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Tidy data structure to support exploration and modeling of temporal data

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Tidy data structure to support exploration and modeling of temporal data

Abstract

Mining temporal data for information is often inhibited by a multitude of time formats: irregular or multiple time intervals, multiple observational units or repeated measurements on multiple individuals, heterogeneous data types. Time series models, in particular, the software supporting time series forecasting makes strict assumptions on data to be provided, typically a matrix of numeric data with an implicit time index. Going from raw data to model-ready data is painful. This work presents a cohesive and conceptual framework for organizing and manipulating temporal data, which in turn flows into visualization and forecasting routines. Tidy data principles are applied, and extended to temporal data: (1) mapping the semantics of a dataset into its physical layout, (2) including an explicitly declared index variable representing time, (3) incorporating a “key” comprised of single or multiple variables to uniquely identify units over time. This tidy data representation most naturally supports thinking of operations on the data as building blocks, forming part of a “data pipeline” in time-based context. A sound data pipeline facilitates a fluent and transparent workflow for analyzing temporal data. Applications are included to illustrate tidy temporal data structure, data pipeline structure and usage. The infrastructure of tidy temporal data has been implemented in the R package **tsibble**.

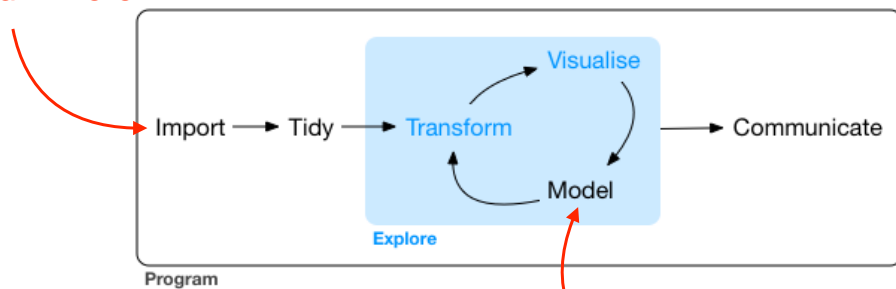
Keywords: temporal data, time series, data structures, data wrangling, tidy data, R, forecasting, data science, exploratory data analysis

1 Introduction

Temporal-context data, X_{jt} , consist of $j = 1, \dots, N_i$ observational units indexed at different time points, $1 \leq t \leq T$. Time forms the contextual basis of temporal data, but it can arrive in many possible formats, which makes preparing it for modeling and forecasting painful. For example, data can be recorded at various time resolutions (hours, minutes, and seconds), and they are typically associated with different time zones with adjustments like summer time. It could be

irregularly recorded, which is particularly true with longitudinal measurements like patient visits to a doctor's office. Temporal data also often contains rich information in addition to time: multiple observational units of different time lengths, multiple and heterogeneous measured variables, multiple grouping factors involving nested or crossed structures. The data problems are grouped into two types of analysis, time series and longitudinal.

Temporal data
should feed in here



**mésalliance between
data and model**

Current time series
data objects

The rest of the paper is structured as follows.

2 Data structures

2.1 Time series and longitudinal data

Despite of exactly the same data input, the representation of time series and longitudinal data diverges due to different modelling approaches.

Time series can be univariate or multivariate, and for modelling requires relatively large in length (i.e. large T). Time series researchers and analysts who are concerned with this large T property, are mostly concerned with stochastic processes, for the primary purpose of forecasting, and characterising temporal dynamics. The time series supporting modeling are represented as vectors or matrices in most statistical software, with the standards being provided by the R (R Core Team 2018) packages `ts`, `zoo` (Zeileis & Grothendieck 2005), and `xts` (Ryan & Ulrich 2018) (*Why include MATLAB (The MathWorks, Inc. 2017)??*). Multivariate time series are typically assumed to be in the format where each row is assumed to hold observations at a time point and each column to contain a single time series. (The tidy data name for this would be **wide**

format.) This implies that data are columns of homogeneous types: numeric or non-numeric, but there are limited supporting methods for non-numeric variables. In addition, time indexes are stripped off the data and implicitly inferred as attributes or meta-information. It strictly requires that the number of observations must be the same across all the series. Data wrangling from the form that data arrives in, to this specialist format can be frustrating and difficult, inhibiting the variety of downstream tasks such as analytics.

For longitudinal analysis, researchers and analysts are primarily interested in explaining trends across and variations among individuals, and making inference about a broader population. Longitudinal data or panel data typically assumes fewer measurements (small T) over a large number of individuals (large N). It often occurs that measurements for individuals are taken at different time points, resulting in an unbalanced panel. Thus, the primary format required for modeling is stacked series, blocks of measurements for each individual, with columns indicating individual, time of measurement and the measurements. (The tidy data name for this would be **long format**.) Evidently, this data organisation saves storage space for many sparse cells, compared to structuring it in that wide format which would have missing values in many cells. A detriment of this format is that demographic information for subjects is often repeated for each time point. However, appealing feature is that data is structured in a concise and semantic manner with reference to observations and variables, with the time index stated explicitly. This opens the door to easily operating on time to make calculations and extract different temporal components, such as month and day of the week. It is conducive to examining the data in many different ways and leading to more comprehensive exploration and forecasting.

Longitudinal data representation has been implemented in Stata's time series module (StataCorp 2017) and R package **plm** (Croissant & Millo 2008). The underpinning data structure is a two-dimensional column-homogeneous array, as other tabular data. Specifying a longitudinal data set from a generic array needs explicitly declaring time and individuals (or panel variable in Stata's `tsset` command). Therefore, each row of the data can be identified by a specific individual and time point. Individuals, however, can be only declared through a single variable, not multiple.

2.2 Tidy data and the grammar of data manipulation

Wickham (2014) coined the term "tidy data", which is a rephrasing of the second and third normal forms in relational databases but in a way that makes more sense to data scientists. A suite of paired verbs such as `gather` and `spread` (Wickham & Henry 2018) were used to

Table 1: *A small subset of estimates of tuberculosis burden generated by World Health Organisation in 2011 and 2012, with 12 observations and 5 variables. The index refers to column `year`, the key to multiple columns: `country` and `gender`, and the measured variable to column `count`.*

country	continent	gender	year	count
Australia	Oceania	Female	2011	120
Australia	Oceania	Female	2012	125
Australia	Oceania	Male	2011	176
Australia	Oceania	Male	2012	161
New Zealand	Oceania	Female	2011	36
New Zealand	Oceania	Female	2012	23
New Zealand	Oceania	Male	2011	47
New Zealand	Oceania	Male	2012	42
United States of America	Americas	Female	2011	1170
United States of America	Americas	Female	2012	1158
United States of America	Americas	Male	2011	2489
United States of America	Americas	Male	2012	2380

describe the reshape processing from messy data to tidy data. Tidy data, which standardized the mapping from the semantics of a dataset to its physical representation, serves remarkably as a fundamental unit of data analysis. R package **ggplot2** (Wickham 2009) pioneered developing the grammar of graphics based on tidy data, thus making it possible mapping from data space to visual elements. **dplyr** (Wickham et al. 2018) generalised a coherent and consistent set of verbs to handle a wide range of data transformation tasks. Wickham & Grolemund (2016) argues that 80% of data analysis tasks can be solved with tidy tools while the remaining 20% requires other tools. [R]

3 Contextual semantics

The choice of tidy representation of temporal data is made from a data-centric perspective, which is taken in the light of the operations that are to be performed on the data. Contextual semantics are introduced to tidy data in order to support more intuitive time-related manipulations and enlighten new perspectives for time series model inputs. Index, key and time interval are the three stone pillars to this new semantically-structured temporal data, which we name as “tsibble”.

Table 1 presents a subset of tuberculosis cases estimated by World Health Organization (2018). It contains 12 observations and 5 variables arranged in a “long” tabular form. Each observation hosts the number of people who are diagnosed tuberculosis for each gender at three selected countries in the years of 2011 and 2012. To turn this data into a tsibble, (1) column `year` is

declared as the index variable; (2) the key can be made up of columns `country` and `gender`. Despite column count is the only measurement in this case, it is sufficiently flexible to hold other measured variables, for example, adding the corresponding population size (if known) in order to calibrate the count later.

3.1 Index

Time provides a contextual basis for temporal data. A variable representing time is indispensable to a *tsibble*, referred to as “index”. The “index” is an intact data column rather than a masked attribute, which makes time visible and accessible to users. It is highly advantageous when manipulating time. For example, one could easily extract time components, such as time of day and day of week, from the index to visualize seasonal effects of response variables. One could also join other data sources to the *tsibble* based on common time indices. The accessibility of *tsibble* index motivates data analysis towards transparency and human readability. When the “index” used to be employed as meta information, it created an obstacle for analysts to write these simple queries in a programmatic manner, which should be discouraged from an analytic point of view.

A variable number of time representation is spotted in the wild. Date-time, universally accepted across systems, is the most commonly used type for representing time. Date-time also typically associates with a time zone with adjustments like summer time. This diversity and time zone is respected and taken into consideration for the *tsibble*’s index.

3.2 Key

The “key” specification contributes to creating a *tsibble* alongside the index. The concept of “key” is introduced to uniquely identify units or subjects that are observed over time in a data table, which is similar to a primary key (Codd 1970) defining each observation in a relational database. In the wide format, each column holds a series of values, so that the column itself serves for the sake of identification. In the long format, all column names are melt to the corresponding “key” values. But the “key” is much more flexible than simply column names. Because it is not constrained to a single field, but can be comprised of multiple fields. The identifying variables that the “key” is constituted of, stay the same as they are in the original table, with no further tweaks.

Each tsibble must hold a “key”. It is normally a priori known by analysts. For example, Table 1 describes the number of tuberculosis cases for each gender across the countries every year. This data description suggests that columns `gender` and `country` have to be declared as the key, similar to a panel variable for longitudinal data. Lacking in either of two will be inadequate for the key and thus fail to construct a tsibble. The key is explicit when multiple units exist in the data. Key can be implicit when it finds a univariate series in the table, but it cannot be absent from a tsibble.

Not only pinpoints a “key” observational units in the tsibble but also provides a solution to seamlessly link between the data, models, and forecasts. This neatly separates the data from models and forecasts, leaving more room for compulsory model components, such as coefficients, fitted values and residuals. More details are given in the following section.

3.3 Interval

One of the cornerstones beneath a tsibble is time interval. This information plays a critical role in computing statistics (e.g. seasonal unit root tests) and building models (e.g. seasonal ARIMA). The principal divide is regularly or irregularly spaced in time. Since a tsibble permits implicit missing time, it is impossible to distinguish regularity from the index. It relies on user’s specification by switching the `regular` argument off, when the data involves irregular intervals. This type of data can flow into event-based data modelling, not models that expect time series.

As for data indexed in regular time space, the time interval is derived by first computing absolute differences of time indices and then the greatest common divisor, which covers all conceivable cases. This implies that all subjects in a tsibble have one and the only interval. Data collected at different intervals should be organized in separate tsibbles, encouraging well-tailored analysis and models, because each subject may underly different data generating process.

4 Data pipeline

There has been a long history of pipeline discussions and implementation centering around data in various aspects. A data pipeline describes the general flow of data through an analysis, and can generally assist in conceptualising the process as it might be applied to a variety of problems. The Extract, Transform, and Load (ETL), from the data warehousing literature, outlines the workflow to prepare data for analysis, dates back to (XXX Caserta, Joe, 1965? REFS needed) can be considered a data pipeline. Building a data pipeline can be technically difficult, to make

it sufficiently general for various data, with many implementation decisions on the interface, input and output objects and functionality. It is useful to articulate the data pipeline induced by new data tools.

Doug McIlroy (1978) coined the term “pipelines” in software development, while developing Unix at Bell Labs. In Unix-based computer operating systems, a pipeline chains together a series of operations on the basis of their standard streams, so that the output of each programme becomes the input to another. This shapes the Unix toolbox philosophy: “each do one simple thing, do it well, and most importantly, work well with each other” (Raymond 2003).

Andreas Buja & McDonald (1988) describes a viewing pipeline for interactive statistical graphics, that takes control of the transformation from data to plot. **xgobi**, **ggobi**, **orca**, Wickham et al. (2010) and Xie, Hofmann & Cheng (2014) implemented data pipelines for the interactive statistical software **xgobi**, **ggobi**, **orca**, **plumbr** and **cranvas**, respectively. The pipeline is typically described with a one way flow, from data to plot. For interactive graphics, where all plots need to be updated when a user interacts with one plot, the events typically trigger the data pipeline to be run. Xie, Hofmann & Cheng (2014) uses a reactive programming framework, to implement the pipeline, in which user’s interactions trigger a sequence of modules to update their views, that is, practically the same as running the data pipeline producing each plot.

The tidy data abstraction lays a pipeline infrastructure for data analysis modules, transformation, visualization and modelling. Each module communicates between each other, requiring tidy input, producing tidy output, and consequently chains a series of operations together to accomplish the analytic tasks at hand.

What is notable about an effective implementation of a data pipeline is that it coordinates a user’s analysis making it cleaner to follow, and permits a wider audience to focus on the data analysis without getting lost in a jungle of computational intricacies. A fluent and fluid pipeline glues tidy data and the grammar of data manipulation together. It helps (1) break up a big problem to into manageable blocks, (2) generate human readable analysis workflow, (3) avoid introducing mistakes, at least making it possible to trace them through the pipeline.

4.1 Time-based pipeline

XXX may be good to have a diagram here showing how the time-based pipeline builds on a regular data pipeline

XXX Put comments in above each paragraph, with the topic of each paragraph. its not clear how this section flows yet. the topics would help.

The time-based pipeline shepards raw temporal data through to time series analysis, and plots. It is advised to scrutinize identical entries of key and index in the right beginning. Duplicates signal the data quality issue, which would likely affect succeeding analyses and hence decision making. Analysts are encouraged to gaze at data as earlier as possible and reason about the process of data cleaning. When the data meets the tsibble standard, it flows into the exploration stage.

Time series models typically assume that the input is a complete and regularly-spaced series, which most temporal data can barely satisfy. Temporal data becomes more granular in time resolution and more disaggregated to individual level. This inevitably goes with implicit missing values and noisiness. Data needs transformation to some extent for modelling. A suite of verbs are introduced to flatten the lumpy path from temporal data to the object that directs to modelling under the tsibble framework, as well as to facilitate transforming tsibble in various kinds of shapes for analysis and visualization. The principle that underpins most verbs is a tsibble in and a tsibble out, thereby striving to retain a valid tsibble by automating index and key updates under the hood. If a tsibble cannot hold, for example swiping index off, an error prompts users to complain and suggest alternatives. This warrants users least surprise and reminds them of time awareness.

Transformation assembles a set of modules. A unit that makes up a module is function or preferably “verb”. A tsibble is an object, conceptually considered as a noun, and hence an action performed on the object can be phrased as a verb. Each verb focuses on one thing and achieve its goal. The verb should be self-explanatory to advise what it is supposed to do or fail, for example `filter()` picking observations, and `select()` picking variables. These general-purpose verbs are made available in the **tidyverse** suite. When manipulating in temporal context, these verbs are adapted to time domain. A perceivable difference is summarizing variables between data frame and tsibble. The former will reduce to a single summary, whereas the latter will obtain the index and their corresponding summaries. New tsibble-specific verbs are proposed to expand the **tidyverse** vocabulary. We believe that users, who are already familiar with **tidyverse**, will experience a gentle learning curve for mastering tsibble verbs and glide into temporal data analysis with low cognitive load.

A table to list the verbs and what they do.

- **implicit missingness:** `has_gaps()`, `count_gaps()`, `fill_gaps()`
- **row-wise:** `filter()`, `slice()`, `arrange()`
- **column-wise:** `mutate()`, `select()`, `summarize()`
- **group-wise:** `index_by()`, `group_by()`
- **reshape:** `gather()`, `spread()`, `nest()`, `unnest()`

Friedman & Wand (2008) asserted “No matter how complex and polished the individual operations are, it is often the quality of the glue that most directly determines the power of the system.” Each verb works with other transformation family members in harmony. This set of verbs can result in many combinations to prepare `tsibble` for a broad range of visualization and modeling problems. Most importantly, the ecosystem for tidy time series analysis has been undertaking on the basis of `tsibble` in R, known as “tidyverts”.

As a special case of data frame, a `tsibble` pipes into the grammar of graphics straight way, making most use of this powerful graphical system. It should be easy to create and extend some specialist plotting methods based on `tsibble` structure, such as autocorrelation plots (**`tsibblestats`**) and calendar-based graphics (**`sugrrants`**).

Modeling is crucial to explanatory and predictive analytics, but often imposes stricter assumptions on `tsibble` data. The verbs listed in Table ?? ease the transition to a `tsibble` that suits modeling. A tidy forecasting framework built on top of `tsibble` is under development, which aims at promoting transparent forecasting practices and concise model representation. A `tsibble` usually contains multiple time series. Batch forecasting will be enabled if a univariate model, such as ARIMA and Exponential Smoothing, is applied to each time series independently. This yields a “mable” (short for model table), where each model only tags to each “key” value in `tsibble` to avoid expensive data copying and reduce model storage. The mable is further supplied to forecasting methods, to produce a `tsibble` in which each “key” along with its future time holds predictions. It also underlines the advantage of `tsibble`’s “key” in linking between data inputs, models and forecasts. Advanced forecasting techniques, such as vector autocorrelation, hierarchical reconciliation, and ensembles, can be developed in alike spirit. The modeling module will be fulfilled and integrated eventually.

We go through the whole exploration circle, and keep iterating and refining until data insights gained. The `tsibble` data structure substantially lubricates between these modules for time-based pipelines. The cohesive and coherent framework results in cleaner, clearer and more expressive code.

4.2 Rolling window in functional programming

- rolling window: `slide()`, `tile()`, `stretch()`

5 Software structure and design decisions

data-centric & human-centered.

5.1 Data first

The prime force that drives the software's design choices is "data". All functions in **tsibble** starts with data or its variants as the first argument, namely "data first". They work naturally with the pipe operator `%>%`, read as "then". This not only lays out a consistent interface but also addresses the significance of the data throughout the software.

Beyond the tools, the print display provides a quick and comprehensive glimpse of data in temporal context, particularly useful when handling a large collection of data. Below conveys the pieces of critical and contextual picture about the data in Table 1: (1) data dimension with its shorthand time interval, alongside time zone if date-times; (2) variables that constitute of the "key" with the number of series. These details aid users in understanding their data better and manipulate the data with care.

```
#> # A tsibble: 12 x 5 [1Y]
#> # Key:      country, gender [6]
#>   country    continent gender  year count
#>   <chr>      <chr>      <chr>  <int> <int>
#> 1 Australia Oceania    Female  2011   120
#> 2 Australia Oceania    Female  2012   125
#> 3 Australia Oceania    Male    2011   176
#> 4 Australia Oceania    Male    2012   161
#> 5 New Zealand Oceania    Female  2011    36
#> # ... with 7 more rows
```

5.2 Modularity

Modular programming is adopted while designing the **tsibble** package. Modularity benefits users with variety and flexibility and developers with easy maintenance.

All user-facing functions can be roughly organized into three major chunks according to their functionality: vector functions (1d), table verbs (2d), and window family. Each chunk is an independent module, but works interdependently. Vector functions in the package mostly deal with time. When collapsing a tsibble to less granular interval, these atomic functions can be combined with the `index_by()` table verb to accomplish this. A different function results in easily switching to aggregation of different time resolution. Since these functions are not exclusive to a tsibble, they can be used in a variety of applications in conjunction with other packages. On the other hand, these tsibble verbs can incorporate many third-party vector functions to step out of current tsibble zone. It is generally easier to trace back the errors users encounter from separating 1d and 2d functions.

5.3 Extensibility

As a fundamental infrastructure, extensibility is a design decision that is focused on from the start of **tsibble**'s development. Contrary to the “data first” principle for end users, extensibility is developer focused and would be mostly used in dependent packages, which heavily relies on S3 classes and methods in R (**adv-r**). It can be extended in two major aspects: custom index and new tsibble class.

Time representation could be arbitrary, for example R's native `POSIXct` and `Date` for versatile date-times, nano time for nanosecond resolution (**R-nanotime**), and pure numbers in simulations. Yet ordered factors can also be a source of time, such as month names from January to December and weekdays from Monday to Sunday. Tsibble supports an extensive range of index types from numerics to nano time, but there might be custom indices used for some occasions, for example school semesters. These academic terms vary from one institute to another within an academic year, which is defined differently from a calendar year. New index would be immediately recognized by the software once `index_valid()` defined, as long as it can be ordered from past to future. The interval regarding semesters is further outlined through `pull_interval()`. As a result, the rest software methods such as `has_gaps()`, `count_gaps()` and `fill_gaps()` will have instant support for data that contains this new index.

The class of tsibble is an underlying basis of temporal data, and there is a demand for subclassing a tsibble. For example, a fable is actually an extension to a tsibble, mentioned in Section 4.1. A low-level constructor `new_tsibble()` provides a vehicle to easily create a new subclass. First of all, this new object itself is a tsibble. It perhaps needs more metadata than those of a tsibble, that gives rise to a new data extension, like prediction distributions to a fable. Tsibble

verbs are also S3 generics. Developers will be able to implement these verbs for the new class if needed.

6 Case studies

6.1 On-time performance for domestic flights in U.S.A

The dataset of 2017 on-time performance for US domestic flights represents event-driven data caught in the wild, sourced from US Bureau of Transportation Statistics (reference). It contains 5,548,445 operating flights with many measurements (such as departure delay, arrival delay in minutes, and other performance metrics) and detailed flight information (such as origin, destination, plane number and etc.) in a tabular format. This kind of event describes each flight scheduled for departure at a time point in its local time zone. Every single flight would be uniquely identified by the flight number and its scheduled departure time, from a passenger's point of view. In fact, it fails to pass the `tsibble` hurdle due to duplicates in the original data. An error is immediately raised when attempting to convert this data into a `tsibble`, and a closer inspection has to be carried out to locate the issue. The **`tsibble`** package provides tools to easily locate the duplicates in the data with `duplicates()`. Below shows the problematic entries.

```
#>   flight_num sched_dep_datetime sched_arr_datetime dep_delay arr_delay
#> 1      NK630 2017-08-03 17:45:00 2017-08-03 21:00:00      140      194
#> 2      NK630 2017-08-03 17:45:00 2017-08-03 21:00:00      140      194
#>   carrier tailnum origin dest air_time distance origin_city_name
#> 1      NK  N601NK   LAX  DEN      107      862      Los Angeles
#> 2      NK  N639NK   ORD  LGA      107      733        Chicago
#>   origin_state dest_city_name dest_state taxi_out taxi_in carrier_delay
#> 1           CA        Denver         CO      69      13              0
#> 2           IL        New York         NY      69      13              0
#>   weather_delay nas_delay security_delay late_aircraft_delay
#> 1           0        194              0              0
#> 2           0        194              0              0
```

The issue is perhaps introduced when updating or entering the data into a system. The same flight is scheduled at exactly the same time, together with the same performance statistics but different flight details, which is very unlikely. Flight NK630 is usually scheduled at 17:45 from

Chicago to New York, searching into the whole records. A decision is made on removal of the first row from the duplicated entries before proceeding to the tsibble creation.

This dataset is intrinsically heterogeneous, encoding in numbers, strings, and date-times. The tsibble framework, as expected, incorporates this type of data, without the loss of data richness and heterogeneity. To declare the flight data as a valid tsibble, column `sched_dep_datetime` is specified as “index”, column `flight_num` as “key” via `id(flight_num)`. As a result of event data, this data is irregularly spaced, and hence switching to irregular option is necessary. The program internally validates if the key and index produce the distinct rows, and then sort the key and the index from past to recent. When the tsibble creation is done, the print display is data-oriented and contextually informative, such as dimensions, irregular interval (5,548,444 x 22 [!] <UTC>) and the number of time-based observational units (`flight_num` [22,562]).

```
#> # A tsibble: 5,548,444 x 22 [!] <UTC>
#> # Key:      flight_num [22,562]
```

Transforming tsibble for exploratory data analysis with a suite of time-specific and general-purpose manipulation verbs can result in well-constructed pipelines. From the perspective of a passenger, one need to travel smart, by choosing an efficient carrier to fly with and the time of day to avoid congestion, for example. We take a drill-down approach to exploring this data, starting with annual carrier performance and followed by disaggregating to finer time resolutions.

Figure 1 visually presents the end product of aggregating the number of on-time and delayed flights to the year interval by carriers. This pipeline is initialized defining a new variable if the flight is delayed, and involves summarizing the tallies of on-time and delayed flights for each carrier annually. To prepare the summarized data for a mosaic plot, it is further manipulated by melting new tallies into a single column. The flow chart shown as Figure 2 demonstrates the operations undertaking in a data pipeline. The input to this pipeline is a tsibble of irregular interval, and the output ends up with a tsibble of unknown interval. The final data is each carrier along with a single year, thereby the interval undetermined. It in turn feeds into the mosaic display. Note that Southwest Airlines, as the largest carrier, operates less efficiently compared to Delta, in Figure 1.

A closer examination of New York airports will give an indication about how well the busiest airports manage the outflow traffic on a daily basis. A subset that contains observations for

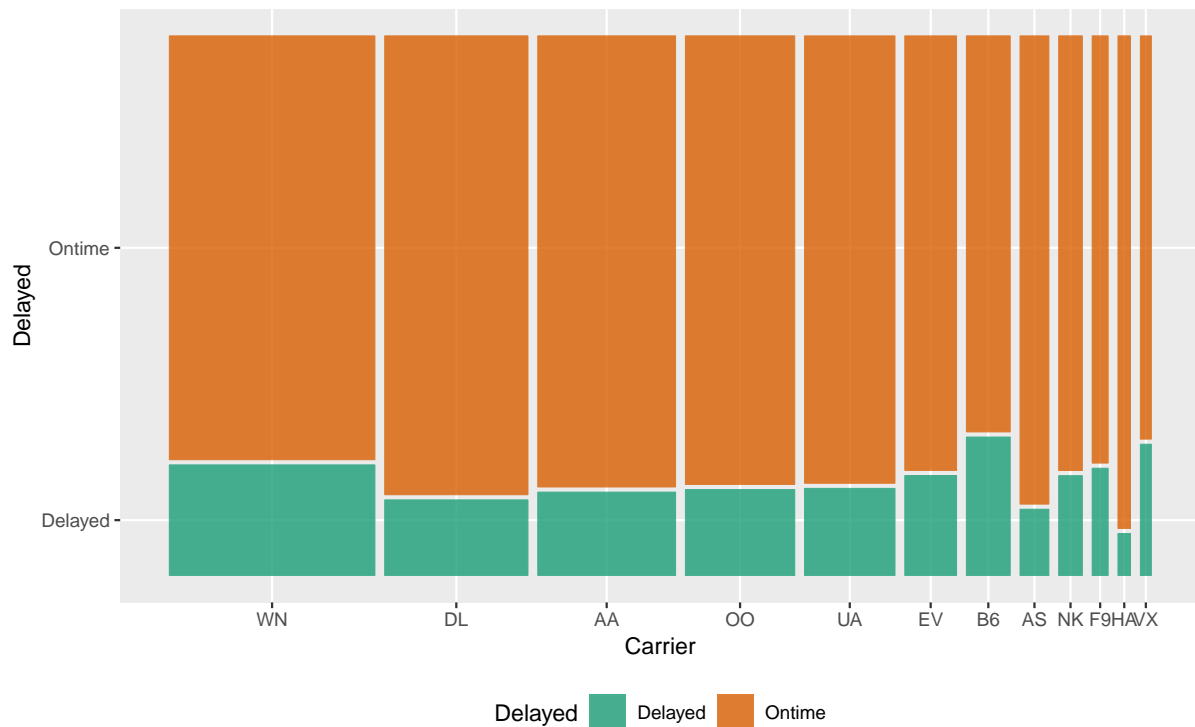


Figure 1: Mosaic plot showing the association between the size of airline carriers and the delayed proportion of departure in 2017. Southwest Airlines is the largest operator, but does not operate as efficient as Delta. Hawaiian Airlines, also as a small operator, outperforms the rest.



Figure 2: Flow chart illustrates the pipeline that pre-processes the data for creating Figure 1.

EWB, JFK and LGA airports is obtained first. The succeeding operations compute delayed percentages every day at each airport, which are framed as grey lines in Figure 3. LGA fluctuates a lot compared to the other two. What superimposes on these lines is two-month moving averages so that a temporal trend is more visible. The number of days for each month is variable. Moving averages for two months call for computing weighted mean. But this can also be accomplished using a pair of commonly used verbs—`nest()` and `unnest()` to handle list-columns, without worrying weights specification. The sliding with large window size smoothes out the fluctuations and gives a stable trend around 25% over the year.

What time of day and day of week should we travel to avoid suffering from horrible delay? Figure 4 plots hourly quantile estimates across day of week in the form of small multiples. The upper-tail delay behaviors are of primary interest, and hence 50%, 80% and 95% quantiles are shown. To reduce the likelihood of delay suffering, it is recommended to avoid the peak hour

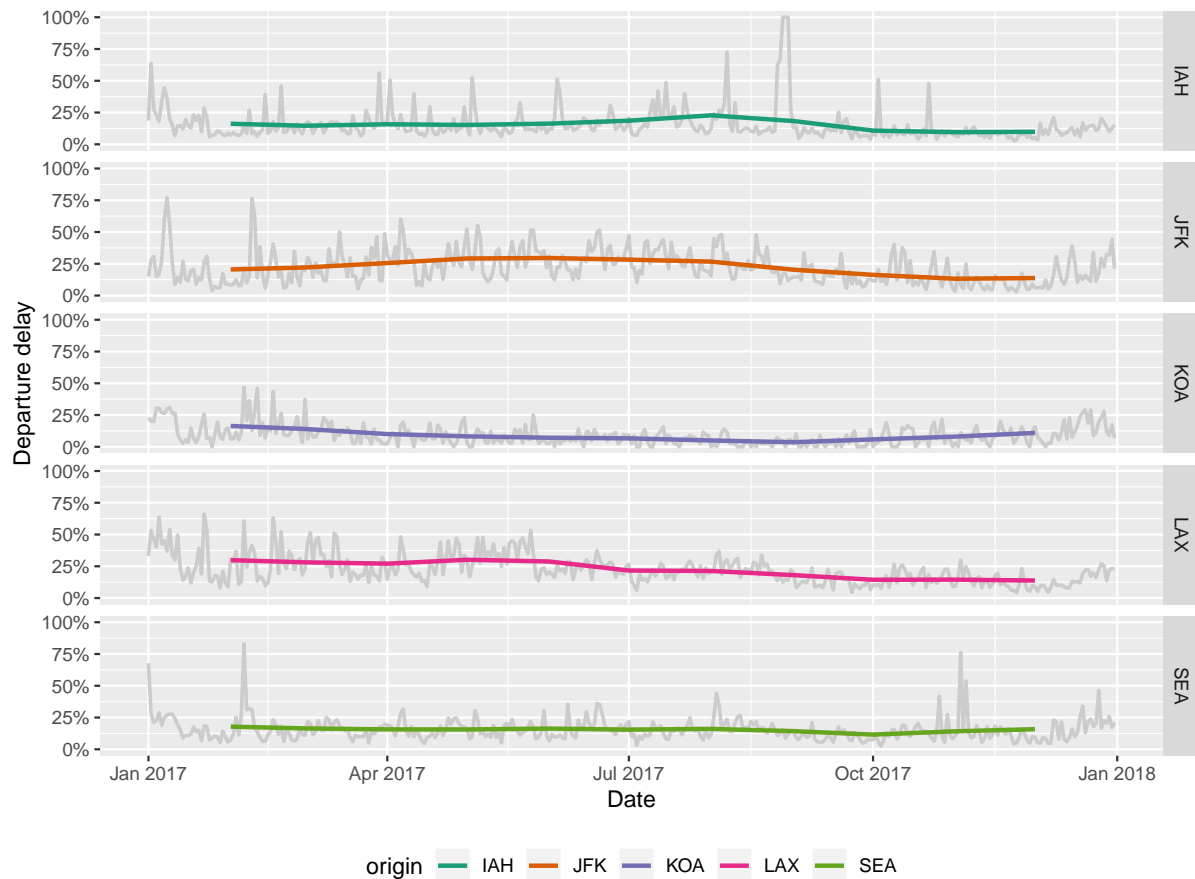


Figure 3: Daily delayed percentages for departure with two-month moving averages overlaid at five international airports. There are many fluctuations observed at LGA airport. The estimates of temporal trend are around 25% across three airports, highlighting relatively less delay in Fall.

at 18. As moving towards the upper extremes, the variations considerably increase, making departure time unpredictable.

6.2 Smart-grid customer data in Australia

Sensors have been put up to collect data for the project of smart city across major cities in Australia. One of the trials is monitoring households' electricity usage through installed smart meters in the area of New Castle over 2010–2014 (**smart-meter**). Year 2013 has been sliced to examine temporal patterns of customer's energy consumption with **tsibble** in this paper. Half-hourly general supply in kWh have been recored for 2,924 customers in the data set, resulting in 46,102,229 observations in total. Customer's demographic data provides explanatory variables other than time in a separate data table. Two data tables might be joined to explore different sources that contribute to daily electricity use when needed.

<https://data.gov.au/dataset/smart-grid-smart-city-customer-trial-data>

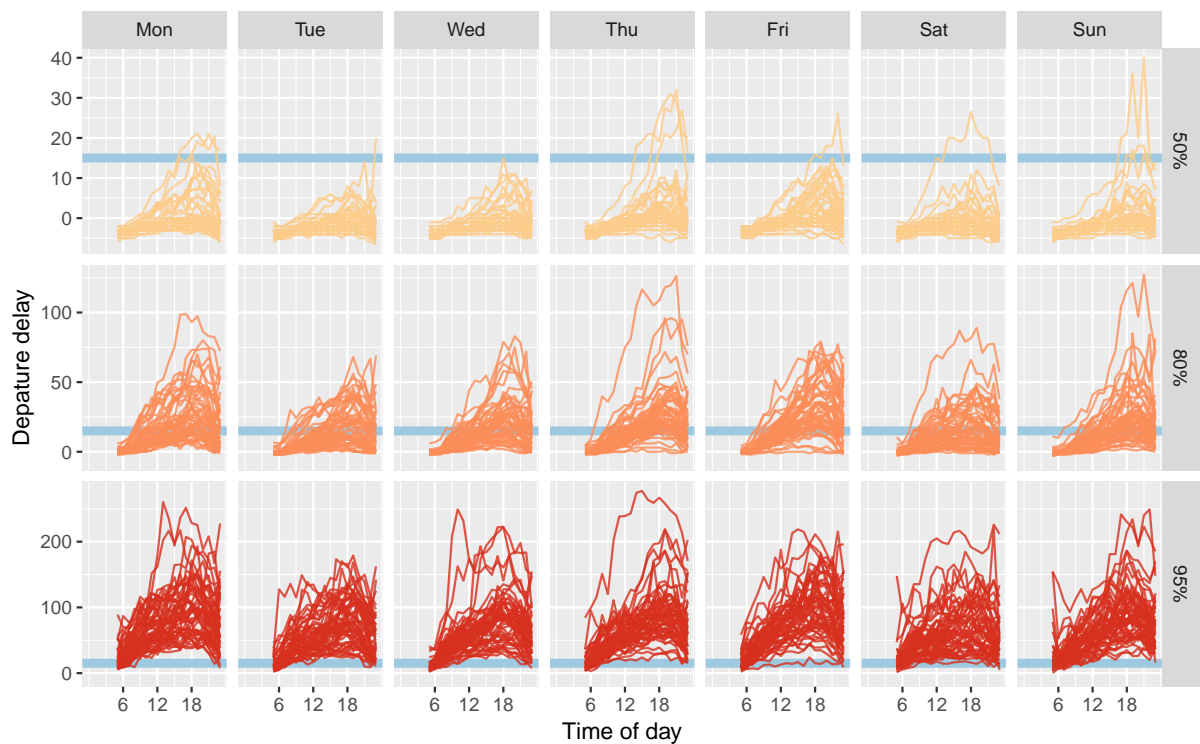


Figure 4: Small multiples of lines about departure delay against time of day, faceting day of week and 50%, 80% and 95% quantiles. A blue horizontal line indicates the 15-minute on-time standard to help grasp the delay severity. Passengers are apt to hold up around 18 during a day, and are recommended to travel early. The variations increase substantially as the upper tails.

7 Conclusion and future work

A tidy representation of time series data, and data pipelines to facilitate data analysis flow have been proposed and discussed. It can be noted that tidy temporal data gains greater flexibility in keeping data richness, making data transformation and visualisation easily. A set of verbs provides a fluent and fluid pipeline to work with tidy time series data in various ways.

A new visualization framework for handling time series with nesting and crossing structure is under development. The proposed data structure proves a natural input (unit time series and parent-children structure) that can be piped into a visualization program. As long as the program understands the embedded structure, it will produce sensible layout and interactivity.

The ground of time series modelling or forecasting is left untouched in this paper. The future plan is to bridge the gap between tidy data and model building. Currently, it is required to casting to matrix from tidy data and therefore building a model. But time series models should be directly applied to tidy data as other wrangling tools do, without such an intermediate step. In particular, a univariate time series model, like ARIMA and Exponential Smoothing, can be

applied to multiple time series independently. A tidy format to represent model summaries and forecasting objects will be developed and implemented in the future. Model summaries include coefficients, fitted values, and residuals; forecasting objects.

When involving multiple variables, one need to distinguish nesting and crossing data variables. “Nesting” refers to a scenario where a variable is nested within another when each category of the former variable co-occurs with only one category of the latter (for example, country nested within continent); on the other hand, “crossing” means that a variable is crossed with another when every category of one variable co-occurs with every category of the other (for example, country crosses with gender). Nesting is a special case of crossing. The former exhibits a hierarchical ordering with lower-level category (children) nested within higher-level category (parent) (more categories in lower level); whereas the ordering of the latter makes no difference. Whilst constructing tidy temporal data, users also need to specify the key that identifies the structure on the data. Rather than creating a separate object that contains the data structure, like what the **hts** does, we propose a syntax-based interface to directly deal with variables, so that it takes advantage of data semantics. The expression of a vertical bar (|) (can be interpreted probabilistically as the conditional distribution for its parent) is used to indicate nesting variables (reflect depths), while a comma (,) for crossing variables. Wilkinson (2005) discussed the distinction between nesting and crossing with respect to facets in graphics, and he used / and * instead for nested and crossed expressions. A crossing structure displays all unique and possible combinations of crossed variables, including those not found in the data, in a graphical layout. However, tidy temporal data finds only the combinations that occur in the data and intentionally respects the structure of incomplete combinations. nclude future time path and distributions generating prediction intervals.

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