7.3. HLDJ n-tog REDA S KONST. KOEF.

ai ER -gledamo: y'm + any y'm + ... + a2y" + a1y + a0y = 0

Emanno da je 17: yh = Cy, + ... + Cnyn

Svakoj HLDJ o kk je pridružen karrahteristični polinomi

 $P_{n}(n) = r^{n} + a_{n-1}r^{n-1} + ... + a_{2}r^{2} + a_{1}r + a_{0}$

Principli da unjedi L(ex) =0 (=> P(i)=0 jer L(e(x) = r"ex + any r-1ex + ... + a, re(x + a, exx = 0

-jeans a det jed bes inkyritanja 0 + Crx (r" + an, r" + ... + a, r + a0) = 0

1 sluccy: nuttacke su realne i rozeicite n, ... n => tada su en, en miserio HLDJ (to su lin nez => prosti gut docorol)

pa je nivornje yn=Cienx+...+Cnernx

2adatak) $r_1 = 0$ $v_2 = -1$ $v_3 = 3$ g" - 2y" - 3y =0 $y_h = C_1 e^{0x} + C_2 e^{-x} + C_3 e^{3x}$ $13 - 2r^2 - 3r = 0$

yn= C1+C2 = +C3=3x 1 (12-21-3)=0 2 sučaj ako je r, nuttočka kratnosti k (r, je K put nultocka od Polr)

=> tada je yn = C, e"x + C2 x e"x + ... + Ck x e"x Zerdortak) $V_{112} = -2$ $y_n = C_1 e^{-2x} + C_2 e^{-2x}$

y"+49'+49=0 r2+4r+4 =0

3 study. Also je y kompleterno sjedanje od Ly=0:

L (Rey+i Jmy)=L(Rey)+iL(Jmy)=0 Datale also je
$$r_{1,2}=d\pm i\beta$$

nullocke polinoma tada $e^{(a\pm i\beta)\times}=e^{a\times}\cdot e^{\pm i\beta\times}=e^{a\times}\left[\cos(\pm\beta\times)+i\sin(\pm\beta\times)\right]$
 $=> e^{(a\pm i\beta)\times}=e^{a\times}\cos(\beta\times)\pm ie^{a\times}\sin(\beta\times)$
 $=> y_h=c_1e^{a\times}\cos\beta\times+c_2e^{a\times}\sin\beta\times$

=>
$$y_n = C_1 e^{-2t} \cos \beta x + C_2 e^{-3t} \sin \beta x$$

2adula (1)
 $y'' + 2y' + 3y = 0$
 $f_{1/2} = \frac{-2t}{2} \frac{2(2i)}{2}$

$$9'' + 2y' + 3y = 0$$

$$1^{2} + 2x' + 3 = 0$$

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$$(11)$$

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$$2adatak)y''-16y=0$$

$$V_1 = 2$$

$$G = 0 \qquad \qquad I_1 = 2 \qquad I_2 = -2 \qquad I_{3,4} = \pm 2i$$

$$(r + 2)(r^2 + 4) = 0$$

$$0 \times 10^{-2x} \qquad 0$$

$$(r-2)(r+2)(r^2+4) = 0$$

 $y_n = Q_e^{ex} + C_2e^{-2x} + C_2coslx + C_4si$

$$y_n = Ge^{ex} + G_2e^{2x} + G_2cos2x + G_4sin2x$$

2000atrel: 21-2021-5) $y''' + 3y'' + 3y' + y = 0$
 $y(0) = 3$ $y'' + 3y'' + 3y' + y = 0$
 $y'' + 3y'' + 3y'' + y = 0$
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$$(7+1)^{3}=0$$

 $1 = -3 + C_2 + 0 = > C_2 = 4$

G'(0) = 1

y'(0) = 4

$$(r+1)^{3}=0 \rightarrow r=-1 \quad 3 \text{ pute}$$

$$= 9 \quad y_{n}=c_{1}e^{-x}+c_{2}xe^{-x}+c_{3}x^{2}e^{x} \quad \text{aprice if accusp}$$

$$y_n = C_1 \in$$

 $y''_{h} = C_{1}e^{x} + C_{2}\left(-e^{x} - (-e^{x} - (-e^{x} - e^{x} - (-e^{x} - e^{x} - e^{x} - e^{x}))\right)$

$$y''(0) = 4 = y_n = c_1 e^{-x} + c_2 x e^{-x} + c_3$$

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