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Abstract

Mining temporal data for information is often inhibited by a multitude of formats: irregular or multiple time intervals, point event that needs aggregating, multiple observational units or repeated measurements on multiple individuals, heterogeneous data types. Time series models, in particular, the software supporting time series forecasting makes strict assumptions on the data to be provided, typically a matrix of numeric data with implicit time indices. Going from raw data to model-ready data is painful. This work presents a cohesive and conceptual framework for organizing and manipulating temporal data, which in turn flows into visualization and forecasting routines. Tidy data principles are extended to temporal data: (1) mapping the semantics of a dataset into its physical layout, (2) including an explicitly declared index variable representing time, (3) incorporating a "key" comprised of single or multiple variables to uniquely identify units over time. This tidy data representation most naturally supports thinking of operations on the data as building blocks, forming part of a "data pipeline" in time-based context. A sound data pipeline facilitates a fluent and fluid workflow for analyzing temporal data. The infrastructure of tidy temporal data has been implemented in the R package tsibble.

Keywords: temporal data, time series, data structures, data wrangling, tidy data, R, forecasting, data science, exploratory data analysis

1 Introduction

Suppose that temporal data consists of N subjects/observational units. Given subject i (i = 1, 2, ..., N), X_{ijt} denotes the jth measurement (j = 1, 2, ..., p) indexed at a unique sequence of time points $0 \le t \le T_i$. Temporal data arrives in many possible formats, so does time. For example, time can carry with various time resolutions (hours, minutes, and seconds), and they are typically associated with different time zones with adjustments like summer time. It

could be irregularly recorded, which is particularly true with longitudinal measurements like patient visits to a doctor's office. Temporal data also often contains rich information: multiple observational units of different time lengths, multiple and heterogeneous measured variables, multiple grouping factors. Wickham & Grolemund (2016) succinctly describes the data science workflow given in Figure 1. It is annotated to emphasize the significant divide between data that feeds into the beginning of analysis and the current time series objects that fits into modelling, making data preparation for modeling and forecasting painful.

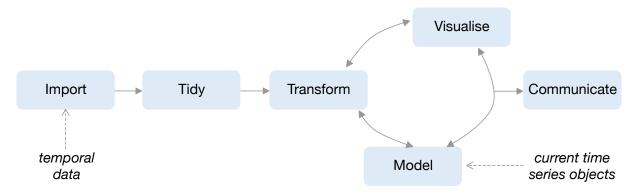


Figure 1: An overview of the data science program centering around data. Temporal data should feed into the import stage, but the existing time series objects are model-focused, thus resulting misalliance between data and model.

Current time series objects, which are model-oriented matrices with little support for nonnumeric values, feed into the framework solely at the modelling stage. Analysts are expected to do their own data pre-processing and take care of anything else needed to get to this stage, which leads to a myriad ad-hoc solutions and duplicated efforts.

The rest of the paper is structured as follows. Section 2 reviews temporal data structures corresponding to time series and longitudinal analysis, and discusses "tidy data" and the grammar of data manipulation. Section 3 proposes contextual semantics for temporal data, built on top of tidy data. The concept of data pipelines with respect to the time domain will be discussed in depth in Section 4, followed by the design choices of software structure in Section 5. Section 6 presents two case studies for temporal data exploration using the newly implemented infrastructure. Section 7 concludes the paper and discusses the future work.

2 Data structures

2.1 Time series and longitudinal data

The data problems are grouped into two types of analysis, time series and longitudinal. Despite of exactly the same data input, the representation of time series and longitudinal data diverges due to different modelling approaches.

Time series can be univariate or multivariate, and for modelling requires relatively large in length (i.e. large *T*). Time series researchers and analysts who are concerned with this large *T* property, are mostly concerned with stochastic processes, for the primary purpose of forecasting, and characterizing temporal dynamics. The time series supporting modeling are represented as vectors or matrices in most statistical software. Multivariate time series are typically assumed to be in the format where each row is assumed to hold observations at a time point and each column to contain a single time series. (The tidy data name for this would be **wide format**.) This implies that data are columns of homogeneous types: numeric or non-numeric, but there are limited supporting methods for non-numeric variables. In addition, time indexes are stripped off the data and implicitly inferred as attributes or meta-information. It strictly requires that the number of observations must be the same across all the series. Data wrangling from the form that data arrives in, to this specialist format can be frustrating and difficult, inhibiting the variety of downstream tasks such as analytics.

For longitudinal analysis, researchers and analysts are primarily interested in explaining trends across and variations among individuals, and making inference about a broader population. Longitudinal data or panel data typically assumes fewer measurements (small T) over a large number of individuals (large N). It often occurs that measurements for individuals are taken at different time points, resulting in an unbalanced panel. Thus, the primary format required for modeling is stacked series, blocks of measurements for each individual, with columns indicating individual, time of measurement and the measurements. (The tidy data name for this would be **long format**.) Evidently, this data organisation saves storage space for many sparse cells, compared to structuring it in that wide format which would have missing values in many cells. A detriment of this format is that demographic information for subjects is often repeated for each time point. However, appealing feature is that data is structured in a concise and semantic manner with reference to observations and variables, with the time index stated explicitly. This opens the door to easily operating on time to make calculations and extract different temporal

components, such as month and day of the week. It is conducive to examining the data in many different ways and leading to more comprehensive exploration and forecasting.

2.2 Tidy data and the grammar of data manipulation

Wickham (2014) coined the term "tidy data", which is a rephrasing of the second and third normal forms in relational databases but in a way that makes more sense to data scientists by referring rows to observations and columns to variables. The principles of "tidy data" attempt to standardize the mapping of the semantics of a dataset to its physical representation. This data structure is the fundamental unit of the **tidyverse**, which is a collection of R packages designed for data science; the prevalence of **tidyverse** reversely testifies to the novelty of "tidy data". The **tidyverse** provides abstract yet functional grammars to manipulate and visualize data in easier-to-comprehend manners. One of the **tidyverse** packages, **dplyr** (Wickham et al. 2018) showcases the value of a grammar as a principled vehicle to transform data for a wide range of data challenges, providing a consistent set of verbs: mutate(), select(), filter(), summarise(), and arrange(). Each verb focuses on a singular task. Most common data tasks can be rephrased and tackled with these five key verbs, by composing them sequentially.

The **tidyverse** largely formalizes exploratory data analysis. The whole R community has quickly adopted the **tidyverse** way of thinking to much broader domains, such as simple features for spatial data in the **sf** package (Pebesma 2018) and missing value handling in the **naniar** package (Tierney & Cook 2018). Temporal data is left behind in this regard.

2.3 Existing time series standards in R

Current standards, provided by native ts object in R and extended by **zoo** (Zeileis & Grothendieck 2005), and **xts** (Ryan & Ulrich 2018), organize temporal data in matrices with implicit time indices. These objects were designed for modelling methods. The diagram correspondingly would place the model at the center of the analytical universe, and all the transformations, visualisations would hinge on that format. This is contrary to the tidyverse conceptualisation, which wholistically captures the full data workflow.

A new temporal data class is needed in the upstream of the workflow, which could incorporate all the downstream modules. A relatively new R package **tibbletime** proposed a data class of *time tibble* to represent temporal data in heterogeneous tabular format. It only requires an index variable to declare a temporal data object, thus placing at the import stage. However, this is a

Table 1: A small subset of estimates of tuberculosis burden generated by World Health Organisation in 2011 and 2012, with 12 observations and 5 variables. The index refers to column year, the key to multiple columns: country and gender, and the measured variable to column count.

country	continent	gender	year	count
Australia	Oceania	Female	2011	120
Australia	Oceania	Female	2012	125
Australia	Oceania	Male	2011	176
Australia	Oceania	Male	2012	161
New Zealand	Oceania	Female	2011	36
New Zealand	Oceania	Female	2012	23
New Zealand	Oceania	Male	2011	47
New Zealand	Oceania	Male	2012	42
United States of America	Americas	Female	2011	1170
United States of America	Americas	Female	2012	1158
United States of America	Americas	Male	2011	2489
United States of America	Americas	Male	2012	2380

loosely-defined structure and insufficient for time series analytics and models. Because it does not define interested subjects (*i*) over time and time uniqueness.

This paper proposes a new tidy representation for temporal data and a unified framework to streamline the workflow from data pre-processing to visualization and forecasting, as an integral part of tidy data analysis.

3 Contextual semantics

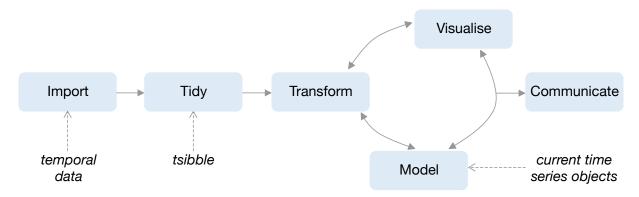


Figure 2: Tsibble's abstraction arises from a data-centric point of view, which could neatly embed into the tidyverse ecosystem. It should be noted that tsibble positions itself at the "tidy" step rather than "import", which ensures valid tidy data to time series analytics and models.

The choice of tidy representation of temporal data arises from a data-centric perspective, which accommodates all of the operations that are to be performed on the data. Figure 2 marks where this new abstraction is placed in the tidy model, which we refer to as "tsibble".

Table 1 presents a subset of tuberculosis cases estimated by World Health Organization (2018). It contains 12 observations and 5 variables arranged in a "long" tabular form. Each observation hosts the number of people who are diagnosed tuberculosis for each gender at three selected countries in the years of 2011 and 2012. To turn this data into a tsibble, (1) column year is declared as the index variable; (2) the key can be made up of columns country and gender. Despite column count is the only measurement in this case, it is sufficiently flexible to hold other measured variables, for example, adding the corresponding population size (if known) in order to calibrate the count later.

It bridges the gap between raw temporal data and model inputs. Contextual semantics are introduced to tidy data in order to support more intuitive time-related manipulations and enlighten new perspectives for time series model inputs. Index, key and time interval are the three stone pillars to this new semantically-structured temporal data.

3.1 Index

Time provides a contextual basis for temporal data. A variable representing time is indispensable to a tsibble, referred to as "index". The "index" is an intact data column rather than a masked attribute, which makes time visible and accessible to users. It is highly advantageous when manipulating time. For example, one could easily extract time components, such as time of day and day of week, from the index to visualize seasonal effects of response variables. One could also join other data sources to the tsibble based on common time indices. The accessibility of tsibble index motivates data analysis towards transparency and human readability. When the "index" used to be employed as meta information, it created an obstacle for analysts to write these simple queries in a programmatic manner, which should be discouraged from an analytic point of view.

A variable number of time representation is spotted in the wild. Date-time, universally accepted across systems, is the most commonly used type for representing time. Date-time also typically associates with a time zone with adjustments like summer time. This diversity and time zone is respected and taken into consideration for the *tsibble*'s index.

3.2 Key

The "key" specification contributes to creating a tsibble alongside the index. The concept of "key" is introduced to uniquely identify units or subjects that are observed over time in a data table,

which is similar to a primary key (Codd 1970) defining each observation in a relational database. In the wide format, each column holds a series of values, so that the column itself serves for the sake of identification. In the long format, all column names are melt to the corresponding "key" values. But the "key" is much more flexible than simply column names. Because it is not constrained to a single field, but can be comprised of multiple fields. The identifying variables that the "key" is constituted of, stay the same as they are in the original table, with no further tweaks.

Each tsibble must hold a "key". It is normally a priori known by analysts. For example, Table 1 describes the number of tuberculosis cases for each gender across the countries every year. This data description suggests that columns gender and country have to be declared as the key, similar to a panel variable for longitudinal data. Lacking in either of two will be inadequate for the key and thus fail to construct a tsibble. The alternative specification of the key is to include a third variable continent. Since country is nested within continent, it is a free variable for use. But this variable brings additional information that can be used for forecasting reconciliation (Hyndman & Athanasopoulos 2017). The key is explicit when multiple units exist in the data. Key can be implicit when it finds a univariate series in the table, but it cannot be absent from a tsibble.

Not only pinpoints a "key" observational units in the tsibble but also provides a solution to seamlessly link between the data, models, and forecasts. This neatly decouples the data from models and forecasts, leaving more room for compulsory model components, such as coefficients, fitted values and residuals. More details are given in the following section.

3.3 Interval

One of the cornerstones beneath a tsibble is time interval. This information plays a critical role in computing statistics (e.g. seasonal unit root tests) and building models (e.g. seasonal ARIMA). The principal divide is regularly or irregularly spaced in time. Since a tsibble permits implicit missing time, it is impossible to distinguish regularity from the index. It relies on user's specification by switching the regular argument off, when the data involves irregular intervals. This type of data can flow into event-based data modelling, not models that expect time series.

As for data indexed in regular time space, the time interval is derived by first computing absolute differences of time indices and then the greatest common divisor, which covers all conceivable cases. This implies that all subjects in a tsibble have one and the only interval. Data collected at

different intervals should be organized in separate tsibbles, encouraging well-tailored analysis and models, because each subject may underly different data generating process.

4 Data pipeline

There has been a long history of pipeline discussions and implementation centering around data in various aspects. A data pipeline describes the general flow of data through an analysis, and can generally assist in conceptualising the process as it might be applied to a variety of problems. The Extract, Transform, and Load (ETL), from the data warehousing literature, outlines the workflow to prepare data for analysis, dates back to Kimball & Caserta (2011) can be considered a data pipeline. Building a data pipeline can be technically difficult, to make it sufficiently general for various data, with many implementation decisions on the interface, input and output objects and functionality. It is useful to articulate the data pipeline induced by new data tools.

Doug McIlroy (1978) coined the term "pipelines" in software development, while developing Unix at Bell Labs. In Unix-based computer operating systems, a pipeline chains together a series of operations on the basis of their standard streams, so that the output of each programme becomes the input to another. This shapes the Unix toolbox philosophy: "each do one simple thing, do it well, and most importantly, work well with each other" (Raymond 2003).

Andreas Buja & McDonald (1988) describes a viewing pipeline for interactive statistical graphics, that takes control of the transformation from data to plot. Swayne, Cook & Buja (1998), Swayne et al. (2003), Sutherland et al. (2000), Wickham et al. (2010) and Xie, Hofmann & Cheng (2014) implemented data pipelines for the interactive statistical software **Xgobi**, **Ggobi**, **Orca**, **plumbr** and **cranvas**, respectively. The pipeline is typically described with a one way flow, from data to plot. For interactive graphics, where all plots need to be updated when a user interacts with one plot, the events typically trigger the data pipeline to be run. Xie, Hofmann & Cheng (2014) uses a reactive programming framework, to implement the pipeline, in which user's interactions trigger a sequence of modules to update their views, that is, practically the same as running the data pipeline producing each plot.

The tidy data abstraction lays a pipeline infrastructure for data analysis modules of transformation, visualization and modelling. Each module communicates between each other, requiring tidy input, producing tidy output, chaining a series of operations together to accomplish the analytic tasks.

What is notable about an effective implementation of a data pipeline is that it coordinates a user's analysis making it cleaner to follow, and permits a wider audience to focus on the data analysis without getting lost in a jungle of computational intricacies. A fluent and fluid pipeline glues tidy data and the grammar of data manipulation together. It helps (1) break up a big problem to into manageable blocks, (2) generate human readable analysis workflow, (3) avoid introducing mistakes, at least making it possible to trace them through the pipeline.

4.1 Time-based pipeline

XXX may be good to have a diagram here showing how the time-based pipeline builds on a regular data pipeline

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The time-based pipeline shepards raw temporal data through to time series analysis, and plots. It is possible and recommended to check for identical entries of key and index before analysis. Duplicates signal the data quality issue, which would likely affect succeeding analyses and hence decision making. Analysts are encouraged to gaze at data early and reason about the process of data cleaning. When the data meets the tsibble standard, it flows neatly into the exploration stage.

Time series models typically assume that the input is a complete and regularly-spaced series, which most temporal data can barely satisfy. Temporal data becomes more granular in time resolution and more disaggregated to individual level. This inevitably goes with implicit missing values and noisiness. Data needs transformation to some extent for modelling. A suite of verbs are introduced to flatten the lumpy path from temporal data to an object that can be directly modeled in the tsibble framework, as well as transformed for visualization. The principle that underpins most verbs is a tsibble in and a tsibble out, thereby striving to retain a valid tsibble by automating index and key updates under the hood. Attention has been paid to error handling. If a tsibble cannot be maintained in the output of a pipeline module, for example the index is dropped by aggregation, an error informs users of the problem and suggests alternatives. This avoids negatively surprising users and reminds them of time context.

Transformation assembles a set of modules. A unit that makes up a module is function or preferably "verb". A tsibble is an object, conceptually considered as a noun, and hence an action performed on the object can be phrased as a verb. Each verb focuses on one thing and

achieve its goal. The verb should be self-explanatory to advise what it is supposed to do or fail, for example filter() picks observations, select() picks variables, and left_join() joins two tables. These general-purpose verbs are made available in the tidyverse suite. When manipulating in temporal context, these verbs are adapted to time domain. A perceivable difference is summarizing variables between data frame and tsibble. The former will reduce to a single summary, whereas the latter will obtain the index and their corresponding summaries. New tsibble-specific verbs are proposed to expand the tidyverse vocabulary. We believe that users, who are already familiar with tidyverse, will experience a gentle learning curve for mastering tsibble verbs and glide into temporal data analysis with low cognitive load.

Table 2: A list of table verbs working with tsibble. Functions in bold originating from the tidyverse and are adapted for tsibble.

	Verb	Description	
	has_gaps()	Test if a tsibble has gaps in time	
Time gaps	scan_gaps()	Report implicit missing entries	
	$count_gaps()$	Summarize time gaps	
	$fill_gaps()$	Fill in gaps by values and functions	
	filter()	Pick rows based on conditions	
Row-wise	filter_index()	Provide a shorthand for time subsettir	
Now-wise	slice()	Select rows based on row positions	
	arrange()	Sort the ordering of row by variables	
	select()	Pick columns by variables	
Column-wise	<pre>mutate()</pre>	Add new variables	
Column-wise	transmute()	Drops existing variables	
	<pre>summarise()</pre>	Aggregate values over time	
	index_by()	Group by index candidate	
Group-wise	group_by()	Group by one or more variables	
	group_by_key()	Group by key variables	
	gather()	Gather columns into long form	
Pochano	spread()	Spread columns into wide form	
Reshape	nest()	Nest values in a list-variable	
	unnest()	Unnest a list-variable	
	left_join()		
Join tables	$right_{-}join()$		
	$full_join()$	Join two tables together	
	inner_join()		
	$semi_join()$		
	anti_join()		

Friedman & Wand (2008) asserted "No matter how complex and polished the individual operations are, it is often the quality of the glue that most directly determines the power of the system." Each verb works with other transformation family members in harmony. This set of verbs can result in many combinations to prepare tsibble for a broad range of visualization and

modeling problems. Most importantly, the ecosystem for tidy time series analysis has been undertaking on the basis of tsibble in R, known as "tidyverts".

As a special case of data frame, a tsibble pipes into the grammar of graphics straight way, making most use of this powerful graphical system. It should be easy to create and extend some specialist plotting methods based on tsibble structure, such as autocorrelation plots and calendar-based graphics (Wang, Cook & Hyndman 2018).

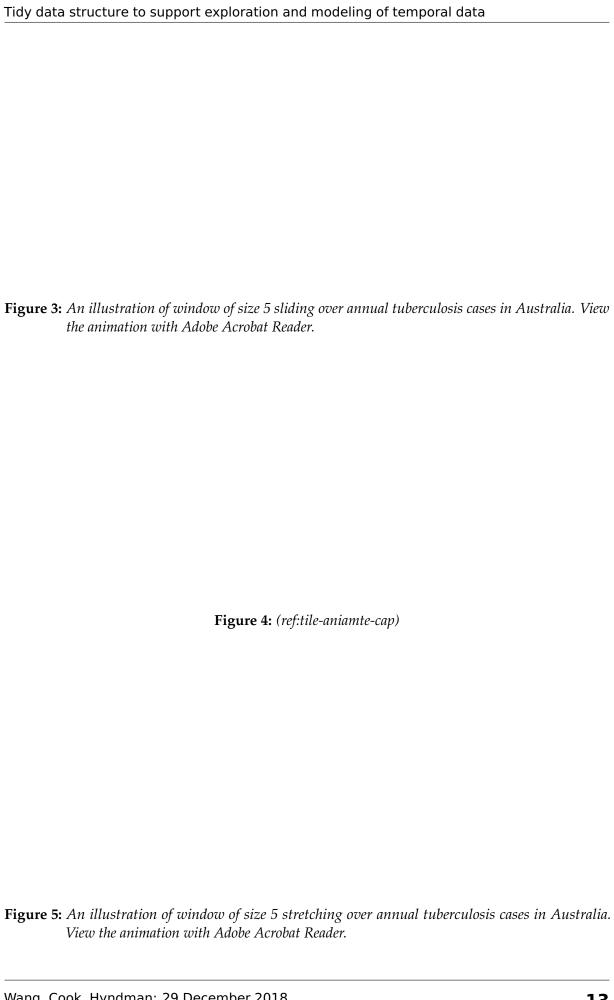
Modeling is crucial to explanatory and predictive analytics, but often imposes stricter assumptions on tsibble data. The verbs listed in Table 2 ease the transition to a tsibble that suits modeling. A tidy forecasting framework built on top of tsibble is under development, which aims at promoting transparent forecasting practices and concise model representation. A tsibble usually contains multiple time series. Batch forecasting will be enabled if a univariate model, such as ARIMA and Exponential Smoothing, is applied to each time series independently. This yields a "mable" (short for model table), where each model only tags to each "key" value in tsibble to avoid expensive data copying and reduce model storage. The mable is further supplied to forecasting methods, to produce a tsibble in which each "key" along with its future time holds predictions. It also underlines the advantage of tsibble's "key" in linking between data inputs, models and forecasts. Advanced forecasting techniques, such as vector autocorrelation, hierarchical reconciliation, and ensembles, can be developed in alike spirit. The modeling module will be fulfilled and integrated eventually.

We go through the whole exploration circle, and keep iterating and refining until data insights gained. The tsibble data structure substantially lubricates between these modules for time-based pipelines. The cohesive and coherent framework results in more graceful and expressive code.

4.2 Rolling window in functional programming

Temporal data often involves moving window calculations. A set of verbs have been implemented to allow for different variations of sliding windows operations:

- slide()/slide2()/pslide(): sliding window with overlapping observations.
- tile()/tile2()/ptile(): tiling window without overlapping observations.
- stretch()/stretch2()/pstretch(): fixing an initial window and expanding to include more observations.



As the name indicates, slide() expects one input, slide2() two inputs, and pslide() multiple inputs. This family of window functions features functional programming. Any function can be mapped and rolled over a block of elements given a specified window size. For type stability, the functions always return lists. Other variants including slide_lgl(), slide_int(), slide_dbl(), slide_chr() return vectors of the corresponding type, as well as slide_dfr() and slide_dfc() for row-binding and column-binding data frames respectively. Their multiprocessing equivalents prefixed by future_ enable rolling in parallel. This family of functions empowers users to incorporate window-related operations in their workflows.

5 Software structure and design decisions

data-centric & human-centered.

5.1 Data first

The prime force that drives the software's design choices is "data". All functions in **tsibble** starts with data or its variants as the first argument, namely "data first". They work naturally with the pipe operator %>%, read as "then". This not only lays out a consistent interface but also addresses the significance of the data throughout the software.

Beyond the tools, the print display provides a quick and comprehensive glimpse of data in temporal context, particularly useful when handling a large collection of data. Below conveys the pieces of critical and contextual picture about the data in Table 1: (1) data dimension with its shorthand time interval, alongside time zone if date-times; (2) variables that constitute of the "key" with the number of series. These details aid users in understanding their data better and manipulate the data with care.

```
#> # A tsibble: 12 x 5 [1Y]
                country, gender [6]
#> # Key:
                 continent gender year count
     country
     <chr>
                 <chr>
                           <chr> <dbl> <dbl>
                         Female 2011
#> 1 Australia
                 Oceania
                                          120
#> 2 Australia
                 Oceania
                           Female 2012
                                          125
#> 3 Australia
                 Oceania
                           Male
                                   2011
                                          176
#> 4 Australia
                 Oceania
                           Male
                                   2012
                                          161
#> 5 New Zealand Oceania
                           Female 2011
                                           36
```

#> # ... with 7 more rows

5.2 Modularity

Modular programming is adopted while designing the **tsibble** package. Modularity benefits users with variety and flexibility and developers with easy maintenance.

All user-facing functions can be roughly organized into three major chunks according to their functionality: vector functions (1d), table verbs (2d), and window family. Each chunk is an independent module, but works interdependently. Vector functions in the package mostly deal with time. When collapsing a tsibble to less granular interval, these atomic functions can be combined with the index_by() table verb to accomplish this. A different function results in easily switching to aggregation of different time resolution. Since these functions are not exclusive to a tsibble, they can be used in a variety of applications in conjunction with other packages. On the other hand, these tsibble verbs can incorporate many third-party vector functions to step out of current tsibble zone. It is generally easier to trace back the errors users encounter from separating 1d and 2d functions. (lost in a web of functions)

5.3 Extensibility

As a fundamental infrastructure, extensibility is a design decision that is focused on from the start of **tsibble**'s development. Contrary to the "data first" principle for end users, extensibility is developer focused and would be mostly used in dependent packages, which heavily relies on S3 classes and methods in R (Wickham 2018). It can be extended in two major aspects: custom index and new tsibble class.

Time representation could be arbitrary, for example R's native POSIXct and Date for versatile date-times, nano time for nanosecond resolution implemented in **nantotime** (Eddelbuettel & Silvestri 2018), and pure numbers in simulations. Yet ordered factors can also be a source of time, such as month names from January to December and weekdays from Monday to Sunday. Tsibble supports an extensive range of index types from numerics to nano time, but there might be custom indices used for some occasions, for example school semesters. These academic terms vary from one institute to another within an academic year, which is defined differently from a calendar year. New index would be immediately recognized by the software upon defining index_valid(), as long as it can be ordered from past to future. The interval regarding semesters is further outlined through pull_interval(). As a result, the rest software methods

such as has_gaps(), count_gaps() and fill_gaps() will have instant support for data that contains this new index.

The class of tsibble is an underlying basis of temporal data, and there is a demand for subclassing a tsibble. For example, a fable is actually an extension to a tsibble, mentioned in Section 4.1. A low-level constructor new_tsibble() provides a vehicle to easily create a new subclass. First of all, this new object itself is a tsibble. It perhaps needs more metadata than those of a tsibble, that gives rise to a new data extension, like prediction distributions to a fable. Tsibble verbs are also S3 generics. Developers will be able to implement these verbs for the new class if needed.

6 Case studies

6.1 On-time performance for domestic flights in U.S.A

The dataset of 2017 on-time performance for US domestic flights represents event-driven data caught in the wild, sourced from US Bureau of Transportation Statistics (Bureau of Transportation Statistics 2018). It contains 5,548,445 operating flights with many measurements (such as departure delay, arrival delay in minutes, and other performance metrics) and detailed flight information (such as origin, destination, plane number and etc.) in a tabular format. This kind of event describes each flight scheduled for departure at a time point in its local time zone. Every single flight would be uniquely identified by the flight number and its scheduled departure time, from a passenger's point of view. In fact, it fails to pass the tsibble hurdle due to duplicates in the original data. An error is immediately raised when attempting to convert this data into a tsibble, and a closer inspection has to be carried out to locate the issue. The **tsibble** package provides tools to easily locate the duplicates in the data with duplicates(). Below shows the problematic entries.

```
flight_num sched_dep_datetime sched_arr_datetime dep_delay arr_delay
          NK630 2017-08-03 17:45:00 2017-08-03 21:00:00
                                                                          194
#> 1
                                                                140
          NK630 2017-08-03 17:45:00 2017-08-03 21:00:00
#> 2
                                                                140
                                                                          194
     carrier tailnum origin dest air_time distance origin_city_name
#> 1
          NK
              N601NK
                        LAX
                             DEN
                                       107
                                                862
                                                         Los Angeles
#> 2
          NK N639NK
                        ORD
                             LGA
                                       107
                                                733
                                                              Chicago
     origin_state dest_city_name dest_state taxi_out taxi_in carrier_delay
#>
```

#> 1	CA	Denver	C0	69	13	0
#> 2	IL	New York	NY	69	13	0
#>	$weather_delay$	nas_delay secu	rity_delay	late_aircr	aft_{delay}	
#> 1	Θ	194	0		0	
#> 2	0	194	0		0	

The issue is perhaps introduced when updating or entering the data into a system. The same flight is scheduled at exactly the same time, together with the same performance statistics but different flight details, which is very unlikely. Flight NK630 is usually scheduled at 17:45 from Chicago to New York, searching into the whole records. A decision is made on removal of the first row from the duplicated entries before proceeding to the tsibble creation.

This dataset is intrinsically heterogeneous, encoding in numbers, strings, and date-times. The tsibble framework, as expected, incorporates this type of data, without the loss of data richness and heterogeneity. To declare the flight data as a valid tsibble, column sched_dep_datetime is specified as "index", column flight_num as "key" via id(flight_num). As a result of event data, this data is irregularly spaced, and hence switching to irregular option is necessary. The program internally validates if the key and index produce the distinct rows, and then sort the key and the index from past to recent. When the tsibble creation is done, the print display is data-oriented and contextually informative, such as dimensions, irregular interval (5,548,444 x 22 [!] <UTC>) and the number of time-based observational units (flight_num [22,562]).

```
#> # A tsibble: 5,548,444 x 22 [!] <UTC>
#> # Key: flight_num [22,562]
```

Transforming tsibble for exploratory data analysis with a suite of time-specific and general-purpose manipulation verbs can result in well-constructed pipelines. From the perspective of a passenger, one need to travel smart, by choosing an efficient carrier to fly with and the time of day to avoid congestion, for example. We take a drill-down approach to exploring this data, starting with annual carrier performance and followed by disaggregating to finer time resolutions.

Figure 6 visually presents the end product of aggregating the number of on-time and delayed flights to the year interval by carriers. This pipeline is initialized defining a new variable if the flight is delayed, and involves summarizing the tallies of on-time and delayed flights for each carrier annually. To prepare the summarized data for a mosaic plot, it is further manipulated

by melting new tallies into a single column. The flow chart shown as Figure 7 demonstrates the operations undertaking in a data pipeline. The input to this pipeline is a tsibble of irregular interval, and the output ends up with a tsibble of unknown interval. The final data is each carrier along with a single year, thereby the interval undetermined. It in turn feeds into the mosaic display. Note that Southwest Airlines, as the largest carrier, operates less efficiently compared to Delta, in Figure 6.

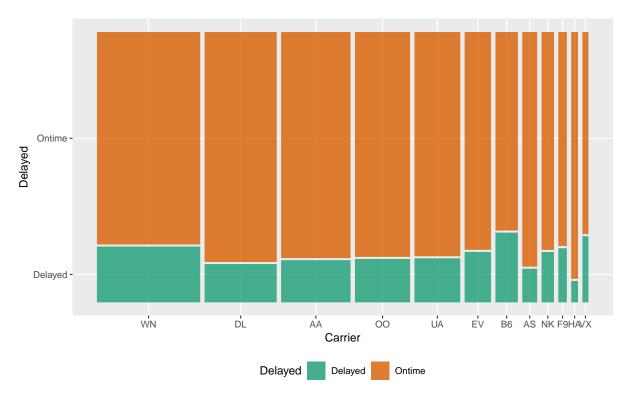


Figure 6: Mosaic plot showing the association between the size of airline carriers and the delayed proportion of departure in 2017. Southwest Airlines is the largest operator, but does not operate as efficient as Delta. Hawaiian Airlines, also as a small operator, outperforms the rest.



Figure 7: Flow chart illustrates the pipeline that pre-processes the data for creating Figure 6.

A closer examination of New York airports will give an indication about how well the busiest airports manage the outflow traffic on a daily basis. A subset that contains observations for EWR, JFK and LGA airports is obtained first. The succeeding operations compute delayed percentages every day at each airport, which are framed as grey lines in Figure 8. LGA fluctuates a lot compared to the other two. What superimposes on these lines is two-month moving averages so that a temporal trend is more visible. The number of days for each month is variable. Moving averages for two months call for computing weighted mean. But this can

also be accomplished using a pair of commonly used verbs—nest() and unnest() to handle list-columns, without worrying weights specification. The sliding with large window size smoothes out the fluctuations and gives a stable trend around 25% over the year.

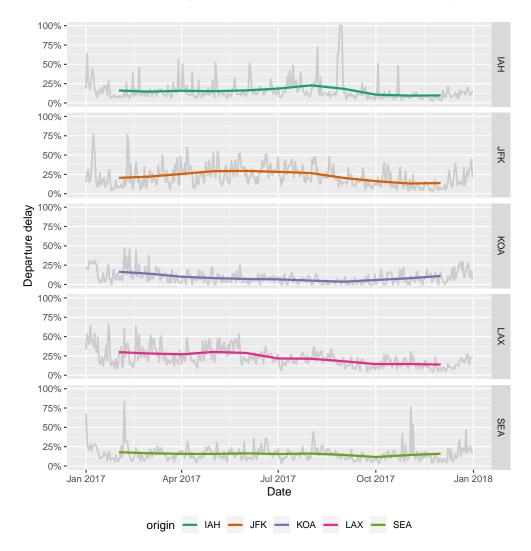


Figure 8: Daily delayed percentages for departure with two-month moving averages overlaid at five international airports. There are many fluctuations observed at LGA airport. The estimates of temporal trend are around 25% across three airports, highlighting relatively less delay in Fall.

What time of day and day of week should we travel to avoid suffering from horrible delay? Figure 9 plots hourly quantile estimates across day of week in the form of small multiples. The upper-tail delay behaviors are of primary interest, and hence 50%, 80% and 95% quantiles are shown. To reduce the likelihood of delay suffering, it is recommended to avoid the peak hour at 18. As moving towards the upper extremes, the variations considerably increase, making departure time unpredictable.

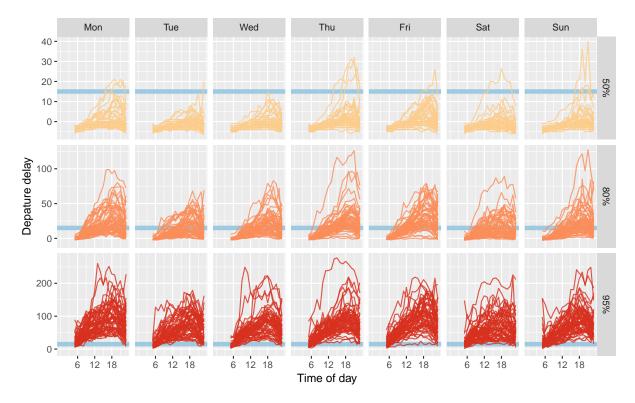


Figure 9: Small multiples of lines about departure delay against time of day, faceting day of week and 50%, 80% and 95% quantiles. A blue horizontal line indicates the 15-minute on-time standard to help grasp the delay severity. Passengers are apt to hold up around 18 during a day, and are recommended to travel early. The variations increase substantially as the upper tails.

6.2 Smart-grid customer data in Australia

Sensors have been put up to collect data for the project of smart city across major cities in Australia. One of the trials is monitoring households' electricity usage through installed smart meters in the area of New Castle over 2010–2014 (Department of the Environment and Energy 2018). Year 2013 has been sliced to examine temporal patterns of customer's energy consumption with **tsibble** in this paper. Half-hourly general supply in kwH have been recored for 2,924 customers in the data set, resulting in 46,102,229 observations in total. Customer's demographic data provides explanatory variables other than time in a different data table. Two data tables might be joined to explore different sources that contribute to daily electricity use when needed.

7 Conclusion and future work

A new data abstraction representing temporal data named as "tsibble" has been proposed, spotlighting the "tidy data" principles brought to time domain. Tidy data begins to take shape in the state of time with the introduction of contextual semantics: index and key. Declared index

provides direct support to time variable; variables that comprise the key defines study subjects over time. These semantics further determines unique data entries required for a valid tsibble. No matter how temporal data arrives, tsibble respects time index and keeps data richness. A tsibble frictionlessly pops into transformation, visualization, modelling and smoothly shifts amongst, allowing for rapid iterations in gaining data insights.

A missing piece of the *tsibble* data is to enable user-defined calendars and respect structural missing observations. For example, a call center operates only between 9:00am and 5:00pm on week days and stock trading resumes on Monday straight after Friday. No data available outside trading hours would be labelled as structural missingess, which *tsibble* currently disregards. However, few R packages provide functionality to create and manage many sorts of calendars, including market-specific business calendar. This delays the implementation. Generally, custom calendars would be easily embedded into the tsibble framework. Consequently these tsibble operators, like fill_gaps(), would work out of box; forecasts would be generated within its definable time range.

The **tsibble** package provides an elegant solution to manage and manipulate medium-sized temporal data in memory.

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