

1. There are n people at a party. Each person shakes hands with every other person. How many handshakes take place?

2. Consider the graph with the following adjacency matrix.

| | A | B | C | D | E | F | G |
|---|---|----|---|---|----|---|----|
| A | 0 | 10 | 6 | 4 | 0 | 7 | 0 |
| B | 0 | 0 | 9 | 0 | 11 | 0 | 18 |
| C | 6 | 9 | 0 | 1 | 1 | 0 | 0 |
| D | 4 | 0 | 1 | 0 | 1 | 2 | 0 |
| E | 0 | 0 | 1 | 1 | 0 | 0 | 14 |
| F | 7 | 0 | 0 | 2 | 0 | 0 | 15 |
| G | 0 | 18 | 0 | 0 | 0 | 0 | 0 |

- a. Draw a picture of the graph represented by this adjacency matrix S without the weights.
- b. Is the graph directed or undirected? Explain.
- c. List the vertices in depth-first order beginning with Vertex A. When there is a choice, process the vertices and edges from left to right.

3. A claim is made that a complete directed graph of n vertices has $n(n-1)$ edges, while a complete undirected graph of n vertices has $n(n-1)/2$ edges. Is this claim true? If so outline a proof. If not, give a counter example.

4. We have a max-heap where nodes are given IDs starting at 0 for the root node, 1 for the left child, and 2 for the right child. We increase node IDs as we move from left to right across one level of the tree.

Identify a pattern for moving from a node with label j to its left child and right child. What labels would be found on the left and right children of node j ?