

# SACE MEETING #5

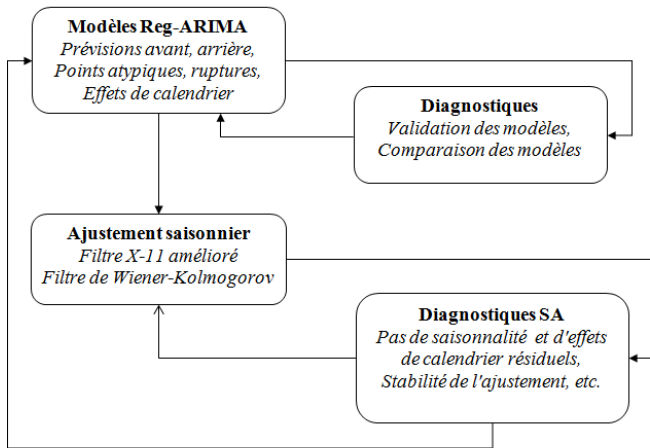


## Stability of Reg-ARIMA estimates: the case of leap year and outliers

DOMINIQUE LADIRAY ET ALAIN QUARTIER-LA-TENTE  
Insee, Seasonal Adjustment Centre of Excellence (SACE)

# Introduction to the seasonal adjustment procedure

## X-13ARIMA-SEATS et TRAMO-SEATS Procédure d'ajustement saisonnier



# Mathematical Writing of Reg-ARIMA

Mathematical writing of the Reg-ARIMA Model in Seasonal Adjustment:

$$\left. \begin{array}{l} \text{Additive:} \\ \text{Multiplicative:} \end{array} \right\} \begin{array}{l} Y_t \\ \log(Y_t) \end{array} = \underbrace{\beta_0 LY_t + \beta_1 WD_t}_{\text{WD regressors}} + \underbrace{\sum_i \gamma_i O_{i,t}}_{\text{outliers}} + \underbrace{\varepsilon_t}_{\sim \text{ARIMA}}$$

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The goal of the study: illustrate some problems of instability of the estimates with examples on:

- the leap year adjustment
- the outliers estimates
- the identification of the ARIMA model

# Sommaire

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## 1. The leap year adjustment

- 1.1 How and when carry out the leap year adjustment?
- 1.2 Methodology of the study
- 1.3 Examples
- 1.4 Results

## 2. Outliers adjustment

## 3. Identification of the ARIMA model

## 4. Conclusion and recommendations

# When carry out the leapy year adjustment?

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A leap year: one additional day in February  $\simeq$  every 4 years

→ takes into account the “length of the month” effect: it is a calendar effect

When to correct it ?

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Study of European IPI (1330 series): the leap year effect exists (but not always measurable due to collection)



# To methods to proceed to the adjustment

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## 1. With the Reg-ARIMA model:

$$LY_t = \begin{cases} 0.75 & \text{in February during leap years} \\ -0.25 & \text{in February during non leap years} \\ 0 & \text{for all other months} \end{cases}$$

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2. Correcting values prior to modelling multiplying by a fixed proportion:

$$\begin{cases} \frac{28.25}{29} \simeq 0.974 & \text{in February during leap years} \\ \frac{28.25}{28} \simeq 1.009 & \text{in February during non leap years} \\ 1 & \text{for all other months} \end{cases}$$

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→ Study of estimates of the 1st method

# Methodology used

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# Methodology used

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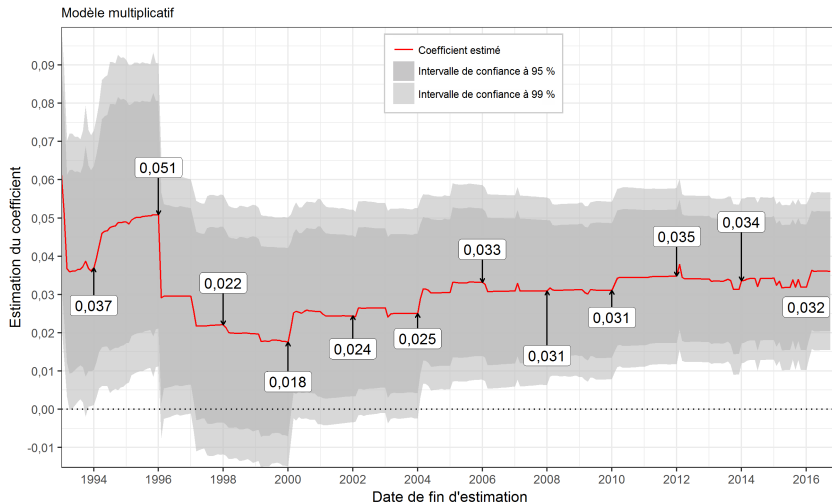
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We considered that the estimate has converged whe the estimated coefficient remains:

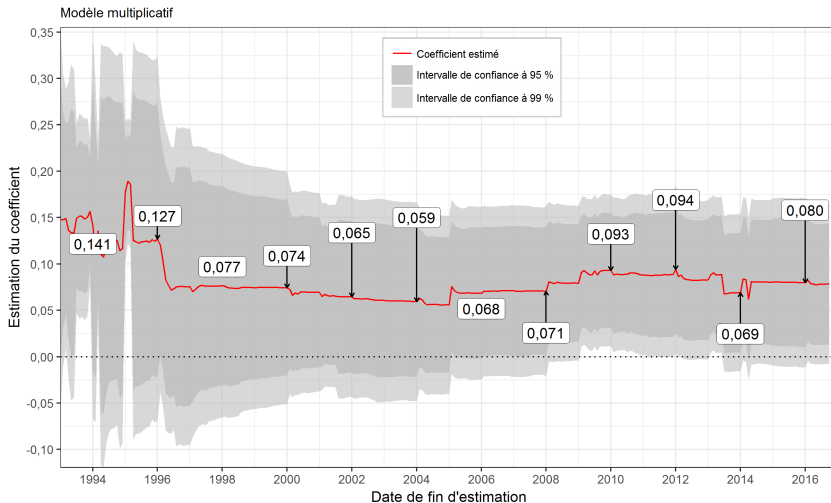
- positive
- not significantly different from last estimation
- significant: stability of the choice to adjust the leap year effect

⇒ European IPI: 410 converge

# Examples (1/2): IPI FR-0610 (extraction of crude petroleum)

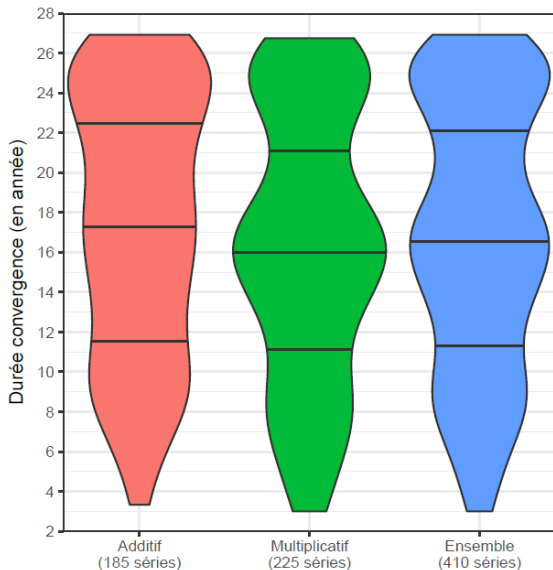


## Examples (2/2): IPI FR-1391 (manufacture of knitted and crocheted fabrics)

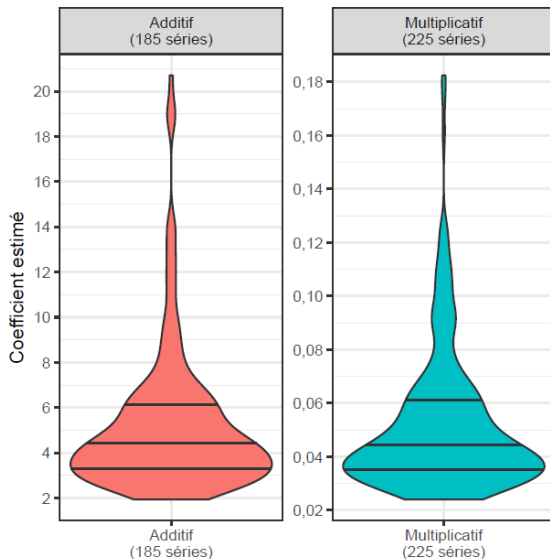




# A rather slow convergence...



## ... Towards a value not always coherent



# Comparison of the two correction methods

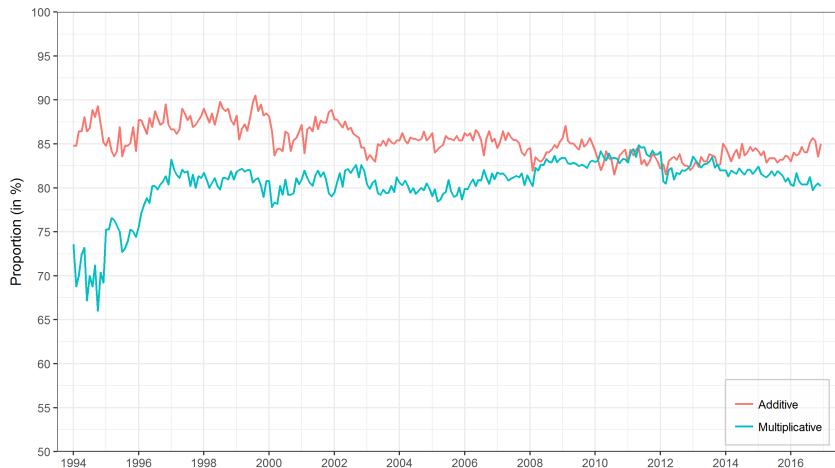


Figure 1: Percentage of series for which the AICC of the 2nd method (LY pre-adjustment) is lower than the AICC of the 1st method (LY regressor)

# Sommaire

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## 1. The leap year adjustment

## 2. Outliers adjustment

### 2.1 Usuals outliers

### 2.2 Methodology of the study

### 2.3 Example

### 2.4 Résultats des simulations

## 3. Identification of the ARIMA model

## 4. Conclusion and recommendations

# Usuals outliers

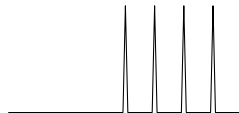
**Additive outlier (AO)**



**Level Shift (LS)**



**Seasonal Outlier (SO)**



**Transitory Change (TC)**



# Methodology used

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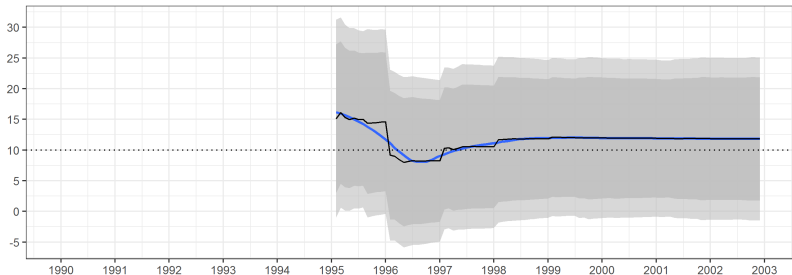
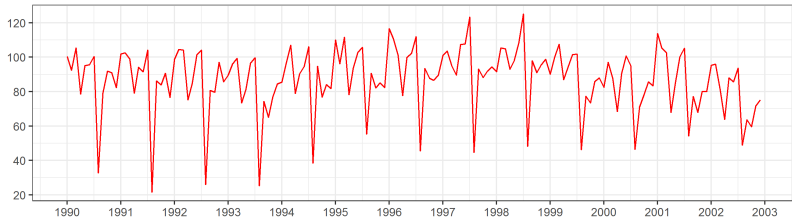
On European IPI: 1. **identification** and **estimation** of the model over 12 years

2. The raw series is corrected for outliers in the year of the introduction of the break and it is rebased to 100 at the month of the introduction of the break
3. simulation of a break, 5 years after the beginning of the time series date, of level 10 for a **additive** model
4. The regressor related to the simulated break is added to the Reg-ARIMA model and its coefficient it is estimated by freezing the estimates of all other parameters and **setting** the first estimated date

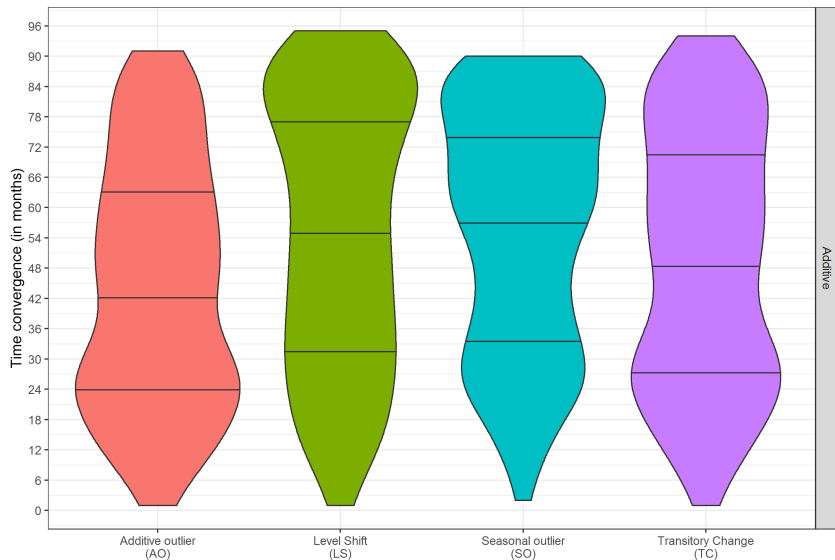
We considered that the series has converged when:

$$\left| \frac{\text{estimated value}}{\text{last estimated value}} - 1 \right| < 5 \%$$

# Example of a AO for IPI IT-1413 (manufacture of other outerwear)



# A rather slow convergence..





... But not always to the right value

	Minimum	25 %	50 %	75 %	Maximum
<b>Additive models</b>					
Additive outlier (AO)	-11.6	7.8	11.1	14.2	36.9
Level Shift (LS)	-11.4	5.6	9.3	12.7	49.8
Seasonal outlier (SO)	-5.8	7.3	8.8	11.0	31.1
Transitory Change (TC)	-17.4	6.5	10.2	14.1	47.2

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# Identification of two equivalent models

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We use the same model in two different forms mathematically equivalent:

1. The leap year regressor is added as a working days regressor
2. The leap year regressor is added as an external regressor

→ study of the automatic models



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## Conclusion and recommendations (1/2)

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Simulations are **questionables** and **can be improved** but highlight a **potential instability** of Reg-ARIMA models often used as black boxes


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Instabilities have a **limited effect** on the SA-WD series. . .  but have an impact on the **short term** history and on **revisions** !

## Conclusion and recommendations (1/2)

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Simulations are questionable and can be improved but highlight a potential instability of Reg-ARIMA models often used as black boxes



Instabilities have a limited effect on the SA-WD series. . .



but have an impact on the short term history and on revisions !




Automatic algorithms use in X-13ARIMA-SEATS and TRAMO-SEATS are **important** and very **useful**



## Conclusion and recommendations (2/2)

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Specify the model **beforehand** at the level of the series **series**:

- base selection procedures on economic reasoning (pay attention to long series)
-  do not use methods like black boxes. . .

## Conclusion and recommendations (2/2)

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Specify the model **beforehand** at the level of the series **series**:

- base selection procedures on economic reasoning (pay attention to long series)
-  do not use methods like black boxes. . . Otherwise, you will be like this statistician who. . .

# Thank you for your attention

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*"He uses statistics as a drunk man uses lamp-posts: for support rather than for illumination.*

Quote widely attributed to Andrew Lang (1844-1912)