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abbreviation top :: "τ"      ("⊤")
abbreviation neg          ("¬")
abbreviation disj         (infixr "⊔" 40)
abbreviation conj         (infixr "⊓" 41)
abbreviation exi_r        ("∃")
abbreviation all_r        ("∀")

abbreviation sub (infixr "⊆" 39)
abbreviation eq  (infixr "≐" 38)

where "⊤ ≡ λx. True"
where "¬A ≡ λx. ¬A(x)"
where "A⊔B ≡ λx. A(x) ∨ B(x)"
where "A⊓B ≡ λx. A(x) ∧ B(x)"
where "∃r A ≡ λx. ∃y. r x y ∧ A(y)"
where "∀r A ≡ λx. ∀y. r x y → A(y)"

where "A⊆B ≡ ∀x. A(x) → B(x)"
where "A ≐ B ≡ A ⊆ B ∧ B ⊆ A"

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(* ALC: Einfache Meta-Theorie; Lemmata aus Vortrag *)

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lemma L1: "⊤ ≐ ¬⊥" by metis
lemma L2: "A⊓B ≐ ¬(¬A⊔¬B)" by metis
lemma L3: "∃r C ≐ ¬(∀r (¬C))" by metis
lemma L4: "(A ⊆ B) ≡ ∃X. (A ≐ (X ⊓ B))" sledgehammer [remote_Leo2] oops
lemma L5: "(A ⊆ B) ≡ ((A ⊓ ¬B) ≐ ⊥)" sledgehammer [remote_Leo2] oops

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(* ALC: Potential Signature *)

100%

☒ Auto update

Update

Detach

Sledgehammering...