# **APS106**



# binary search trees.

**Week 12** Lecture 2 (12.2)



### This Week's Content

- Lecture 12.1
  - Linked lists, binary trees
  - Reading: Chapter 14
- **Lecture 12.2** 
  - Binary search trees
  - Reading: Chapter 14
- Lecture 12.3
  - Design Problem: 20 Questions



# Clearing things up.



```
class LinkedList:
                                            class LinkedList:
                                                                                        class LinkedList:
   def __init__(self):
                                                                                            def __init__(self):
                                                def __init__(self):
        (self) -> NoneType
                                                    (self) -> NoneType
                                                                                                (self) -> NoneType
       Create an empty linked list.
                                                   Create an empty linked list.
                                                                                                Create an empty linked list.
       self.length = 0
                                                    self.length = 0
                                                                                                self.length = 0
       self.head = None
                                                    self.head = None
                                                                                                self.head = None
   def str (self): ...
                                               def __str__(self): ...
                                                                                            def __str__(self): ...
   def add_to_head(self, cargo): ...
                                                def add to head(self, cargo): ...
                                                                                            def add to head(self, cargo): ...
   def add_to_tail(self, cargo):
                                                def add to tail(self, cargo):
                                                                                            def add to tail(self, cargo):
        (self, object) -> NoneType
                                                    (self, object) -> NoneType
                                                                                                (self, object) -> NoneType
       Add cargo to the tail of the list.
                                                    Add cargo to the tail of the list.
                                                                                                Add cargo to the tail of the list.
       on = self.head
                                                    on = self.head
                                                                                                on = self.head
       while on.next:
                                                   while on.next is not None:
                                                                                                while on.next != None:
           on = on.next
                                                        on = on.next
                                                                                                    on = on.next
       on.next = Node(cargo)
                                                   on.next = Node(cargo)
                                                                                                on.next = Node(cargo)
   def get at index(self, index): ...
                                               def get at index(self, index): ...
                                                                                            def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
                                               def delete_by_cargo(self, cargo): ...
                                                                                      def delete_by_cargo(self, cargo): ...
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
       Create an empty linked list.
       self.length = 0
       self.head = None
   def str (self): ...
   def add_to_head(self, cargo): ...
   def add_to_tail(self, cargo):
        (self, object) -> NoneType
       Add cargo to the tail of the list.
       on = self.head
       while on.next:
           on = on.next
       on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
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class LinkedList:
    def __init__(self):
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```
class LinkedList:
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    def get at index(self, index): ...
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```
class LinkedList:
   def __init__(self):
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        Create an empty linked list.
       self.length = 0
        self.head = None
   def __str__(self): ...
   def add to head(self, cargo): ...
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        Add cargo to the tail of the list.
        on = self.head
        while on.next is not None:
            on = on.next
        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- •is is an identity test.
- It checks whether the right-hand side and the left-hand side are the very same object.

```
>>> a = 'hello world'
>>> b = 'hello world'
>>> a is b
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
       self.length = 0
        self.head = None
   def __str__(self): ...
   def add to head(self, cargo): ...
   def add_to_tail(self, cargo):
        (self, object) -> NoneType
        Add cargo to the tail of the list.
        on = self.head
        while on.next is not None:
            on = on.next
        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- is an identity test.
- It checks whether the right-hand side and the left-hand side are the very same object.

```
>>> a = 'hello world'
>>> b = 'hello world'
>>> a is b
False

>>> id(a)
1603648396784

>>> id(b)
1603648426160
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
        self.length = 0
        self.head = None
   def __str__(self): ...
   def add to head(self, cargo): ...
   def add to tail(self, cargo):
        (self, object) -> NoneType
        Add cargo to the tail of the list.
        on = self.head
        while on.next is not None:
            on = on.next
        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- is an identity test.
- It checks whether the right-hand side and the left-hand side are the very same object.

```
>>> a = None
>>> b = None
>>> a is b
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
       self.length = 0
        self.head = None
   def __str__(self): ...
   def add to head(self, cargo): ...
   def add_to_tail(self, cargo):
        (self, object) -> NoneType
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        on = self.head
        while on.next is not None:
            on = on.next
        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- is an identity test.
- It checks whether the right-hand side and the left-hand side are the very same object.

```
>>> a = None
>>> b = None
>>> a is b
True

>>> id(a)
140718929239264

>>> id(b)
140718929239264
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
       self.length = 0
        self.head = None
   def __str__(self): ...
   def add to head(self, cargo): ...
   def add_to_tail(self, cargo):
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        Add cargo to the tail of the list.
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        while on.next is not None:
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   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- •is an identity test.
- It checks whether the right-hand side and the left-hand side are the very same object.

```
while on.next is not None:

>>> Node() is not None
True

>>> None is not None
False
```



```
class LinkedList:
                                            class LinkedList:
   def __init__(self):
                                                def __init__(self):
        (self) -> NoneType
                                                    (self) -> NoneType
       Create an empty linked list.
                                                    Create an empty linked list.
       self.length = 0
                                                    self.length = 0
       self.head = None
                                                    self.head = None
   def str (self): ...
                                                def __str__(self): ...
   def add_to_head(self, cargo): ...
                                                def add to head(self, cargo): ...
   def add_to_tail(self, cargo):
                                                def add to tail(self, cargo):
        (self, object) -> NoneType
                                                    (self, object) -> NoneType
       Add cargo to the tail of the list.
                                                    Add cargo to the tail of the list.
       on = self.head
                                                    on = self.head
       while on.next:
                                                    while on.next is not None:
           on = on.next
                                                        on = on.next
       on.next = Node(cargo)
                                                    on.next = Node(cargo)
   def get_at_index(self, index): ...
                                                def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
                                                def delete_by_cargo(self, cargo): ...
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```
class LinkedList:
    def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
        self.length = 0
        self.head = None
    def __str__(self): ...
    def add to head(self, cargo): ...
    def add to tail(self, cargo):
        (self, object) -> NoneType
        Add cargo to the tail of the list.
        on = self.head
        while on.next != None:
            on = on.next
        on.next = Node(cargo)
    def get at index(self, index): ...
    def delete by cargo(self, cargo): ...
```



```
class LinkedList:
   def __init__(self):
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   def add to head(self, cargo): ...
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        on = self.head
        while on.next != None:
            on = on.next
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   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- == is an equality test.
- It checks whether the right-hand side and the left-hand side are equal objects.

```
>>> a = 'hello world'
>>> b = 'hello world'
>>> a == b
```



### class LinkedList: def \_\_init\_\_(self): (self) -> NoneType Create an empty linked list. self.length = 0 self.head = None def \_\_str\_\_(self): ... def add to head(self, cargo): ... def add\_to\_tail(self, cargo): (self, object) -> NoneType Add cargo to the tail of the list. on = self.head while on.next != None: on = on.next on.next = Node(cargo) def get at index(self, index): ... def delete\_by\_cargo(self, cargo): ...

- == is an equality test.
- It checks whether the right-hand side and the left-hand side are equal objects.

```
>>> a = 'hello world'
>>> b = 'hello world'
>>> a == b
True

>>> id(a)
1603648396784

>>> id(b)
1603648426160
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
       self.length = 0
        self.head = None
   def __str__(self): ...
   def add to head(self, cargo): ...
   def add_to_tail(self, cargo):
        (self, object) -> NoneType
        Add cargo to the tail of the list.
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        while on.next != None:
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        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- == is an equality test.
- It checks whether the right-hand side and the left-hand side are equal objects.

```
while on.next != None:

>>> Node() != None
True

>>> None != None
False
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
       Create an empty linked list.
       self.length = 0
       self.head = None
   def str (self): ...
   def add_to_head(self, cargo): ...
   def add_to_tail(self, cargo):
        (self, object) -> NoneType
       Add cargo to the tail of the list.
       on = self.head
       while on.next:
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   def get at index(self, index): ...
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```

```
class LinkedList:
                                             class LinkedList:
    def __init__(self):
                                                 def __init__(self):
        (self) -> NoneType
                                                     (self) -> NoneType
       Create an empty linked list.
                                                     Create an empty linked list.
        self.length = 0
                                                     self.length = 0
        self.head = None
                                                     self.head = None
    def __str__(self): ...
                                                 def __str__(self): ...
    def add to head(self, cargo): ...
                                                 def add to head(self, cargo): ...
    def add to tail(self, cargo):
                                                 def add to tail(self, cargo):
        (self, object) -> NoneType
                                                     (self, object) -> NoneType
        Add cargo to the tail of the list.
                                                     Add cargo to the tail of the list.
        on = self.head
                                                     on = self.head
       while on.next is not None:
                                                     while on.next != None:
            on = on.next
                                                         on = on.next
       on.next = Node(cargo)
                                                     on.next = Node(cargo)
    def get at index(self, index): ...
                                                def get at index(self, index): ...
    def delete_by_cargo(self, cargo): ...
                                                def delete by cargo(self, cargo): ...
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
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   def add to head(self, cargo): ...
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        Add cargo to the tail of the list.
        on = self.head
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            on = on.next
        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- Truthy and Falsy Values in Python.
- Expressions with operands and operators evaluate to either True or False and they can be used in an if or while condition to determine if a code block should run.

```
>>> if 5 > 3:
    print("True")
True
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
        self.length = 0
        self.head = None
   def __str__(self): ...
   def add to head(self, cargo): ...
   def add to tail(self, cargo):
        (self, object) -> NoneType
        Add cargo to the tail of the list.
        on = self.head
       while on.next:
            on = on.next
        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- Truthy and Falsy Values in Python.
- What do you think would be the output of this code?

```
>>> a = 4
>>> if a:
print(a)
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
        self.length = 0
        self.head = None
   def __str__(self): ...
   def add to head(self, cargo): ...
   def add to tail(self, cargo):
        (self, object) -> NoneType
        Add cargo to the tail of the list.
        on = self.head
       while on.next:
            on = on.next
        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- Truthy and Falsy Values in Python.
- What do you think would be the output of this code?

```
>>> a = 4
>>> if a:
    print(a)
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
       self.length = 0
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   def add to head(self, cargo): ...
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        Add cargo to the tail of the list.
        on = self.head
       while on.next:
            on = on.next
        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- Truthy and Falsy Values in Python.
- What do you think would be the output of this code?

```
>>> a = 0
>>> if a:
    print(a)
```



```
class LinkedList:
   def __init__(self):
        (self) -> NoneType
        Create an empty linked list.
       self.length = 0
        self.head = None
   def __str__(self): ...
   def add_to_head(self, cargo): ...
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        on.next = Node(cargo)
   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- Truthy and Falsy Values in Python.
- In Python, individual values can evaluate to either True or False.
- They do not necessarily have to be part of a larger expression to evaluate to a truth value because they already have one that has been determined by the rules of the Python language?
  - Values that evaluate to False are considered Falsy.
  - Values that evaluate to True are considered Truthy.



```
class LinkedList:
   def __init__(self):
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        self.head = None
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   def add to head(self, cargo): ...
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        on.next = Node(cargo)
    def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- Falsy Values
- Sequences and Collections
  - Empty lists []
  - Empty tuples ()
  - Empty dictionaries { }
  - Empty sets set ()
  - Empty strings ""
  - Empty ranges range (0)

#### Numbers

- Zero of any numeric type.
- Integer: 0
- Float: 0.0
- Complex: 0j

#### Constants

- None
- False



```
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   def get at index(self, index): ...
   def delete_by_cargo(self, cargo): ...
```

- Truthy Values
- By default, an object is considered True.
- Non-empty sequences or collections (lists, tuples, strings, dictionaries, sets).
- Numeric values that are not zero.
- True



# **Clearing things up**

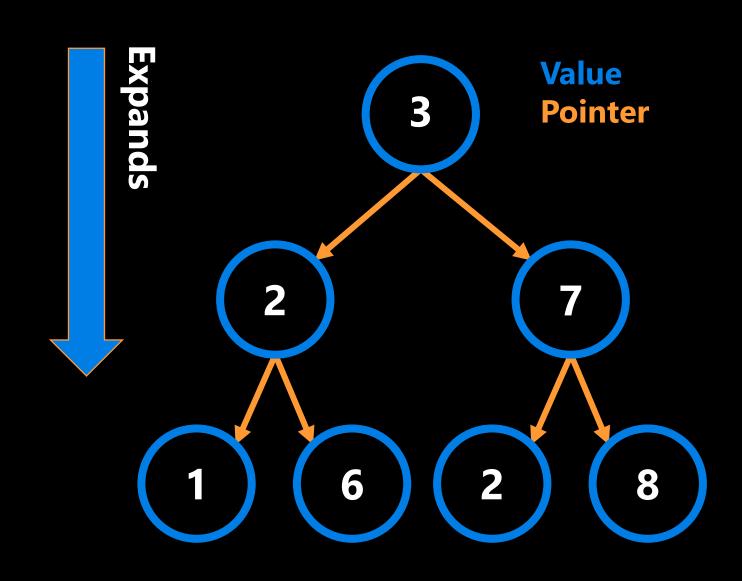
When in doubt, try it out!

# Open your notebook

Click Link:
1. Truthy and Falsy Values

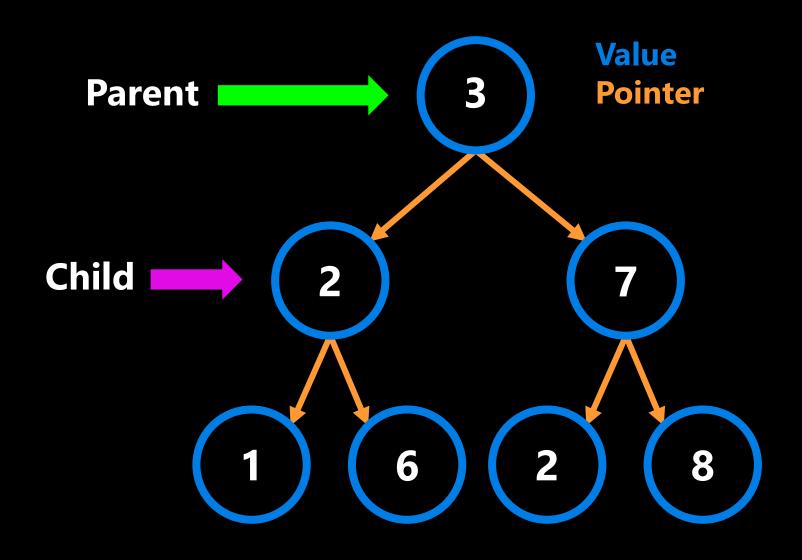


- Trees expand in one direction.
- Trees are made up of parents and children.
  - These are relative terms for nodes.
  - Every parent can be a child.



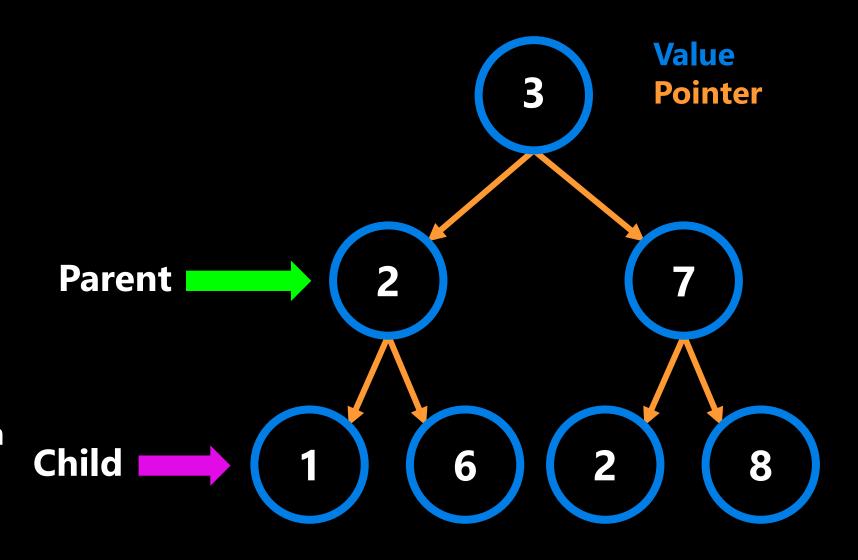


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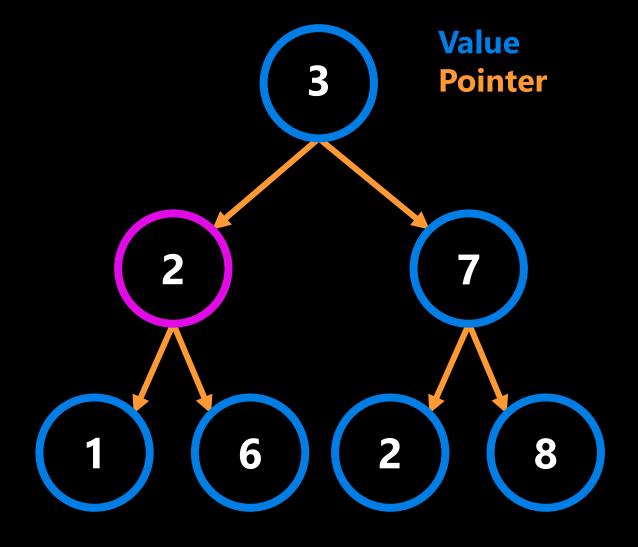


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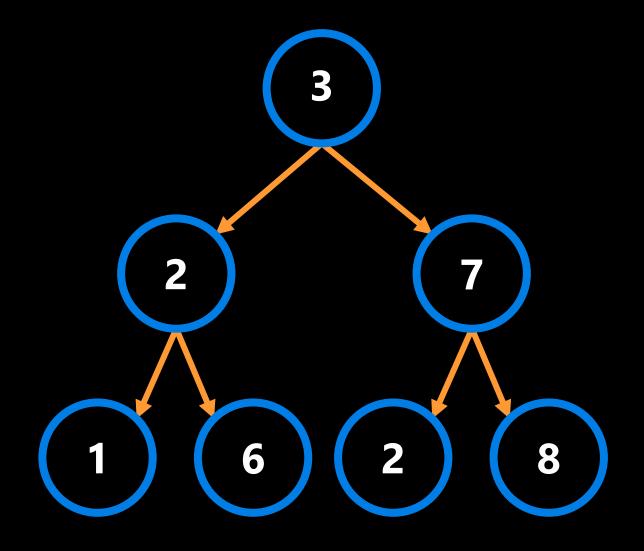


- Node 2 is a child of Node 3 and a parent of Node 1 and Node 6.
- Every node can only have one parent but can have many children.



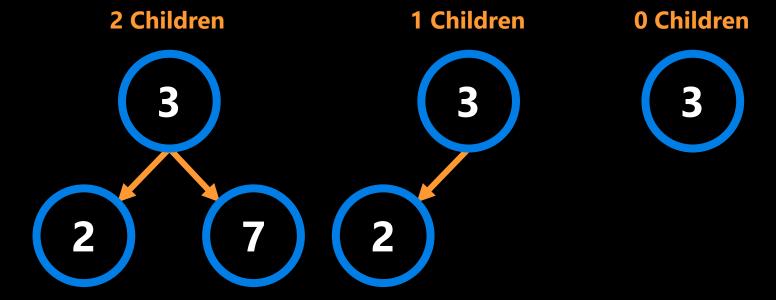


- There are many different types of trees.
  - Family Trees.
  - Decision Trees.
  - Heaps.
  - Tries.
  - HTML Trees.
  - Binary Trees (We will focus on these).



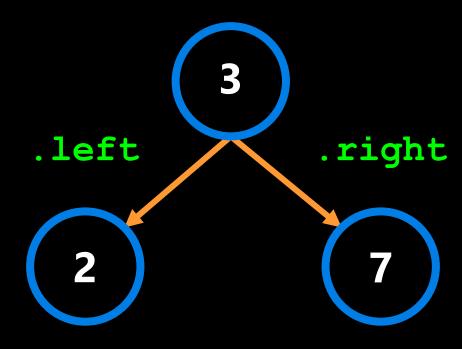


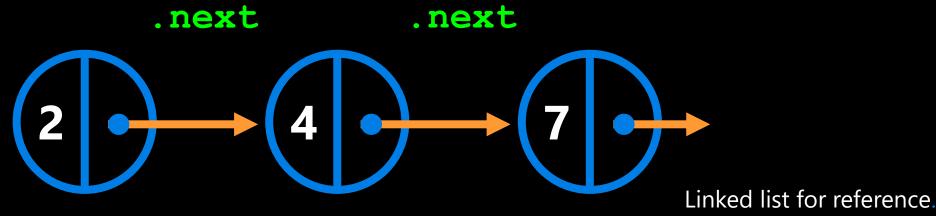
- Main Rule:
  - Each Node can have a maximum of two children (Pointers).
    - 0 Children
    - 1 Children
    - 2 Children





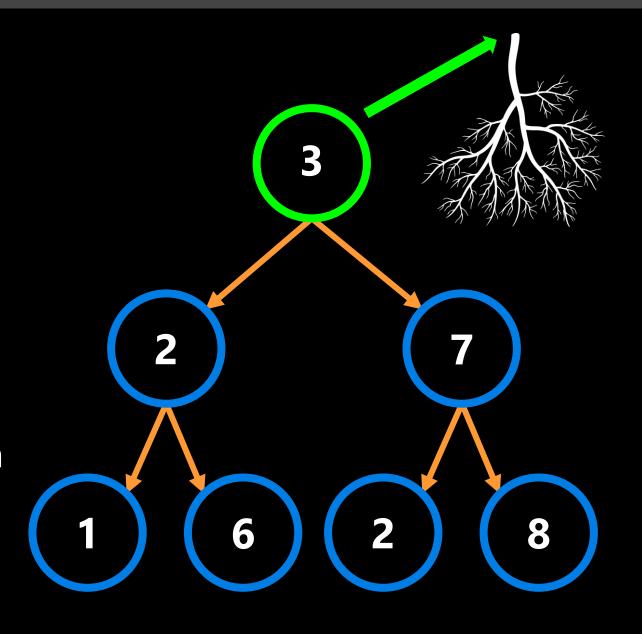
Children are represented using .left and .right.





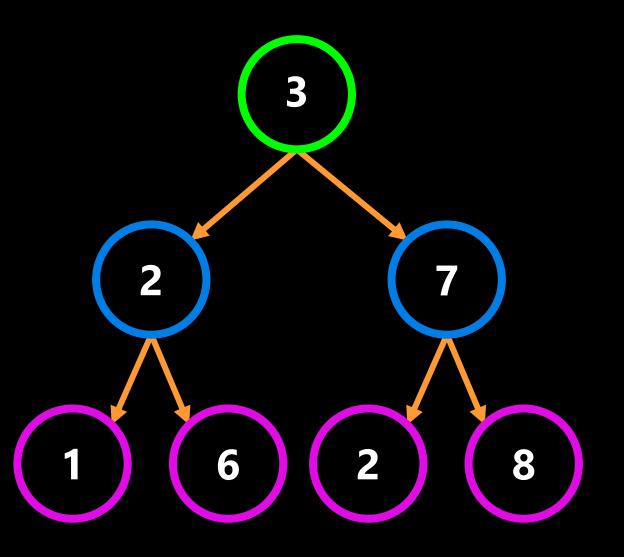


- Terminology
- The top node is called the root node.
- Any node without children is called a leaf node.
- The path between the root node and a leaf node is called a branch.



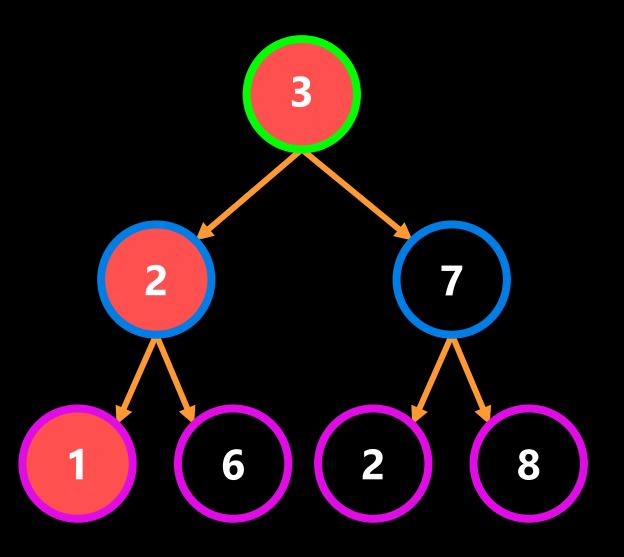


- Terminology
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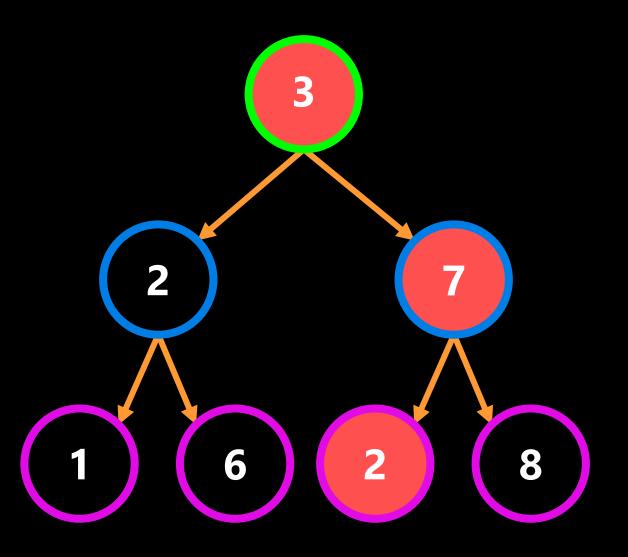


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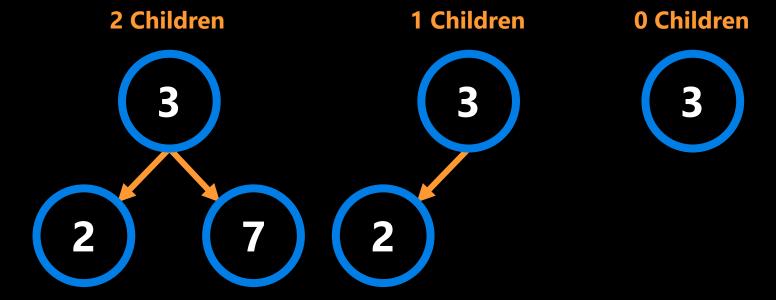


- Terminology
- The top node is called the root node.
- Any node without children is called a leaf node.
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- Main Rule:
  - Each Node can have a maximum of two children (Pointers).
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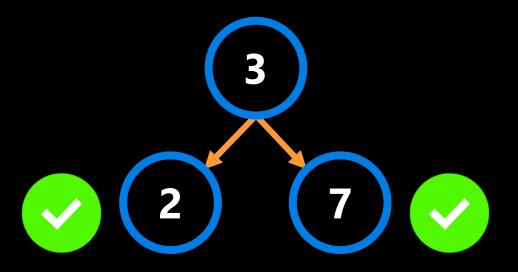




# **Binary Search Trees**

- Main Rule:
  - Each Node can have a maximum of two children (Pointers).
    - 0 Children
    - 1 Children
    - 2 Children
  - node.cargo must be more than node.left.cargo and less than node.right.cargo.
    - **3** > 2
    - **3** < 7

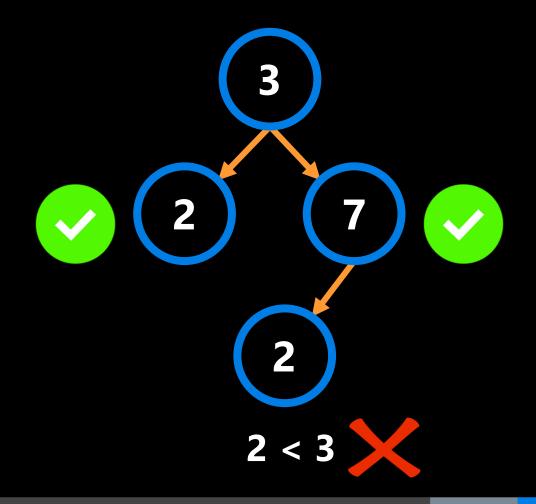
# A special case of the binary tree.





## **Binary Search Trees**

- Main Rule:
  - Each Node can have a maximum of two children (Pointers).
    - 0 Children
    - 1 Children
    - 2 Children
  - node.cargo must be more than node.left.cargo and less than node.right.cargo.
    - **3** > 2
    - **3** < 7
  - This rule must be true for the entire tree.
    - Everything to the right of 3 must be greater than 3.





### **The Binary Search Tree Class**

Let's check out the BinarySearchTree class functionality.

# Open your notebook

Click Link:2. BinarySearchTreeClass



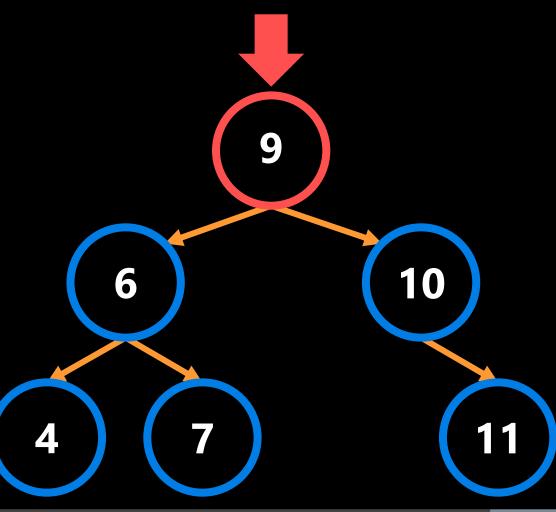
# Let's try with a valid binary search tree.



```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
   def print_tree(self): ...
   def is_valid(self):
        (self) -> NoneType
        Checks if self.root is a valid binary search tree.
       on = self.root
        stack = []
        prev = None
       while len(stack) > 0 or on is not None:
           while on is not None:
                stack.append(on)
                on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
                return False
            prev = on
           on = on.right
       return True
```

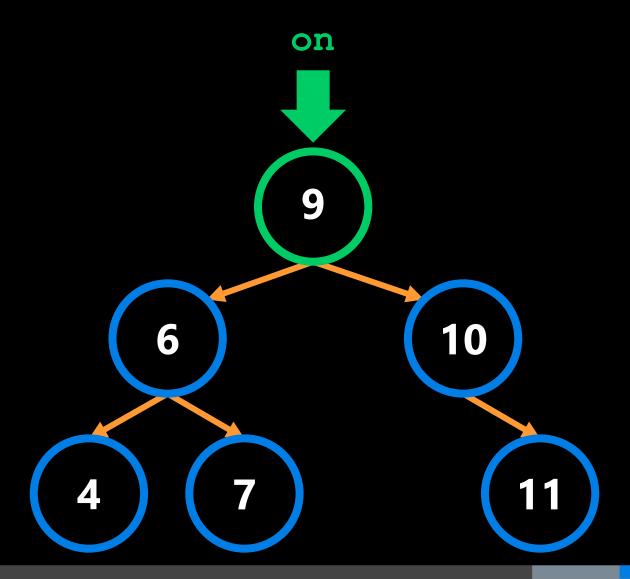
#### This is a Valid Tree





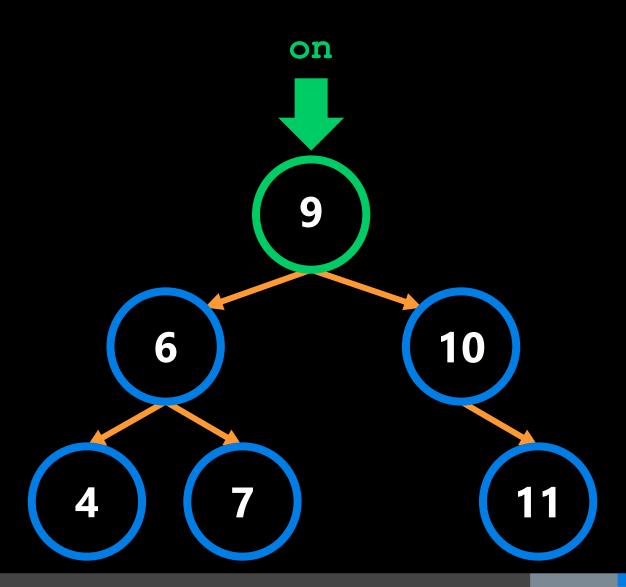


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
   def print_tree(self): ...
   def is_valid(self):
        (self) -> NoneType
        Checks if self.root is a valid binary search tree.
       on = self.root
                                Set on position.
       stack = []
        prev = None
       while len(stack) > 0 or on is not None:
           while on is not None:
                stack.append(on)
                on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
                return False
           prev = on
           on = on.right
       return True
```



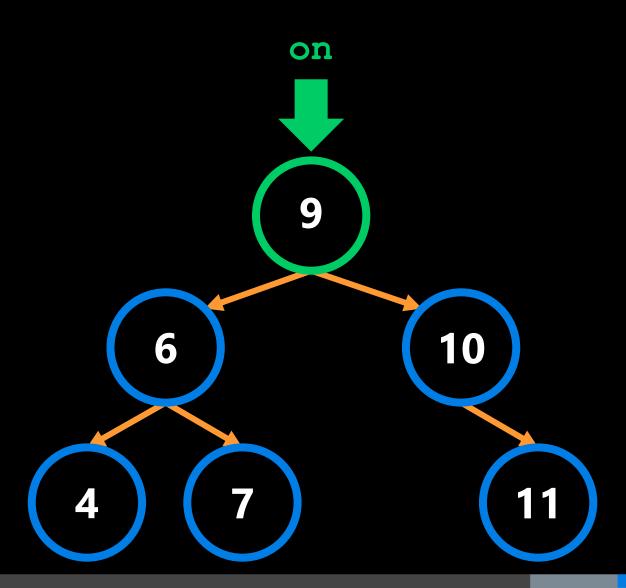


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
                                         stack =
        self.root = root
   def print_tree(self): ...
   def is_valid(self):
        (self) -> NoneType
        Checks if self.root is a valid binary search tree.
       on = self.root
                            Create stack list.
        stack = []
        prev = None
       while len(stack) > 0 or on is not None:
           while on is not None:
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



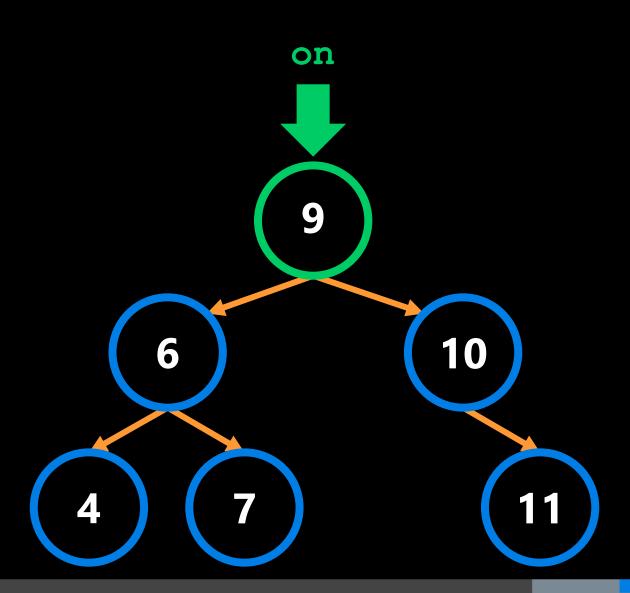


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                         stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
                            Initialize previous node.
       prev = None
       while len(stack) > 0 or on is not None:
           while on is not None:
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



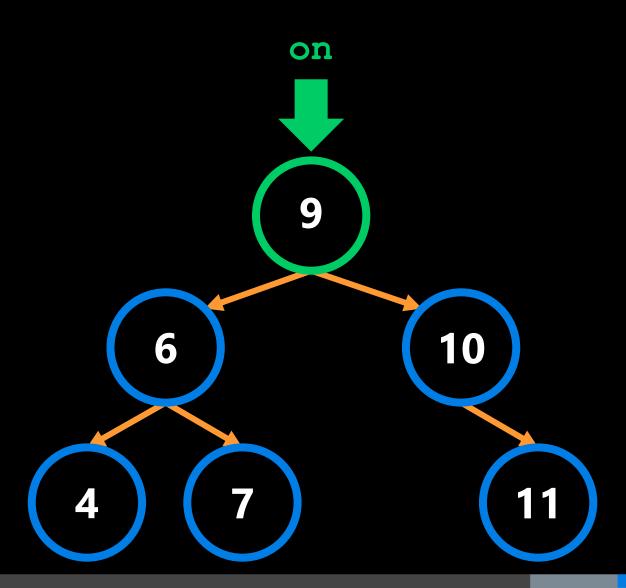


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                         stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None:
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



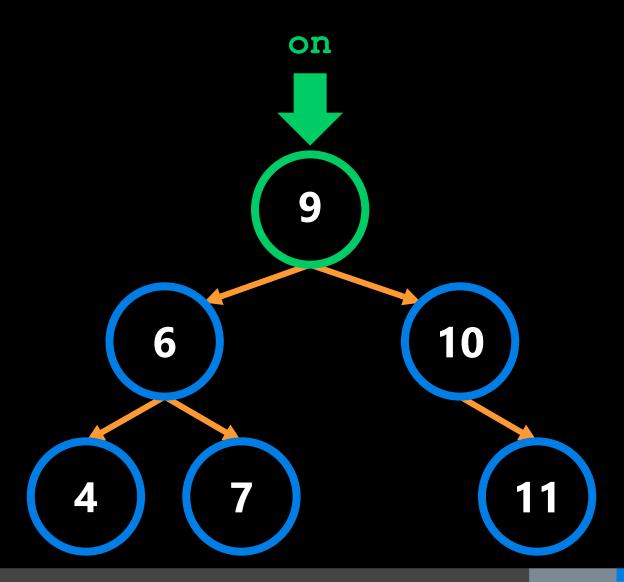


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None:
                                  True
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



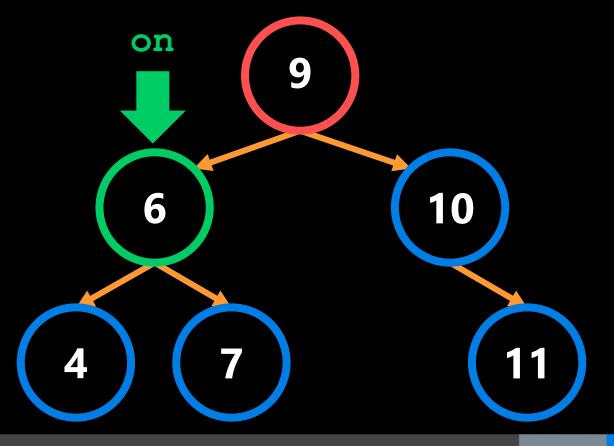


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
                                    True
           while on is not None:
                                        Add on to stack.
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



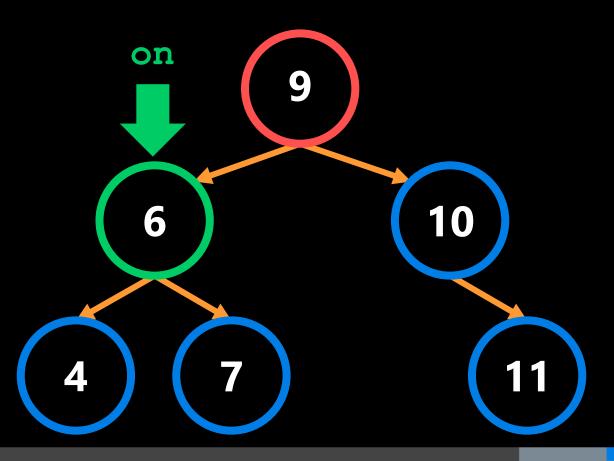


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: True
               stack.append(on)
                                     Move on to left
               on = on.left
                                     node pointer.
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



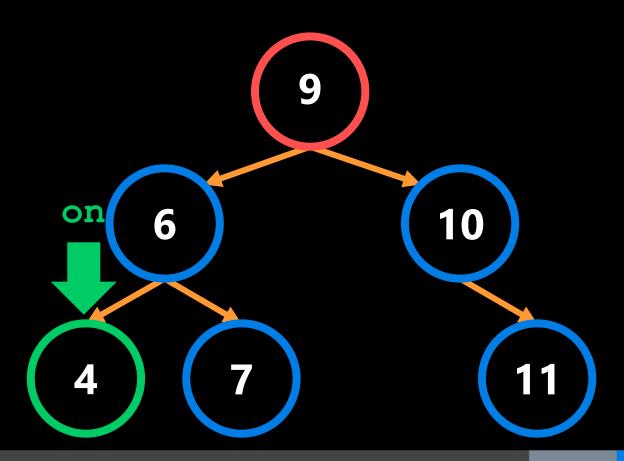


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
                                    True
           while on is not None:
                                        Add on to stack.
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



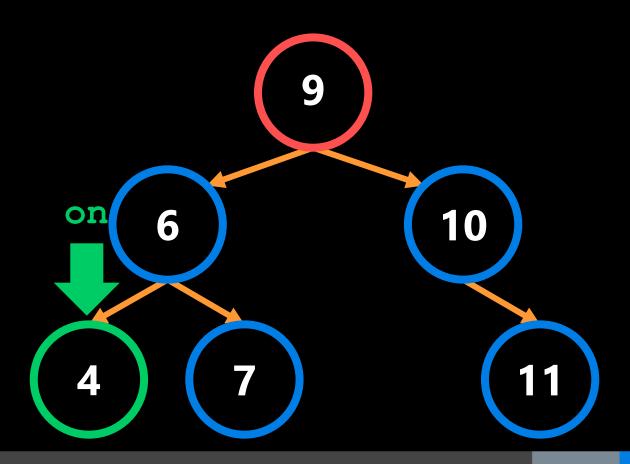


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
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       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: True
               stack.append(on)
                                     Move on to left
               on = on.left
                                     node pointer.
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```





```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
                                    True
           while on is not None:
                                        Add on to stack.
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



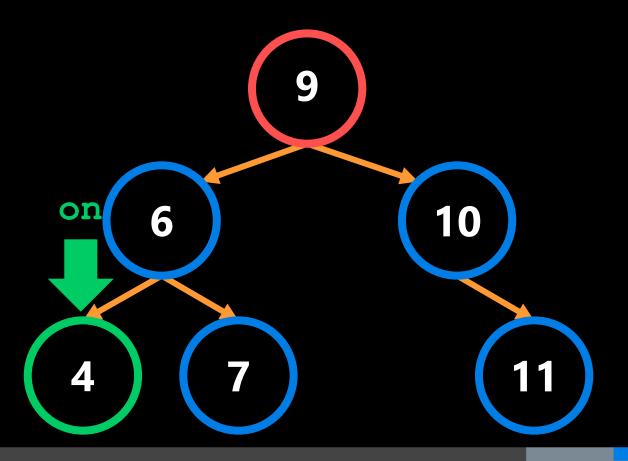


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                       stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: True
               stack.append(on)
                                    Move on to left
               on = on.left
                                    node pointer.
           on = stack.pop()
                                                               on
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
                                                             None
       return True
```

```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                       stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
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       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
           on = stack.pop()
                                                                on
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
                                                              None
       return True
```

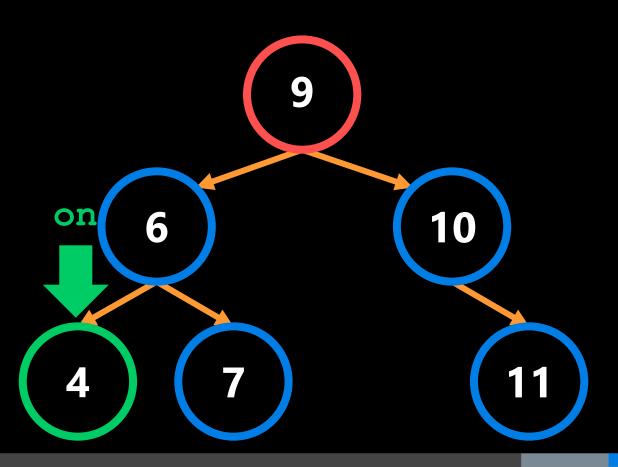


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
                                    Set on to left node
                                    in stack.
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



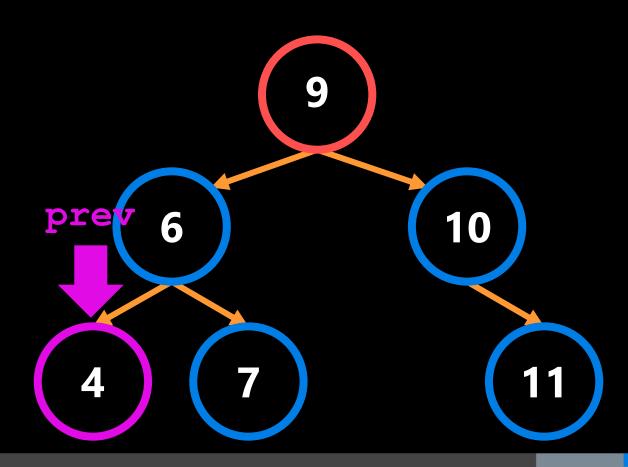


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
   def is_valid(self):
      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
          prev = on
          on = on.right
      return True
```

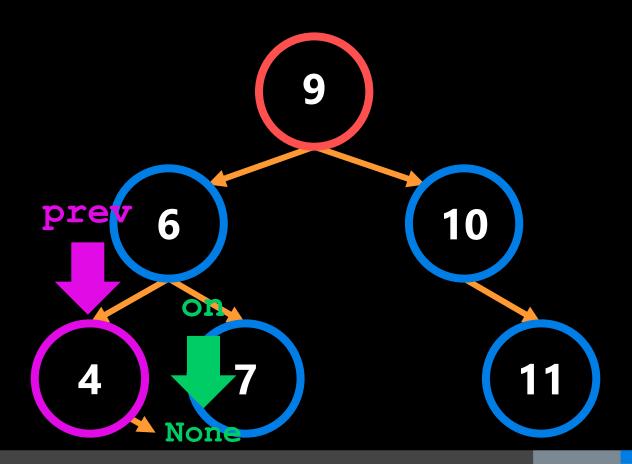




```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
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      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
                          Set prev to on.
          prev = on
          on = on.right
      return True
```

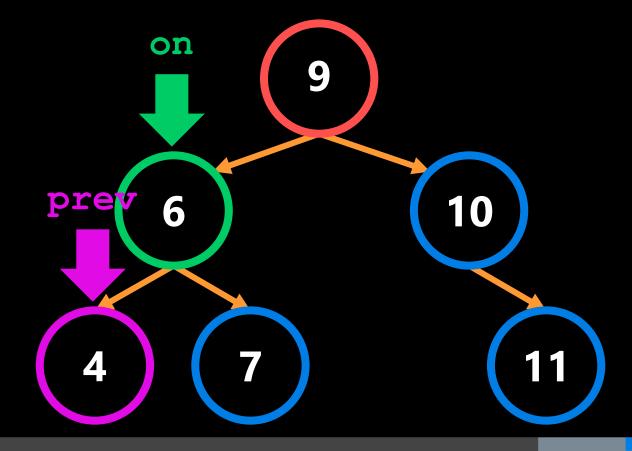


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
   def is_valid(self):
      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
         on = stack.pop()
          return False
          prev = on
                              Move on to the
          on = on.right
                              right pointer.
      return True
```



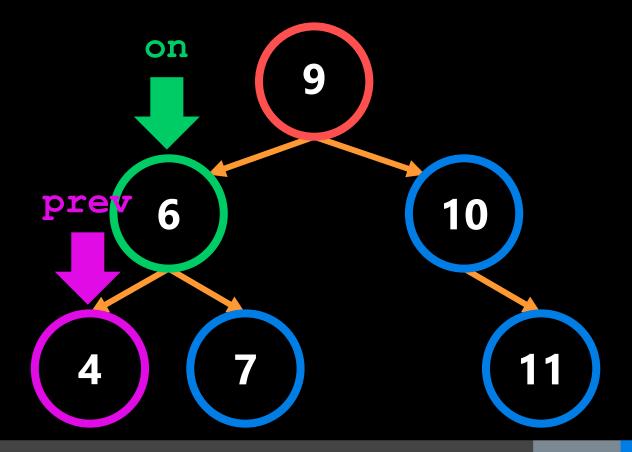


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
                                    Set on to left node
                                    in stack.
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



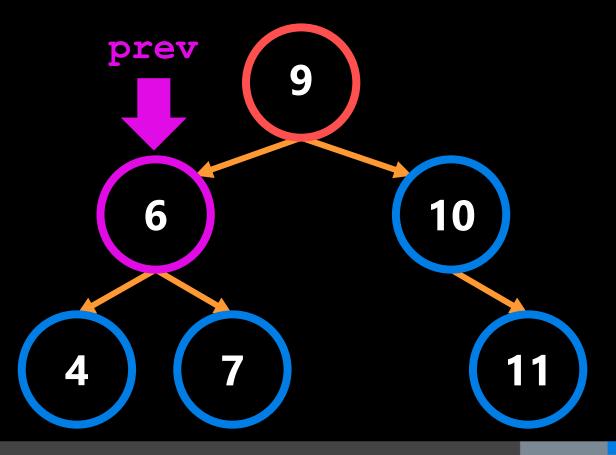


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
   def is_valid(self):
      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
          prev = on
          on = on.right
      return True
```



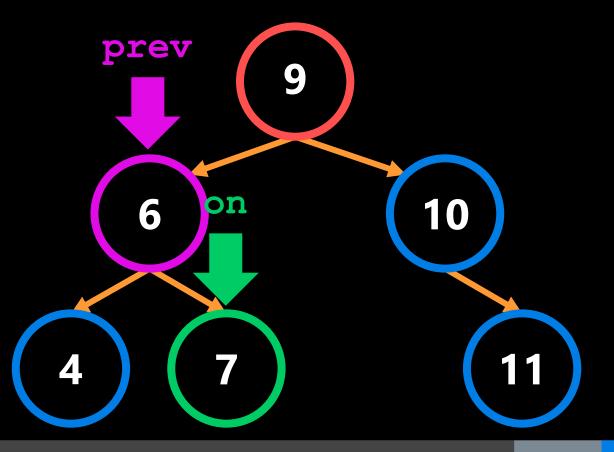


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
   def is_valid(self):
      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
                          Set prev to on.
          prev = on
          on = on.right
      return True
```



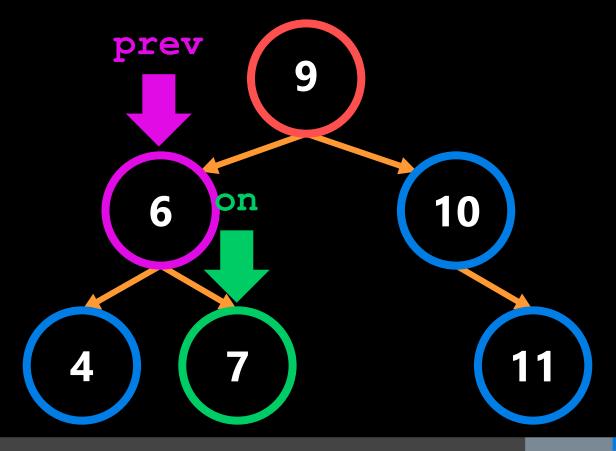


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
   def is_valid(self):
      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
          prev = on
                              Move on to the
          on = on.right
                              right pointer.
      return True
```



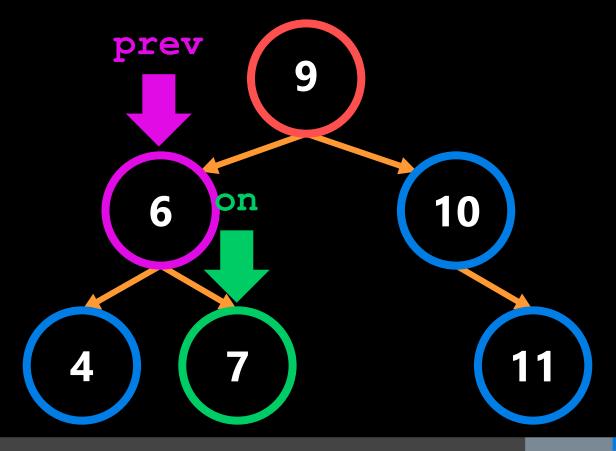


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None:
                                  True
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



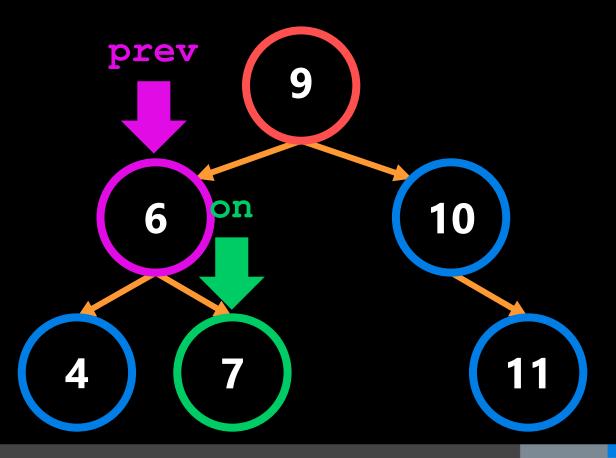


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
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               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



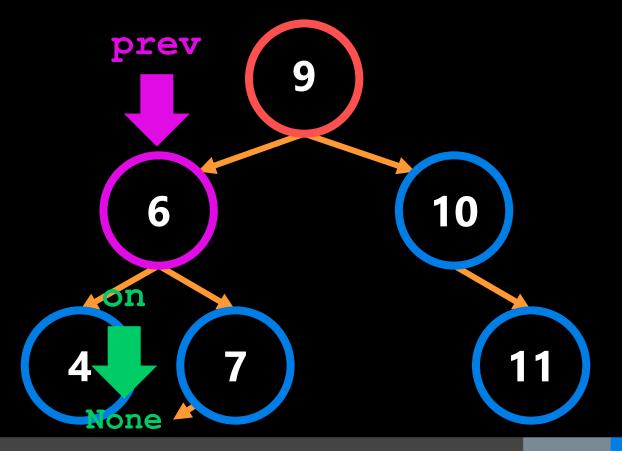


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                                    True
           while on is not None:
                                        Add on to stack.
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



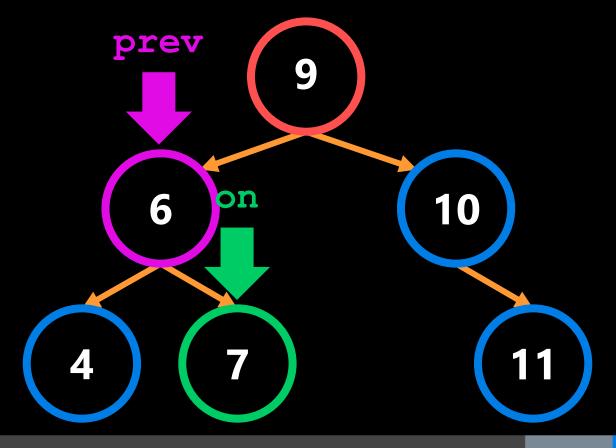


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
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               stack.append(on)
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           on = on.right
       return True
```



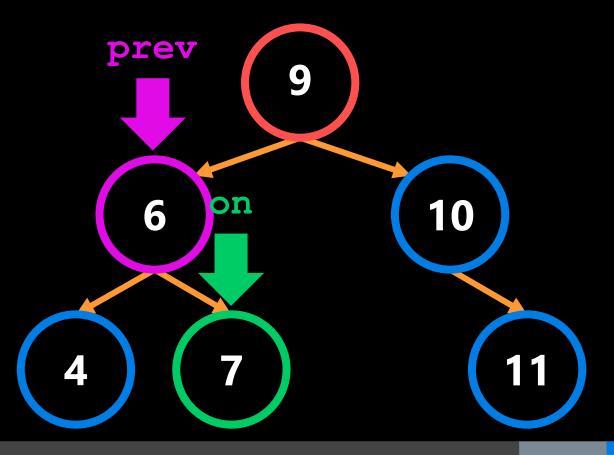


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    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
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       self.root = root
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       on = self.root
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           while on is not None:
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               stack.append(on)
               on = on.left
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       return True
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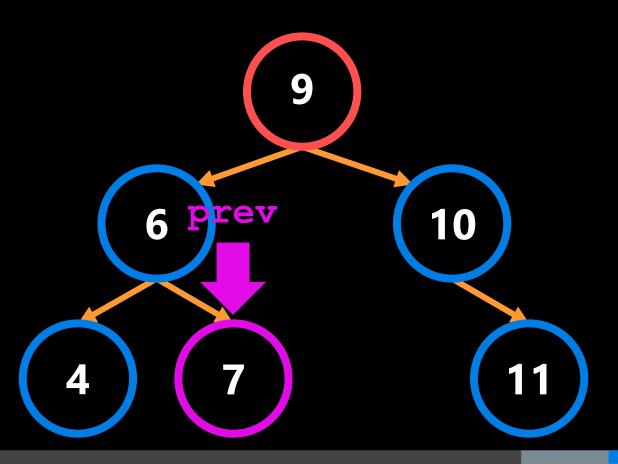


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   """A Node class used by a binary search tree class."""
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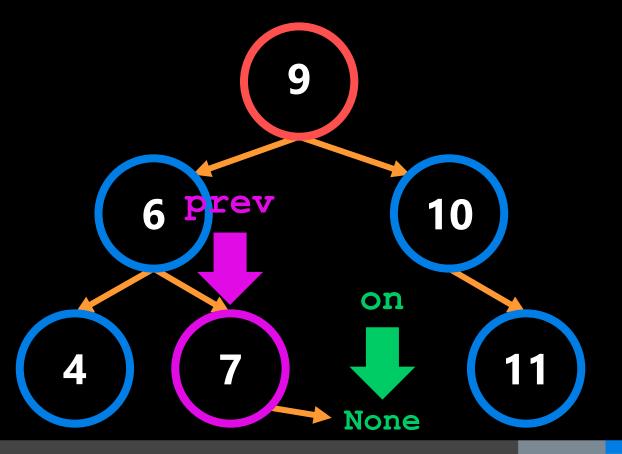


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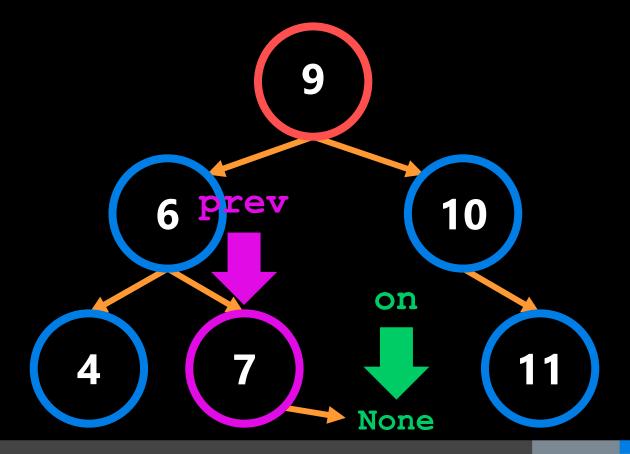


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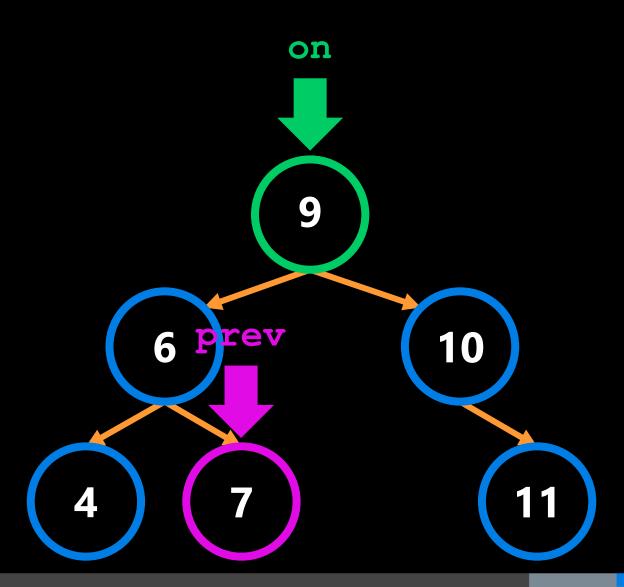


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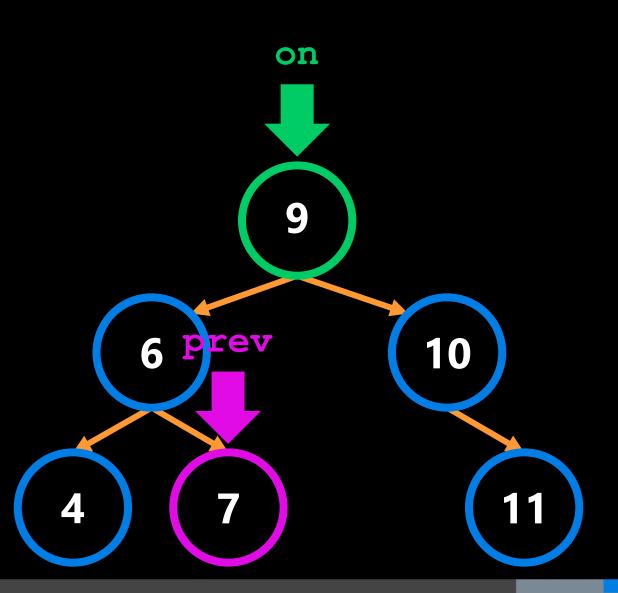


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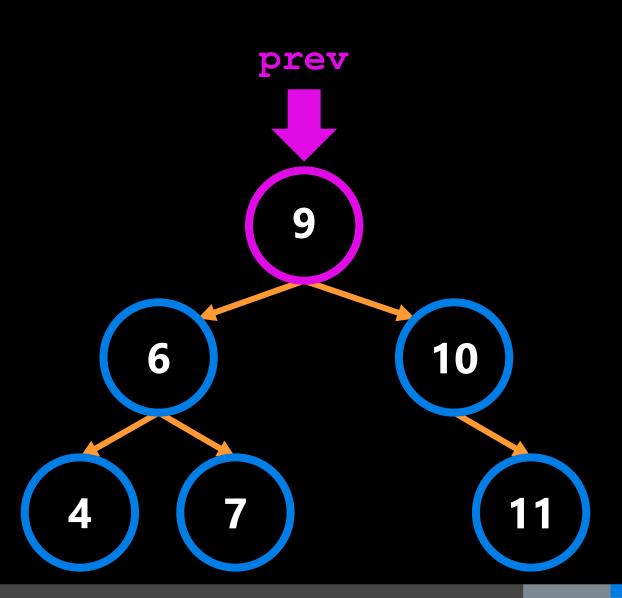


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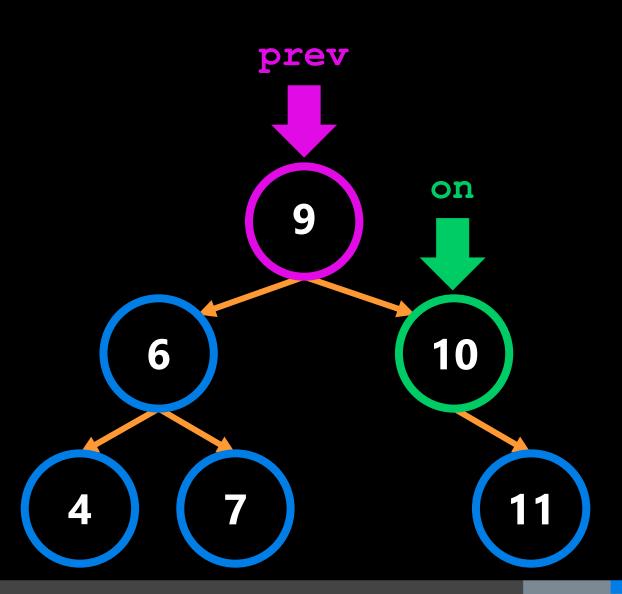


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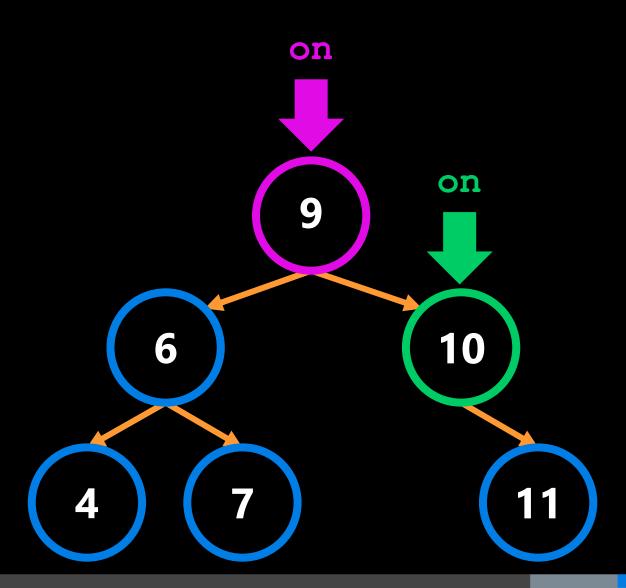


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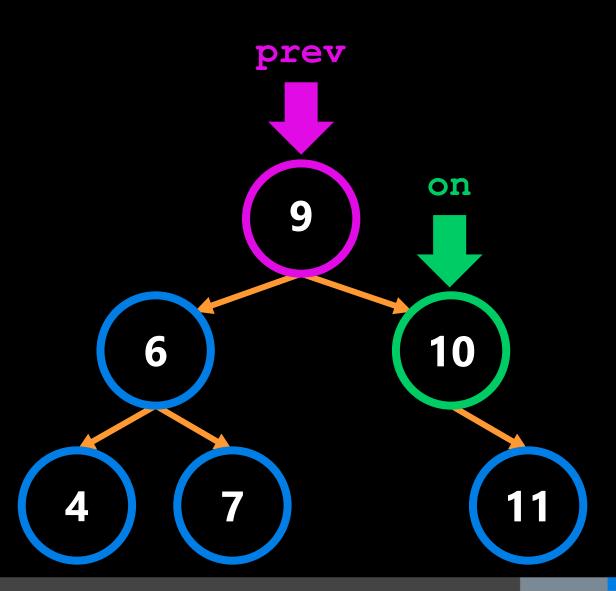


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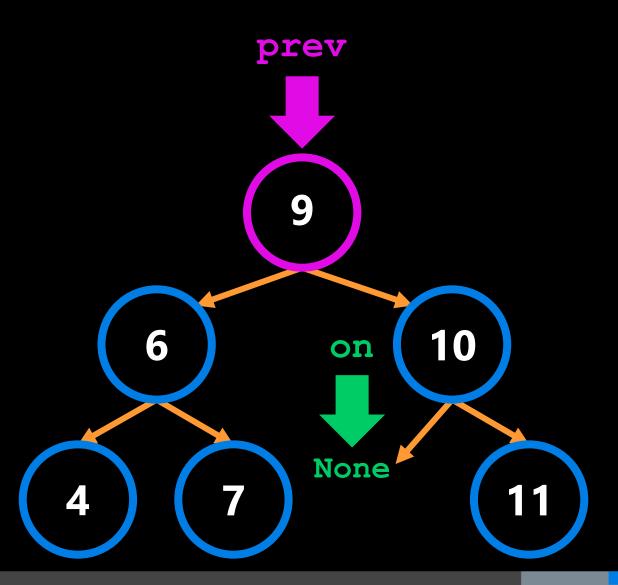


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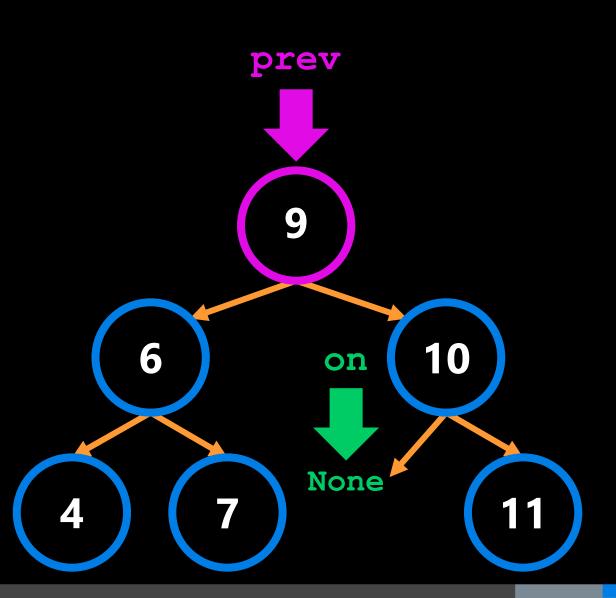


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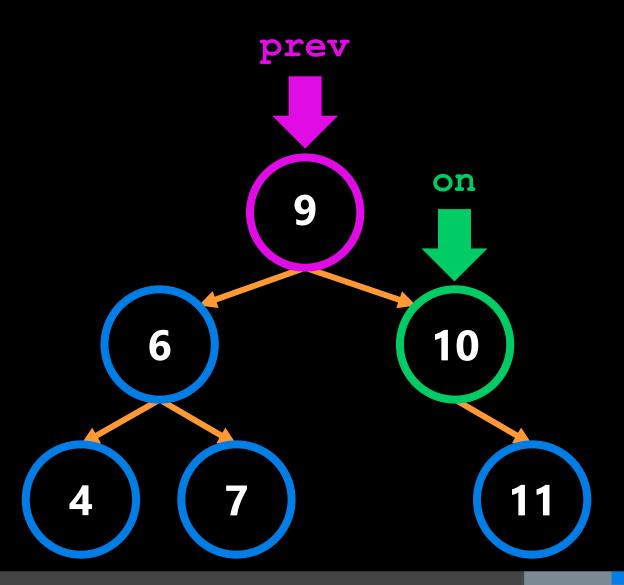


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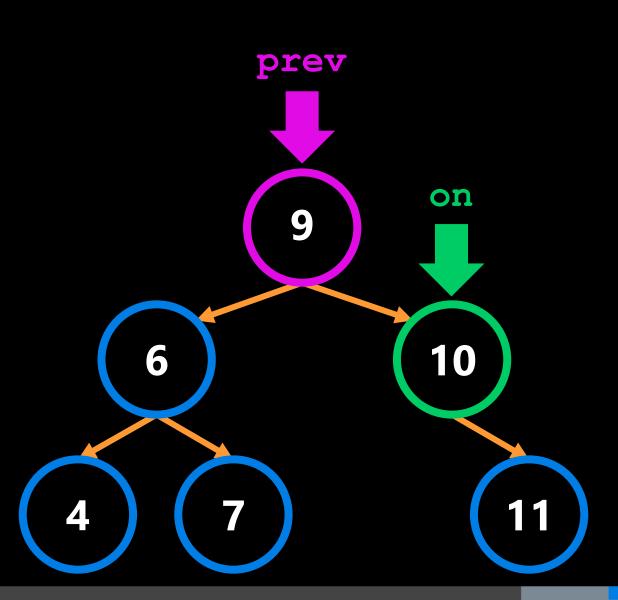


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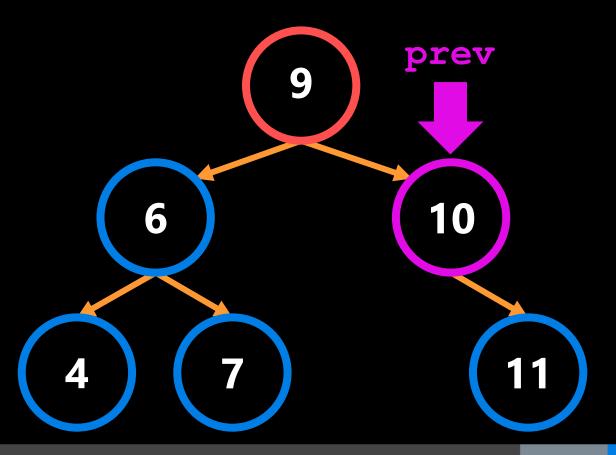


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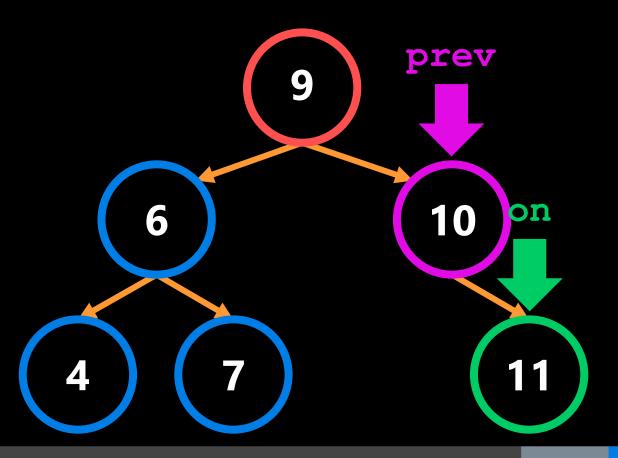


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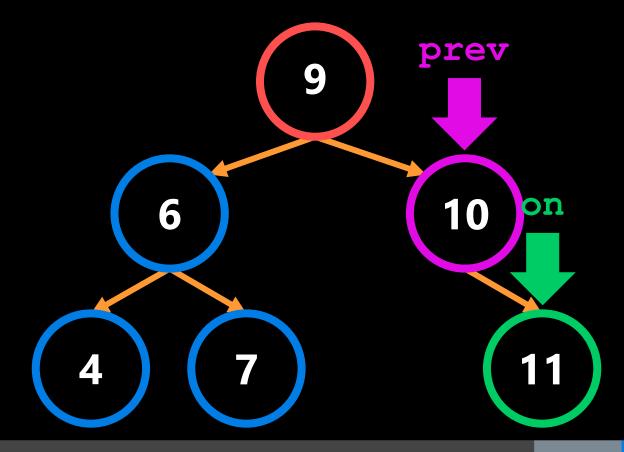


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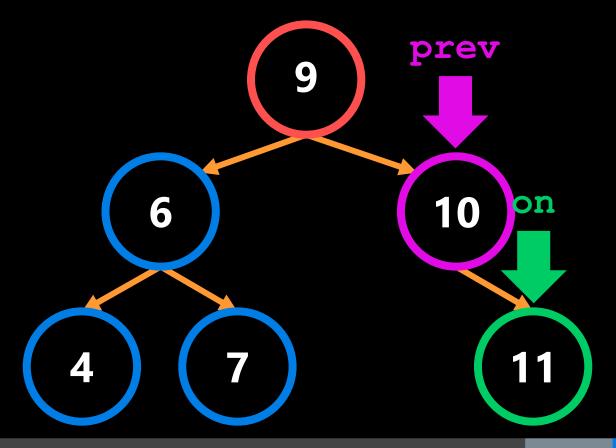


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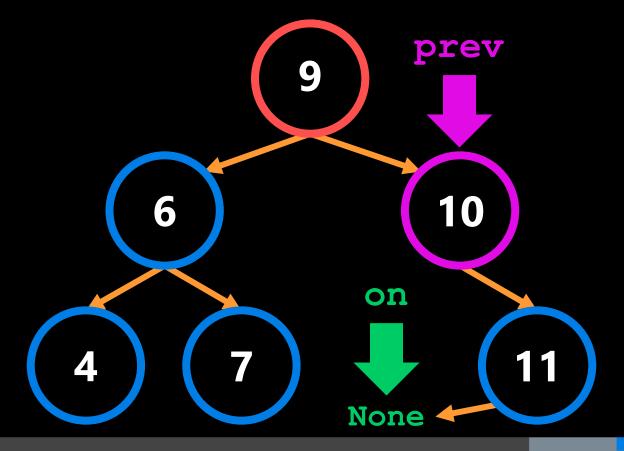


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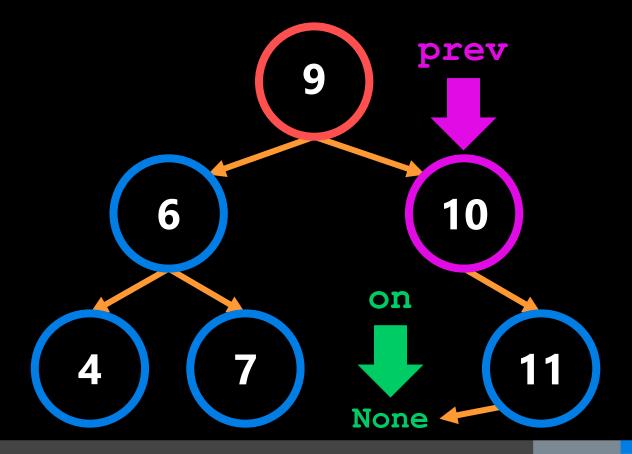


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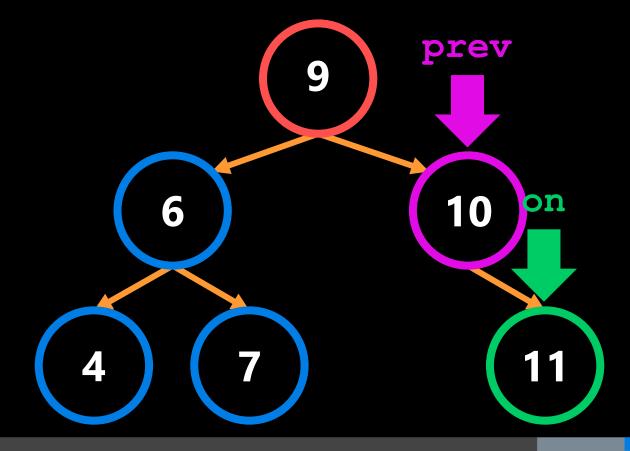


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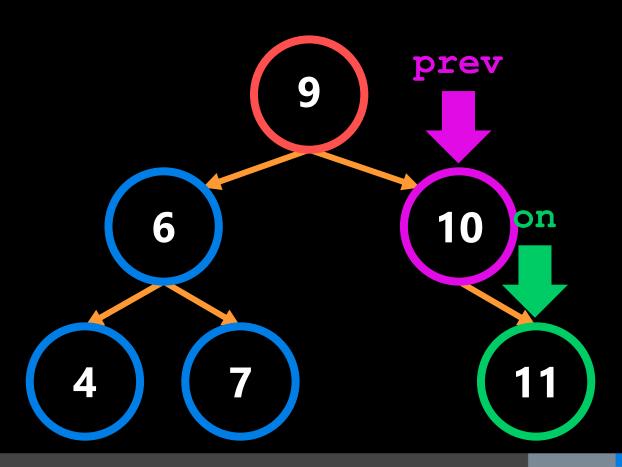


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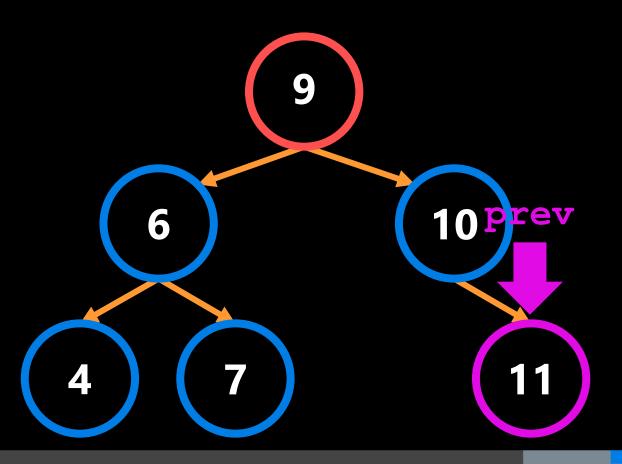


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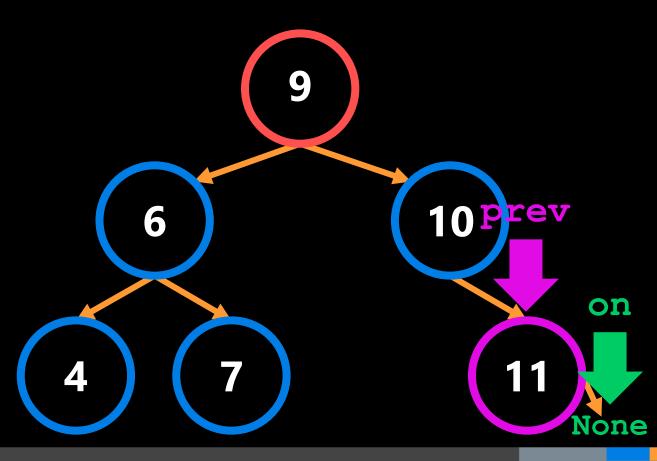


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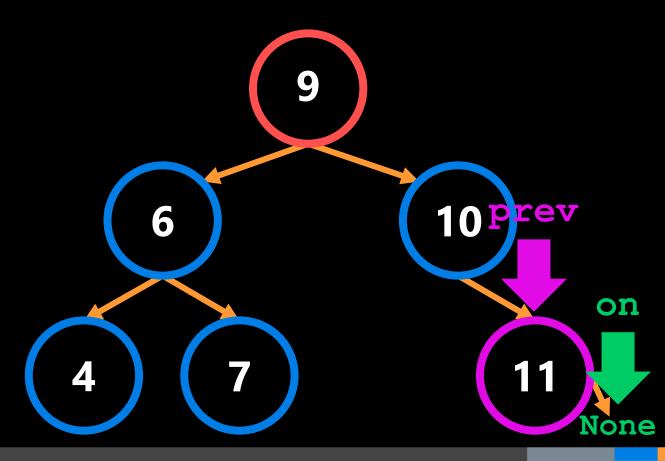


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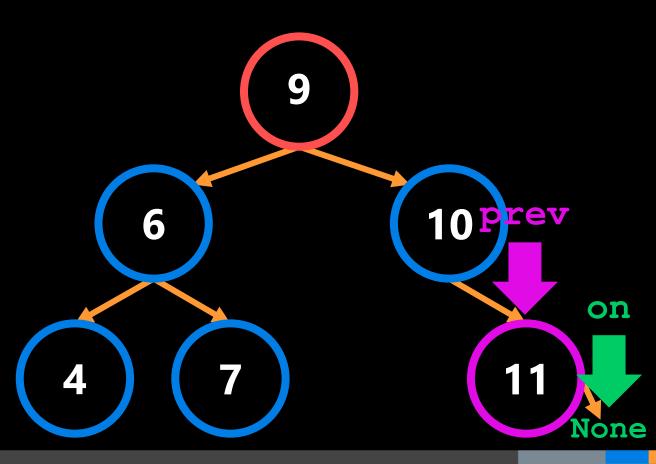
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## This is a Valid Binary Search Tree!



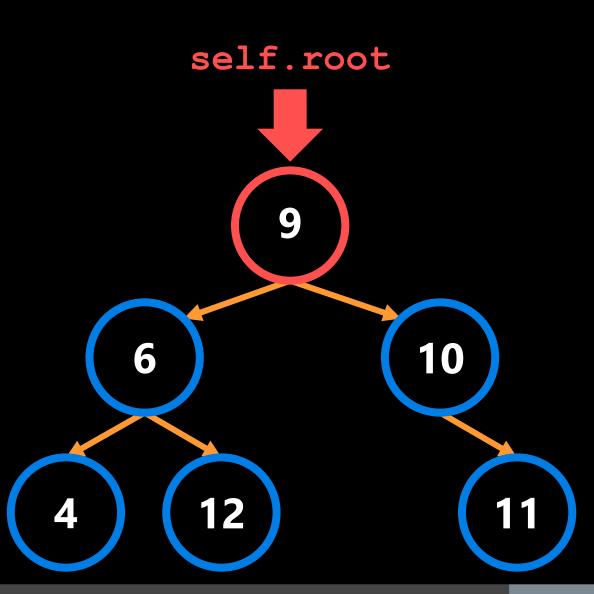


## Let's try with an invalid binary search tree.



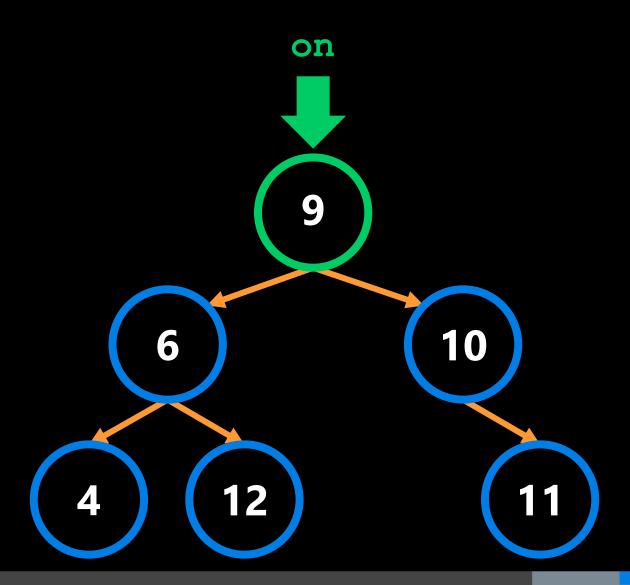
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                return False
            prev = on
           on = on.right
       return True
```

## This is an Invalid Tree



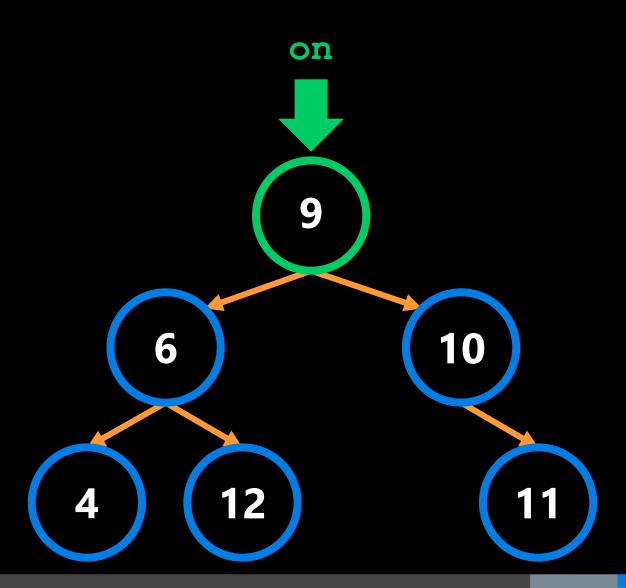


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
   def print_tree(self): ...
   def is_valid(self):
        (self) -> NoneType
        Checks if self.root is a valid binary search tree.
       on = self.root
                                Set on position.
       stack = []
        prev = None
       while len(stack) > 0 or on is not None:
           while on is not None:
                stack.append(on)
                on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
                return False
           prev = on
           on = on.right
       return True
```



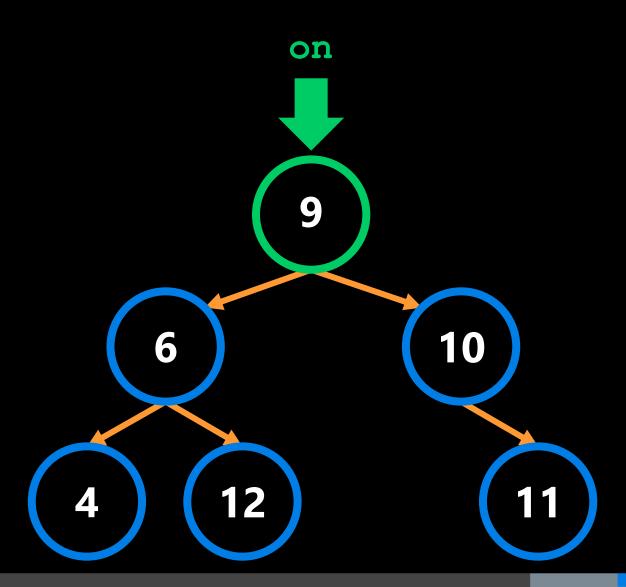


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
                                         stack =
        self.root = root
   def print_tree(self): ...
   def is_valid(self):
        (self) -> NoneType
        Checks if self.root is a valid binary search tree.
       on = self.root
                            Create stack list.
        stack = []
        prev = None
       while len(stack) > 0 or on is not None:
           while on is not None:
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



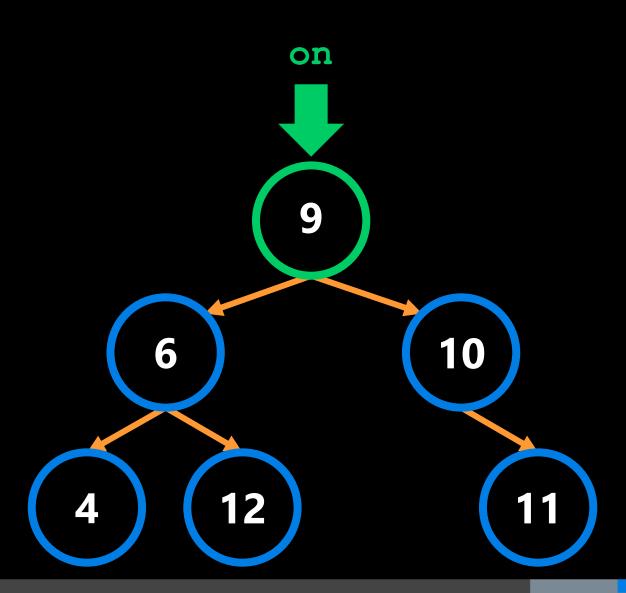


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                         stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
                            Initialize previous node.
       prev = None
       while len(stack) > 0 or on is not None:
           while on is not None:
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



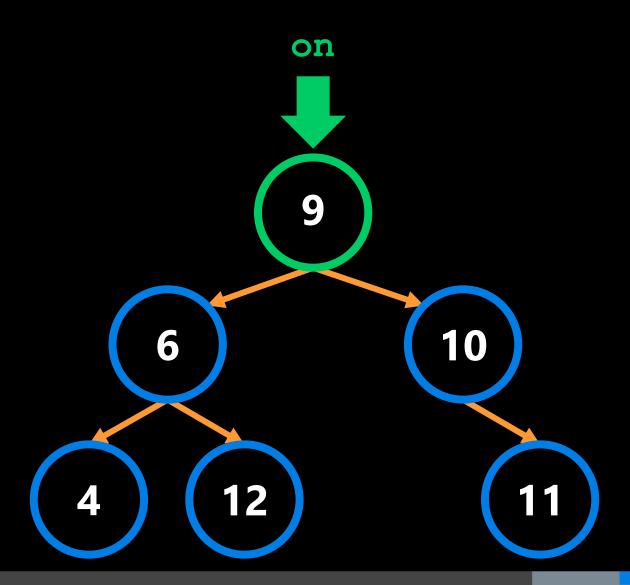


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
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       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None:
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



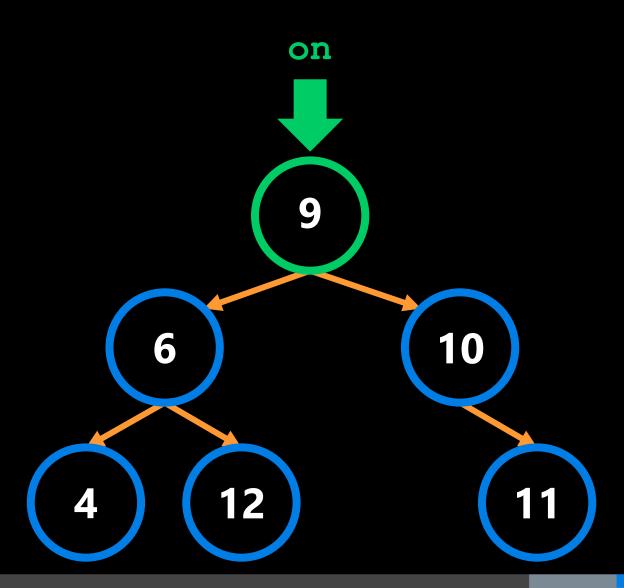


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: <
                                  True
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



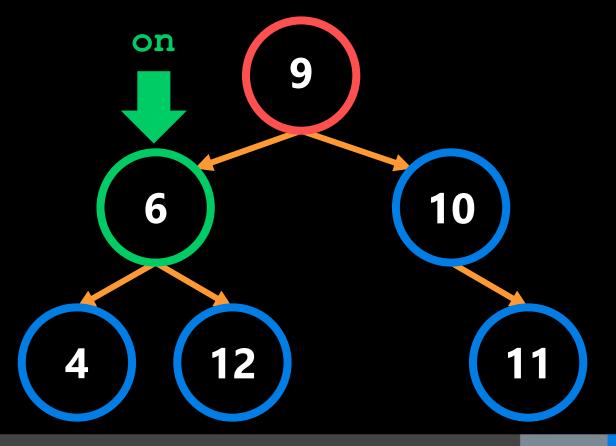


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
                                    True
           while on is not None:
                                        Add on to stack.
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



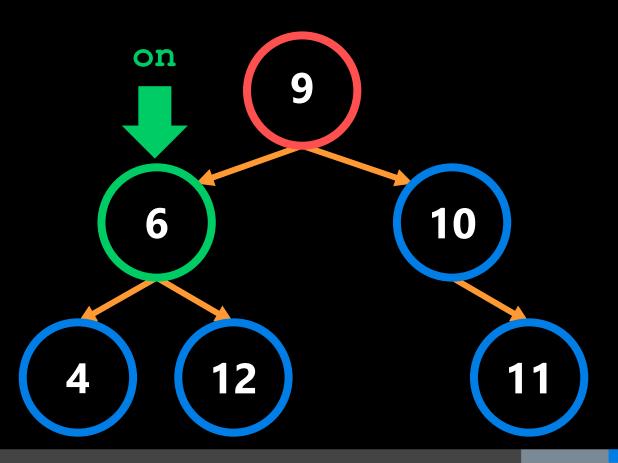


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: True
               stack.append(on)
                                     Move on to left
               on = on.left
                                     node pointer.
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



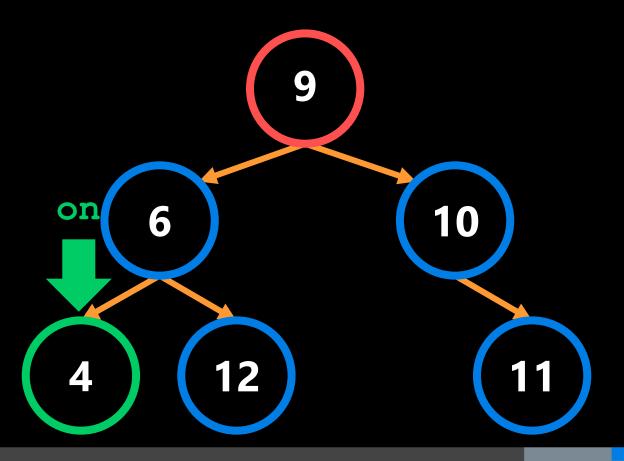


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
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       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
                                    True
           while on is not None:
                                        Add on to stack.
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



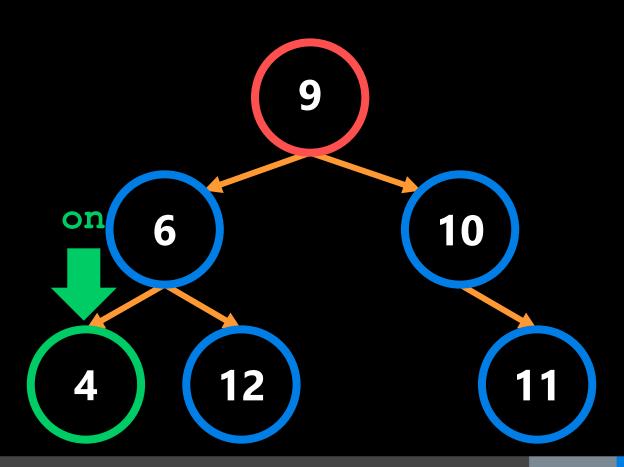


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class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
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       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: True
               stack.append(on)
                                     Move on to left
               on = on.left
                                     node pointer.
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```





```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
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       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
                                    True
           while on is not None:
                                        Add on to stack.
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



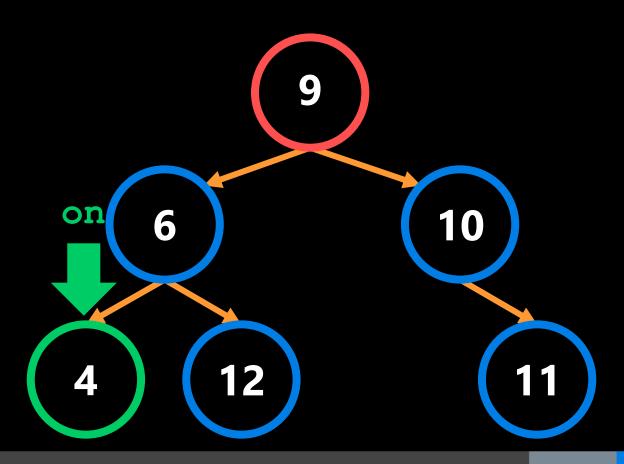


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                       stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
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       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: True
               stack.append(on)
                                    Move on to left
               on = on.left
                                    node pointer.
           on = stack.pop()
                                                               on
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
                                                                                                 12
           prev = on
           on = on.right
                                                             None
       return True
```

```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                       stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
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       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
           on = stack.pop()
                                                                on
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
                                                                                                   12
           prev = on
           on = on.right
                                                             None
       return True
```

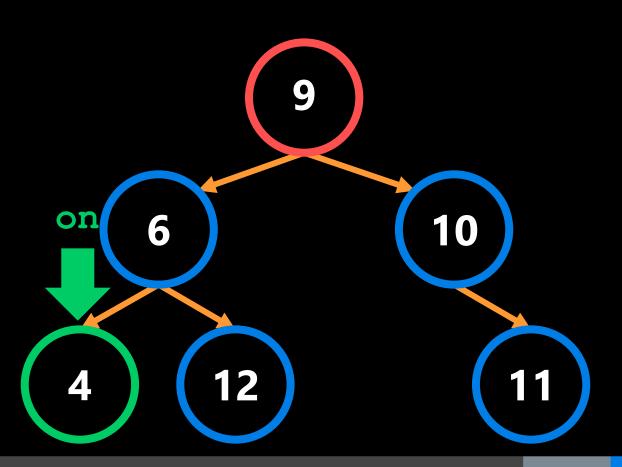


```
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    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
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       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
                                    Set on to left node
                                    in stack.
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



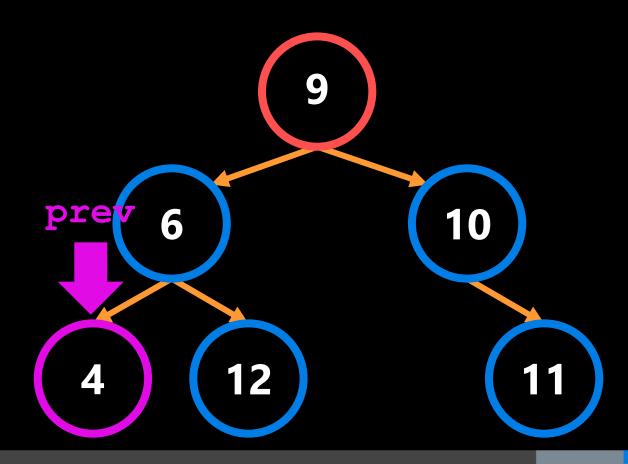


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   """A Node class used by a binary search tree class."""
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      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
   def is_valid(self):
      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
          prev = on
          on = on.right
      return True
```

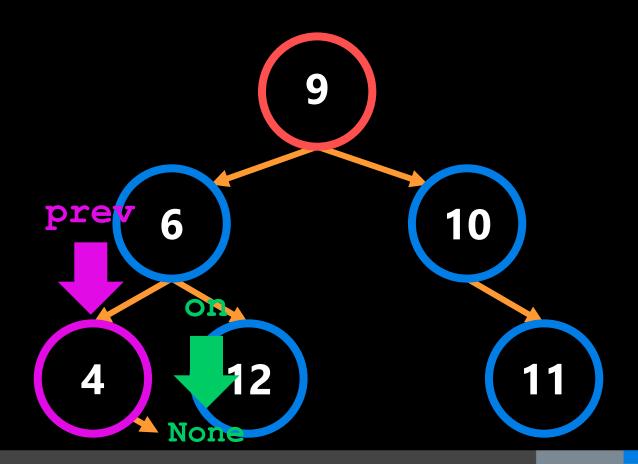




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      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
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      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
                          Set prev to on.
          prev = on
          on = on.right
      return True
```

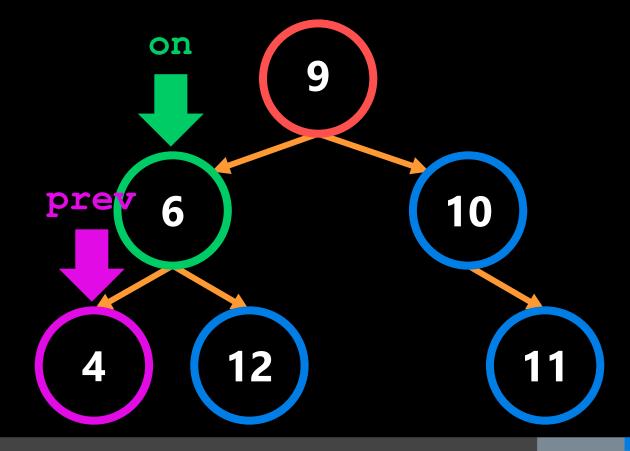


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      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
         on = stack.pop()
          return False
          prev = on
                              Move on to the
          on = on.right
                              right pointer.
      return True
```



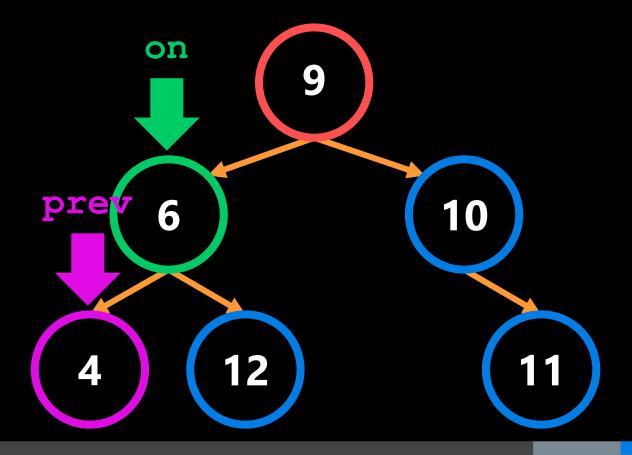


```
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    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
                                    Set on to left node
                                    in stack.
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



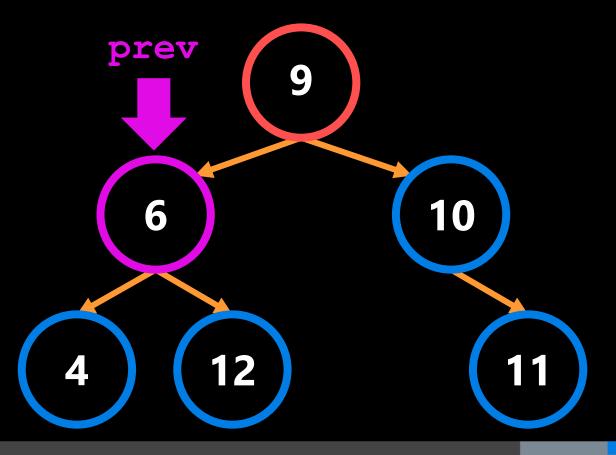


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   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
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   def is_valid(self):
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      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
          prev = on
          on = on.right
      return True
```



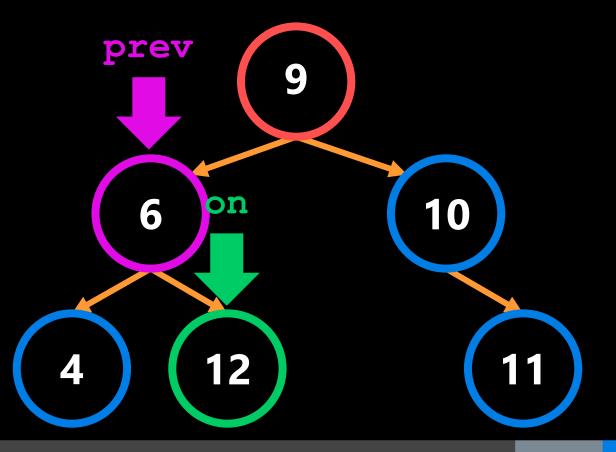


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
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      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
                          Set prev to on.
          prev = on
          on = on.right
      return True
```



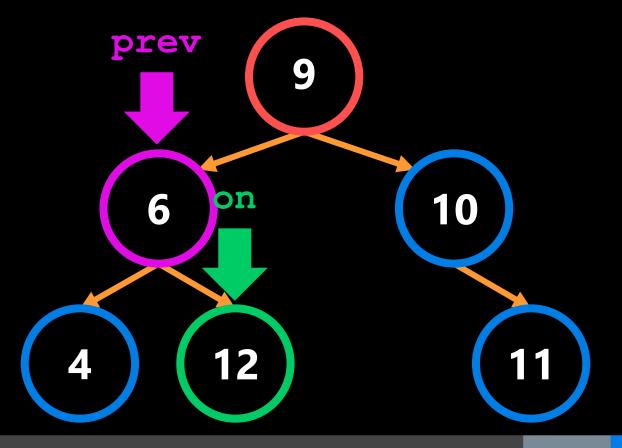


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
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      (self) -> NoneType
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      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None: False
             stack.append(on)
             on = on.left
         on = stack.pop()
          return False
          prev = on
                              Move on to the
          on = on.right
                              right pointer.
      return True
```



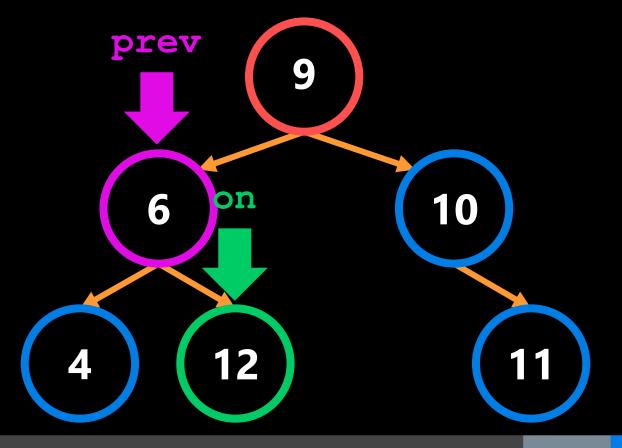


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    """A Node class used by a binary search tree class."""
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       (self) -> NoneType
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               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



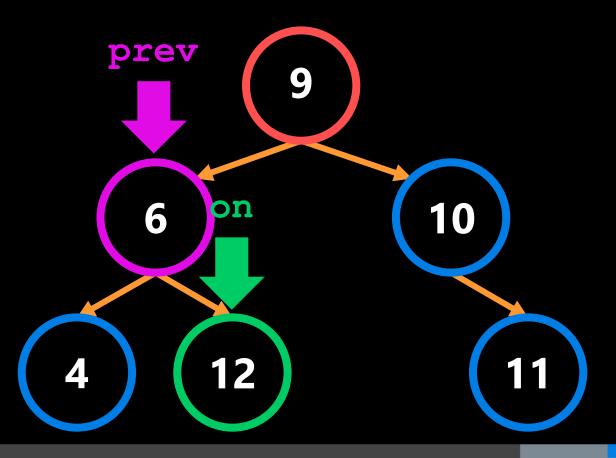


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           while on is not None:
                                  True
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               on = on.left
           on = stack.pop()
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               return False
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           on = on.right
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```

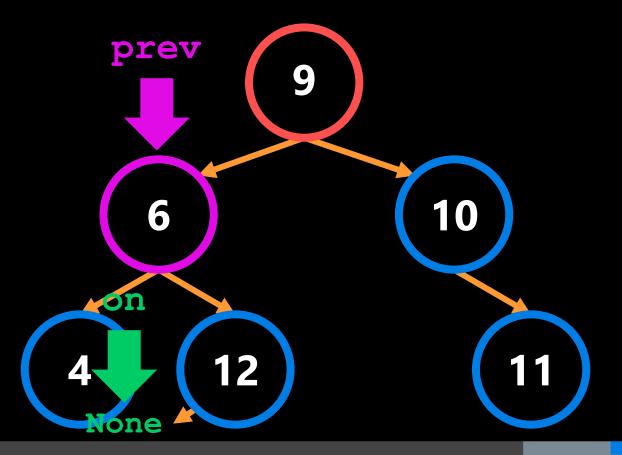




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           while on is not None:
                                        Add on to stack.
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```

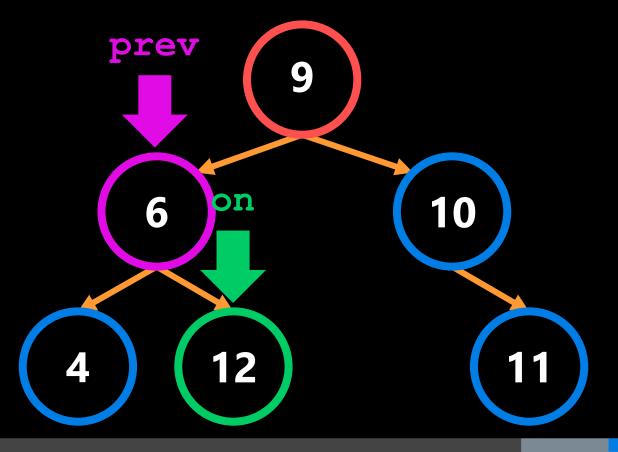


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           while on is not None: True
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               on = on.left
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```



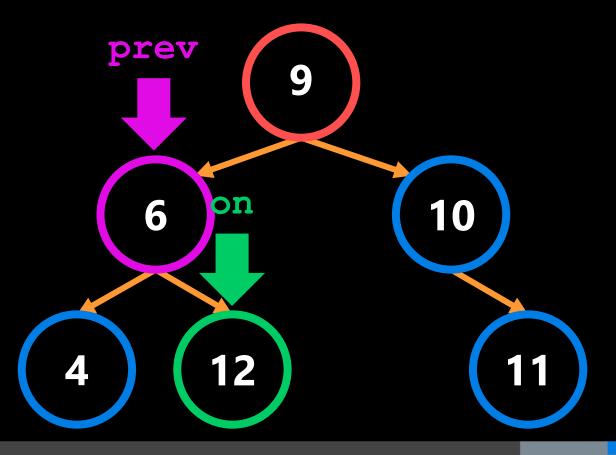


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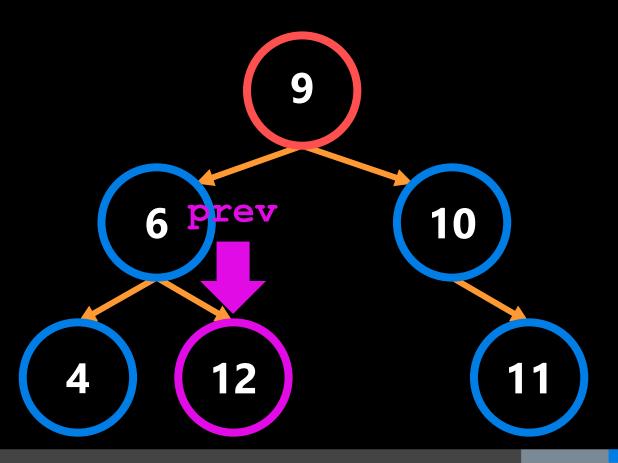


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                              True
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
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          on = on.right
      return True
```



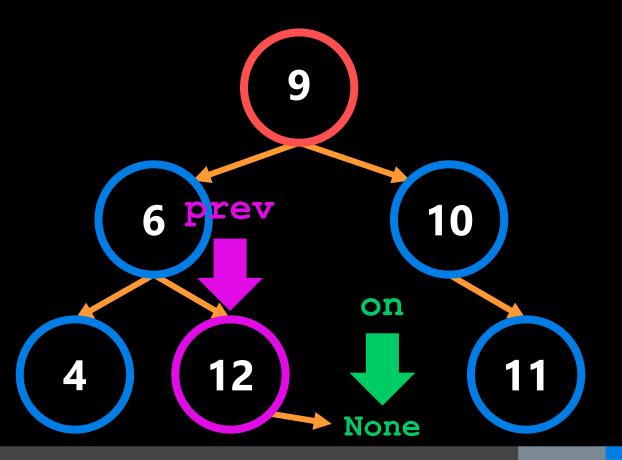


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   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
   def is_valid(self):
      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
                              True
          while on is not None: <
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
                          Set prev to on.
          prev = on
          on = on.right
      return True
```



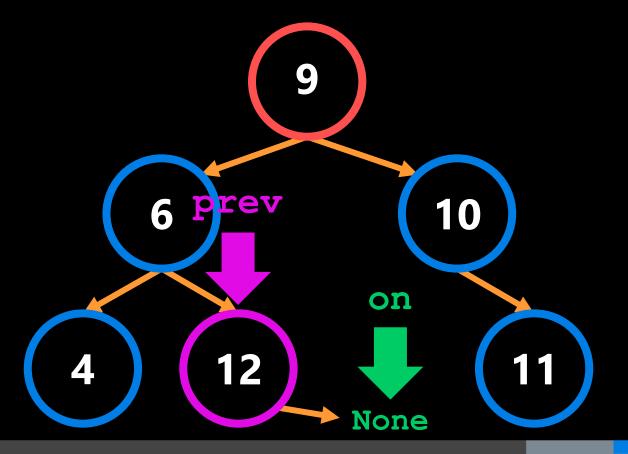


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
      (self) -> NoneType
      Create an empty binary tree.
                                   stack =
      self.root = root
   def print_tree(self): ...
   def is_valid(self):
      (self) -> NoneType
      Checks if self.root is a valid binary search tree.
      on = self.root
      stack = []
      prev = None
      while len(stack) > 0 or on is not None: True
          while on is not None:
                              True
             stack.append(on)
             on = on.left
          on = stack.pop()
          return False
          prev = on
                              Move on to the
          on = on.right
                              right pointer.
      return True
```



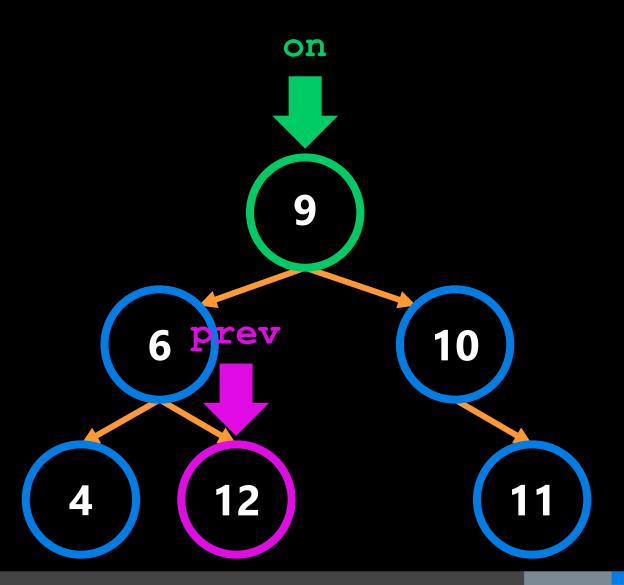


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



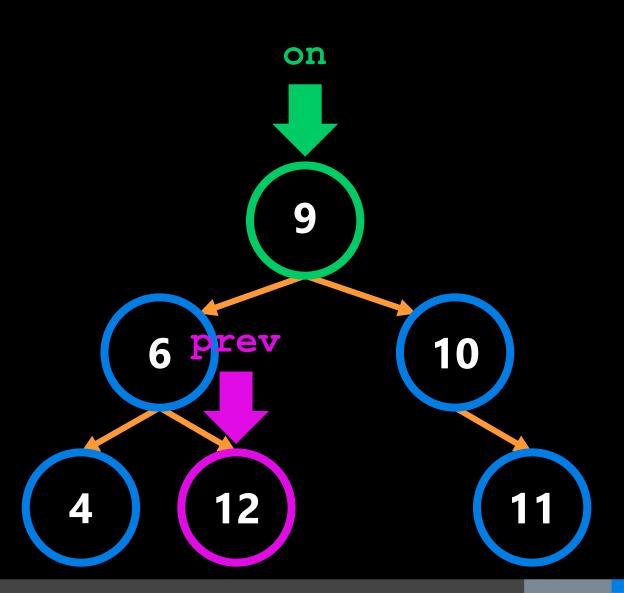


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                        stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
                                    Set on to left node
                                    in stack.
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo:</pre>
               return False
           prev = on
           on = on.right
       return True
```



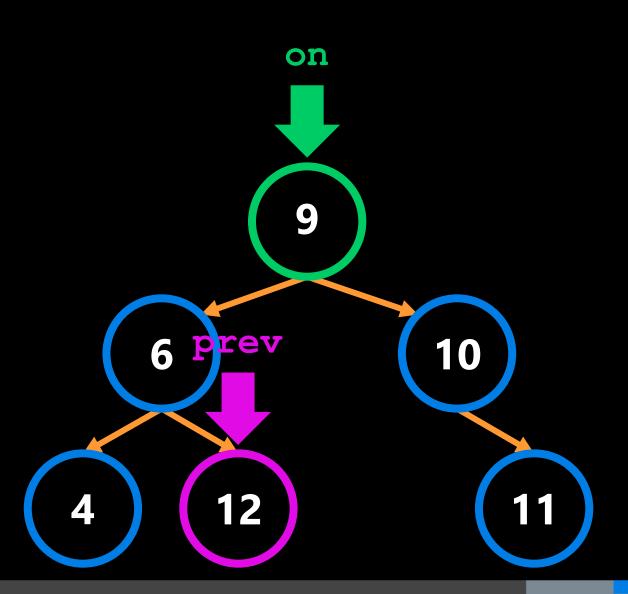


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                       stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo: True
               return False
           prev = on
           on = on.right
       return True
```



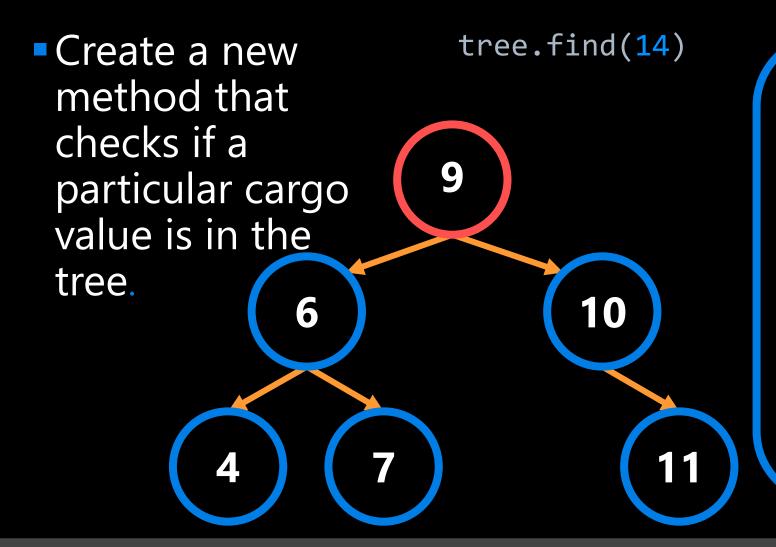


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
                                       stack =
       self.root = root
   def print_tree(self): ...
   def is_valid(self):
       (self) -> NoneType
       Checks if self.root is a valid binary search tree.
       on = self.root
       stack = []
       prev = None
       while len(stack) > 0 or on is not None: True
           while on is not None: False
               stack.append(on)
               on = on.left
           on = stack.pop()
           if prev is not None and on.cargo <= prev.cargo: True
               return False
                                  Return False.
           prev = on
           on = on.right
       return True
```





### **Breakout Session**



# Open your notebook

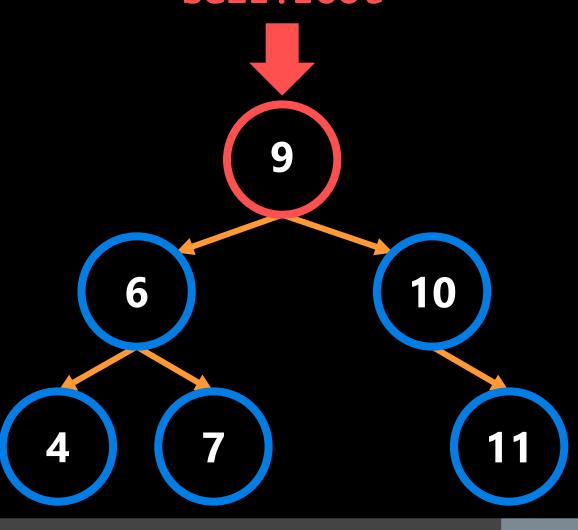
**Click Link:** 

3. Breakout Session



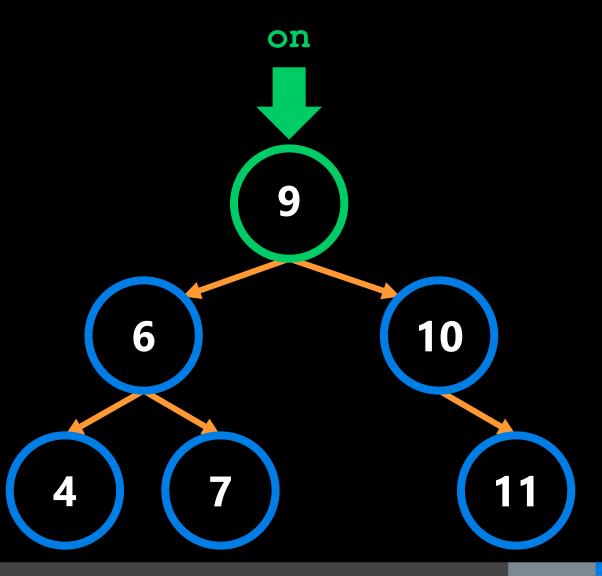
```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
        if not self.is_valid():
            print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
        on = self.root
        while on is not None:
            if cargo > on.cargo:
                on = on.right
            elif cargo < on.cargo:</pre>
                on = on.left
            else:
                return True
        return False
```

#### self.root



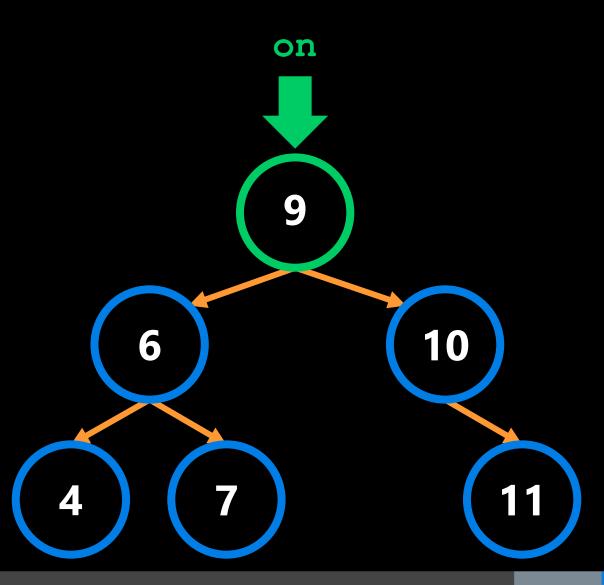


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
                                 Set on position.
       on = self.root
       while on is not None:
           if cargo > on.cargo:
                on = on.right
            elif cargo < on.cargo:</pre>
                on = on.left
            else:
                return True
        return False
```



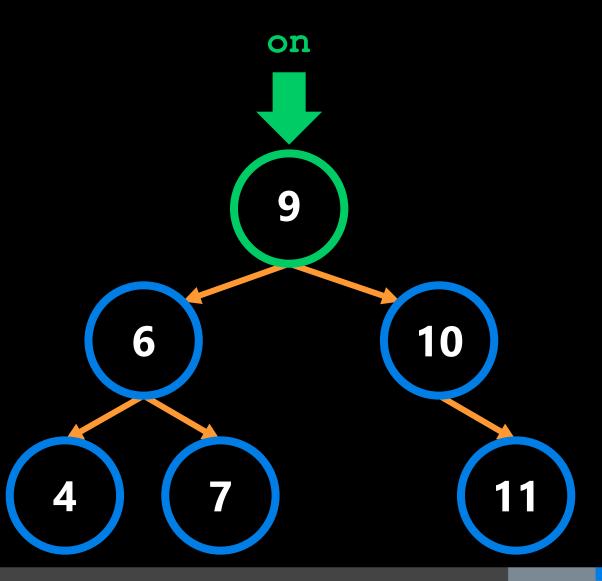


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                                 True
           if cargo > on.cargo:
               on = on.right
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
                return True
        return False
```



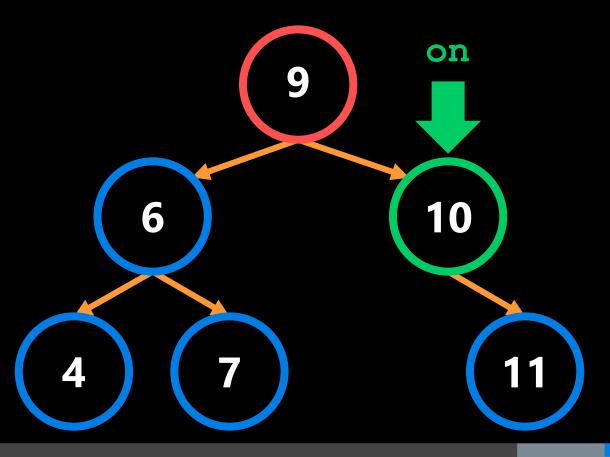


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                                True
           if cargo > on.cargo: True (14 > 9)
               on = on.right
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
               return True
       return False
```



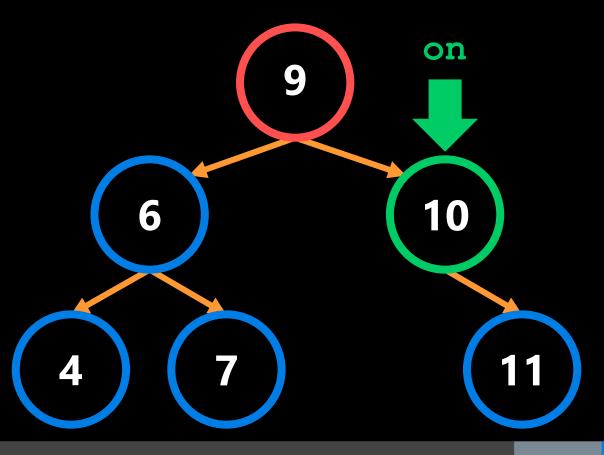


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None: <
                                 True
                                    True (14 > 9)
           if cargo > on.cargo:
                                      Move on to
               on = on.right
                                      the right.
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
               return True
       return False
```



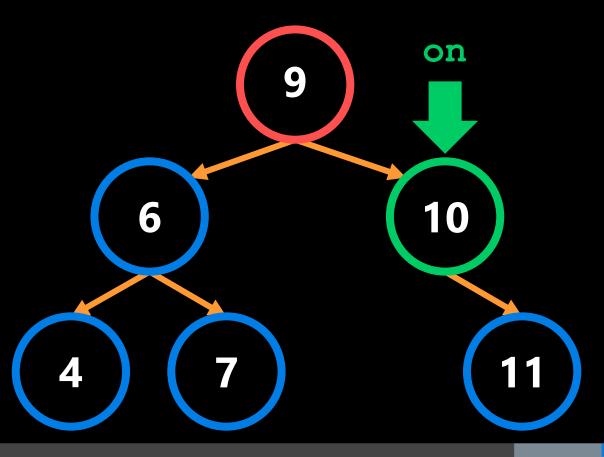


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                                 True
           if cargo > on.cargo:
               on = on.right
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
                return True
        return False
```



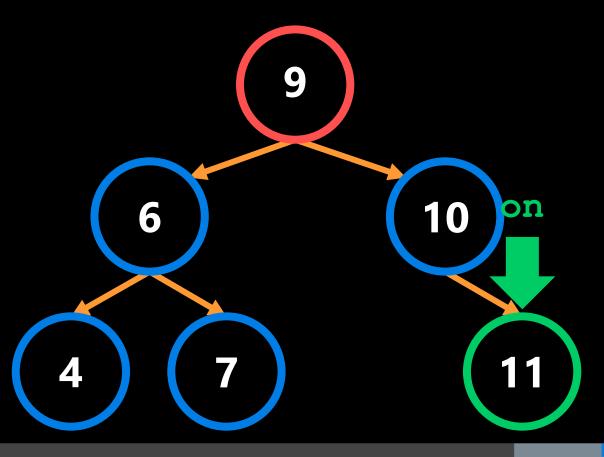


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                                 True
           if cargo > on.cargo: True (14 > 10)
               on = on.right
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
               return True
       return False
```



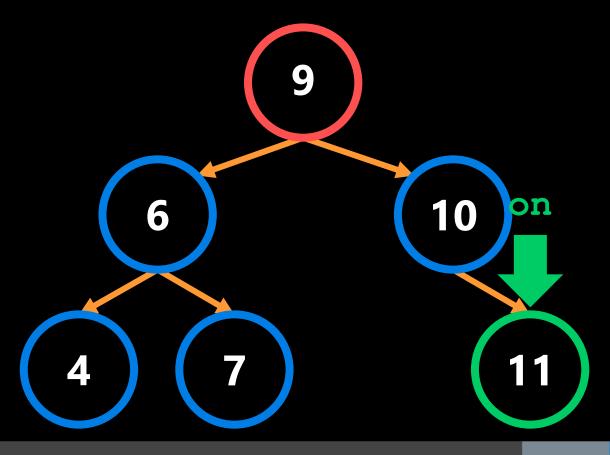


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None: <
                                 True
                                    True (14 > 10)
           if cargo > on.cargo:
                                      Move on to
               on = on.right
                                      the right.
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
               return True
       return False
```



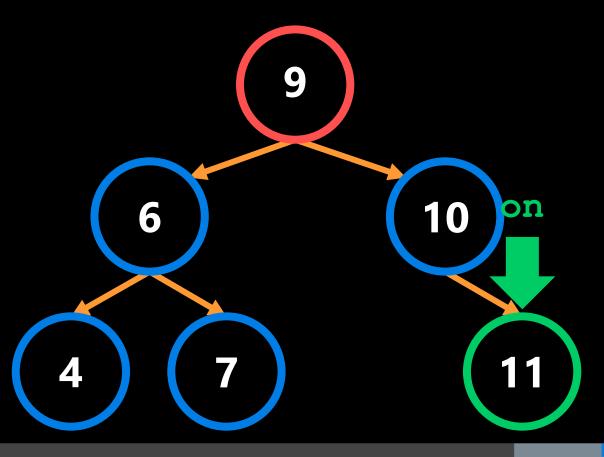


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                                 True
           if cargo > on.cargo:
               on = on.right
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
                return True
        return False
```



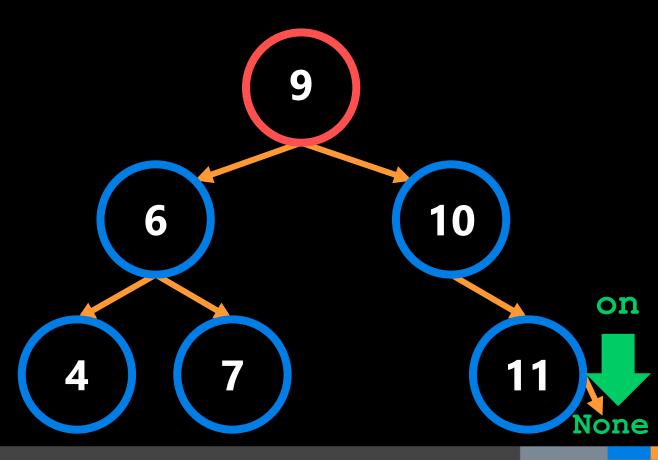


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                                 True
           if cargo > on.cargo: True (14 > 11)
               on = on.right
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
               return True
       return False
```



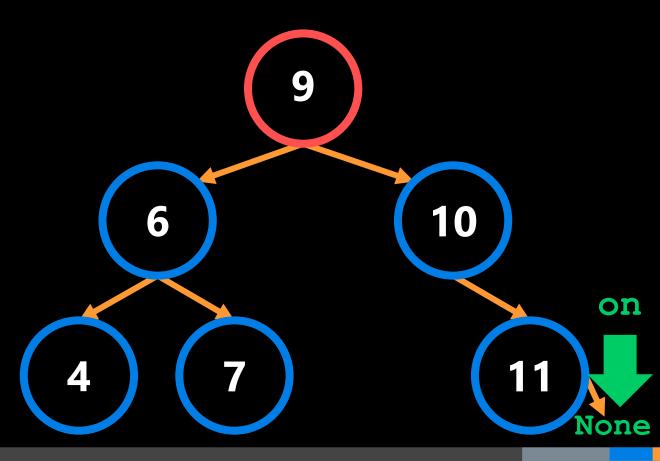


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None: <
                                 True
                                   True (14 > 11)
           if cargo > on.cargo:
                                      Move on to
               on = on.right
                                      the right.
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
               return True
       return False
```



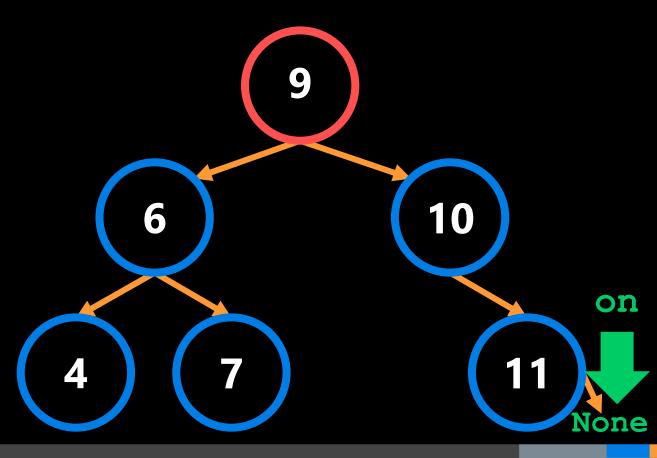


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
       on = self.root
       while on is not None: Talse
           if cargo > on.cargo:
               on = on.right
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
                return True
        return False
```





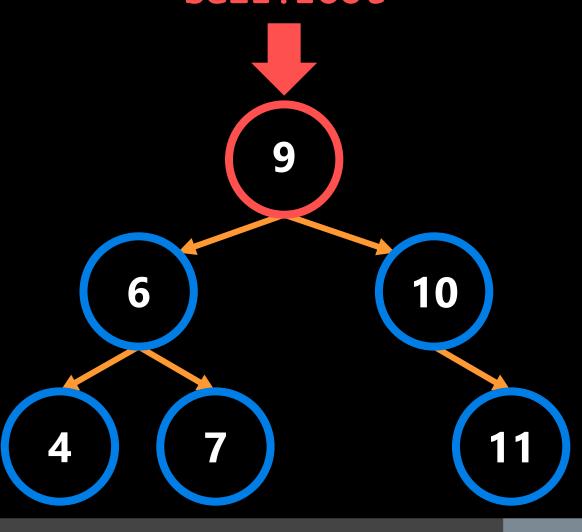
```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
           if cargo > on.cargo:
                on = on.right
            elif cargo < on.cargo:</pre>
                on = on.left
            else:
                return True
                               Didn't find the value.
        return False
```





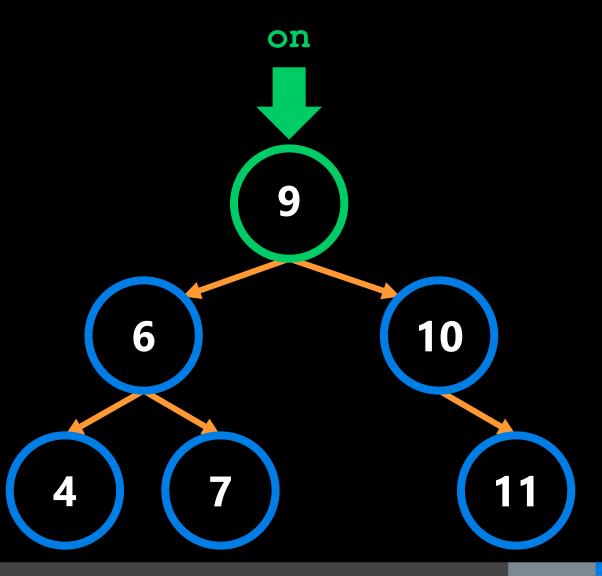
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    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
        if not self.is_valid():
            print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
        on = self.root
        while on is not None:
            if cargo > on.cargo:
                on = on.right
            elif cargo < on.cargo:</pre>
                on = on.left
            else:
                return True
        return False
```

#### self.root



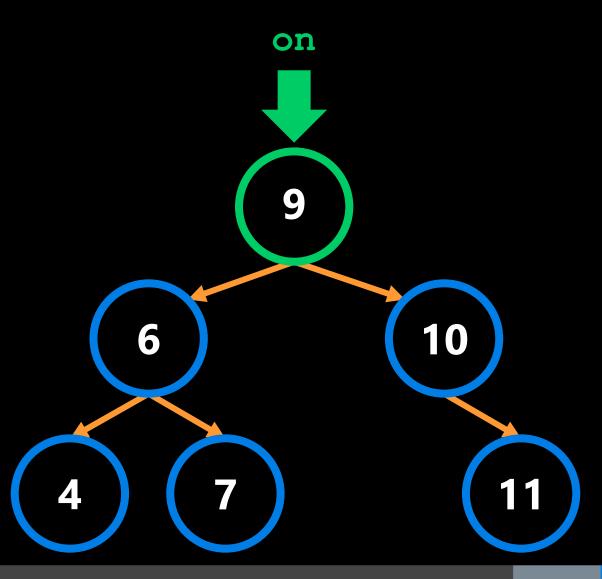


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class BinarySearchTree:
    """A Node class used by a binary search tree class."""
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        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
                                 Set on position.
       on = self.root
       while on is not None:
           if cargo > on.cargo:
                on = on.right
            elif cargo < on.cargo:</pre>
                on = on.left
            else:
                return True
        return False
```



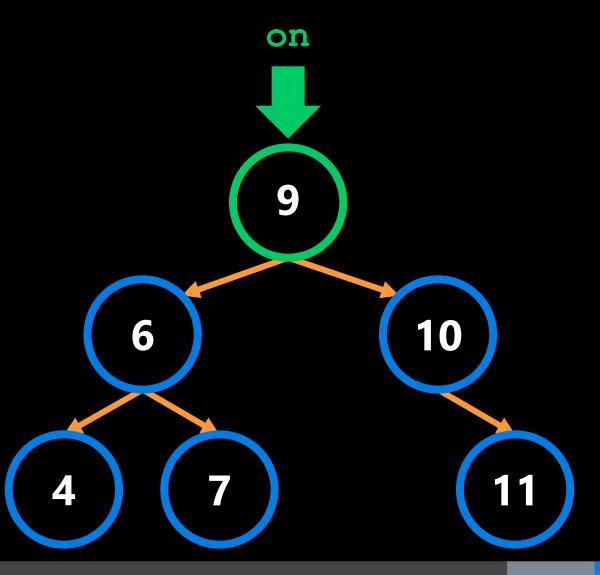


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                                 True
           if cargo > on.cargo:
               on = on.right
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
                return True
        return False
```



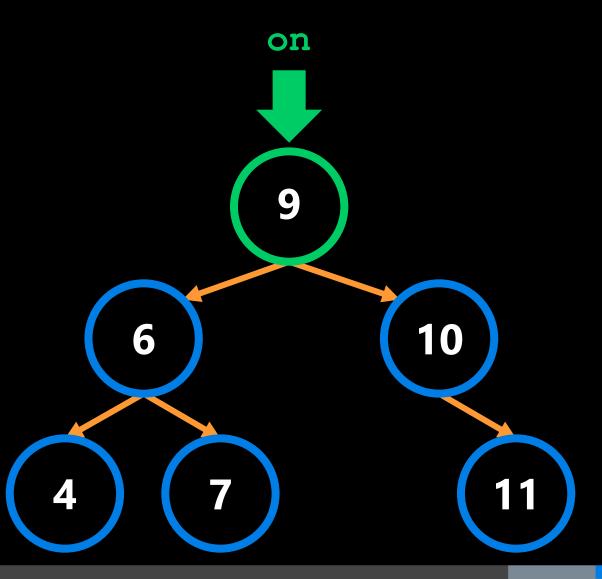


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
          print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None: True
          on = on.right
          elif cargo < on.cargo:</pre>
              on = on.left
          else:
              return True
       return False
```





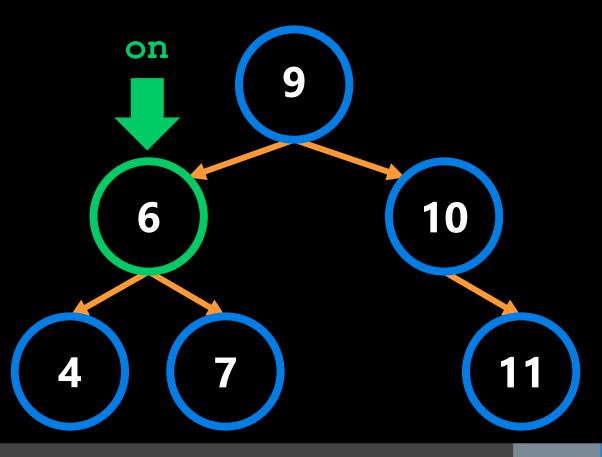
```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
      if not self.is_valid():
          print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
      on = self.root
      while on is not None:
                             True
          on = on.right
          elif cargo < on.cargo: True (4 < 9)
              on = on.left
          else:
              return True
       return False
```





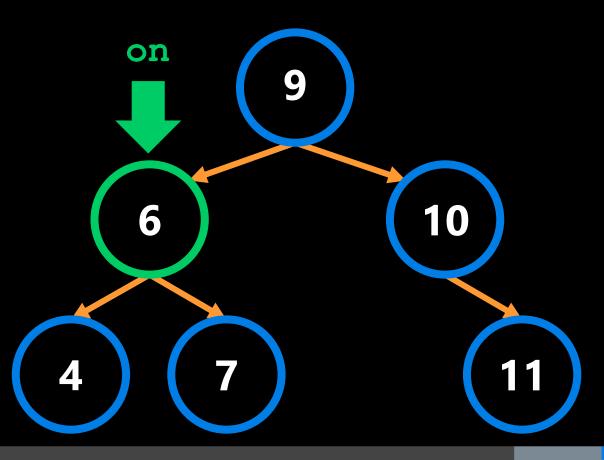
```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
          print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                              True
          on = on.right
                                 True (4 < 9)

Move on to
          elif cargo < on.cargo: <</pre>
              on = on.left
                                   the left.
          else:
              return True
       return False
```



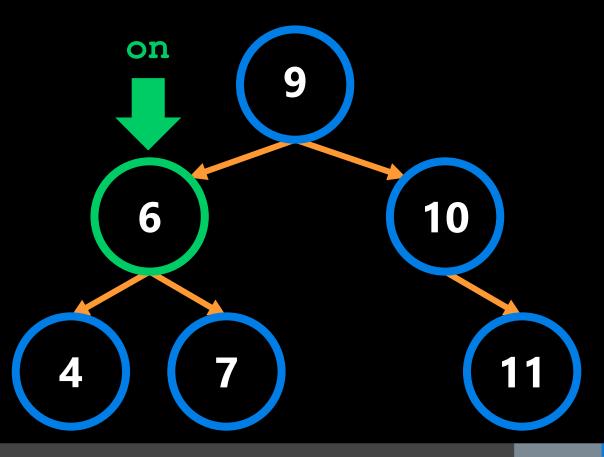


```
class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
        (self) -> NoneType
        Create an empty binary tree.
        self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
        (self, number) -> bool
        Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                                 True
           if cargo > on.cargo:
               on = on.right
           elif cargo < on.cargo:</pre>
               on = on.left
           else:
                return True
        return False
```



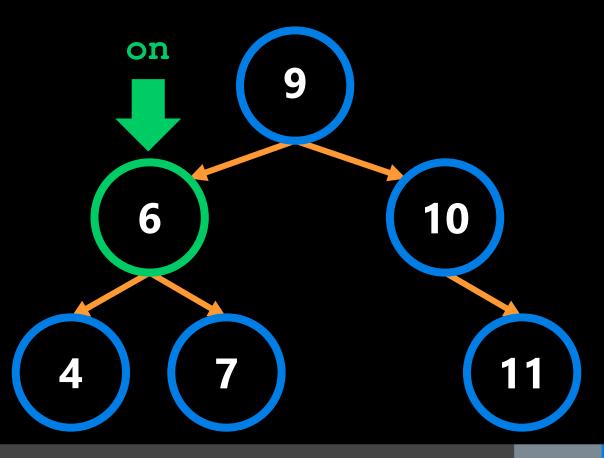


```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
          print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None: True
          on = on.right
          elif cargo < on.cargo:</pre>
              on = on.left
          else:
              return True
       return False
```



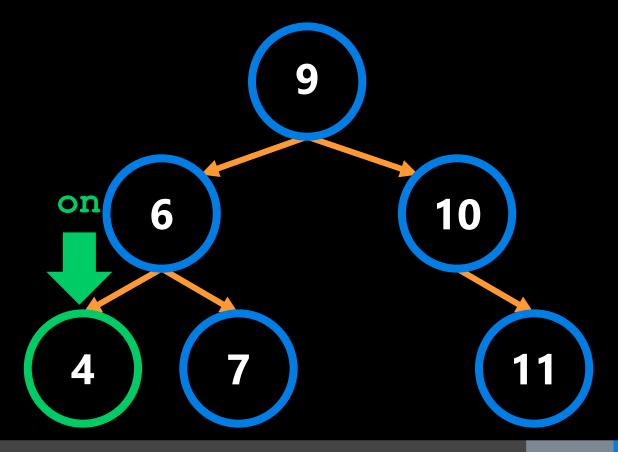


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class BinarySearchTree:
    """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
       self.root = root
       if not self.is_valid():
           print('This is not a valid binary search tree.')
   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None:
                               True
           if cargo > on.cargo: False (4 !> 6)
               on = on.right
           elif cargo < on.cargo: True (4 < 6)
               on = on.left
           else:
               return True
       return False
```



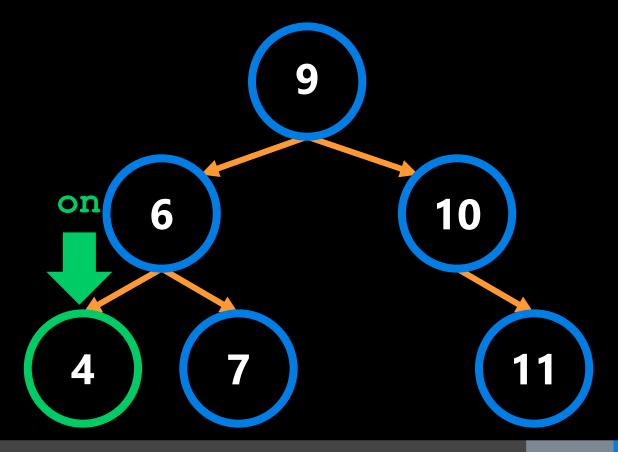


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Move on to
           elif cargo < on.cargo: <</pre>
               on = on.left
                                      the left.
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       return False
```



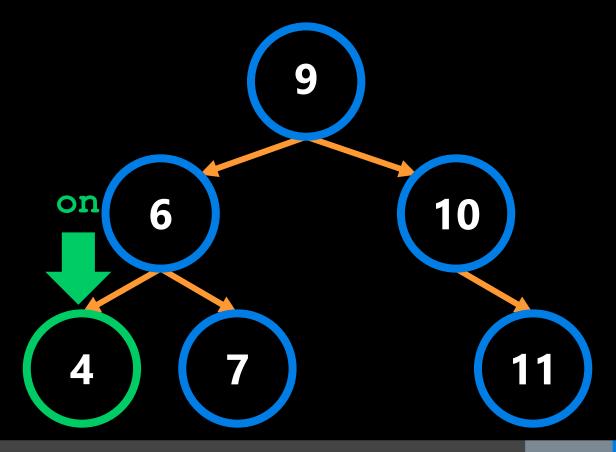


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           else:
                return True
        return False
```



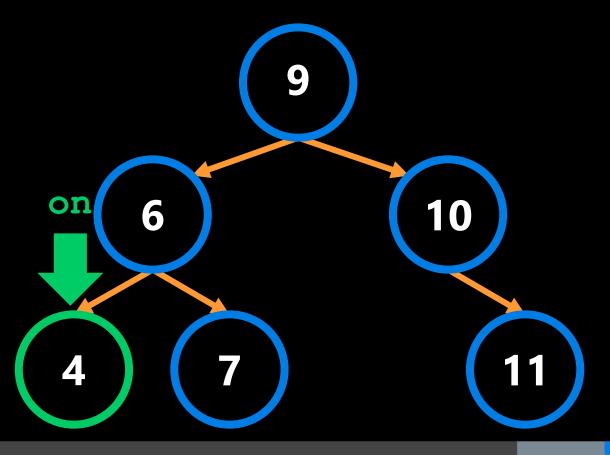


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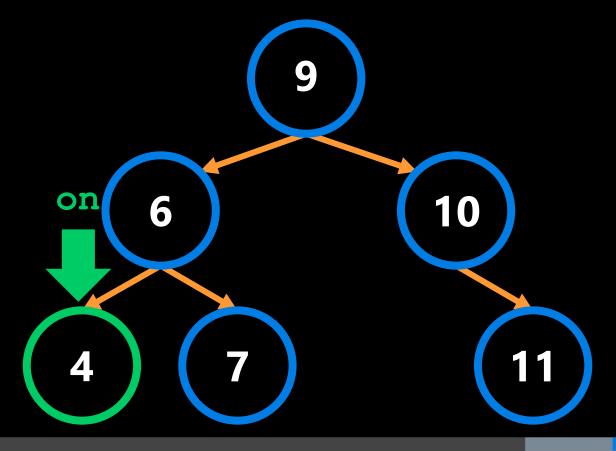


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   def print_tree(self): ...
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   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
      on = self.root
      while on is not None:
                             True
          on = on.right
          elif cargo < on.cargo: False (4 !< 4)
             on = on.left
          else:
              return True
       return False
```





```
class BinarySearchTree:
   """A Node class used by a binary search tree class."""
   def __init__(self, root=None):
       (self) -> NoneType
       Create an empty binary tree.
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   def print_tree(self): ...
   def is_valid(self): ...
   def find(self, cargo):
       (self, number) -> bool
       Checks if cargo value is in the tree.
       on = self.root
       while on is not None: <
                             True
          on = on.right
          elif cargo < on.cargo: False (4 !< 4)
              on = on.left
          else:
                                  Value is in the tree.
              return True
       return False
```



## **APS106**



## binary search trees.

**Week 12** Lecture 2 (12.2)