#### 1

# Assignment 1

### Aman Pratap Singh

## **Area of Triangle**

Abstract—This document contains the solution to find the area of a triangle, from the given coordinates of the vertices.

Download all python codes from

https://github.com/AP1920/Assignment1/blob/main/assignment1.py

Download latex-tikz codes from

https://github.com/AP1920/Assignment1/blob/main/main.tex

### 1 Problem

Solve: Problem set: Vector2, Example-2,6

Find the area of the triangle the coordinates of whose angular points are respectively: A(-1,2), B(2,3) and C(4,-3)

### 2 Solution

We will be using vectors for calculating the area of the triangle formed by above three points.

$$(\mathbf{B} - \mathbf{A}) = \begin{pmatrix} 2 \\ 3 \end{pmatrix} - \begin{pmatrix} -1 \\ 2 \end{pmatrix}$$

$$(\mathbf{B} - \mathbf{A}) = \begin{pmatrix} 3 \\ 1 \end{pmatrix} \tag{2.0.1}$$

$$(\mathbf{C} - \mathbf{A}) = \begin{pmatrix} 4 \\ -3 \end{pmatrix} - \begin{pmatrix} -1 \\ 2 \end{pmatrix}$$

$$(\mathbf{C} - \mathbf{A}) = \begin{pmatrix} 5\\ -5 \end{pmatrix} \tag{2.0.2}$$

: Area of the Triangle = 
$$\frac{1}{2} \| (\mathbf{B} - \mathbf{A}) \times ((\mathbf{C} - \mathbf{A})) \|$$
 (2.0.3)

As the vector cross product of two vectors can also be expressed as the product of a skew-symmetric matrix and a vector.

$$\mathbf{P} \times \mathbf{Q} = \begin{pmatrix} 0 & -a_3 & a_2 \\ a_3 & 0 & -a_1 \\ -a_2 & a_1 & 0 \end{pmatrix} \times \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} \tag{2.0.4}$$

Substituting values from equation 2.0.1 and 2.0.2 in above equation 2.0.4, we'll get:

$$(\mathbf{B} - \mathbf{A}) \times (\mathbf{C} - \mathbf{A}) = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & -3 \\ -1 & 3 & 0 \end{pmatrix} \times \begin{pmatrix} 5 \\ -5 \\ 0 \end{pmatrix}$$

$$(\mathbf{B} - \mathbf{A}) \times (\mathbf{C} - \mathbf{A}) = \begin{pmatrix} 0 \\ 0 \\ -20 \end{pmatrix}$$

Substituting value from equation 2.0.5 in equation 2.0.3, we'll get area of triangle:

$$\implies \frac{1}{2}(20) = 10units^2$$

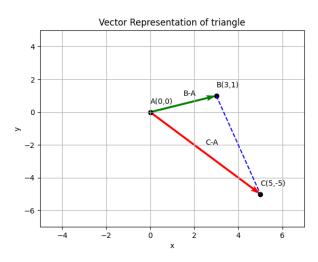


Fig. 1: Plot obtained from Python code