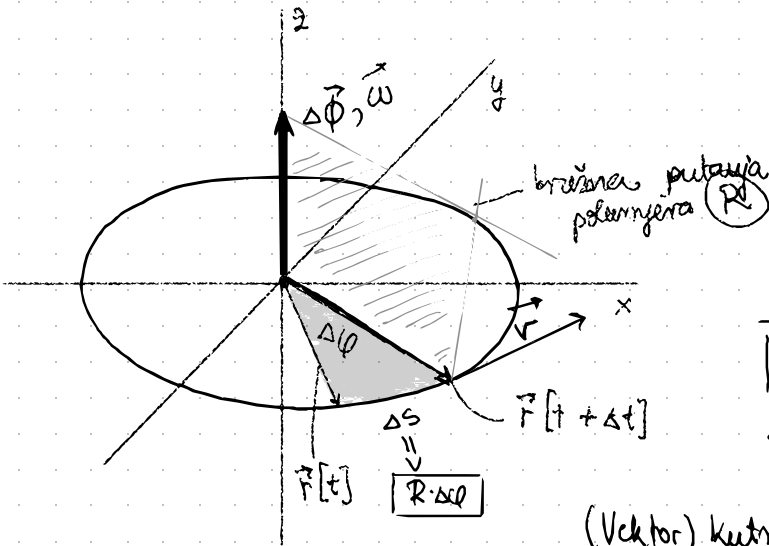


# KRUŽNO GIBANJE

radijani!



Vektor zakreta

$$|\Delta \vec{\phi}| = \Delta \varphi$$

smjer = pravilo desne ruke

(Vektor) kutne brzine

$$\vec{\omega} = \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{\phi}}{\Delta t} = \frac{d\vec{\phi}}{dt}$$

Brzina:  $\vec{v} = \vec{\omega} \times \vec{r}$

$$v = |\vec{v}| = |\vec{\omega} \times \vec{r}| = |\vec{\omega}| |\vec{r}| \sin \varphi \rightarrow 1 \text{ jer je } \varphi = \frac{\pi}{2}$$

$$= \frac{\Delta \varphi}{\Delta t} R = \frac{\Delta s}{\Delta t}$$

Akceleracija:  $\vec{a} = \frac{d\vec{v}}{dt} = \frac{d}{dt}(\vec{\omega} \times \vec{r}) = \frac{d\vec{\omega}}{dt} \vec{r} + \vec{\omega} \frac{d\vec{r}}{dt}$

$\hookrightarrow \vec{a}_{\text{tang}}$ 
 $\downarrow$

Kutna akceleracija:

$$\vec{\alpha} = \frac{d\vec{\omega}}{dt}$$

(identiteti su 0)

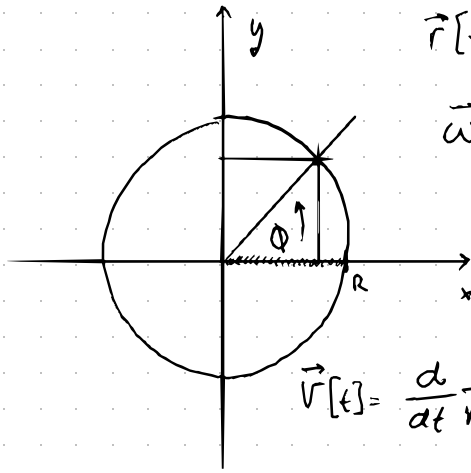
$$\vec{\omega} \times \vec{r} = \vec{\omega} \times (\vec{\omega} \times \vec{r})$$

$$= (\vec{\omega} \cdot \vec{r}) \vec{\omega} - (\vec{\omega} \cdot \vec{\omega}) \vec{r}$$

$$= -\vec{\omega}^2 \vec{r} = \vec{a}_{\text{cp}}$$

opći identitet:  $\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \cdot \vec{c}) \vec{b} - (\vec{a} \cdot \vec{b}) \vec{c}$

# Kružno gibanje u 2D (povrat. koordinat.)



$$\vec{r}[t] = R (\cos \varphi[t] \hat{x} + \sin \varphi[t] \hat{y})$$

$$\vec{\omega}[t] = \frac{d}{dt} \varphi[t] \hat{z} = \dot{\varphi}[t] \hat{z}$$

$$\begin{aligned} \vec{v}[t] &= \frac{d}{dt} \vec{r}[t] = R (-\sin \varphi[t] \dot{\varphi}[t] \hat{x} + \cos \varphi[t] \dot{\varphi}[t] \hat{y}) \\ &= \underbrace{R \dot{\varphi}[t]}_{\text{iznos brzine}} \underbrace{(-\sin \varphi[t] \hat{x} + \cos \varphi[t] \hat{y})}_{\text{odnosi se na smjer } \vec{r}[t]} \end{aligned}$$

$$\vec{v}[t] = \vec{\omega}[t] \times \vec{r}[t] =$$

$$= \dot{\varphi}[t] \hat{z} \times R (\cos \varphi[t] \hat{x} + \sin \varphi[t] \hat{y})$$

$$= \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ 0 & 0 & \dot{\varphi}[t] \\ R \cos \varphi & R \sin \varphi & 0 \end{vmatrix}$$

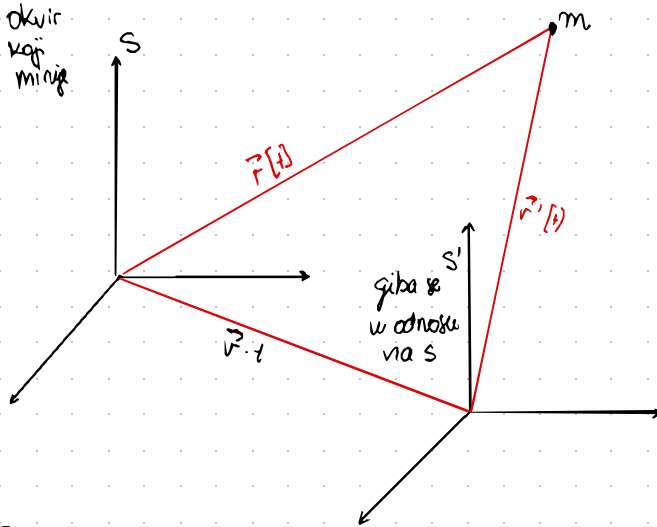
$$= \hat{x} (-\dot{\varphi}[t] \cdot R \sin \varphi) - \hat{y} (-\dot{\varphi}[t] R \cos \varphi) + \hat{z} \cdot 0$$

$$= -R \sin \varphi \cdot \dot{\varphi}[t] \hat{x} + R \cos \varphi \cdot \dot{\varphi}[t] \hat{y}$$

$$= \underline{R \dot{\varphi}[t] (-\sin \varphi \cdot \hat{x} + \cos \varphi \cdot \hat{y})}$$

# Galilejeve transformacije:

↳ relacije koji povezuju vektore položaja, brzine i akceleracije čestice u dva referentna okvira koji se međusobno gibaju stalnom brzinom



$$\vec{r}[t] = \vec{v} \cdot t + \vec{r}'[t] \quad \left| \frac{d}{dt} \right.$$

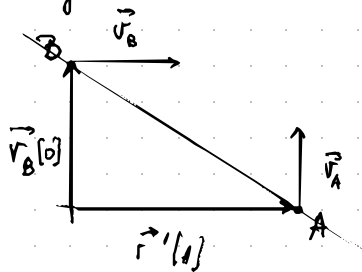
nije deriv. nego određena putanj

$$\vec{v}[t] = \vec{v} + \vec{v}'[t] \quad \left| \frac{d}{dt} \right.$$

$$\vec{a}[t] = \vec{a}'[t]$$

nije deriv. nego v u S'

Primjer:



Kako pilot iz A gleda u gibanje aviona B?

Sustav vezan za avion A:

$$\vec{v} = \vec{v}_A \quad (\text{jer A na taj način u sust. miruje})$$

$$\vec{v}[t] = \vec{v} + \vec{v}'[t]$$

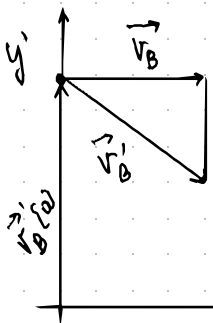
$$\vec{v}_B = \vec{v} + \vec{v}'_B$$

$$\vec{v}_B = \vec{v}_A + \vec{v}'_B \rightarrow \vec{v}'_B = \vec{v}_B - \vec{v}_A$$

$$\vec{r}'_B = \vec{r}_B - \vec{v}_A \cdot t$$

$$\vec{r}'_B = (\vec{r}_B[0] + \vec{v}_B \cdot t) - \vec{v}_A \cdot t$$

$$\vec{r}'_B = \vec{r}_B[0] + (\vec{v}_B - \vec{v}_A) \cdot t$$



$-\vec{v}_A$  gibanje aviona B u refer. sustavu u kojem je A u centru (također gibanje aviona B pilot aviona A vidi na radaru)

