



Asymmetric Linear Filters for Seasonal Adjustment Applications to the COVID-19

ALAIN QUARTIER-LA-TENTE (LEMNA, INSEE)

Ongoing research under supervision of:

Dominique Ladiray (Independent) and Olivier Darné (Lemna)

With the help of Jean Palate (NBB)

Introduction (1/2)

Ongoing research real-time detection of turning points with linear filters

- ➔ Under supervision of Dominique Ladiray and Olivier Darné
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In this presentation:

- First results comparing 4 methods for trend-cycle extraction:
 - Current X-13ARIMA algorithm (Henderson filter)
 - Local Polynomial filters (Proietti and Luati (2008))
 - Fidelity-Smoothness-Timeliness approach (Grun-Rehomme, Guggemos, and Ladiray (2018))
 - RKHS filters (Dagum and Bianconcini (2008))


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 - RKHS filters (Dagum and Bianconcini (2008))
-  package `rjdfilters` (<https://github.com/palatej/rjdfilters>, development version: <https://github.com/AQLT/rjdfilters>)

Introduction (2/2)

A raw time series can be decompose as (additive decomposition):

$$X_t = \underbrace{TC_t}_{\text{trend-cycle}} + \underbrace{S_t}_{\text{seasonality}} + \underbrace{I_t}_{\text{irregular}}$$

And TC_t generally estimated on a series *without* seasonality

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$$M_{\theta}(X_t) = \sum_{k=-p}^{+f} \theta_k X_{t+k}$$

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- ➡ For **real-time estimates**, we must rely on *asymmetric* filters ($p > f$): revisions and delay in turning points detection (*phase-shift*): this is the case of the COVID-19

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- ➡ Comparison of 3 methods that could be included in X-13-ARIMA

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1. Introduction

2. Description of the methods

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2.2 Local Polynomials

2.3 Linear Filters and Reproducing Kernel Hilbert Space (RKHS)

2.4 Minimization under constraints: FST approach

3. Comparison of the methods

4. Conclusion

X-13-ARIMA

1. Series extend over 1 year by ARIMA model
2. Trend-Cycle component extracted using symmetric **Henderson** moving average

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 - ➡ X-11: iteratively decomposes X_T in TC_t , S_t and I_t with automatic outlier correction
 - ➡ Comparison of 3 alternatives modern approaches that can reproduce Henderson filter

Local polynomials: rjdfilters::lp_filter()

Assumption: $y_t = \mu_t + \varepsilon_t$ with $\varepsilon_t \stackrel{i.i.d}{\sim} \mathcal{N}(0, \sigma^2)$

μ_t locally approximated by polynomial of degree d :

$$\forall j \in \llbracket -h, h \rrbracket : y_{t+j} = m_{t+j} + \varepsilon_{t+j}, \quad m_{t+j} = \sum_{i=0}^d \beta_i j^i$$

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Estimation using WLS using *kernels*: $\hat{\beta} = (X' K X)^{-1} X' K y$ and

$$\hat{m}_t = \hat{\beta}_0 = w' y = \sum_{j=-h}^h w_j y_{t-j} \Rightarrow \text{equivalent to symmetric moving average}$$

\Rightarrow Henderson filter using a specific kernel and $d = 3$.

Asymmetric filters: `rjdfilters::lp_filter()`

Several solutions:

1. Same method with less data (DAF) \iff Minimize revisions under same polynomial constraints (reproduce cubic trend)

➡ **no bias but lots of variance**

Asymmetric filters: `rjdfilters::lp_filter()`

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2. Minimization of revisions filter under polynomial constraints:

2.1 *Linear-Constant* (LC): y_t linear and v reproduce constant trends (*Musgrave filter*)

2.2 *Quadratic-Linear* (QL): y_t quadratic and v reproduce linear trends

2.3 *Cubic-Quadratic* (CQ): y_t cubic and v reproduce quadratic trends

➡ Asymmetric filters v depends on a ratio linked to “IC-Ratio”

Asymmetric filters: `rjdfilters::lp_filter()`

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 Asymmetric filters v depends on a ratio linked to “IC-Ratio”



simple models with easy interpretation



Timeliness not controlled  method extended in `rjdfilters::lp_filter()`

RKHS filters: rjdfilters::rkhs_filter()

- RKHS theory used to approximate Henderson filter
- With K_p the **kernel function**, the symmetric filter:

$$\forall j \in \llbracket -h, h \rrbracket : w_j = \frac{K_p(j/b)}{\sum_{i=-h}^h K_p(i/b)}$$

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- For asymmetric filters:

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➡ with $b = h + 1$ and a specific K_p you have the Henderson filter

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➡ b chosen by optimization, e.g. minimizing revisions linked to phase-shift:

$$b_{q,\varphi} = \min_{b_q} \int_0^{2\pi/12} \rho_s(\lambda) \rho_\theta(\lambda) \sin^2 \left(\frac{\varphi_\theta(\omega)}{2} \right) d\omega$$

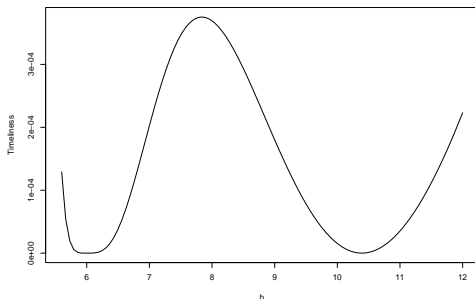
Filtres asymétriques



several local extremum

```
fun <- rkhs_optimization_fun(horizon = 6,
                             leads = 5, degree = 3,
                             asymmetricCriterion = "Timeliness")
plot(fun, 5.6, 12, xlab = "b",
      ylab = "Timeliness", main = "6X5 filter")
```

6X5 filter



```
rkhs_optimal_bw()
```

```
##      q=0      q=1      q=2      q=3      q=4      q=5
## 6.0000 6.0000 6.3875 8.1500 9.3500 6.0000
```



Generalizable to
create filters that could
be applied to irregular
frequency series

FST approach: `rjdfilters::fst_filter()`

Minimization of a weighted sum of 3 criteria under polynomial constraints:

$$\begin{cases} \min_{\theta} & J(\theta) = \alpha F_g(\theta) + \beta S_g(\theta) + \gamma T_g(\theta) \\ \text{s.c.} & C\theta = a \end{cases}$$




F_g : Fidelity (variance reduction ratio), S_g : Smoothness (Henderson criterion), T_g timeliness (phase-shift)

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-  Unique solution
-  Asymmetric filters independent of data and symmetric filter
-  Non-normalized weights

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1. Introduction

2. Description of the methods

3. Comparison of the methods

3.1 Methodology

3.2 Time delay

3.3 Revision

3.4 Some examples

4. Conclusion

Methodology

2 404 calendar adjusted series (`sts_inpr_m`, industrial production indices of EU):

1. Seasonal adjustment with X-13ARIMA (RJDemetra::x13) for each date to extract: linearized component, length of trend and seasonal filters, decomposition mode and I-C ratio

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2. Seasonal adjustment using *fixed* linearized component (est. overall period) and same length/decomposition/I-C ratio with X-11 using custom trend-cycle filters (`rjdfilters::x11()`).

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3. For each estimate, downturns and upturns:
 - upturn: $y_{t-3} \geq \dots \geq y_{t-1} < y_t \leq y_{t+1}$
 - downturn: $y_{t-3} \leq \dots \leq y_{t-1} > y_t \geq y_{t+1}$

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Time-delay: time to detect the correct turning point without further revisions

Methods compared: RKHS minimizing phase-shift and local polynomial filters

Time delay to detect turning points in 2020

For series for which the optimal trend-cycle symmetric filter is of length 13 (900 series)

	X-13-ARIMA	RKHS	LC	QL	CQ	DAF
Min	2.0	2.00	2.00	2.00	2.00	2.00
D1	2.0	5.00	3.00	2.00	2.00	2.00
D2	3.0	5.00	3.00	3.00	2.00	2.00
D3	3.0	5.00	4.00	3.00	3.00	3.00
D4	3.0	5.00	4.00	3.00	5.00	3.00
Median	4.0	5.00	4.00	4.00	6.00	5.00
D6	4.0	7.00	4.00	5.00	6.00	6.00
D7	4.0	7.00	5.00	7.00	7.00	7.00
D8	5.0	7.00	5.00	7.00	7.00	7.00
D9	9.0	9.00	8.00	9.00	9.00	9.00
Max	14.0	14.00	14.00	14.00	14.00	14.00
Mean	4.4	6.29	4.69	4.97	5.32	5.09

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MAE in 2020

For series for which the optimal trend-cycle symmetric filter is of length 13

R_t : relative revision error between first and last estimates.

Distribution of $\frac{MAE(R_t)}{MAE(R_t^{X-13})}$

	RKHS	LC	QL	CQ	DAF
Min	0.4	0.5	0.5	0.5	0.5
D1	0.9	0.9	1.1	1.1	1.1
D2	1.0	1.0	1.3	1.4	1.3
D3	1.1	1.1	1.4	1.5	1.5
D4	1.1	1.2	1.6	1.7	1.6
Median	1.2	1.3	1.7	1.8	1.8
D6	1.3	1.4	1.9	2.0	1.9
D7	1.4	1.5	2.0	2.3	2.2
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D3	1.1	1.1	1.4	1.5	1.5
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D6	1.3	1.4	1.9	2.0	1.9
D7	1.4	1.5	2.0	2.3	2.2
D8	1.5	1.6	2.3	2.6	2.4
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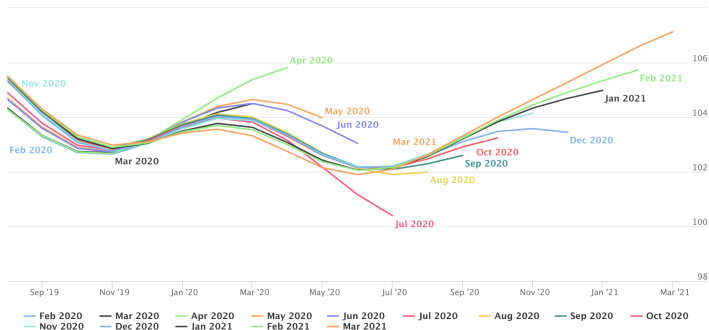
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IPI in the manufacture of fabricated metal products, except machinery and equipment (C25) in Sweden (turning point in February 2020)

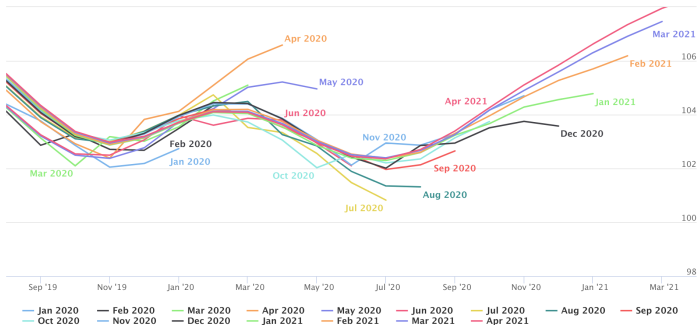
Trend-cycle estimation of the series C25_SE with the method X12-ARIMA

Time-delay = 5 months



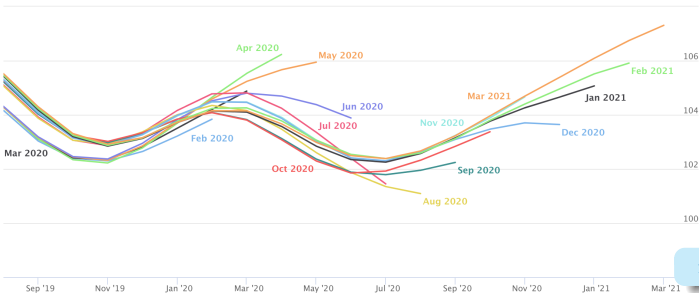
Trend-cycle estimation of the series C25_SE with the method RKHS

Time-delay = 13 months



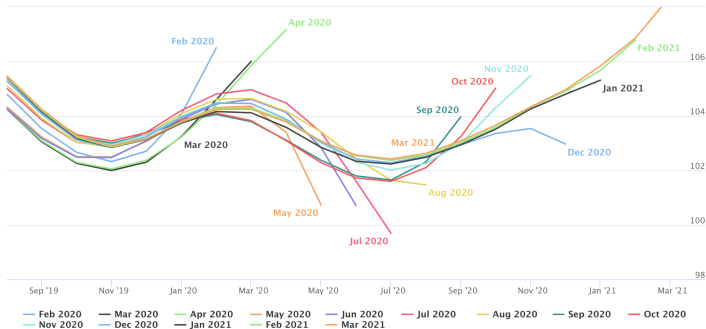
Trend-cycle estimation of the series C25_SE with the method LC

Time-delay = 13 months



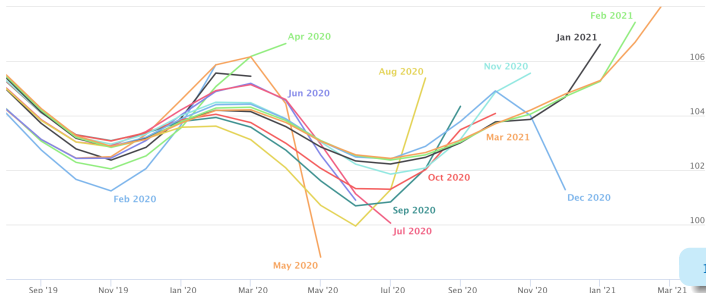
Trend-cycle estimation of the series C25_SE with the method QL

Time-delay = 14 months



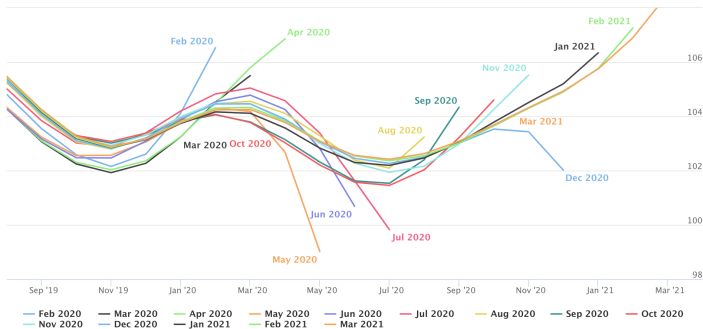
Trend-cycle estimation of the series C25_SE with the method CQ

Time-delay = 14 months



Trend-cycle estimation of the series C25_SE with the method DAF

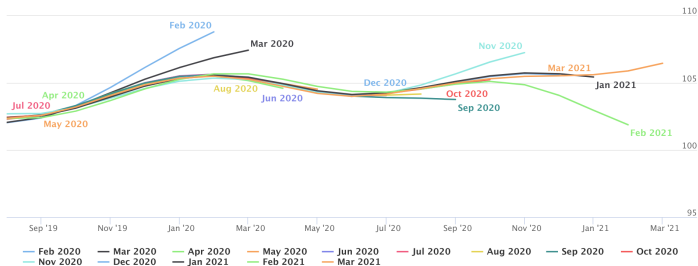
Time-delay = 14 months



IPI in the manufacture of cement, lime and plaster (C235) in Germany (turning point in February 2020)

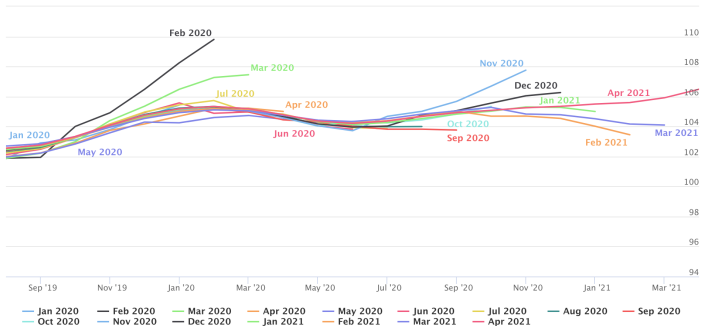
Trend-cycle estimation of the series C235_DE with the method X12-ARIMA

Time-delay = 13 months



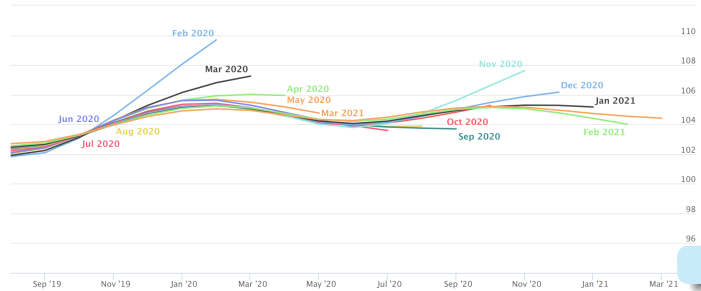
Trend-cycle estimation of the series C235_DE with the method RKHS

Time-delay = 5 months



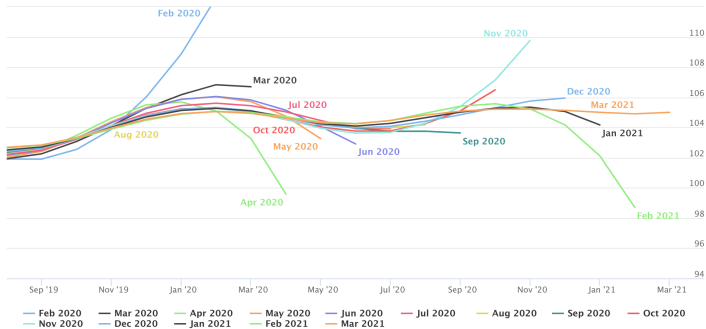
Trend-cycle estimation of the series C235_DE with the method LC

Time-delay = 3 months



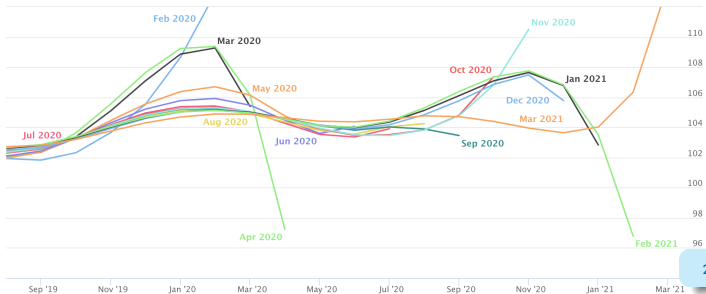
Trend-cycle estimation of the series C235_DE with the method QL

Time-delay = 3 months



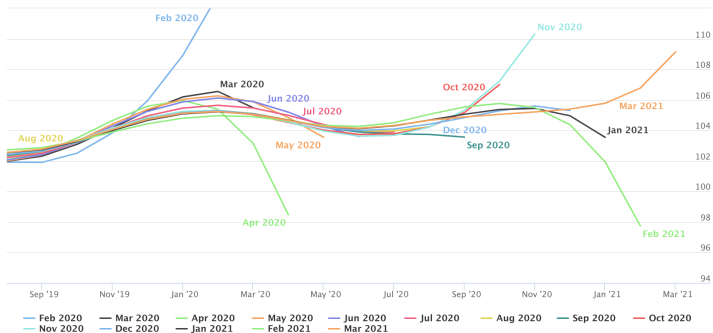
Trend-cycle estimation of the series C235_DE with the method CQ

Time-delay = 2 months



Trend-cycle estimation of the series C235_DE with the method DAF

Time-delay = 3 months



Conclusion

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- During the COVID-19, the current X-13-ARIMA algorithm seems to produce on average satisfying results
- In some cases, we could prefer others trend-cycle filters ➡ `rjdfilters` can help

What next?

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- FST can lead to filters that performs better in terms of Fidelity, Smoothness, Timeliness than:
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- Impact of outliers? Study of robust methods?

Thanks for your attention

🔗 package: 🍷 palatej/rjdfilters

About me: 🍷 AQLT

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