

Class Design

For this project, I decided to use 3 classes based on how the project guideline seemed to separate tasks into 3 parts: a deque, core, and cpu class. A cpu class can have multiple cores, and each core contains a deque. I could have combined the core and deque classes but I found how deque was fundamentally a concept itself so keeping them separate allowed me to implement the deque easily and then add the core functions on top of it.

The deque was made using a dynamic circular array to store integers in a buffer that can be accessed from the front and back. When full, it doubles capacity. When 1/4, it halves capacity.

int* arr: dynamically allocated circular array

int cap: current capacity

int size: current number of tasks

int front: index of the logical front

Cores each contain a deque and wrap around it to implement tasks like stealing.

int id: the core's index

dq dq1: the core's task queue

CPU manages all the cores, using a fixed array of core pointers to objects in core. Handles all the work stealing logic here as this is the control center or "brain" for the cores.

core cores:** array of dynamically allocated cores

int num: number of cores

bool active: whether the CPU has been initialized with ON

UML Diagram

cpu	core	dq
- cores : core** - num : int - active: bool	- id : int - dq1 : dq	- arr : int* - cap : int - size : int - front : int
+ cpu() + ~cpu() + on(n:int) : bool + off() : void + spawn(pid:int, cid:int&) : bool + run(cid:int, pid:int&, empty:bool&) : bool + sleep(cid:int) : bool + shutdown() : bool + size(cid:int, out:int&) : bool + capacity(cid:int, out:int&) : bool + isOn() : bool	+ core(i:int) + getId() : int + addTask(pid:int) : void + runTask() : int + stealTask() : int + taskCount() : int + getCap() : int + hasTasks() : bool	+ dq(startCap:int=4) + ~dq() + pushBack(x:int) : void + pushFront(x:int) : void + popBack() : int + popFront() : int + getSize() : int + getCap() : int + isEmpty() : bool - resize(newCap:int) : void

Function Design

Deque key functions:

pushBack, pushFront: Add tasks at either end

popBack, popFront: Remove tasks while maintaining circular indexing

resize(): Doubles or halves capacity depending on usage

Core key functions:

addTask(int): push to back of the deque

runTask(): pop from the front

stealTask(): pop from the back when another core is idle

taskCount() and **getCap()**: provide statistics for load balancing

CPU key functions:

findLeast(): decides where to assign tasks by finding the least-loaded core

findMost(int skip): chooses where to steal from by finding the most-loaded core

sleep(int cid): redistributes tasks one by one, recomputing least load each time

shutdown(): removes all remaining tasks in core order (0 to N-1) to match the spec

spawn(int pid, int &cid): returns true/false to signal validity (instead of throwing errors)

run(int cid, int &pid, bool &empty): passes back both the task ID and a flag if core was empty

Runtime Analysis

Deque push/pop	$O(1)$	Uses modular arithmetic indexing, constant work
Deque resize	$O(C)$ (C = old cap)	Copies all elements when capacity changes
Spawn	$O(C)$ worst case (C = old cap)	Usually $O(1)$, but resizing makes it $O(C)$ in the worst case
Run	$O(1)$	Pops a single element, optional steal involves constant work (no loops)
Sleep	$O(T \times N)$ worst case	For T tasks and N cores, each reassignment recomputes least-loaded core
Shutdown	$O(A)$ (A = all tasks)	Pops and prints every remaining task once

[1] OpenAI, "ChatGPT (GPT-5)," *chat.openai.com*, accessed Oct. 5 2025.

Spelling, grammar & portions of UML description were corrected with assistance from ChatGPT.