# Bees Algorithm\*

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#### Abstract

The Clever Algorithms project aims to describe a large number of Artificial Intelligence algorithms in a complete, consistent, and centralized manner, to improve their general accessibility. The project makes use of a standardized algorithm description template that uses well-defined topics that motivate the collection of specific and useful information about each algorithm described. This report describes the Bees Algorithm using the standardized algorithm template.

Keywords: Clever, Algorithms, Description, Optimization, Bees, Algorithm

## 1 Introduction

The Clever Algorithms project aims to describe a large number of algorithms from the fields of Computational Intelligence, Biologically Inspired Computation, and Metaheuristics in a complete, consistent and centralized manner [1]. The project requires all algorithms to be described using a standardized template that includes a fixed number of sections, each of which is motivated by the presentation of specific information about the technique [2]. This report describes the Bees Algorithm using the standardized algorithm template.

### 2 Name

Bees Algorithm, BA

# 3 Taxonomy

The Bees Algorithm beings to Bee Inspired Algorithms and the field of Swarm Intelligence, and more broadly the fields of Computational Intelligence and Metaheuristics. The Bees Algorithm is related to other Bee Inspired Algorithms, such as Bee Colony Optimization, and other Swarm Intelligence algorithms such as Ant Colony Optimization and Particle Swarm Optimization.

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# 4 Inspiration

The Bees Algorithm is inspired by the foraging behavior of honey bees. Honey bees collect nectar from vast areas around their hive (more than 10 kilometers). The have been observed to send bees to collect nectar from patches relative to the amount of food available at each flower patch. Finally, bees communicate with each other via a waggle dance that informs other bees in the hive as to the direction, distance, and quality rating of food sources.

# 5 Metaphor

Honey bees collect nectar from flower patches as a food source for the hive. The hive sends out scout's that locate patches of flowers, then return to the hive and inform other bees as to the fitness and location of a food source via a waggle dance. The scout returns to the flower patch with follower bees. A small number of scouts continue to search for new patches, while bees returning from flower patches continue to communicate the quality of the patch.

# 6 Strategy

The information processing objective of the algorithm is to locate and explore good sites within a problem search space. Scouts are sent out to randomly sample the problem space and locate good sites. The good sites are exploited via the application of a local search, where a smaller number of good sites are explored more than the others. Good sites are continually explored, although many scouts are sent out each iteration always in search of additional good sites.

#### 7 Procedure

Algorithm 1 provides a pseudo-code listing of the Bees Algorithm for minimizing a cost function.

## 8 Heuristics

- The Bees Algorithm was developed to be used with continuous and combinatorial function optimization problems.
- The  $Patch_{size}$  variable is used as the neighborhood size. For example, in a continuous function optimization problem, each dimension of a site would be sampled as  $x_i \pm (rand() \times Patch_{size})$ .
- The *Patch*<sub>size</sub> variable is decrease each iteration, typically by a constant amount (such as 0.95).
- The number of elite sites ( $EliteSites_{num}$ ) must be < the number of sites ( $Sites_{num}$ ), and the number of elite bees ( $EliteBees_{num}$ ) is traditionally < the number of other bees ( $OtherBees_{num}$ ).

# 9 Code Listing

Listing 1 provides an example of the Bees Algorithm implemented in the Ruby Programming Language. The demonstration problem is an instance of a continuous function optimization that seeks minf(x) where  $f = \sum_{i=1}^{n} x_i^2$ ,  $-5.0 \le x_i \le 5.0$  and n = 3. The optimal solution for this basin function is  $(v_0, \ldots, v_{n-1}) = 0.0$ . The algorithm is an implementation of the Bees Algorithm as described in the seminal paper [4]. A fixed patch size decrease factor of 0.95 was applied each iteration.

#### **Algorithm 1**: Pseudo Code for the Bees Algorithm.

```
Input: Problem<sub>size</sub>, Bees<sub>num</sub>, Sites<sub>num</sub>, EliteSites<sub>num</sub>, PatchSize<sub>init</sub>, EliteBees<sub>num</sub>,
             Other Bees_{num}
    Output: Bee_{best}
 1 Population \leftarrow InitializePopulation(Bees_{num}, Problem_{size});
 2 while ¬StopCondition() do
        EvaluatePopulation(Population);
 3
        Bee_{best} \leftarrow \texttt{GetBestSolution(Population)};
 4
        NextGeneration \leftarrow 0;
        Patch_{size} \leftarrow (PatchSize_{init} \times PatchDecrease_{factor});
 6
        Sites_{best} \leftarrow SelectBestSites(Population, Sites_{num});
 7
        foreach Site_i \in Sites_{best} do
 8
            RecruitedBees_{num} \leftarrow 0;
 9
10
            if i < EliteSites_{num} then
                RecruitedBees_{num} \leftarrow EliteBees_{num};
11
            else
12
             | RecruitedBees_{num} \leftarrow OtherBees_{num};
13
            end
14
            Neighborhood \leftarrow 0;
15
            for j to RecruitedBees_{num} do
16
              Neighborhood \leftarrow CreateNeighbourhoodBee(Site_i, Patch_{size});
            end
18
            NextGeneration ← GetBestSolution(Neighborhood);
19
        end
20
21
        RemainingBees_{num} \leftarrow (Bees_{num} - Sites_{num});
        for j to RemainingBees_{num} do
22
            NextGeneration ← CreateRandomBee();
23
        end
        Population \leftarrow NextGeneration;
26 end
27 return Bee_{best};
```

```
def objective_function(vector)
1
2
     return vector.inject(0.0) {|sum, x| sum + (x ** 2.0)}
3
4
   def random_vector(problem_size, search_space)
     return Array.new(problem_size) do |i|
6
       search_space[i][0] + ((search_space[i][1] - search_space[i][0]) * rand())
8
   end
9
10
   def create_random_bee(problem_size, search_space)
11
12
     bee[:vector] = random_vector(problem_size, search_space)
13
14
   \quad \text{end} \quad
16
   def create_neighborhood_bee(site, patch_size, search_space)
^{17}
     vector = []
18
     site.each_with_index do |v,i|
19
       v = (rand()<0.5) ? v+rand()*patch_size : v-rand()*patch_size
20
       v = search_space[i][0] if v < search_space[i][0]</pre>
21
```

```
v = search_space[i][1] if v > search_space[i][1]
22
       vector << v
23
     end
24
     bee = \{\}
25
     bee[:vector] = vector
26
27
     return bee
28
   end
29
   def search_neighborhood(site, neighborhood_size, patch_size, search_space)
30
     neighborhood = []
31
     neighborhood_size.times do
32
       neighborhood << create_neighborhood_bee(site[:vector], patch_size, search_space)</pre>
33
34
     neighborhood.each{|bee| bee[:fitness] = objective_function(bee[:vector])}
35
     return neighborhood.sort{|x,y| x[:fitness]<=>y[:fitness]}.first
36
37
38
   def search(max_gens, problem_size, search_space, num_bees, num_sites, elite_sites, patch_size,
39
        e_bees, o_bees)
40
     best = nil
     pop = Array.new(num_bees){ create_random_bee(problem_size, search_space) }
41
     max_gens.times do |gen|
42
       pop.each{|bee| bee[:fitness] = objective_function(bee[:vector])}
43
       pop.sort!{|x,y| x[:fitness]<=>y[:fitness]}
44
       best = pop.first if best.nil? or pop.first[:fitness] < best[:fitness]</pre>
45
46
       next_generation = []
       pop[0...num_sites].each_with_index do |site, i|
47
         neighborhood_size = (i<elite_sites) ? e_bees : o_bees</pre>
48
49
         next_generation << search_neighborhood(site, neighborhood_size, patch_size, search_space)</pre>
50
       (num_bees-num_sites).times do
51
         next_generation << create_random_bee(problem_size, search_space)</pre>
52
       end
53
54
       pop = next_generation
       patch_size = patch_size * 0.95
55
       puts " > iteration=#{gen+1}, patch_size=#{patch_size}, fitness=#{best[:fitness]}"
56
57
     end
     return best
58
59
   end
60
   if __FILE__ == $0
61
     problem_size = 3
62
     search_space = Array.new(problem_size) {|i| [-5, 5]}
63
     max_gens = 500
64
     num_bees = 45
65
66
     num_sites = 3
     elite_sites = 1
67
     patch_size = 3.0
68
     e_bees = 7
69
     o_bees = 2
70
71
     best = search(max_gens, problem_size, search_space, num_bees, num_sites, elite_sites,
72
          patch_size, e_bees, o_bees)
     puts "done! Solution: f=#{best[:fitness]}, s=#{best[:vector].inspect}"
73
   end
74
```

Listing 1: Bees Algorithm in the Ruby Programming Language

## 10 References

#### 10.1 Primary Sources

The Bees Algorithm was proposed by Pham, et al. in a technical report in 2005 [5], and later published [4]. In this work, the algorithm was applied to standard instances of continuous function optimization problems.

#### 10.2 Learn More

The majority of the work on the algorithm has concerned its application to various problem domains. The following is a selection of popular application papers: the optimization of linear antenna arrays by Guney and Onay [3], the optimization of codebook vectors in the Learning Vector Quantization algorithm for classification by Pham, et al. [7], optimization of neural networks for classification by Pham, et al. [8], and the optimization of clustering methods by Pham, et al. [6].

### 11 Conclusions

This report described the Bees Algorithm using the standardized algorithm template.

#### 12 Contribute

Found a typo in the content or a bug in the source code? Are you an expert in this technique and know some facts that could improve the algorithm description for all? Do you want to get that warm feeling from contributing to an open source project? Do you want to see your name as an acknowledgment in print?

Two pillars of this effort are i) that the best domain experts are people outside of the project, and ii) that this work is subjected to continuous improvement. Please help to make this work less wrong by emailing the author 'Jason Brownlee' at jasonb@CleverAlgorithms.com or visit the project website at http://www.CleverAlgorithms.com.

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