

Class Design

For this project, I decided to use 3 classes based on how the project guideline seemed to separate tasks into 3 parts: a deque, core, and cpu class. A cpu class can have multiple cores, and each core contains a deque. I could have combined the core and deque classes but I found how deque was fundamentally a concept itself so keeping them separate allowed me to implement the deque easily and then add the core functions on top of it.

The deque was made using a dynamic circular array to store integers in a buffer that can be accessed from the front and back. When full, it doubles capacity. When 1/4, it halves capacity.

int* arr: dynamically allocated circular array

int cap: current capacity

int size: current number of tasks

int front: index of the logical front

Cores each contain a deque and wrap around it to implement tasks like stealing.

int id: the core's index

dq dq1: the core's task queue

CPU manages all the cores, using a fixed array of core pointers to objects in core. Handles all the work stealing logic here as this is the control center or "brain" for the cores.

core cores:** array of dynamically allocated cores

int num: number of cores

bool active: whether the CPU has been initialized with ON

UML Diagram

| cpu | core | dq |
|---|--|--|
| <ul style="list-style-type: none">- cores : core**- num : int- active: bool | <ul style="list-style-type: none">- id : int- dq1 : dq | <ul style="list-style-type: none">- arr : int*- cap : int- size : int- front : int |
| <ul style="list-style-type: none">+ cpu()+ ~cpu()+ on(n:int) : bool+ off() : void+ spawn(pid:int, cid:int&) : bool+ run(cid:int, pid:int&, empty:bool&) : bool+ sleep(cid:int) : bool+ shutdown() : bool+ size(cid:int, out:int&) : bool+ capacity(cid:int, out:int&) : bool+ isOn() : bool | <ul style="list-style-type: none">+ core(i:int)+ getId() : int+ addTask(pid:int) : void+ runTask() : int+ stealTask() : int+ taskCount() : int+ getCap() : int+ hasTasks() : bool | <ul style="list-style-type: none">+ dq(startCap:int=4)+ ~dq()+ pushBack(x:int) : void+ pushFront(x:int) : void+ popBack() : int+ popFront() : int+ getSize() : int+ getCap() : int+ isEmpty() : bool- resize(newCap:int) : void |

Function Design

Deque key functions:

pushBack, pushFront: Add tasks at either end

popBack, popFront: Remove tasks while maintaining circular indexing

resize(): Doubles or halves capacity depending on usage

Core key functions:

addTask(int): push to back of the deque

runTask(): pop from the front

stealTask(): pop from the back when another core is idle

taskCount() and getCap(): provide statistics for load balancing

CPU key functions:

findLeast(): decides where to assign tasks by finding the least-loaded core

findMost(int skip): chooses where to steal from by finding the most-loaded core

sleep(int cid): redistributes tasks one by one, recomputing least load each time

shutdown(): removes all remaining tasks in core order (0 to N-1) to match the spec

spawn(int pid, int &cid): returns true/false to signal validity (instead of throwing errors)

run(int cid, int &pid, bool &empty): passes back both the task ID and a flag if core was empty

Runtime Analysis

| | | |
|-------------------|-------------------------------------|---|
| Deque push/pop | O(1) | Uses modular arithmetic indexing, constant work |
| Deque resize | O(C) (C = old cap) | Copies all elements when capacity changes |
| Spawn | O(C) worst case (C = old cap) | Usually O(1), but resizing makes it O(C) in the worst case |
| Run | O(1) | Pops a single element, optional steal involves constant work (no loops) |
| Sleep | O(T × N) worst case | For T tasks and N cores, each reassignment recomputes least-loaded core |
| Shutdown | O(A) (A = all tasks) | Pops and prints every remaining task once |

[1] OpenAI, "ChatGPT (GPT-5)," chat.openai.com, accessed Oct. 5 2025.

Spelling, grammar & portions of UML description were corrected with assistance from ChatGPT.