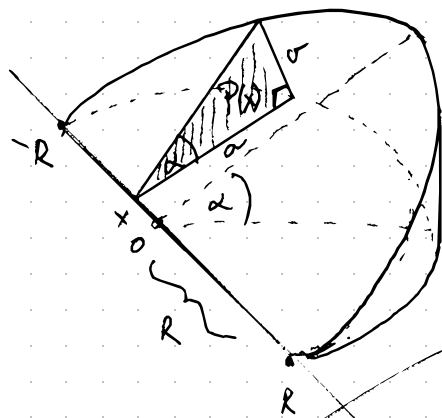
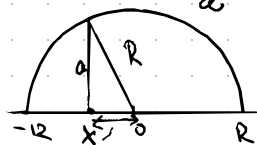


Primer:



TOČRT
odredimo
 a



$$V = \int_{-R}^R P(x) dx$$

$$v = ?$$

$$\operatorname{tg} \alpha = \frac{v}{a}$$

\Leftarrow

$$R^2 = a^2 + x^2$$

$$a = \sqrt{R^2 - x^2}$$

$$v = \operatorname{tg} \alpha \cdot a = \operatorname{tg} \alpha \cdot \sqrt{R^2 - x^2}$$

$$P(x) = \frac{a \cdot v}{2}$$

\downarrow

$$V = \int_{-R}^R \frac{\sqrt{R^2 - x^2} \cdot \sqrt{R^2 - x^2} \cdot \operatorname{tg} \alpha}{2} dx = \frac{1}{2} \operatorname{tg} \alpha \int_{-R}^R (R^2 - x^2) dx = 2 \cdot \frac{1}{2} \operatorname{tg} \alpha \int_0^R (R^2 - x^2) dx$$

integral parne fije

$$V = \operatorname{tg} \alpha \left(R^2 x - \frac{x^3}{3} \right) \Big|_0^R = \boxed{\frac{2}{3} R^3 \operatorname{tg} \alpha}$$