



# The (In)stability of Reg-Arima Estimations

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# Outline

- 1 Introduction
- 2 Estimation of the Leap-Year Effect
  - How and when carry out the leap year adjustment?
  - Methodology of the study
  - Examples
  - Results
- 3 Outliers
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  - Example
  - Results
- 4 Identification of the ARIMA model
- 5 Conclusion

Never, never forget. . .

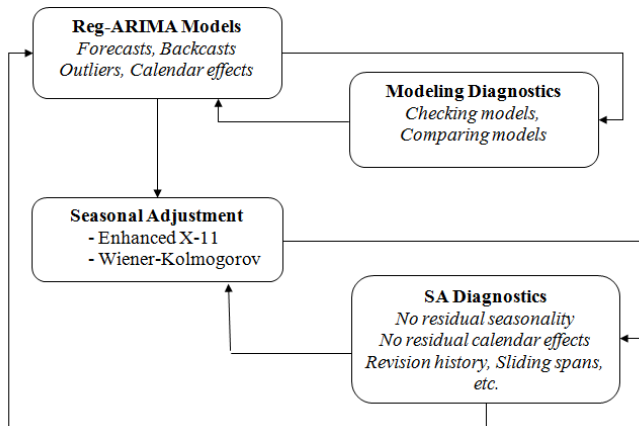
“All models are false, but some are  
useful”

George E. P. Box

Box, G.E.P. (1979), “Robustness in the Strategy of Scientific Model Building”, in R.L. Launer and G.N. Wilkinson (eds.), Robustness in Statistics: Proceedings of a Workshop, Academic Press.

# The 2-Step Seasonal Adjustment Procedure

## X-13ARIMA-SEATS and TRAMO-SEATS Seasonal Adjustment Process



# Reg-ARIMA modelling

The Reg-ARIMA Model commonly used in SA can be written:

$$\left. \begin{array}{l} \text{Additive:} \\ \text{Multiplicative:} \end{array} \right\} \begin{array}{l} Y_t \\ \log(Y_t) \end{array} = \underbrace{\beta_0 LY_t + \beta_1 WD_t}_{\text{WD regressors}} + \underbrace{\sum_i \gamma_i O_{i,t}}_{\text{outliers}} + \underbrace{\varepsilon_t}_{\sim \text{ARIMA}}$$

The main objective of the presentation is to illustrate potential instability problems in the estimations. We focus on 3 examples:

- Leap Year effect
- Outliers estimates
- Identification of the ARIMA model

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# The Leap-Year Effect

- The Gregorian calendar is a solar calendar where the length of the year is supposed to represent the time the Earth takes to make a complete revolution around the Sun.
- To achieve this equality on the long run, a day is added to February if the year is divisible by 4 but not by 100, unless the year is also divisible by 400.
- The Leap-Year effect is therefore a calendar effect which estimates the impact of this extra day.
- According to the “ESS Guidelines on SA”:
  - CA should be done for those time series for which there is an economic rationale for the existence of calendar effects and statistical evidence.
  - Moreover, CA should not result in frequent large revisions when additional data become available, if it does, it is an indication that the method's estimates are not reliable.

# Estimation of the Leap-Year Effect

Two main methods:

- 1 Using the Reg-ARIMA model with a specific regressor:

$$LY_t = \begin{cases} 0.75 & \text{for leap year Februaries} \\ -0.25 & \text{for non leap year Februaries} \\ 0 & \text{Otherwise} \end{cases}$$

- 2 Pre-adjustment of February values (X12-ARIMA, see Bell[1992]):

$$\begin{cases} \frac{28.25}{29} \simeq 0.974 & \text{for leap year Februaries} \\ \frac{28.25}{28} \simeq 1.009 & \text{for non leap year Februaries} \\ 1 & \text{Otherwise} \end{cases}$$



# Methodology (1/2)

To assess the quality of the Leap Year estimate using Reg-Arima model, we use the following methodology:

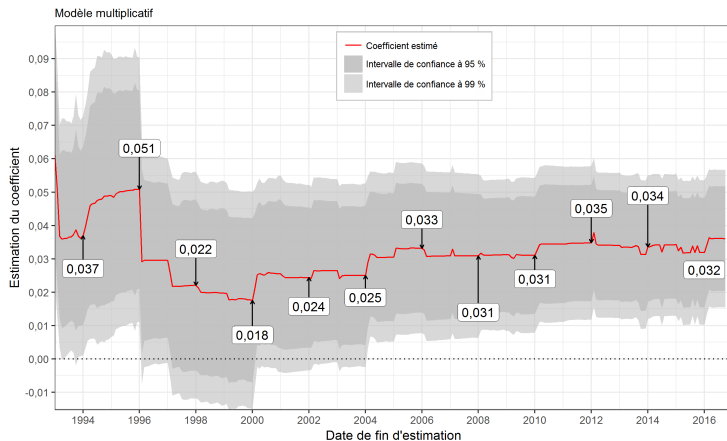
- We use the European monthly industrial production indexes and turnover indexes (NACE rev. 2 at 2, 3 and 4 digits).
  - These series are likely to present a leap year effect. We focus on the 2 198 series longer than 12 years only.
- Step 1: For each series the decomposition model, the ARIMA model, outliers and trading-day effects are identified and estimated on the complete span.
- Step 2: Then, the reg-ARIMA model is re-estimated on the 48 first observations.
- Step 3: The process is repeated adding each time a new observation. Thus, for a 13-year series, we will obtain  $12 \times 13 - 48 = 108$  estimations of the LY coefficient.

## Methodology (2/2)

- These simulations allows studying the convergence of the LY coefficient.
- We assume that the convergence is reached when: (1) the LY coefficient remains positive (2) significant and (3) when the last estimations are not statistically different.
- Other specifications have been tested (changing the first estimation period, ARIMA model not fixed etc.) with similar results.
- We present here the results for the 410 IPI series which reached convergence.

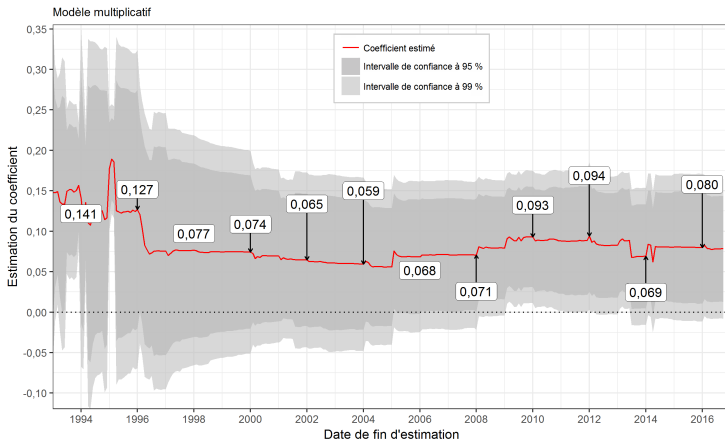
# Examples (1/2)

Series IPI FR-0610: extraction of crude petroleum.



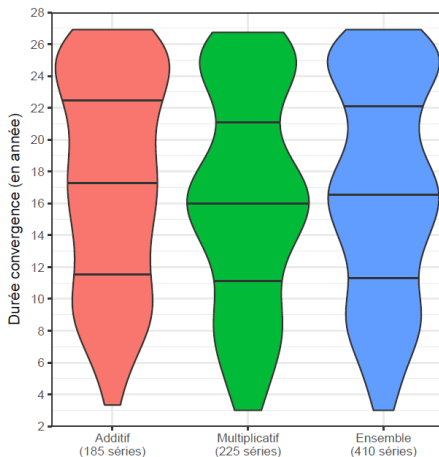
# Examples (2/2)

Series IPI FR-1391: manufacture of knitted and crocheted fabrics.



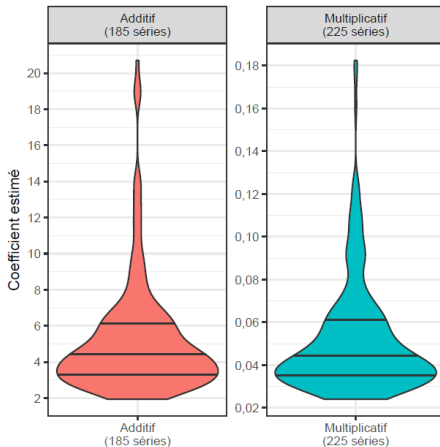
# A pretty slow convergence...

For 50% of the series, more than 18 years of observations are required for the estimation to converge.



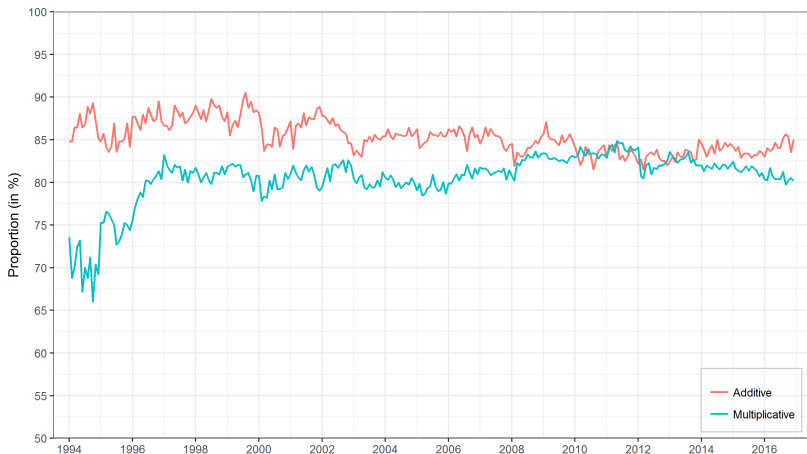
# ... Towards a sometimes curious value

For at least 25% of the series, the convergence value looks suspect.



# Comparison of the two correction methods

Percentage of series for which the AICC of the pre-adjustment method is lower than the AICC of the Reg-Arima method (on the 2 198 series).



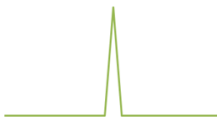
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# Usuals outliers

Additive Outlier (AO)



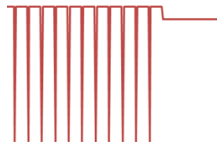
Level Shift (LS)



Transitory Change (TC)



Seasonal Outlier (SO)

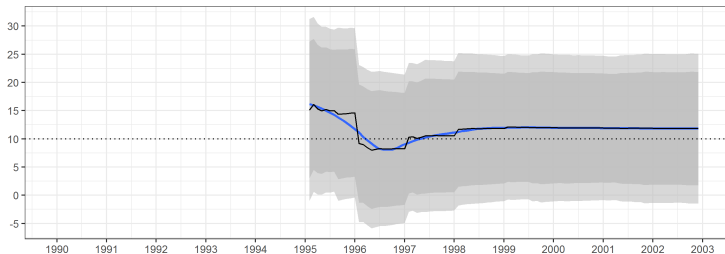
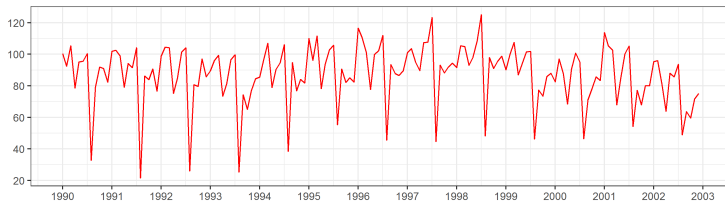


# Methodology

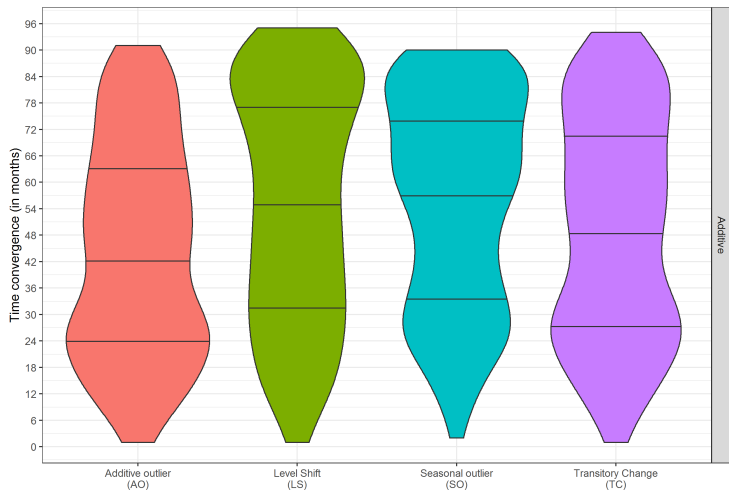
- 1 Simulations done on the European IPIs, NACE2, 4 digits;
- 2 We keep the 12 first years of observations. The decomposition model, the ARIMA model, outliers and TD effect are identified and estimated on the 12 years. The decomposition model and the ARIMA model are kept fixed for the study;
- 3 The rupture will be introduced at observation 49 so:
  - The series is corrected for any outlier detected at observations 49 to 50 (one year).
  - To facilitate the estimations and the comparisons, each series is rebased at 100 at observation 49;
- 4 The rupture is introduced with a level 10 for an additive model and 1.1 for a multiplicative model;
- 5 The estimation of the outlier coefficient is done adding each time a new observation. Thus, for a 12-year series, we obtain  $12 \times 12 - 48 = 96$  estimations of the coefficient.
- 6 We assume that the convergence is reached when
$$\left| \frac{\text{estimated value}}{\text{last estimated value}} - 1 \right| < 5 \%$$

# Example

IPI IT-1413 (manufacture of other outerwear): AO introduced in January 1995.



# Results: A rather slow convergence...



... And not always to the correct value

	Minimum	25 %	50 %	75 %	Maximum
<b>Additive Models</b>					
Additive outlier (AO)	-11.6	7.8	11.1	14.2	36.9
Level Shift (LS)	-11.4	5.6	9.3	12.7	49.8
Seasonal outlier (SO)	-5.8	7.3	8.8	11.0	31.1
Transitory Change (TC)	-17.4	6.5	10.2	14.1	47.2

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# Identification of two “equivalent” models

We use the same leap year regressor in 2 different, but mathematically equivalent, forms:

- 1 The leap year regressor is added in the trading-day regressors;
- 2 The leap year regressor is added as an external (not calendar) regressor.

→ and we run an AMI.

# An example where we get quite different models

## Le régresseur LY est dans les effets de calendrier

### Summary

Estimation span: [1-1990 - 11-2016]

323 observations

Trading days effects (7 variables)

3 detected outliers

### Arima model

[(2,0,0)(0,1,1)]

	Coefficients	T-Stat	P[ T  > t]
Phi(1)	-0,5256	-9,46	0,0000
Phi(2)	-0,2878	-5,17	0,0000
BTheta(1)	-0,7913	-20,56	0,0000

### Correlation of the estimates

	Phi(1)	Phi(2)	BTheta(1)
Phi(1)	1,0000	-0,7388	-0,0184
Phi(2)	-0,7388	1,0000	0,0489
BTheta(1)	-0,0184	0,0489	1,0000

### Leap year

	Coefficients	T-Stat	P[ T  > t]
Leap year	4,3861	2,65	0,0085

## Le régresseur LY est dans les régresseurs externes

### Summary

Estimation span: [1-1990 - 11-2016]

323 observations

No trading days effects

8 detected outliers

### Arima model

[(0,1,1)(0,1,1)]

	Coefficients	T-Stat	P[ T  > t]
Theta(1)	-0,5051	-10,08	0,0000
BTheta(1)	-0,7533	-18,80	0,0000

### Correlation of the estimates

	Theta(1)	BTheta(1)
Theta(1)	1,0000	0,0280
BTheta(1)	0,0280	1,0000

### User variables

	Coefficients	T-Stat	P[ T  > t]
Leap year	4,5569	2,92	0,0038



# Conclusions



These simulations are certainly questionable and can be improved; but they highlight the instability of Reg-ARIMA models often used as black boxes.



These instabilities usually have a limited effect on the SCA



series. . . but might have an impact on the short term history and on revisions.



Automatic algorithms in X-13ARIMA-SEATS and TRAMO-SEATS are important and useful but do not prevent you from a precise specification of the model for each series.



Remains at the end that it is difficult to estimate some effects. For example, the estimation of a LY effect requires a long series; but in this case it will be difficult to suppose ONE Arima model for the time span.