Assignment 1

Aman Pratap Singh

Area of Triangle

***Abstract*—This document contains the solution to find the Area of a Triangle, given the coordinates of the vertices.**

Download all python codes from

https://github.com/AP1920/Assignment1/blob/main/assignment1.py

Download latex-tikz codes from

https://github.com/AP1920/Assignment1/blob/main/main.tex

1 Problem

Solve: Problem set: Vector2, Example-2,6

Find the areas of the triangles the coordinates of whose angular points are respectively: P(-1,2), Q(2,3) and R(4,-3)

2 Solution

We will be using vectors for calculating the area of the triangle formed by above three points.

$$\mathbf{QP} = \begin{pmatrix}2\\3\end{pmatrix} - \begin{pmatrix}-1\\2\end{pmatrix}$$

$$\mathbf{QP} = \begin{pmatrix}3\\1\end{pmatrix} \tag{2.0.1}$$

$$\mathbf{RP} = \begin{pmatrix}4\\-3\end{pmatrix} - \begin{pmatrix}-1\\2\end{pmatrix}$$

$$\mathbf{RP} = \begin{pmatrix}5\\-5\end{pmatrix} \tag{2.0.2}$$

$$\because \textit{Area of the triangle} = \frac{1}{2}|\mathbf{QP} \times \mathbf{RP}| \tag{2.0.3}$$

As the vector cross product of two vectors can also be expressed as the product of a skew-symmetric matrix and a vector.

$$\mathbf{A} \times \mathbf{B} = \begin{pmatrix}0 & -a_3 & a_2\\ a_3 & 0 & -a_1\\ -a_2 & a_1 & 0\end{pmatrix} \times \begin{pmatrix}b_1\\b_2\\b_3\end{pmatrix} \tag{2.0.4}$$

Substituting values from equation 2.0.1 and 2.0.2 in above equation 2.0.4, we'll get:

$$\mathbf{QP} \times \mathbf{RP} = \begin{pmatrix}0 & 0 & 1\\ 0 & 0 & -3\\ -1 & 3 & 0\end{pmatrix} \times \begin{pmatrix}5\\-5\\0\end{pmatrix}$$

$$\mathbf{QP} \times \mathbf{RP} = \begin{pmatrix}0\\0\\-20\end{pmatrix}$$

$$\therefore |\mathbf{QP} \times \mathbf{RP}| = \sqrt{0^2 + 0^2 + (-20)^2} = 20 \tag{2.0.5}$$

Substituting value from equation 2.0.5 in equation 2.0.3, we'll get area of triangle:

$$\implies \tfrac{1}{2}(20) = 10 units^2$$

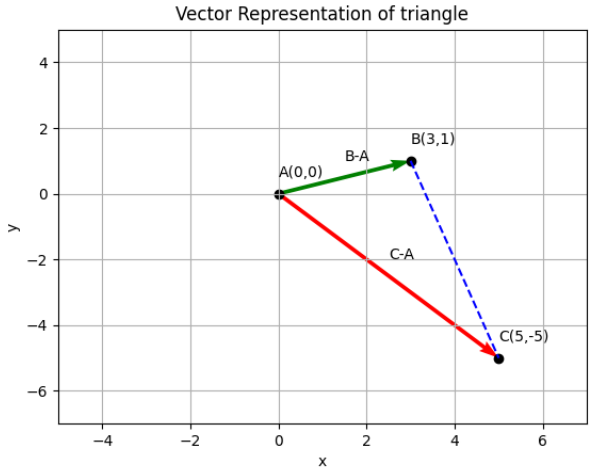

Fig. 1: Plot obtained from Python code