

③

Soit la compliance $C = f^T u = u^T \underline{K} u = u^T K u$

$$\frac{dC}{dx} = 2 u^T K \frac{du}{dx} + u^T \frac{dK}{dx} u \quad [1] \quad \begin{matrix} \text{T.F.I} \\ \text{(Chain rule)} \end{matrix}$$

mais en structure $Ku = f$ (f ne dépend pas de x)

$$\frac{dK}{dx} u + K \frac{du}{dx} = \frac{df}{dx} = 0 \text{ ici} \quad \begin{matrix} \nearrow \\ \text{(T.F.I.)} \end{matrix}$$

$$\boxed{K \frac{du}{dx} = - \frac{dK}{dx} u} \rightarrow \text{dans [1], il vient}$$

$$-2 u^T \frac{dK}{dx} u + u^T \frac{dK}{dx} u = - u^T \frac{dK}{dx} u$$

$$\boxed{\frac{dC}{dx} = - u^T \frac{dK}{dx} u}$$

simple ?