Computer-Assisted Analysis of the Anderson-Hájek Ontological Controversy

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The axioms in Gödel's ontological proof [7, 8] (cf. Appendix A) entail what is called modal collapse [20, 9]: the formula $\varphi \to \Box \varphi$, abbreviated as MC, holds for any formula φ and not just for $\exists x. God(x)$ as intended. This fact, which has recently been confirmed with higher-order automated theorem provers [1, 3], has led to strong criticism of the argument and stimulated attempts to remedy the problem. Hájek [17, 14] proposed the use of cautious instead of full comprehension principles, and Fitting [11] took greater care of the semantics of higher-order quantifiers in the presence of modalities. Others, such as Anderson [18], Hájek [12] and Bjørdal [15], proposed emendations of Gödel's axioms and definitions. They require neither comprehension restrictions nor more complex semantics. Therefore, they are technically simpler to analyze with computer support. We have formalized them using the proof assistant Isabelle/HOL [13] together with the automated higher-order reasoners Leo-II [6], Satallax [4], Metis [10], and Nitpick [5]. Our formalizations¹ employ the embedding of higher-order modal logic (HOML) in classical higher-order logic (HOL) as introduced in previous work [1, 3, 2]. We explored the effect of different domain conditions on the provability of lemmas, theorems and even axioms. This was motivated by a controversy between Hájek and Anderson regarding the redundancy of some axioms in Anderson's emendation. In constant domain semantics, the individual domains are the same in all possible worlds. In varying domain semantics, the domains may vary from world to world. This variation is technically encoded with the help of an existence relation expressing which individuals actually exist in each world. Quantifiers are then uniformly formalized as actualistic quantifiers (i.e. guarded by the existence relation). Our main results are summarized here.

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¹The formalizations are available in the subdirectories Anderson, Hajek and Bjordal at github.com/FormalTheology/GoedelGod/blob/master/Formalizations/Isabelle/.

For all emendations and variants discussed here, the axioms and definitions have been shown to be consistent and not to entail modal collapse.

For both constant domain semantics and varying domain semantics, the following results hold for Anderson's Emendation (cf. Appendix B): the theorems T1, C and T3' can be quickly automated (in logics K, K and KB, respectively); the axioms A4 and A5 are proven redundant² (the former in logic K4B and the latter already in K); a trivial countermodel (consisting of two worlds and two individuals) for MC is generated by Nitpick (for all mentioned logics); all axioms and definitions are shown to be mutually consistent.

The redundancy of A4 and A5 is particularly controversial. Magari [19] claimed that A4 and A5 are superfluous³, arguing that T3 is true in all models of the other axioms and definitions by Gödel. Hájek [17, p. 5-6] investigated this further, refuted Magari's claim, but claimed that A4 and A5 are indeed superfluous under the assumption of an additional axiom (PEP, pointwise equality for positiveness), which Magari probably assumed silently. Moreover, Hájek [17, p. 2] cites his earlier work⁴ [14], where he claims (in Theorem 5.3) that for Anderson's emended theory [18], A4 and A5 are not only superfluous, but also redundant. Anderson and Gettings [16, footnote 1 in p. 1], in a footnote, rebutted Hájek's claim, arguing that the redundancy of A4 and A5 holds only under constant domain semantics, while Anderson's emended theory ought to be taken under Cocchiarella's semantics [21] (a varying domain semantics). Our results show that Hájek was originally right, under both constant and varying domain semantics.

Nevertheless, Hájek [12, p. 7] (in page 7) acknowledges Anderson's rebuttal, and apparently accepts it, as evidenced by his use⁵ of A4 and A5, as well as varying domain semantics, in his new emendation (named $\mathcal{AOE}'[12,$ sec. 4], cf. Appendix C), which replaces Anderson's A:A1 and A2 by a simpler axiom H:A12. Surprisingly, the computer-assisted formalization of \mathcal{AOE}' shows that A4 and A5 are still superfluous (not needed for proving T3). Moreover, A4 and A5 are independent⁶ of the other axioms and definitions. Therefore, A4 and A5 are not redundant, despite their superfluousness.

Although, Hájek did not notice the superfluousness of A4 and A5 in his \mathcal{AOE}' , he did describe yet another emendation (his \mathcal{AOE}'_0 , cf. Appendix D) where A4 and A5 are superfluous (though no claim is made w.r.t. to their redundancy), if A3 is replaced by a stronger axiom (H:A3) additionally stating that the property of actual existence is positive [12, sec. 5]. Formalization of \mathcal{AOE}'_0 shows that A4 is not only superflous, but also redundant.

 $^{^2}$ An axiom A is redundant w.r.t. a set of axioms S iff A is entailed by S.

³An axiom A is superfluous w.r.t. a set of axioms S iff T3 is entailed by $S \setminus \{A\}$.

⁴Although [14] precedes [17] in writing, it was published only 5 years later, in German.

⁵A4 and A5 are used by Hájek [12, p. 11] (page 11) in the proofs of, respectively, Lemma 4 and Theorem 4

 $^{^6}$ An axiom A is *independent* of a set of axioms S iff there are models of S where A is true and other models of S where A if false.

For A5, no conclusive results were achieved; neither a proof nor a countermodel could be automatically generated. Surprisingly, a countermodel for the weaker A3 was successfully generated. This is somewhat unsatisfactory (for theistic goals), because it shows that \mathcal{AOE}'_0 does not entail the positiveness of being God-like.

Nevertheless, \mathcal{AOE}_0' is explicitly regarded by Hájek [12, p. 12] (page 12) as just an intermediary step towards a more natural theory, based on a more sophisticated notion of positiveness. That is his final emendation (\mathcal{AOE}'' , cf. E), which restores A3 and does use A4 and A5, albeit in a modified form (i.e. H:A4 and H:A5). The formalization of \mathcal{AOE}'' shows that H:A4 is independent. The old A5 is independent as well, and both H:A4 and H:A5 are superfluous, but no conclusive results were achieved regarding independence or redundancy of H:A5.

Additionally, Anderson's 14th footnote [18, footnote 14] remarks that only the quantifiers in T3' and in A:D2 need to be interpreted as actualistic quantifiers, while others may be taken as possibilistic quantifiers. Our computer-assisted study of this mixed variant shows that A4 is still redundant, but A5 becomes independent (hence not redundant). Unfortunately, T3 then becomes unprovable.

The controversy over the superfluousness of A4 and A5 indicates a trend to reduce the ontological argument to its bare essentials. In this regard, already Anderson [18, p. 7] indicates that, by taking a notion of defective as primitive and defining the notion of positive upon it, axioms A:A1, A2 and A4 become derivable. These claims have been confirmed by the automated theorem provers. Within the same trend, the alternative proposed by Bjørdal [15] (cf. Appendix F) achieves a high level of minimality. He takes the property of being God-like as a primitive and defines (B:D1) the positive properties as those properties necessarily possessed by every God-like being. He then briefly indicates (B:L1) that B:D1 is logically equivalent, under modal logic S4, to the conjunction of D, A2, A3 and A4. This has been confirmed in the computer-assisted formalization: A2 and A3 can be quickly automatically derived in logic K. A4 can be proved in logic KT (i.e. assuming reflexivity of the accessibility relation). Proving D1 is possible in logic **K4**. Conversely, the proof that B:D1 is entailed by D1, A2, A3 and A4 is possible already in logic K. The provers also show that theorem T3 follows from B:D1, B:D2, B:D3, A:A1 and A5 already in logic **KB**. Bjordal's last paragraph briefly mentions Hájek's ideas about the superfluousness of A5 and claims that it is possible, with certain additional presuppositions, to eliminate A5 from his theory as well. Without any additional presupposition, the automated reasoners show that A5 is actually not superfluous. All these results hold for both constant and varying domain semantics.

Using our approach, the formalization and (partly) automated analysis of several variants of Gödel's ontological argument has been surprisingly straightforward. The provers not only confirmed many claimed results, but also exposed a few mistakes and novel insights in a long standing controversy.

We believe the technology employed in this work is ready to be fruitfully adopted in larger scale by philosophers.

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Appendix A. Scott's version of Gödel's ontological argment

A1 Either a property or its negation is positive, but not both:

$$\forall \varphi [P(\neg \varphi) \leftrightarrow \neg P(\varphi)]$$

A2 A property necessarily implied by a positive property is positive:

$$\forall \varphi \forall \psi [(P(\varphi) \land \Box \forall x [\varphi(x) \to \psi(x)]) \to P(\psi)]$$

T1 Positive properties are possibly exemplified:

$$\forall \varphi [P(\varphi) \to \Diamond \exists x \varphi(x)]$$

D1 A God-like being possesses all positive properties:

$$G(x) \equiv \forall \varphi [P(\varphi) \to \varphi(x)]$$

A3 The property of being God-like is positive:

C Possibly, a God-like being exists:

$$\Diamond \exists x G(x)$$

A4 Positive properties are necessarily positive:

$$\forall \varphi [P(\varphi) \to \Box P(\varphi)]$$

D2 An essence of an individual is a property possessed by it and necessarily implying any of its properties:

$$\varphi \ ess \ x \equiv \varphi(x) \land \forall \psi(\psi(x) \to \Box \forall y(\varphi(y) \to \psi(y)))$$

T2 Being God-like is an essence of any God-like being:

$$\forall x [G(x) \to G \ ess \ x]$$

D3 Necessary existence of an individual is the necessary exemplification of all its essences:

$$NE(x) \equiv \forall \varphi [\varphi \ ess \ x \to \Box \exists y \varphi(y)]$$

A5 Necessary existence is a positive property:

L1 If a god-like being exists, then necessarily a god-like being exists:

$$\exists x G(x) \to \Box \exists y G(y)$$

L2 If possibly a god-like being exists, then necessarily a god-like being exists:

$$\Diamond \exists x G(x) \to \Box \exists y G(y)$$

$$\Box \exists x G(x)$$

Appendix B. Anderson's Emendation

A:A1 If a property is positive, its negation is not positive:

$$\forall \varphi [P(\varphi) \to \neg P(\neg \varphi)]$$

A2 A property necessarily implied by a positive property is positive:

$$\forall \varphi \forall \psi [(P(\varphi) \land \Box \forall x [\varphi(x) \to \psi(x)]) \to P(\psi)]$$

T1 Positive properties are possibly exemplified:

$$\forall \varphi [P(\varphi) \to \Diamond \exists x \varphi(x)]$$

A:D1 A God-like being necessarily possesses those and only those properties that are positive:

$$G_A(x) \equiv \forall \varphi [P(\varphi) \leftrightarrow \Box \varphi(x)]$$

A3' The property of being God-like is positive:

$$P(G_A)$$

C Possibly, a God-like being exists:

$$\Diamond \exists x G(x)$$

A4 Positive properties are necessarily positive:

$$\forall \varphi [P(\varphi) \to \Box P(\varphi)]$$

A:D2 An essence of an individual is a property that necessarily implies those and only those properties that the individual has necessarily:

$$\varphi \ ess_A \ x \equiv \forall \psi [\Box \psi(x) \leftrightarrow \Box \forall y (\varphi(y) \rightarrow \psi(y))]$$

T2' Being God-like is an essence of any God-like being:

$$\forall x[G_A(x) \to G_A \ ess_A \ x]$$

D3' Necessary existence of an individual is the necessary exemplification of all its essences:

$$NE_A(x) \equiv \forall \varphi [\varphi \ ess_A \ x \to \Box \exists y \varphi(y)]$$

A5' Necessary existence is a positive property:

$$P(NE_A)$$

L1' If a god-like being exists, then necessarily a god-like being exists:

$$\exists x G_A(x) \rightarrow \Box \exists y G_A(y)$$

L2' If possibly a god-like being exists, then necessarily a god-like being exists:

$$\Diamond \exists x G_A(x) \to \Box \exists y G_A(y)$$

$$\Box \exists x G_A(x)$$

Appendix C. Hájek's First Emendation \mathcal{AOE}'

A:A1 If a property is positive, its negation is not positive:

$$\forall \varphi [P(\varphi) \to \neg P(\neg \varphi)]$$

A2 A property necessarily implied by a positive property is positive:

$$\forall \varphi \forall \psi [(P(\varphi) \land \Box \forall x [\varphi(x) \to \psi(x)]) \to P(\psi)]$$

T1 Positive properties are possibly exemplified:

$$\forall \varphi [P(\varphi) \to \Diamond \exists x \varphi(x)]$$

A:D1 A God-like being necessarily possesses those and only those properties that are positive:

$$G_A(x) \equiv \forall \varphi [P(\varphi) \leftrightarrow \Box \varphi(x)]$$

A3' The property of being God-like is positive:

$$P(G_A)$$

C Possibly, a God-like being exists:

$$\Diamond \exists x G(x)$$

A4 Positive properties are necessarily positive:

$$\forall \varphi [P(\varphi) \to \Box P(\varphi)]$$

A:D2 An essence of an individual is a property that necessarily implies those and only those properties that the individual has necessarily:

$$\varphi \ ess_A \ x \equiv \forall \psi [\Box \psi(x) \leftrightarrow \Box \forall y (\varphi(y) \rightarrow \psi(y))]$$

T2' Being God-like is an essence of any God-like being:

$$\forall x[G_A(x) \to G_A \ ess_A \ x]$$

D3' Necessary existence of an individual is the necessary exemplification of all its essences:

$$NE_A(x) \equiv \forall \varphi [\varphi \ ess_A \ x \to \Box \exists y \varphi(y)]$$

A5' Necessary existence is a positive property:

$$P(NE_A)$$

L1' If a god-like being exists, then necessarily a god-like being exists:

$$\exists x G_A(x) \to \Box \exists y G_A(y)$$

L2' If possibly a god-like being exists, then necessarily a god-like being exists:

$$\Diamond \exists x G_A(x) \to \Box \exists y G_A(y)$$

$$\Box \exists x G_A(x)$$

Appendix D. Hájek's Second Emendation \mathcal{AOE}'_0

A:A1 If a property is positive, its negation is not positive:

$$\forall \varphi [P(\varphi) \to \neg P(\neg \varphi)]$$

A2 A property necessarily implied by a positive property is positive:

$$\forall \varphi \forall \psi [(P(\varphi) \land \Box \forall x [\varphi(x) \to \psi(x)]) \to P(\psi)]$$

T1 Positive properties are possibly exemplified:

$$\forall \varphi [P(\varphi) \to \Diamond \exists x \varphi(x)]$$

A:D1 A God-like being necessarily possesses those and only those properties that are positive:

$$G_A(x) \equiv \forall \varphi [P(\varphi) \leftrightarrow \Box \varphi(x)]$$

A3' The property of being God-like is positive:

$$P(G_A)$$

C Possibly, a God-like being exists:

$$\Diamond \exists x G(x)$$

A4 Positive properties are necessarily positive:

$$\forall \varphi [P(\varphi) \to \Box \ P(\varphi)]$$

A:D2 An essence of an individual is a property that necessarily implies those and only those properties that the individual has necessarily:

$$\varphi \ ess_A \ x \equiv \forall \psi [\Box \psi(x) \leftrightarrow \Box \forall y (\varphi(y) \rightarrow \psi(y))]$$

T2' Being God-like is an essence of any God-like being:

$$\forall x[G_A(x) \to G_A \ ess_A \ x]$$

D3' Necessary existence of an individual is the necessary exemplification of all its essences:

$$NE_A(x) \equiv \forall \varphi [\varphi \ ess_A \ x \to \Box \exists y \varphi(y)]$$

A5' Necessary existence is a positive property:

$$P(NE_A)$$

L1' If a god-like being exists, then necessarily a god-like being exists:

$$\exists x G_A(x) \rightarrow \Box \exists y G_A(y)$$

L2' If possibly a god-like being exists, then necessarily a god-like being exists:

$$\Diamond \exists x G_A(x) \rightarrow \Box \exists y G_A(y)$$

$$\Box \exists x G_A(x)$$

Appendix E. Hájek's Third Emendation \mathcal{AOE}''

A:A1 If a property is positive, its negation is not positive:

$$\forall \varphi [P(\varphi) \to \neg P(\neg \varphi)]$$

A2 A property necessarily implied by a positive property is positive:

$$\forall \varphi \forall \psi [(P(\varphi) \land \Box \forall x [\varphi(x) \to \psi(x)]) \to P(\psi)]$$

T1 Positive properties are possibly exemplified:

$$\forall \varphi [P(\varphi) \to \Diamond \exists x \varphi(x)]$$

A:D1 A God-like being necessarily possesses those and only those properties that are positive:

$$G_A(x) \equiv \forall \varphi [P(\varphi) \leftrightarrow \Box \varphi(x)]$$

A3' The property of being God-like is positive:

$$P(G_A)$$

C Possibly, a God-like being exists:

$$\Diamond \exists x G(x)$$

A4 Positive properties are necessarily positive:

$$\forall \varphi [P(\varphi) \to \Box P(\varphi)]$$

A:D2 An essence of an individual is a property that necessarily implies those and only those properties that the individual has necessarily:

$$\varphi \ ess_A \ x \equiv \forall \psi [\Box \psi(x) \leftrightarrow \Box \forall y (\varphi(y) \rightarrow \psi(y))]$$

T2' Being God-like is an essence of any God-like being:

$$\forall x[G_A(x) \to G_A \ ess_A \ x]$$

D3' Necessary existence of an individual is the necessary exemplification of all its essences:

$$NE_A(x) \equiv \forall \varphi [\varphi \ ess_A \ x \to \Box \exists y \varphi(y)]$$

A5' Necessary existence is a positive property:

$$P(NE_A)$$

L1' If a god-like being exists, then necessarily a god-like being exists:

$$\exists x G_A(x) \rightarrow \Box \exists y G_A(y)$$

L2' If possibly a god-like being exists, then necessarily a god-like being exists:

$$\Diamond \exists x G_A(x) \to \Box \exists y G_A(y)$$

$$\Box \exists x G_A(x)$$

Appendix F. Bjordal's Alternative

In Bjordal's emendation G (God-like) is taken as primitive and P (Positive) is defined (cf. definition D).

B:D1 A formulas ϕ is positive iff it is necessarily the case that anything which is God-like has the property ϕ .

$$P(\phi) \equiv \Box \forall x (G(x) \to \phi(x))$$

B:L1 D is logically equivalent in S4 with the union of Gödel's definition D1 and axioms A2, A3 and A4.

$$D \leftrightarrow D1 \land A2 \land A3 \land A4$$

The proof splits into the two implication directions $B:L1^{\rightarrow}$ and $B:L1^{\leftarrow}$. $B:L1^{\rightarrow}$ can be further split into four single steps.

B:D2 ϕ is a maximal composite of object x's positive properties iff x has ϕ and ϕ is positive and all positive properties ψ which x has are such that is necessarily the case that all objects which have ϕ also have ψ .

$$MCP(\phi, x) \equiv (\phi(x) \land P(\phi)) \land \forall \psi((\psi(x) \land P(\psi)) \rightarrow \Box \forall y(\phi(y) \rightarrow \psi(y)))$$

B:D3 x has the N-property iff x is such that if ϕ is a maximal composite of x's positive properties then it is necessary that some object y has the property ϕ .

$$N(x) \equiv \forall \phi(MCP(\phi, x) \rightarrow \Box \forall y \phi(y))$$

A:A1 If a property is positive, its negation is not positive:

$$\forall \varphi [P(\varphi) \to \neg P(\neg \varphi)]$$

A5' The N-property is positive.

T3' Necessarily, a God-like being exists:

$$\Box \exists x G(x)$$

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