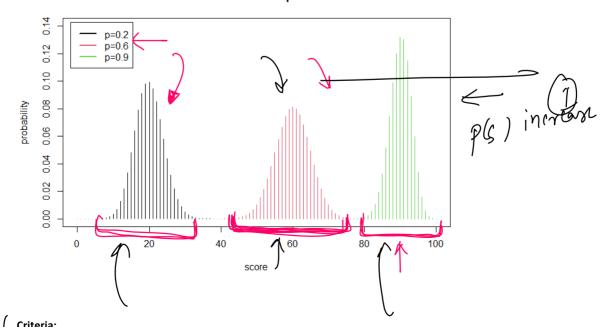


The Bernoulli distribution is commonly used in machine learning for modelling binary outcomes, such as whether a customer will make a purchase or not, whether an email is spam or not, or whether a patient will have a certain disease or not.

Binomial dissipulin



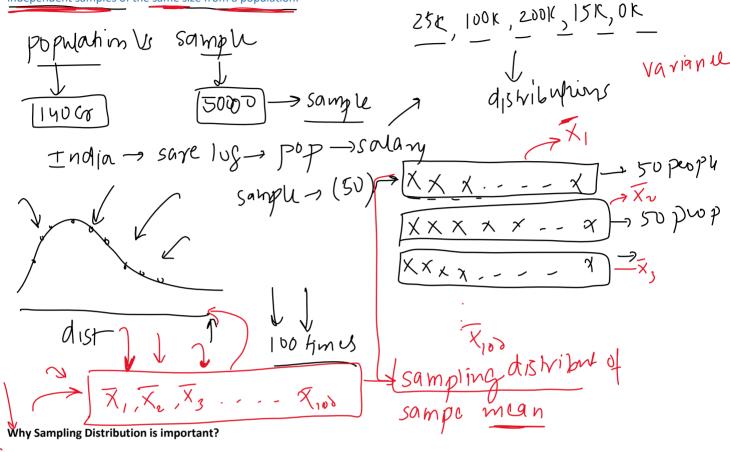
Binomial distribution with different probabilities of success



Criteria:

- 1. The process consists of n trials
- 2. Only 2 exclusive outcomes are possible, a success and a failure.
- 3. P(success) = p and P(failure) = 1-p and it is fixed from trial to trial
- 4. The trials are independent.
- 1. **Binary classification problems**: In binary classification problems, we often model the probability of an event happening as a binomial distribution. For example, in a spam detection system, we may model the probability of an email being spam or not spam using a binomial distribution.
- Hypothesis testing: In statistical hypothesis testing, we use the binomial
 distribution to calculate the probability of observing a certain number of
 successes in a given number of trials, assuming a null hypothesis is true. This can
 be used to make decisions about whether a certain hypothesis is supported by
 the data or not.
- 3. Logistic regression: Logistic regression is a popular machine learning algorithm used for classification problems. It models the probability of an event happening as a logistic function of the input variables. Since the logistic function can be viewed as a transformation of a linear combination of inputs, the output of logistic regression can be thought of as a binomial distribution.
- 4. A/B testing: A/B testing is a common technique used to compare two different versions of a product, web page, or marketing campaign. In A/B testing, we randomly assign individuals to one of two groups and compare the outcomes of interest between the groups. Since the outcomes are often binary (e.g., click-through rate or conversion rate), the binomial distribution can be used to model the distribution of outcomes and test for differences between the groups.

Sampling distribution is a probability distribution that describes the statistical properties of a sample statistic such as the sample mean or sample proportion) computed from multiple independent samples of the same size from a population.



Sampling distribution is important in statistics and machine learning because it allows us to estimate the variability of a sample statistic, which is useful for making inferences about the population. By analysing the properties of the sampling distribution, we can compute confidence intervals, perform hypothesis tests, and make predictions about the population based on the sample data. I central limit morme

Central Limit Theorem

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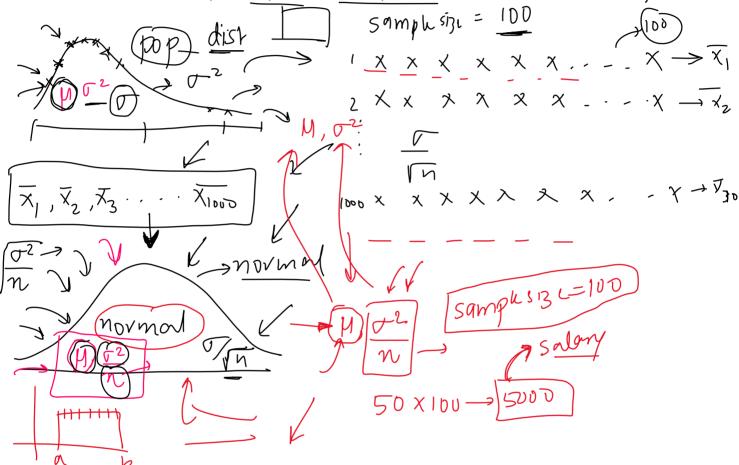


The Central Limit Theorem (CLT) states that the distribution of the sample means of a large number of independent and identically distributed random variables will approach a normal distribution, regardless of the underlying distribution of the variables.

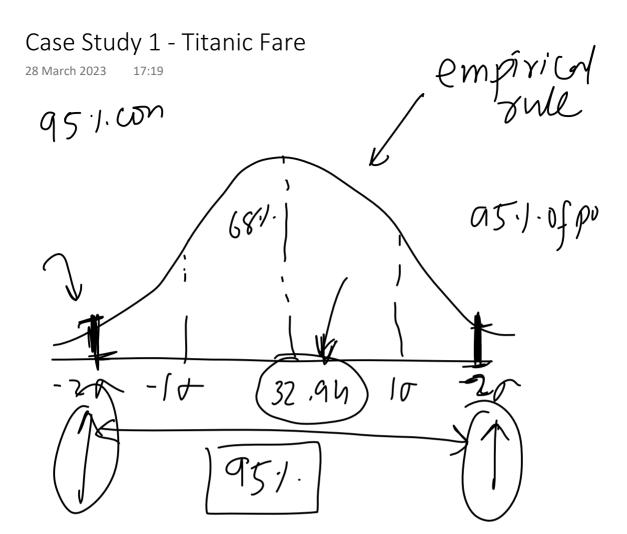
The conditions required for the CLT to hold are:

- 1. The <u>sample</u> size is large enough, typically greater than or equal to 30.
- 2. The sample is drawn from a finite population or an infinite population with a finite variance.

3. The random variables in the sample are independent and identically distributed.



The CLT is important in statistics and machine learning because it allows us to make probabilistic inferences about a population based on a <u>sample of data</u>. For example, <u>we can use the CLT</u> to construct <u>confidence</u> intervals, perform hypothesis tests, and make predictions about the population mean based on the <u>sample data</u>. The CLT also provides a theoretical justification for many commonly used statistical techniques, such as t-tests, ANOVA, and linear regression.



Case Study - What is the average income of Indians

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Step-by-step process:

- 1. Collect multiple random samples of salaries from a representative group of Indians. Each sample should be large enough (usually, n > 30) to ensure the CLT holds. Make sure the samples are representative and unbiased to avoid skewed results.
- 2. Calculate the sample mean (average salary) and sample standard deviation for each sample.
- 3. Calculate the average of the sample means. This value will be your best estimate of the population mean (average salary of all Indians).
- 4. Calculate the standard error of the sample means, which is the standard deviation of the sample means divided by the square root of the number of samples.
- 5. Calculate the confidence interval around the average of the sample means to get a range within which the true population mean likely falls. For a 95% confidence interval:

```
lower_limit = average_sample_means - 1.96 * standard_error
upper limit = average sample means + 1.96 * standard error
```

6. Report the estimated average salary and the confidence interval.

Python code

Remember that the validity of your results depends on the quality of your data and the representativeness of your samples. To obtain accurate results, it's crucial to ensure that your samples are unbiased and representative.