



COMPILER DESIGN

Module 2 Part 1

CST302

SYLLABUS



Module - 2 (Introduction to Syntax Analysis)

Role of the Syntax Analyser – Syntax error handling. Review of Context Free Grammars -Derivation and Parse Trees, Eliminating Ambiguity.
Basic parsing approaches - Eliminating left recursion, left factoring.
Top-Down Parsing - Recursive Descent parsing, Predictive Parsing,LL (1) Grammars.

PRACTICAL APPLICATIONS



- Syntax Used in programming language Analysis
- Parsers, SQL query parsing in databases, and browser engines.



phases of compiler

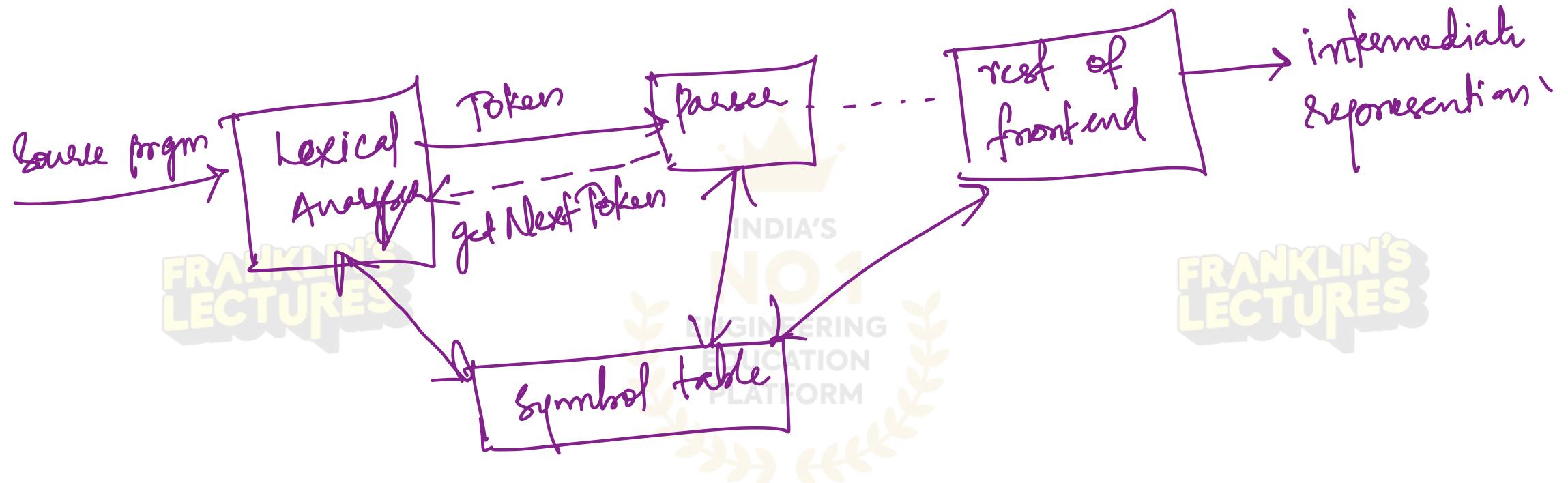
1. lexical Analyse ✓
2. Syntax Analyse
3. Semantitic Analyse
4. Intermediate code generation
5. code optimization
6. code generation



SYNTAX ANALYSIS



- Syntax of programming language constructs can be described by CFG or BNF.
- The role of parser
- The parser obtains a string of tokens from the lexical analyser as shown in the figure and verifies that the String can be generated by the grammar for the source language. A parser should report any syntax error.



- **Syntax error handling**



A good compiler should assist the programmer in identifying and locating errors. Errors in a program can be

- Lexical, such as mis-spelling an identifier, keyword or operator.
- Syntactic, such as an arithmetic expression with unbalanced parenthesis.
(a+b/c)
- Semantic, such as an operator applied to an incompatible operands.
- Logical, such as an infinite recursive calls.

Often many of the **error detection and recovery** in a compiler
is done during the **Syntax analysis** phase.



The error handler in a parser has the following goals.

- 1) It should **report** presence of **errors clearly and accurately**
- 2) It should **recover** from each error **quickly** enough to be able to detect subsequent errors.
- 3) It should not subsequently **slow down** the processing of correct program.

Error recovery strategies.

[Essay 7,5,6]



There are many different general strategies that a parser can employ to recover from a Syntactic error.

Some error recovery strategies are,

- ✓ 1) Panic mode recovery.
- ✓ 2) Phrase level recovery.
- ✓ 3) Error production.
- ✓ 4) global correction.



1. Panic mode recovery → quick'



This is the simplest method to implement and can be used by most of the parsing method. On discovering an error the parser discards input symbols one at a time until one of a designated set of synchronizing tokens are found. The synchronizing tokens are usually delimiters such as semicolon, end, } etc. The Panic mode error correction often skips a considerable amount of inputs without checking for additional errors. It has the advantages of simplicity and it is guaranteed not to go into an infinite loop.

inf a ; ,
/// .
, end. } {

2. Phrase level recovery :

int a ; int a ,
 ^
 → int a ;



On discovering an error, parser may perform local correction on remaining input. A typical local error correction would be to replace a comma by a semicolon, delete an extraneous Semi colon or insert a missing semi colon.

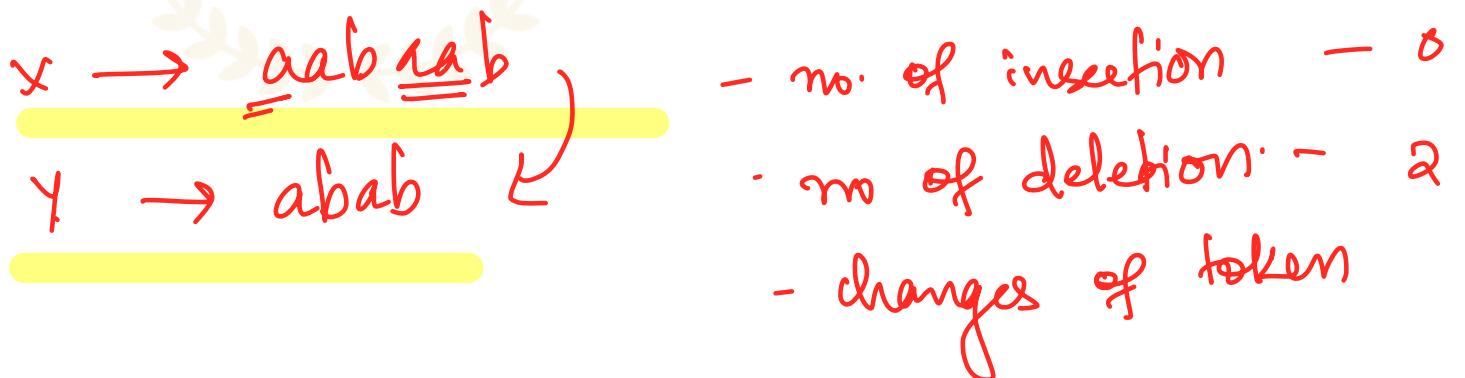
3. Error production :

If an error production is used by the parser we can generate appropriate error diagnostics, to indicate the erroneous construct that have been recognised in the input. (line no, which type error etc are provided).

4) Global correction :

aabab

A compiler would make a few changes as possible for processing an incorrect input string. There are algorithms for choosing a minimal sequence of changes to obtain a globally least cost correction. Given an incorrect input string 'x' and grammar 'G', these algorithm will find a parse tree for a related string 'y' such that the number of insertions, deletions and changes of tokens required to transform 'x' into 'y' is as small as Possible. These methods are too costly to implement in terms of time and space.



(3)

- Context Free grammar

$$'G' \quad G = (V, T, P, S)$$



- It is also called Type 2 grammar.
- A grammar $G = (V, T, P, S)$ is called a context Free grammar if every productions in the grammar are in the form of $A \rightarrow \beta$, here A is a variable and β is a strings of terminals and variables.

i.e $A \in V$ and $\beta \in (VUT)^*$.

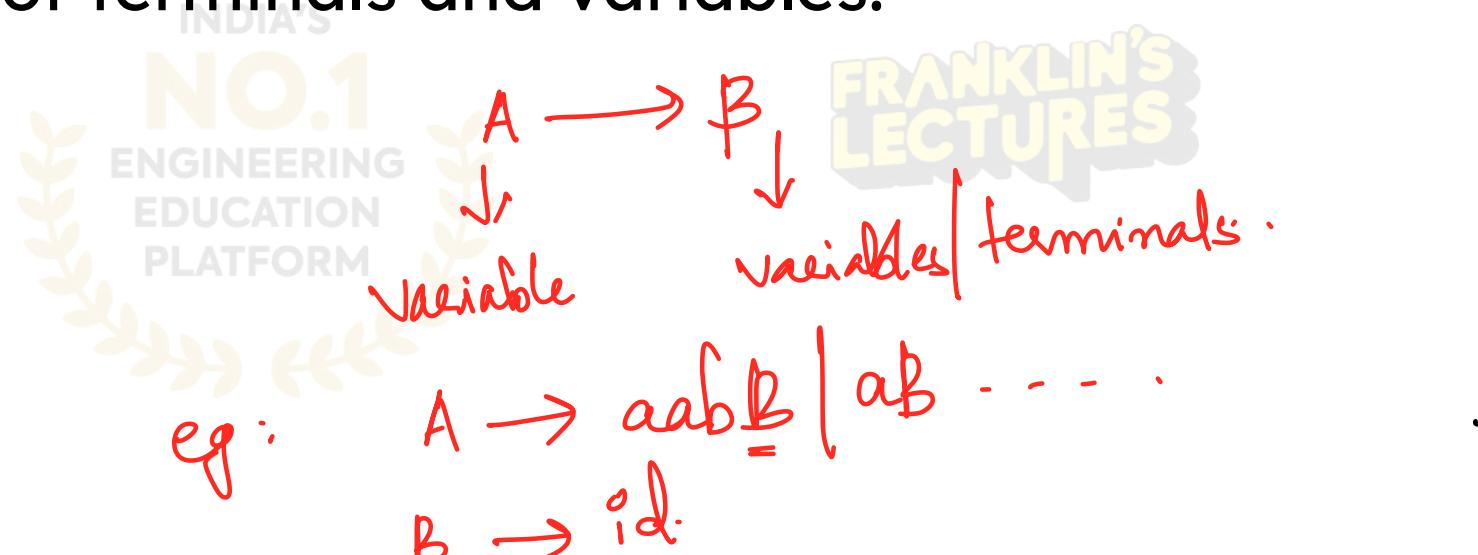
$G = (V, T, P, S)$, here,

✓ $V \rightarrow$ Variable.

✓ $T \rightarrow$ Terminals.

✓ $P \rightarrow$ Productions.

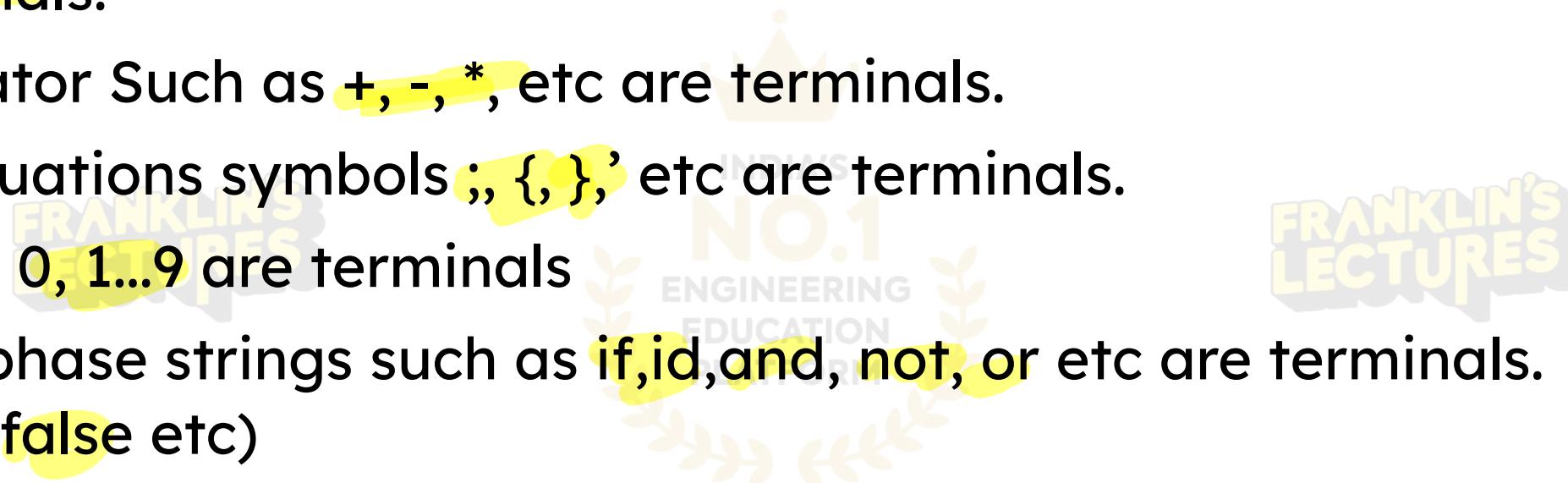
✓ $S \rightarrow$ start symbol.



Notational conventions:-

Terminal :-

- Lowercase letters early in the alphabets Such as a, b, c are terminals.
- Operator Such as +, -, *, etc are terminals.
- Punctuations symbols ;, {, }, ' etc are terminals.
- Digits 0, 1...9 are terminals
- Bold phase strings such as if, id, and, not, or etc are terminals.
(true, false etc)



Non terminals / variable.



- Upper case letters early is the alphabet A, B,C.
- The letter S → Start symbol.
- Lower case italic names such as expr, stmt etc.
- Upper case letters such as X,Y,Z represents grammar symbol.i.e, non-terminals or terminals
- Lower case letters late is the alphabet u, v, z represent strings of terminals.
- Lower case greek letters α, β ... for example represents strings of grammar symbol.

Derivations



It Is an approach used to define the language of a grammar. Two types of derivations are,

- 1) Right most derivation
- 2) Left most derivation

Left most derivations - In this at each step of derivation we replace the left most variable by one of its rules.

Eg:-Consider the grammar.

$$S \rightarrow aAS|a.$$

$$A \rightarrow SbA | ba.$$

aabbba

$$S \rightarrow aAs \quad | \quad \textcircled{a} - \quad a$$

$$A \rightarrow SbA \quad | \quad \underline{\underline{ba}}$$

$\Rightarrow \underline{\underline{aabbaa}}$

$$S \rightarrow a\underline{AS} \quad \underline{abas} \times$$

$$\rightarrow a\underline{SbAS}$$

$$\rightarrow aab\underline{A}S$$

$$\rightarrow aabb\underline{a}S$$

$$\rightarrow a\underline{\underline{abbbaa}}$$

left most derivation

right most derivation

$$S \rightarrow aAS$$

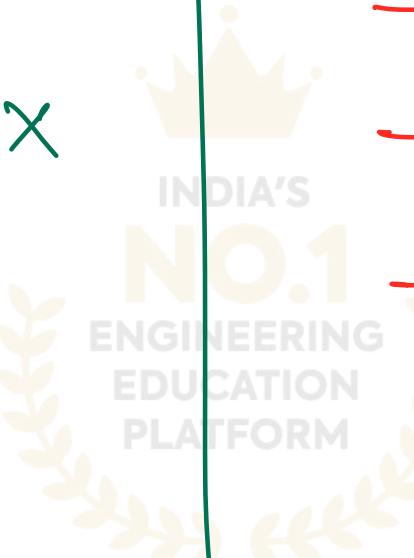
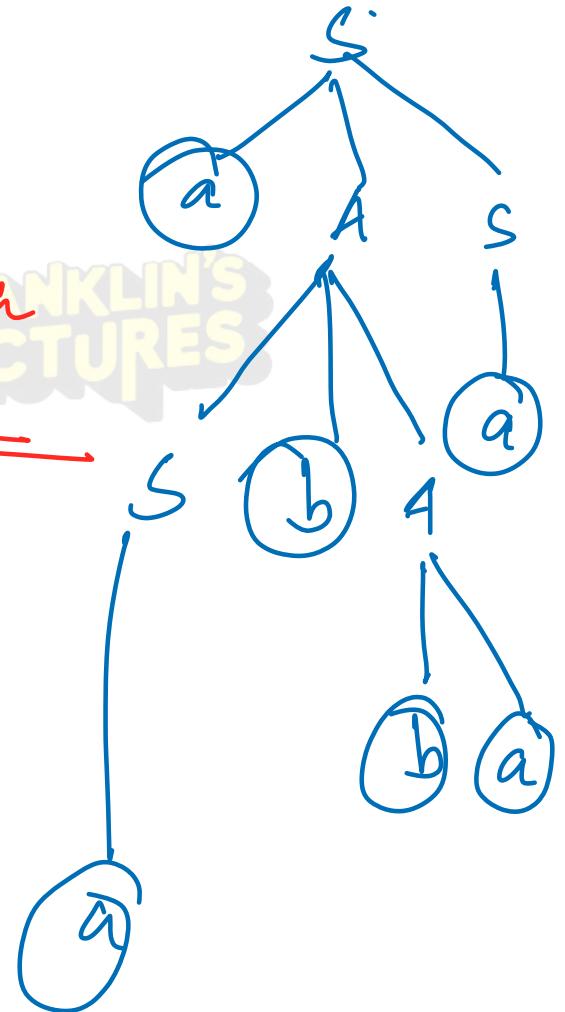
$$\rightarrow a\underline{A}a$$

$$\rightarrow aS\underline{bA}a$$

$$\rightarrow a\underline{Sbbaa}$$

$$\rightarrow aabb\underline{baa}$$

FRANKLIN'S
LECTURES



The leftmost derivation for the string aabbaa is

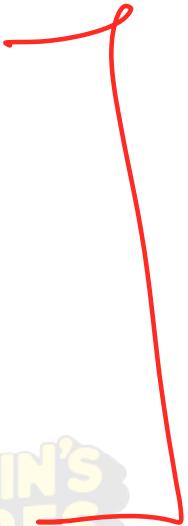
$$S \rightarrow a \underline{A} S$$

$$\rightarrow a \underline{S} b A S$$

$$\rightarrow a a b a \underline{A} S$$

$$\rightarrow a a b b a \underline{S}$$

$$\rightarrow a a b b a a$$



left most derivation



2) Right most derivations: - In this at each step of derivation way we replace the right most variable by one of its rules.
eg:- consider the grammar given above, the right most derivation for the string aabbaa is,

$S \rightarrow aAS$
 $\rightarrow aAa$
 $\rightarrow aSbAa$
 $\rightarrow aSbbAA$
 $\rightarrow aabbaa.$



right most derivation

FRANKLIN'S
LECTURES



FRANKLIN'S
LECTURES

Derivation Tree (parse Tree)



A derivation in a CFG can be represented by **using trees** called **derivation tree** or **parse tree**. ie, graphical representation of derivation is called parse tree that gives the choice of replacement. Derivation on a parse tree for a CFG, $G = (V, T, P, S)$ is a tree which satisfies the following conditions.

1. Every vertex or node has a label which is a variable or a terminal symbol or ϵ .
2. The root node has the label S
3. The bottom most nodes called leaf nodes are labelled from $T \cup \{\epsilon\}$

4. If an interior node is labelled by $A \in V$ and its children are labelled as x_1, x_2, \dots, x_n from left to right, then $A \rightarrow x_1, x_2, \dots, x_n \in P$

Eg - Consider the grammar,

$S \rightarrow aAS|a|SS$

$A \rightarrow SbA|ba$ derivation tree for the string, aabaa is,



INDIA'S
NO.1
ENGINEERING
EDUCATION
PLATFORM



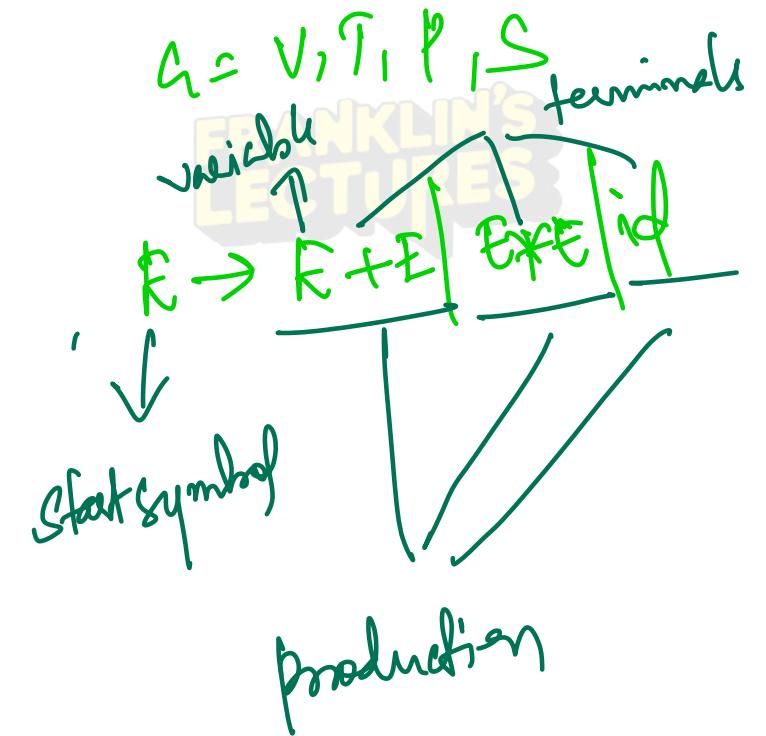
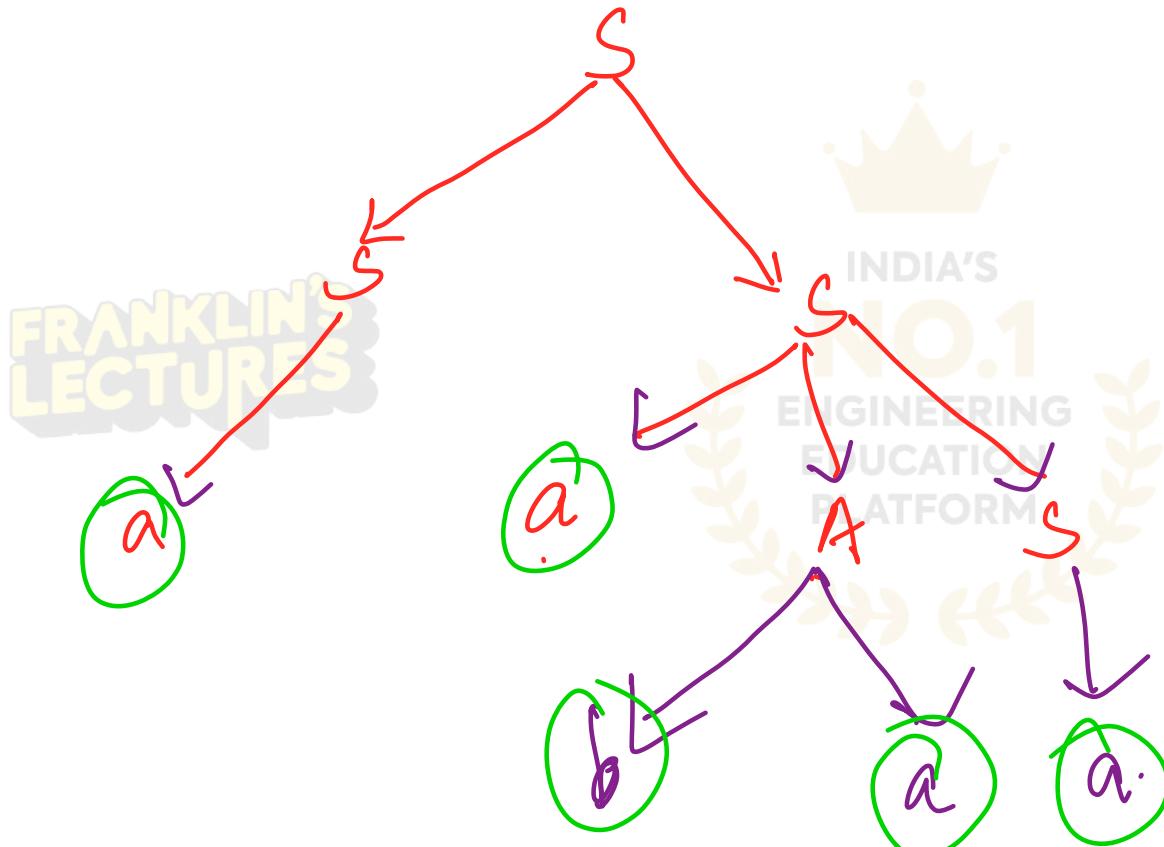
FIGURE

$$S \rightarrow a \underline{A} S | \underline{a} | \underline{\underline{SS}}$$

$$A \rightarrow S b A | \underline{\underline{ba}}$$

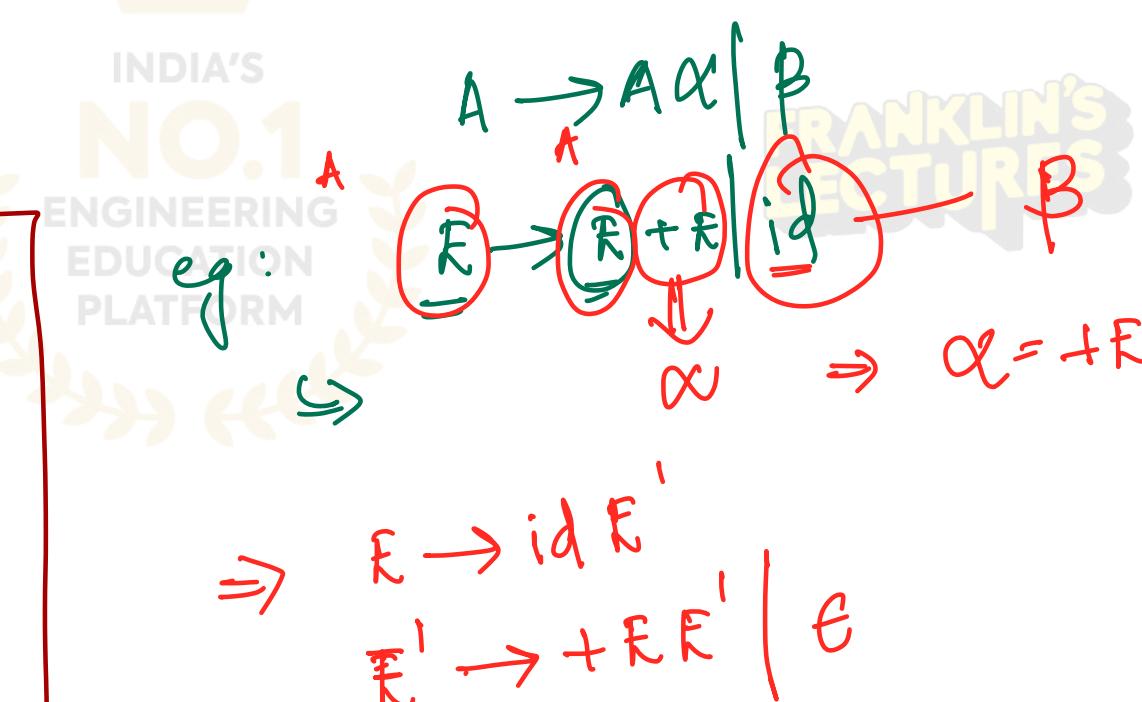
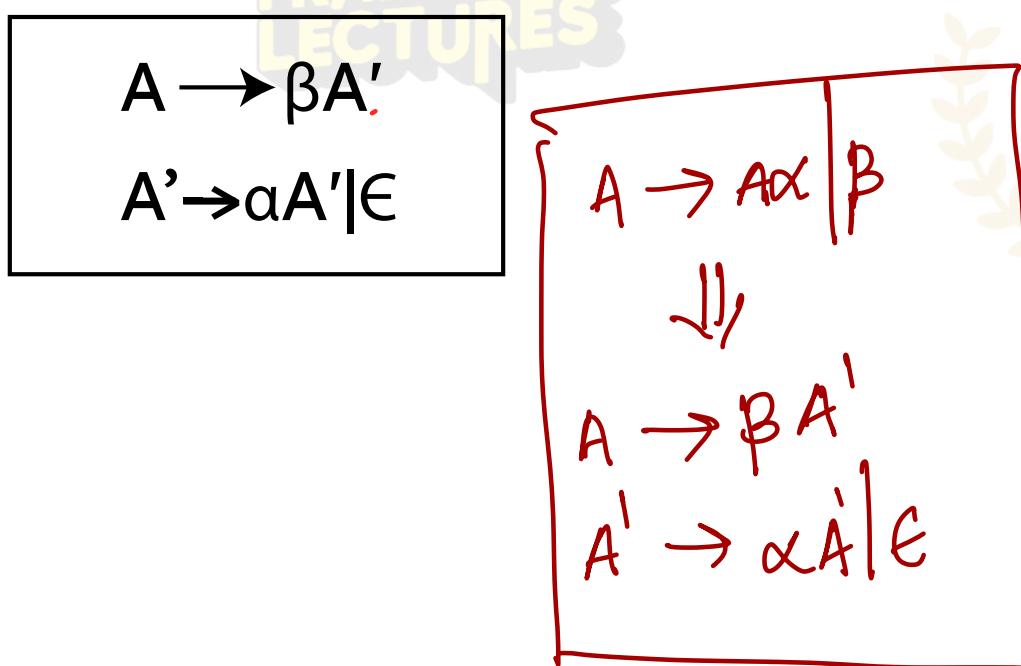
aabaa

FRANKLIN'S
LECTURES



Elimination of left recursion

A grammar which contains the production of the form $A \rightarrow A\alpha/\beta$
Top down parser can't parse left recursive grammar. So we have
to eliminate left recursion. Left recursion can be eliminated by the
following productions,

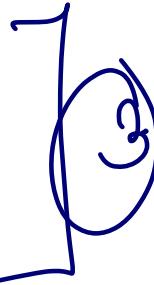


Q:- Eliminate left recursion from the grammar,

$$E \rightarrow E + T | T$$

$$T \rightarrow T^* F | F$$

$$F \rightarrow (E) | id$$



First two productions are left recursive after eliminations of left recursion, the grammar becomes,

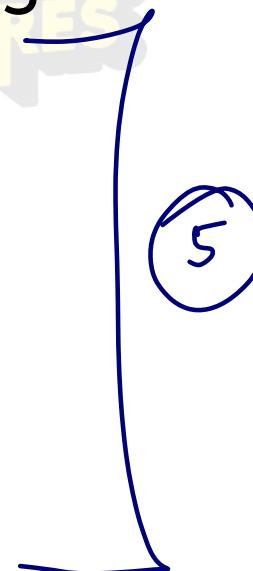
$$E \rightarrow TE'$$

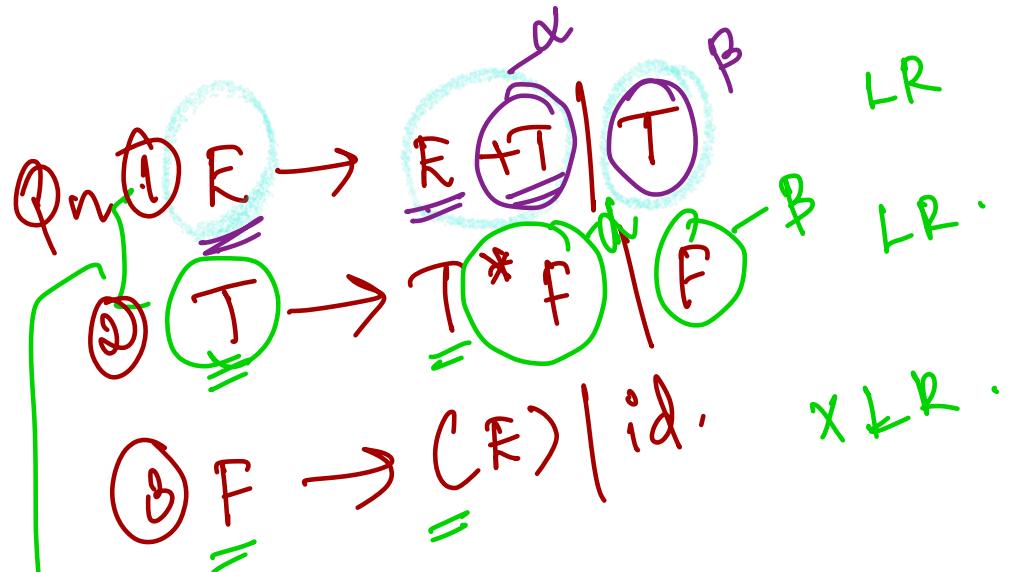
$$E' \rightarrow + TE' | \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow * F T' | \epsilon$$

$$F \rightarrow (E) | id$$





$A \rightarrow A\alpha \mid \beta \Rightarrow$ left recursive.

FRANKLIN'S
LECTURES



E → $\frac{TE'}{\alpha} \mid \frac{E'}{\beta}$

$E' \rightarrow \frac{+TE'}{\alpha} \mid \frac{\epsilon}{\beta}$

T → $\frac{FT'}{\alpha} \mid \frac{\epsilon}{\beta}$

$T' \rightarrow \frac{*FT'}{\alpha} \mid \frac{\epsilon}{\beta}$

F → $\frac{(E)}{\alpha} \mid id$

FRANKLIN'S
LECTURES

Left factoring



Left factoring is a grammar transformation that is useful for predictive parsers. If there are two alternatives for a production, we do left factoring,

$A \rightarrow \underline{\alpha\beta_1} \mid \underline{\alpha\beta_2}$, can be left factored as follows.

$$\begin{array}{l} A \rightarrow \underline{\alpha A'} \\ \vdots \\ A' \rightarrow \underline{\beta_1} \mid \underline{\beta_2} \end{array}$$

eg :- $S \rightarrow iEtSeS \mid iEtS$ can be left factored as

$$S \rightarrow iEtSS'$$

$$S' \rightarrow eS \mid \epsilon$$

$$\begin{array}{l} S \rightarrow iEtSS' \\ S' \rightarrow eS \mid \epsilon \end{array}$$

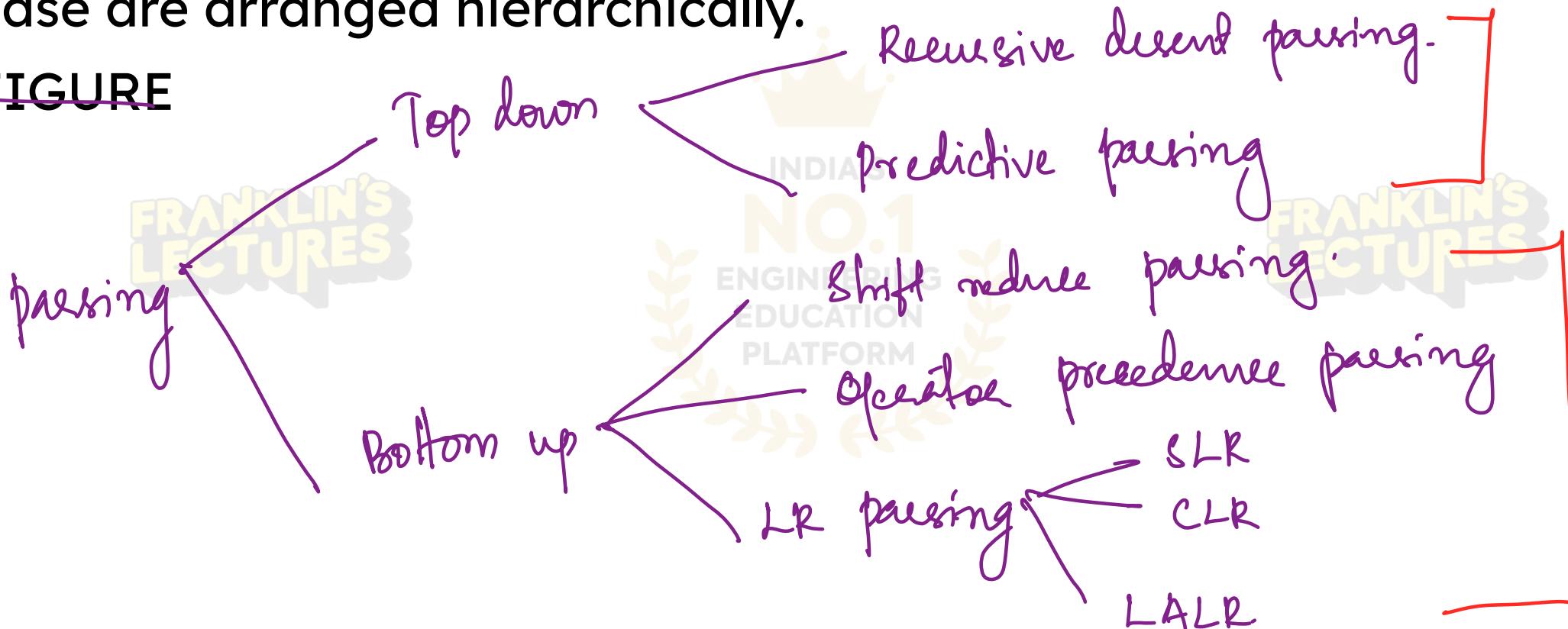
$$\begin{array}{l} S \rightarrow \underline{aab E} \mid \underline{aab ba} \\ \quad \quad \quad \underline{\alpha} \quad \underline{\beta_1} \quad \underline{\alpha} \quad \underline{\beta_2} \\ S \rightarrow aab S' \\ S' \rightarrow E \mid a \end{array}$$

$$\begin{array}{l} A \rightarrow \alpha\beta_1 \mid \alpha\beta_2 \\ \Downarrow \\ A \rightarrow \alpha A' \\ A' \rightarrow \beta_1 \mid \beta_2 \end{array}$$

Parsing

Second phase of compiler. Here tokens obtained during lexical analysis Phase are arranged hierarchically.

- **FIGURE**



Top down parsing



In top down parsing, the parser build parse trees from the top to the bottom. ie construction of parse trees for the input string from the root and creating the nodes of the parse tree in Preorder. Top down parsing can be classified into two,

- 1) Recursive descent parsing.
- 2) Predictive parsing.

Recursive descent parsing



In top down parsing the parser find a left most derivation from the input string. It constructs a parse tree for the input String starting from the root and creating the nodes of parse tree in preorder.

- Recursive descend parsing is the general forms of top down parsing that involve back tracking. ie, making repeated scans of the input.
- eg:- given the grammar $S \rightarrow cAd$, $A \rightarrow ab|a$
- And input string $w = cad$.
- To construct a parse tree for the above example in top down, initially create a tree consisting of single node labelled S . An input pointer points to 'c', the first symbol of ' w ', that use the production for S .

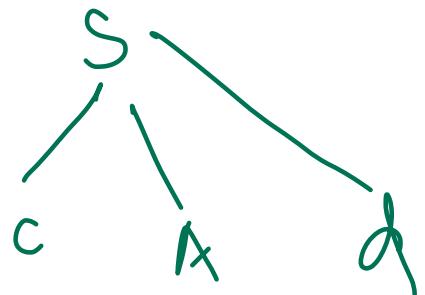
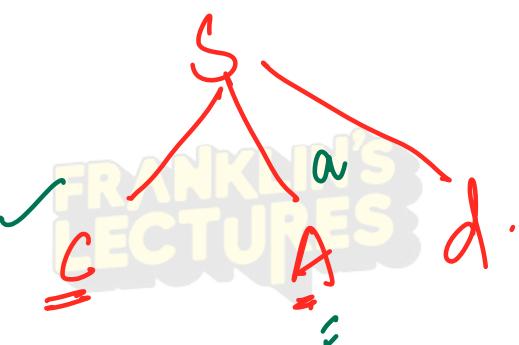
- The leftmost leaf labelled 'c' matches first symbol of 'w'. So now advance the input pointer to 'a', the second symbol of 'w' & consider the next leaf labelled 'A'. Now expand 'A' using first alternative for 'A'. Now have a match for second input symbol. So advance input pointer to 'd', the third input Symbol and compare 'd' to next leaf Labelled 'b'. 'b' does not match 'd'. So report a failure & go back to 'A' to see whether there is another alternative for 'A' that might, produce a match a In going back to 'A' reset the input pointer to position 2. ie, try for second alternatives for A to obtain the tree. The leaf a matches the second symbol of 'w' and the leaf 'd' matches the third Symbol. So we get a parse tree for w.

Figure

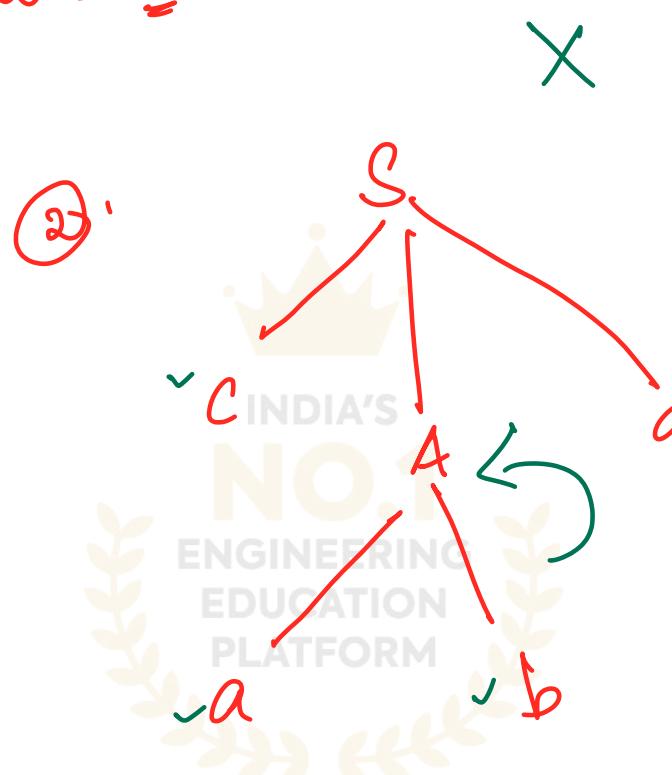
$$= S \rightarrow CAd$$

$$A \rightarrow ab \mid a.$$

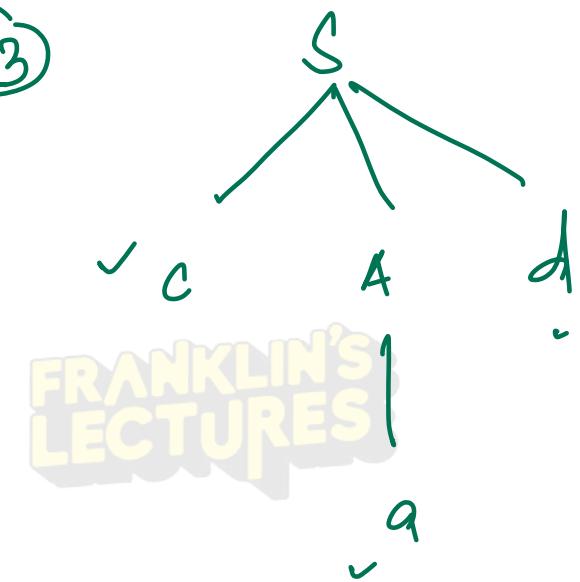
①



$$w = \underline{cad}^*$$



②



FRANKLIN'S
LECTURES

'cad'

Problems in recursive descent parsing.



1. **Left recursion**: - In left recursion the grammar has productions of the form $A \rightarrow A\alpha | \beta \Rightarrow A \rightarrow \beta A' \quad A' \rightarrow \alpha A' | \epsilon$
2. Backtracking :- It occurs when there is more than one alternative in the production while parsing the input string.

eg-

$$S \rightarrow cAd$$

$$A \rightarrow ab|a$$

Two alternatives for A.

3. It is very difficult to identify the position of the errors.

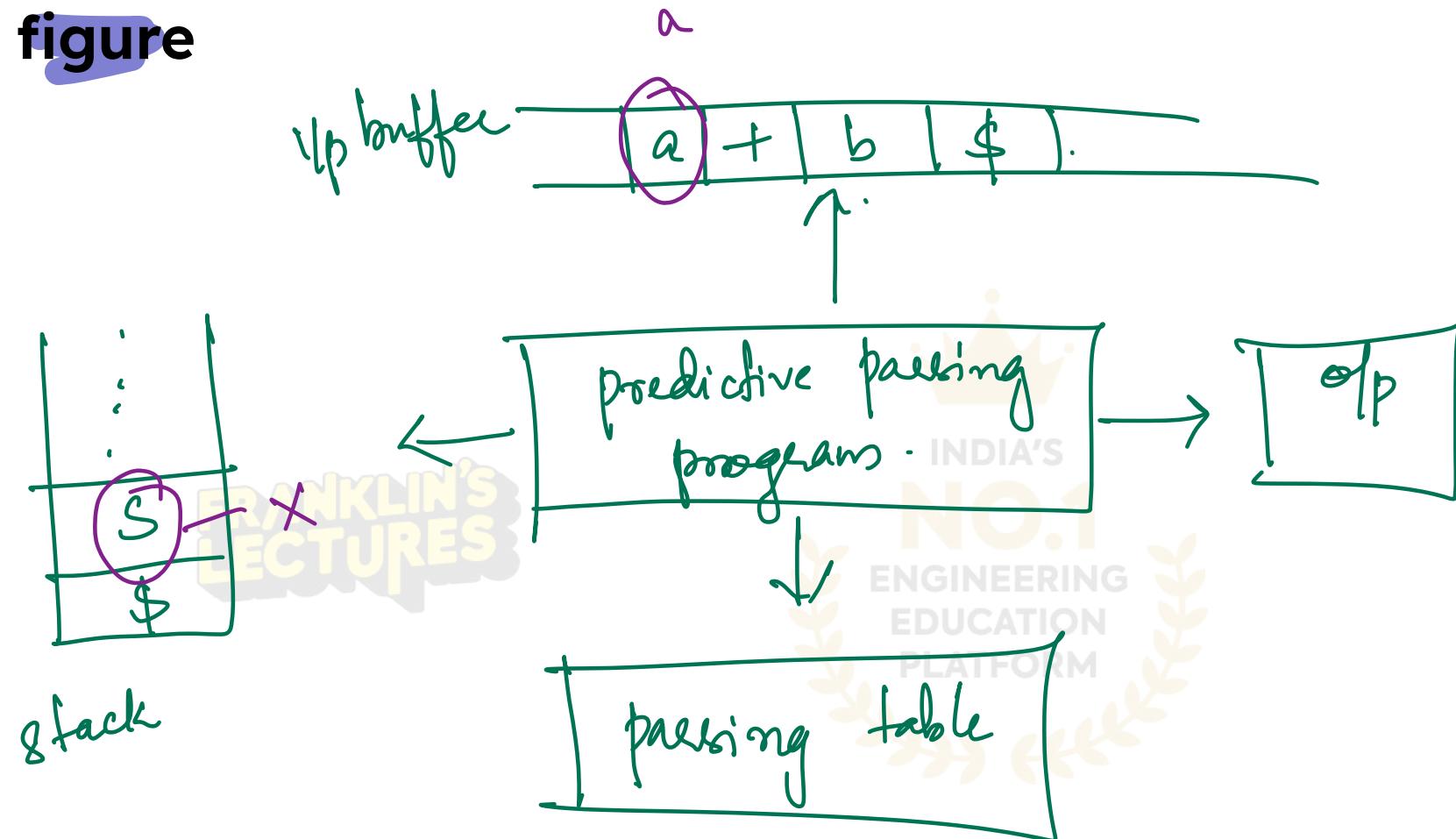
Predictive parsing



For parsing an input string using Predictive parsing technique the grammar should not be left recursive and left factoring is to be done.

A predictive parser has an input buffer, a stack, a parsing table & an output Stream. The input buffer contains the string to be parsed followed by \$, a Symbol used as right end marker to indicate end of input string. The stack contains the sequence of grammar symbols with \$ on the bottom to indicate bottom of the stack. Initially stack contains the start symbol of the grammar on top of the \$. The parsing table is a two dimensional array $M[A, a]$ where 'A' is a non terminal and 'a' is a terminal or \$ symbol.

- figure



FRANKLIN'S
LECTURES

FRANKLIN'S
LECTURES

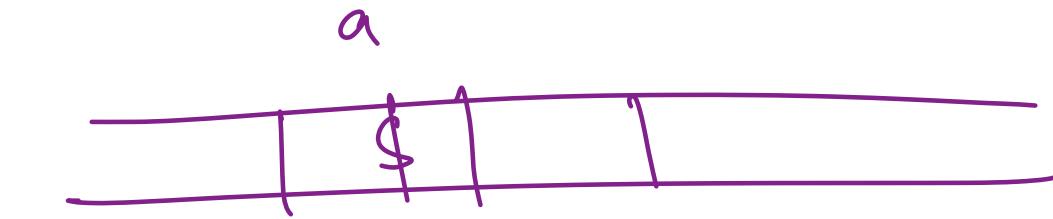
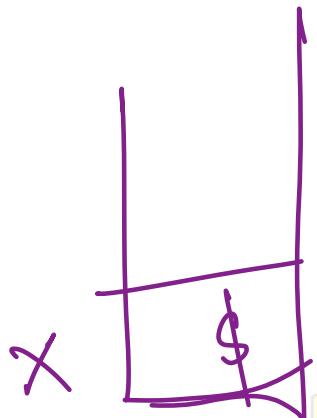
The parser is controlled by a Program that behaves as follows:



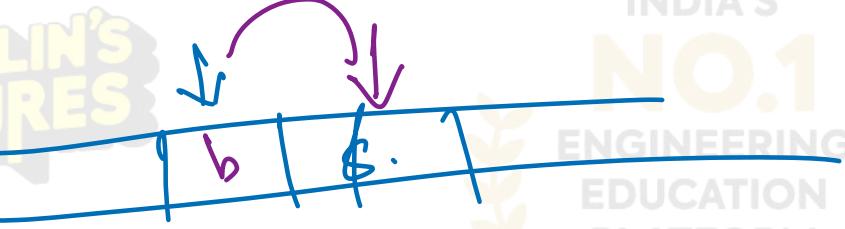
The program consider 'X', the symbol on top of the stack and 'a' the current input symbol. These two symbols determine the actions of parser. There are three Possibilities.

1. If $X = a = \$$, the parser halts and announces successful completion of parsing.
2. If $X=a\neq \$$, the parser pops 'X' out of the Stack and advances input pointer to the next input symbol.
3. If 'X' is a non terminal the program consults parsing table entry $M[X, a]$. This entry will be either an X production of the grammar or an error entry.

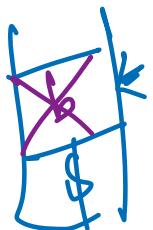
1



$$= x = a = \$ - \checkmark \text{ successfully completed}$$



$$\begin{matrix} x = a \\ b \neq \$ \end{matrix} \Rightarrow$$



2



$$S \nearrow a/b$$

Predictive parsing Algorithm



Input: A string ' w ' and a parsing table M for grammar G

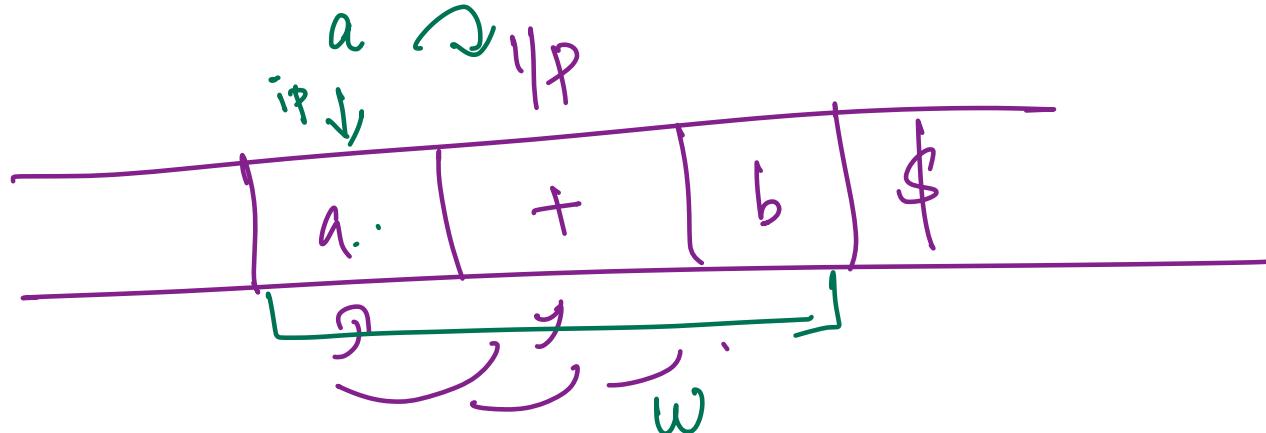
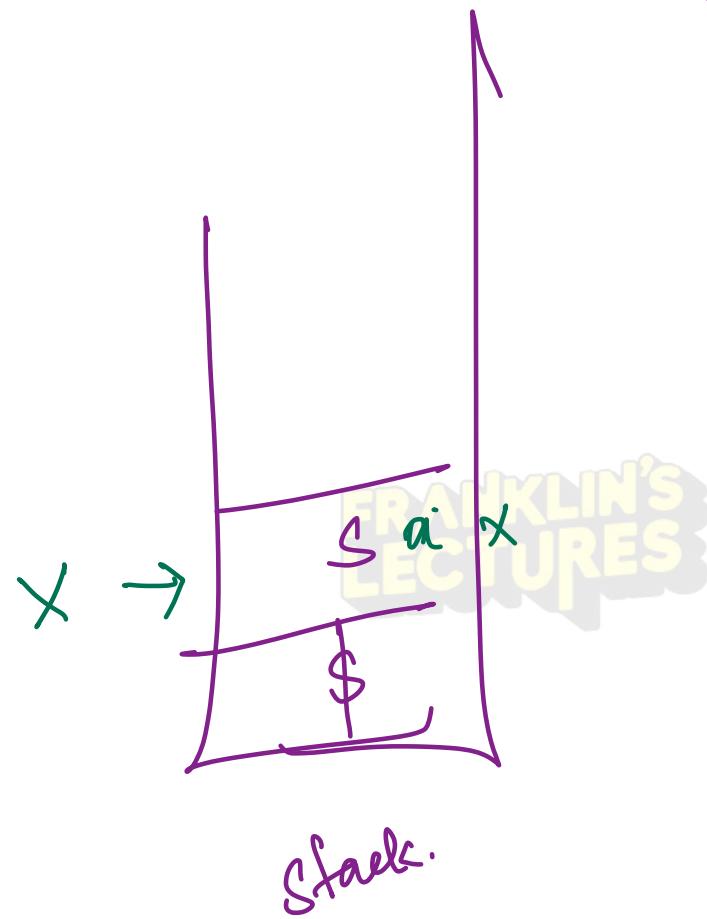
Output: If ' w ' is in $L(G)$, a leftmost derivation of ' w ', otherwise an error indication.

Method: Initially the parser is in a configuration in which it has '\$' on the stack with 'S' the start symbol of 'G' on top and $w\$$ in the input buffer.

set ip (i/p pointer) to point to the first Symbol of $w\$$.

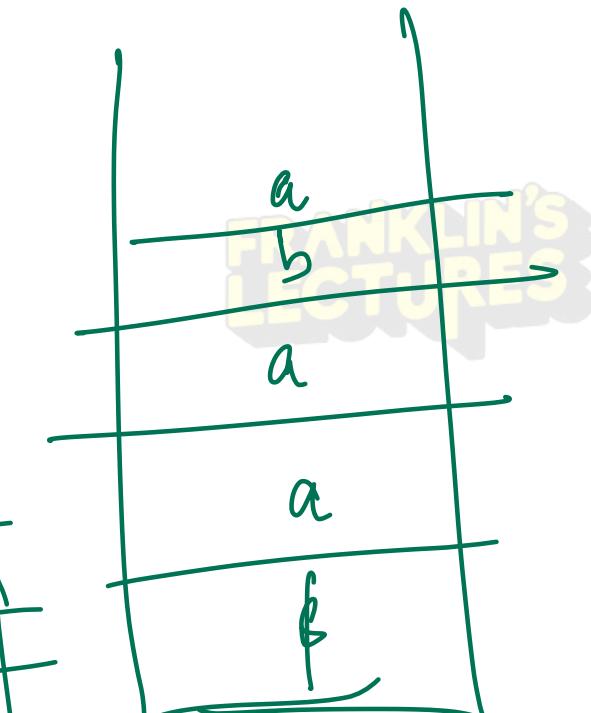
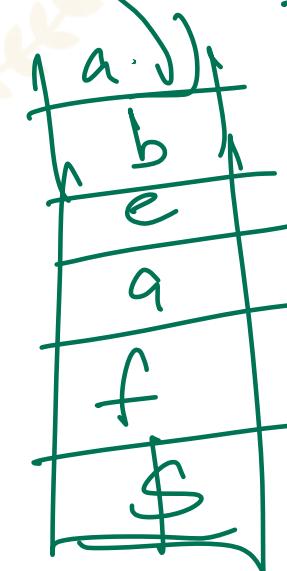


INDIA'S
NO.1
ENGINEERING
EDUCATION
PLATFORM



S → abac

S → abe af



Repeat

Let 'X' be the top stack symbol and 'a' the symbol pointed to by ip.

If 'X' is a terminal or \$ then If $X = a$ then

Pop X from stack and advance ip.

else

error()

else /* X is a non terminal */



If $M[A, a] = X \rightarrow Y_1 Y_2 \dots Y_k$ then

begin

pop 'X' from stack

Push $y_k Y_{k-1} \dots Y_1$ onto the stack with Y_1 on the top.

Output the production $X \rightarrow Y_1 Y_2 \dots Y_k$.

end.

else

error()

until $X = \$$ /* stack empty */



FIRST() and FOLLOW()



- First () and FOLLOW() are two functions associated with the grammar that help us to fill the entries of M table (predictive parsing table)
- FIRST():- Is a function which gives a set a terminals that begins the Strings derived from the production rule.
- FOLLOW():- Is a function which gives set of terminals that can appear immediately to the right of a given symbol.

$$S \rightarrow \underline{aab} \quad \text{FIRST}(CS) = \{a\}$$
$$S \rightarrow asb \mid a \quad \text{Follow}(S) = \{b\}$$

Algorithm to compute FIRST(X) for a grammar Symbol X



- 1) IF X is a terminal, then $\text{FIRST}(X) = \{x\}$
- 2) If $X \rightarrow \epsilon$ is a production then add ' ϵ ' to the set of $\text{FIRST}(X)$.
- 3) If 'X' is a non-terminal and,

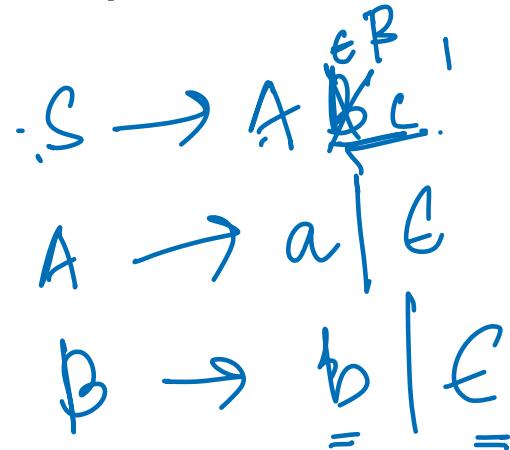
$X \rightarrow y_1, y_2, \dots, Y_k$ is a production then $\text{FIRST}(Y_1)$ is added to $\text{FIRST}(X)$ and If $\text{FIRST}(Y_1)$ contains ϵ then add $\text{FIRST}(Y_2)$ to $\text{FIRST}(X)$ and if $\text{FIRST}(Y_2)$ contains ϵ then add $\text{FIRST}(Y_3)$ to $\text{FIRST}(X)$ and so on. Finally add ϵ to $\text{FIRST}(X)$ if $\text{FIRST}(Y_i)$ contains ϵ

$$S \rightarrow \cancel{ABC} | \underline{\epsilon}$$
$$A \rightarrow \underline{a} | \underline{\epsilon}$$
$$B \rightarrow \underline{b} | \underline{\epsilon}$$
$$C \rightarrow \underline{c} | \underline{\epsilon}$$
$$\text{FIRST}(CS) = \{a, b, c, \epsilon\}$$

Algorithm to Find FOLLOW (A)



- 1) Place $\$$ in FOLLOW(S) where 'S' is the start symbol and $\$$ is the input right end marker.
- 2) If there is a production $A \rightarrow aB\beta$, then everything in FIRST(β) except for ϵ is placed in FOLLOW(B). *(non-term)*
- 3) If there is a production $A \rightarrow aB$ or $A \rightarrow aB\beta$ where FIRST(β) contains ϵ (ie, $\beta \rightarrow^* \epsilon$) then everything in FOLLOW(A) is in FOLLOW(B).



$$\text{FOLLOW}(A) = \{ b, \$, c \}$$

Q. Find FIRST() and FOLLOW(Y) of the Grammar given below.

Start symbol
 $E \rightarrow T E'$

$E' \rightarrow + T E' \mid \epsilon.$

$T \rightarrow F T'$

$T' \rightarrow * F T' \mid \epsilon$

$F \rightarrow (E) \mid id.$



$$E \rightarrow T E'$$

$$E' \rightarrow \pm T E' | \epsilon$$

~~$$T \rightarrow F T'$$~~

$$T' \rightarrow * F T' | \epsilon$$

$$F \rightarrow (E) | id$$

FRANKLIN'S
LECTURES

FIRSTC)

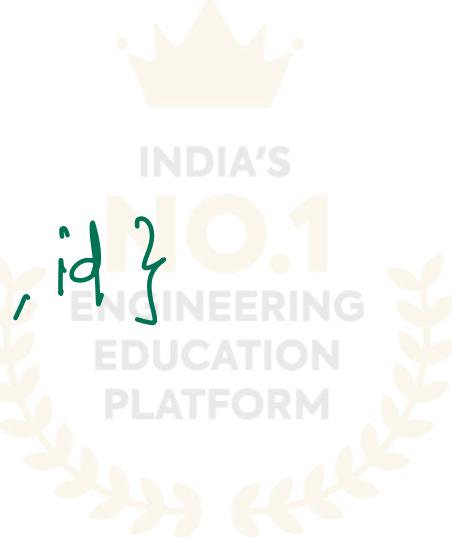
$$\text{FIRST}(C) = \text{FIRST}(T) = \text{FIRST}(F) = \{c, id\}$$

$$\text{FIRST}(E') = \{+, \epsilon\}$$

$$\text{FIRST}(T) = \text{FIRST}(F) = \{c, id\}$$

$$\text{FIRST}(T') = \{\underline{*}, \epsilon\}$$

$$\text{FIRST}(F) = \{c, id\}$$



FOLLOW()

$$\text{FOLLOW}(E) = \{ \$,) \}$$

$$\text{FOLLOW}(E') = \{ \$,) \}$$

$$\text{FOLLOW}(T) = \{ +, \text{FOLLOW}(E') \} = \{ +, \$,) \}$$

$$\text{FOLLOW}(J') = \text{FOLLOW}(T) = \{ +, \$,) \}$$

$$\text{FOLLOW}(F) = \{ * \cup \text{FOLLOW}(I') \} = \{ *, +, \$,) \}$$

Q. Find FIRST() and FOLLOW()

$S \rightarrow A$

$A \rightarrow aB|Ad$

$B \rightarrow bBC|f$

$C \rightarrow g.$



$S \rightarrow \underline{A}$

$A \rightarrow \underline{aB} | \underline{A}$

$B \rightarrow \underline{b} \underline{BC} | f$

$C \rightarrow \underline{g}$

FRANKLIN'S
LECTURES

FIRST(S) = FIRST(A) = {a}

FIRST(A) = {a}

FIRST(B) = {b, f}

FIRST(C) = {g}

FOLLOW(S) = { \$ }

FOLLOW(A) = { \$, d } = FOLLOW(S) ∪ d

FOLLOW(B) = FOLLOW(A) ∪ FIRST(C)

= { \$, d, g }

FOLLOW(C) = FOLLOW(B)

= { \$, d, g }

CONSTRUCTION OF PREDICTIVE PARSING TABLE



The following Algorithm can be used to construct a predictive parsing table for a grammar 'G'.

Algorithm: Construction of predictive Parsing table.

Input: Grammar "G".

Output: parsing table M.



Method:



- 1) For each production $A \rightarrow a$ of the form do steps 2 and 3.
- 2) For each terminal in $\text{FIRST}(a)$ add $A \rightarrow a$ to $M[A, a]$
- 3) If ' ϵ ' is in $\text{FIRST}(a)$ add $A \rightarrow a$ to $M[A, b]$ for each terminal b in $\text{FOLLOW}(A)$. If ' ϵ ' is in $\text{FIRST}(a)$ and '\$' is in $\text{FOLLOW}(A)$ add $A \rightarrow a$ to $M[A, \$]$

Q. Construct predictive parsing table for the following grammar...



$$\begin{array}{l}
 E \rightarrow E+T|T \\
 | \quad \overline{\alpha} \quad \overline{\beta} \quad \text{LR} \\
 T \rightarrow T^*F|F \\
 | \quad \overline{\alpha} \quad \overline{\beta} \quad \text{L} \\
 F \rightarrow (E)|id \\
 | \quad \overline{\alpha} \quad \overline{\beta}
 \end{array}$$

+ * () id

Step1: Eliminate left recursion if the given grammar is left recursive:

Given grammar is left recursive.

So after left recursion elimination grammar becomes,

$$\begin{array}{l}
 E \rightarrow TE' \\
 | \quad \overline{\alpha} \quad \overline{\beta} \\
 E' \rightarrow +TE'|\epsilon
 \end{array}
 \quad \left. \begin{array}{l}
 \leftarrow R \rightarrow E+T|T \\
 | \quad \overline{\alpha} \quad \overline{\beta}
 \end{array} \right.$$

$$\begin{array}{l}
 A \rightarrow A\alpha \quad \overline{\beta} \\
 A \rightarrow \beta A' \\
 A' \rightarrow \alpha A' \quad \overline{\beta}
 \end{array}$$



Step 1 : Eliminate left recursion.

Step 2 : eliminate left factoring -

Step 3 : find FIRST & FOLLOW.

Step 4 : Table construction .



$T \rightarrow FT'$

$T' \rightarrow *FT'| \epsilon$

$F \rightarrow (E)|id$

1



$$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2$$

$$\Rightarrow A \rightarrow \alpha A' \\ A' \rightarrow \beta_2 \mid \beta_2'$$



Step2: Left factoring :

-
In this grammar there is no need of left factoring

Step3: Find FIRST() and FOLLOW() of the all grammar symbols.

$$\text{FIRST}(E) = \{(, \text{id}\}$$

$$\text{FIRST}(E') = \{+, \epsilon\}.$$

$$\text{FIRST}(T) = \{(, \text{id}\}.$$

$$\text{FIRST}(T') = \{*, \epsilon\}.$$

$$\text{FIRST}(F) = \{(, \text{id}\}$$



$E \rightarrow T E'$ - $E' \rightarrow + T E' \in$ $T \rightarrow FT'$: $T \rightarrow *FT' \in$ $F \rightarrow C(E) \mid id$.



$FIRST(E) = FIRST(CT) = FIRST(F) = \{c, id\}$

$FIRST(E') = \{+, \epsilon\}$

$FIRST(T) = FIRST(F) = \{c, id\}$

$FIRST(T') = \{*, \epsilon\}$

$FIRST(F) = \{c, id\}$

$FOLLOW(C) = \{\$,)\}$

$FOLLOW(E') = FOLLOW(E) = \{\$,)\}$

$FOLLOW(T) = FIRST(F) = \{+\} \cup FOLLOW(E')$
 $= \{+, \$,)\}$

$FOLLOW(CT') = FOLLOW(F)$
 $= \{+, \$,)\}$

$FOLLOW(F) = FIRST(T')$
 $= \{*\} \cup FOLLOW(T')$
 $= \{*, +, \$,)\}$



FOLLOW (E) = { \$,) }
FOLLOW (E') = { \$,) }
FOLLOW (T) = { +, \$,) }.
FOLLOW (T') = { +, \$,) }.
FOLLOW (F) = { *, +, \$,) }.

Step 4: Construction of predictive Parsing table.

	E	E'	T	T'	F
FIRST	c, id	+ , ε	c, id	* , ε	c, id
FOLLOW	\$,)	\$,)	+ , \$,)	+ , \$,)	* , + , \$,)

FRANKLIN'S LECTURES

Non terminals	id	+	*	()	\$	
E	$E \rightarrow TE'$			$E \rightarrow TE'$			
E'		$E' \rightarrow +TE'$					
T	$T \rightarrow FT'$			$T \rightarrow FT'$			
T'		$T \rightarrow G$	$T \rightarrow *FT'$		$T \rightarrow E$		$T \rightarrow E$
F	$F \rightarrow id$			$F \rightarrow (E)$			$F \rightarrow (E) id$
					$E' \rightarrow +TE'$		$F \rightarrow (E)$
					$E' \rightarrow E$		$F \rightarrow id$

Moves made by predictive parser on
input $\text{id} + \text{id}^* \text{id} \$$



TABLE





STACK

\$ E

\$ E' T

\$ E' T' F

\$ E' T' id

\$ E' T' ±

\$ E' T' T

\$ E' T' id

\$ E' T' F *

INPUT

id + id * id \$

+ id * id \$

- id * id \$

id * id \$

id * id \$

= id \$

OUTPUT

E → TE'

T → FT'

T' → E

E' → +TE'

T → FT'

F → id

T' → *FT'

E → TE'

E' → +TE' | E

T → FT'

T' → *FT' | E

F → (E) | id

$\frac{f}{f} E' T' id$

$\frac{f}{f} F' T'$

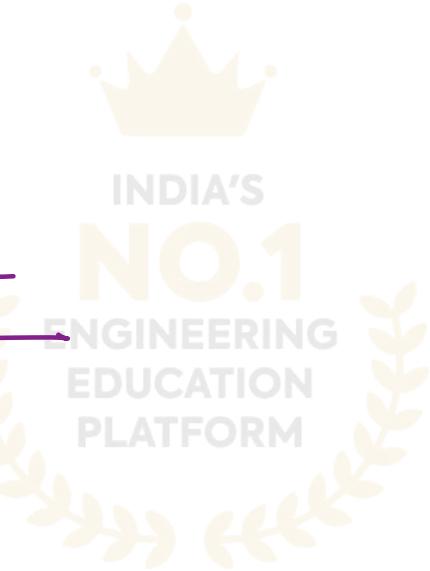
$\frac{f}{f} F' K'$

$\frac{f}{f}$

**FRANKLIN'S
LECTURES**

$id \frac{f}{f} \frac{f}{f}$

$\frac{f}{f}$



$F \rightarrow id$

$T' \rightarrow E$

$F' \rightarrow E$

**FRANKLIN'S
LECTURES**

**FRANKLIN'S
LECTURES**

LL(1) Grammar :



A grammar whose parsing table has no multiply defined entries is said to be LL(1). The first L in LL(1) stands for scanning input from left to right, the second L for left most derivation and 1 for using 1 input symbol.

To become a grammar LL(1):

- 1) The grammar should not be an ambiguous grammar.
- 2) The grammar should not be left recursive.
- 3) The grammar should be deterministic
- 4) The parsing table should not contain multiply defined entries.

Q. How we can check whether a grammar is LL(1) or not without constructing a predictive parsing table?



The grammar is said to be LL(1) grammar if the following two conditions are satisfied:



Conditions:



1. For every productions of the form

$$A \rightarrow a_1 | a_2 | \dots | a_n$$

$$\text{FIRST}(a_i) \cap \text{FIRST}(a_j) = \emptyset \quad \forall i, j \geq 1$$

where $i \neq j$

- 2) For every non-terminal A if $\text{FIRST}(A)$ contains ϵ then,

$$\text{FIRST}(A) \cap \text{FOLLOW}(A) = \emptyset$$

Q. Check whether the grammar

$$S \rightarrow iEtSA | a$$

$$A \rightarrow eSe | \epsilon.$$

$E \rightarrow b$ is LL(1) or not without constructing Predictive parsing pable.

$$\text{FOLLOW}(S) = \$.$$

$$S \rightarrow iEtSA | a \Rightarrow \text{FIRST}(iEtSA) \cap \text{FIRST}(a)$$

$$= \{i\} \cap \{a\} = \emptyset \quad \checkmark$$

$$A \rightarrow eSe | \epsilon = \text{FIRST}(eS) \cap \text{FIRST}(\epsilon)$$

$$= \{e\} \cap \{\epsilon\} = \emptyset$$

Condition 1



a) $S \rightarrow iEtSA | a$: FIRST ($iEtSA$) \cap FIRST (a)
 $\{\mathbf{i}\} \cap \{a\} = \emptyset$

b) $A \rightarrow eS | \epsilon$: FIRST (eS) \cap FIRST (ϵ)
 $\{e\} \cap \{\epsilon\} = \emptyset$

$$\text{FOLLOW}(S) = \{ \$ \} \cup \text{FIRST}(A) = \{ \$, e \}$$

$$\text{FOLLOW}(A) = \{ \$, e \}$$

Condition 2



According to condition 2 $\text{FIRST}(A)$ has ϵ so $\text{FIRST}(A) \cap \text{FOLLOW}(A)$ is empty .

check whether the condition 2 is satisfied or not Satisfied

So $\text{FIRST}(A) \cap \text{FOLLOW}(A) = \emptyset$

but $\underline{\{e, \epsilon\}} \cap \underline{\{\$, e\}} = \{e\}$. Thus we can say that condition 2 is not Satisfied
Since one of the condition fails

so the given grammar is not LL(1).



THANK YOU