

CS & IT ENGINEERING

Data Structure



Tree
Chapter- 5
Lec- 10



By- Pankaj Sharma sir

TOPICS TO BE
COVERED

Tree-X

infix : $a \times b + e/f - g$

\times $/$
 $+$ $-$

Expression tree :

leaf : Operands

Internal
nodes : operators



$\Rightarrow a \times b$

inorder : $a \times b$

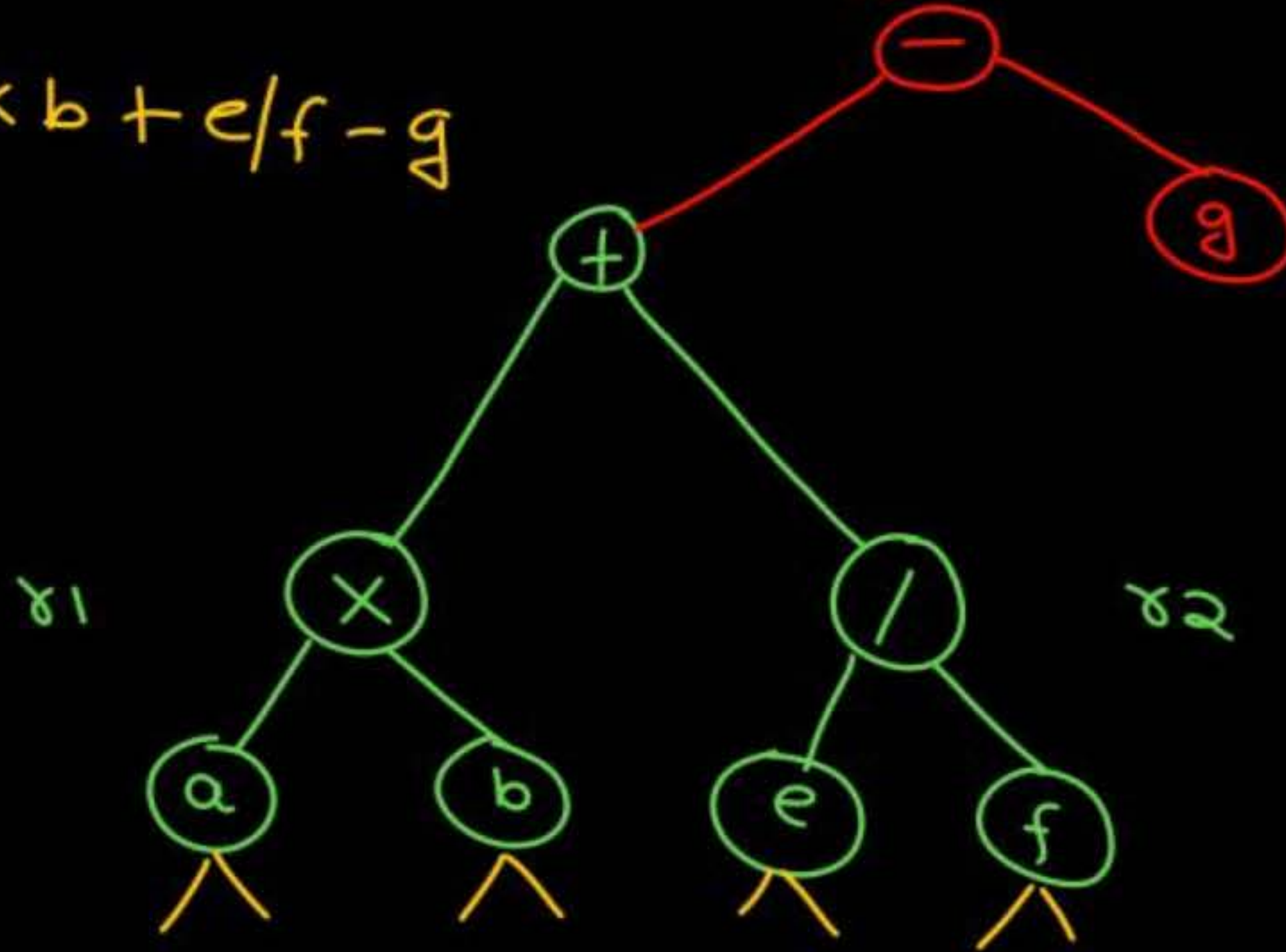
infix: $(a \times b) + \frac{e}{f} - g$

γ_1 γ_2

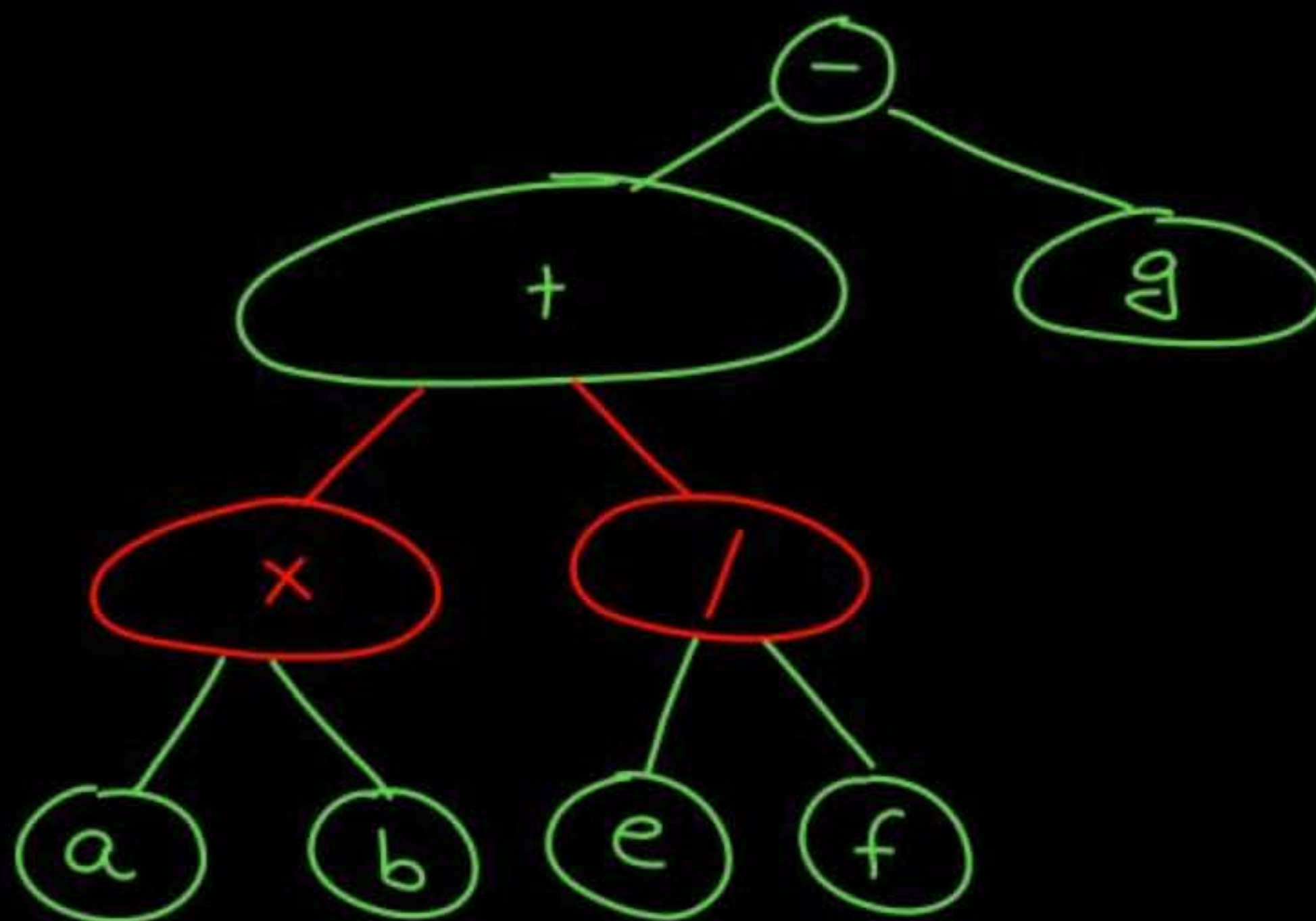
$\gamma_1 + \gamma_2 - g$

$B - \gamma$

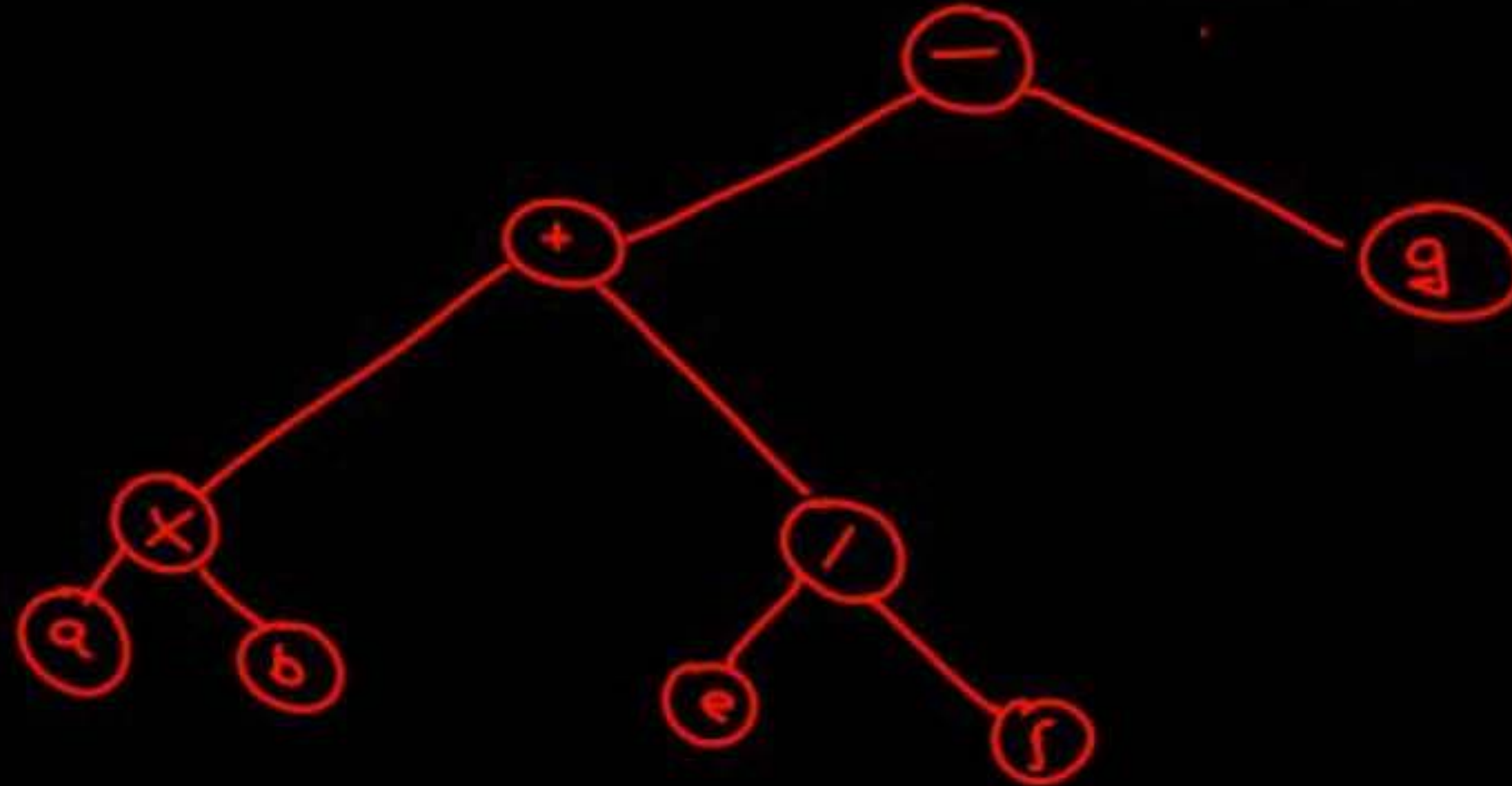
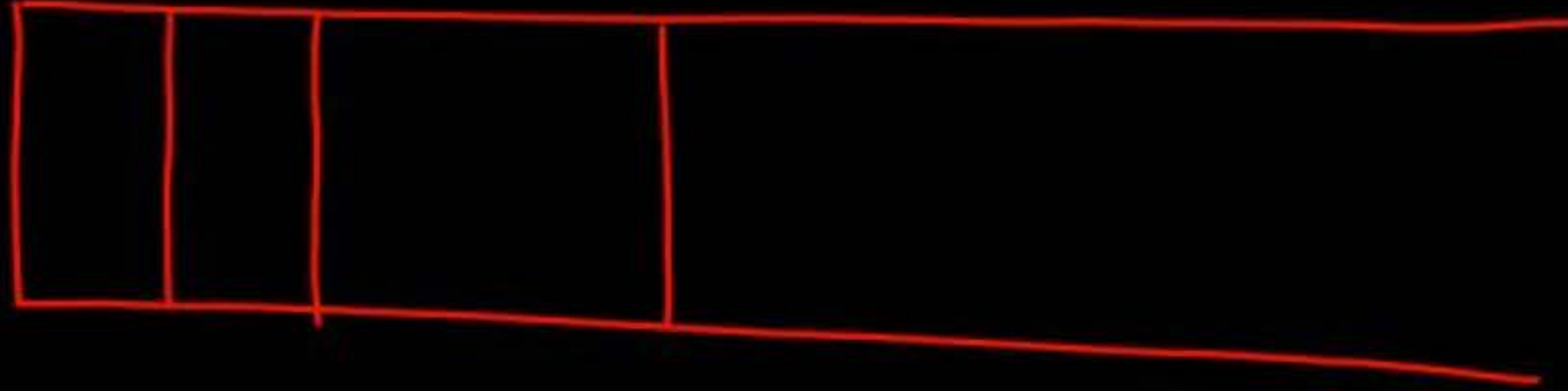
inorder: $a \times b + e/f - g$

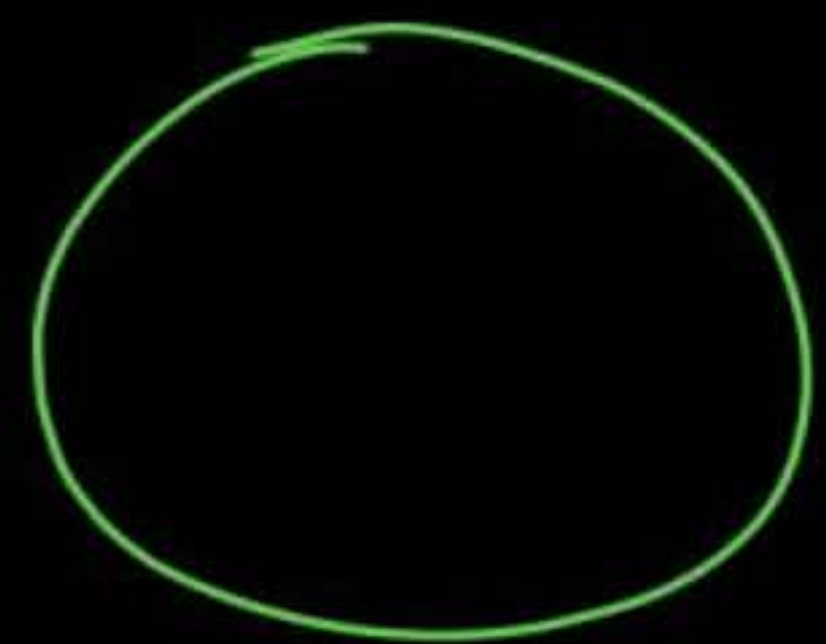
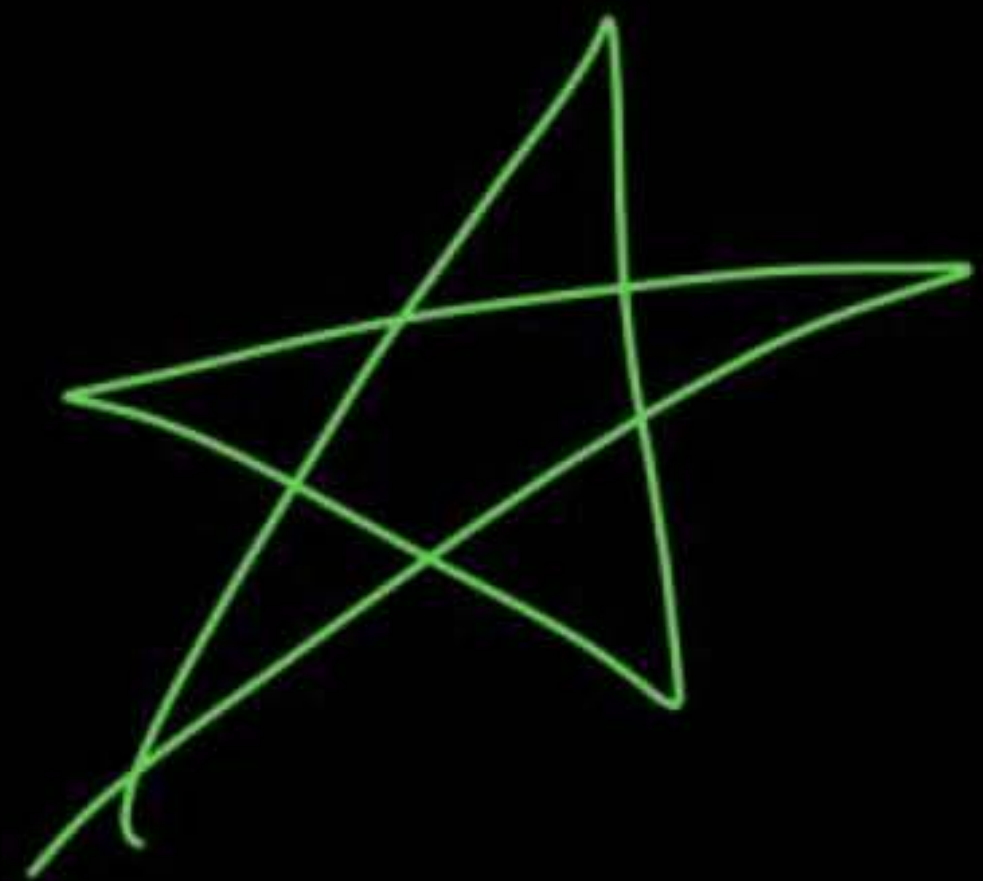


$a \times b + e / f - g$ ← last



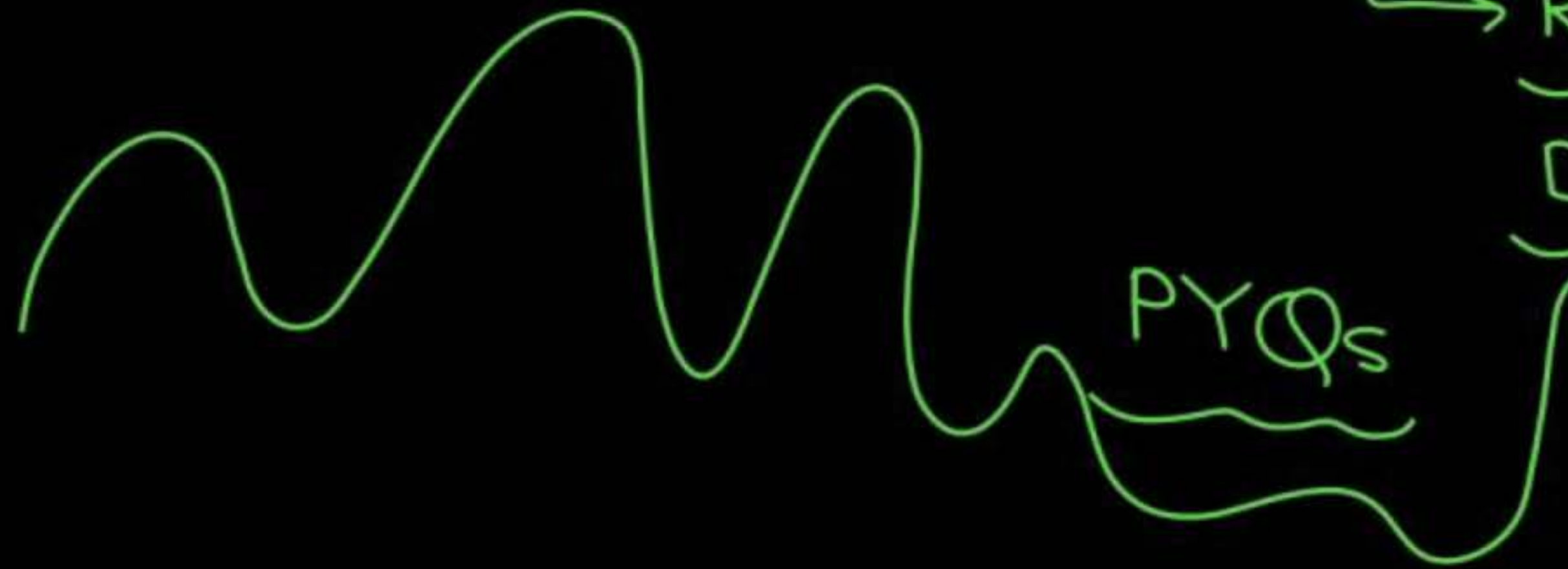
infix: $a \times b + e / f - g$
Postfix: $a b \times e f / + g -$





Algo
Graph
⇒ 1 lecture

Tree
└→ Revise
Doubt



PYQs



+ DPP
+ P/Q
+ Test Series

10 hrs \rightarrow 2 days

Hard rules

\rightarrow follow

200 pages $\times 10$

= 2000 pages

✓ infix: $2+3 \times 4$

Prefix: $+2 \times 34$

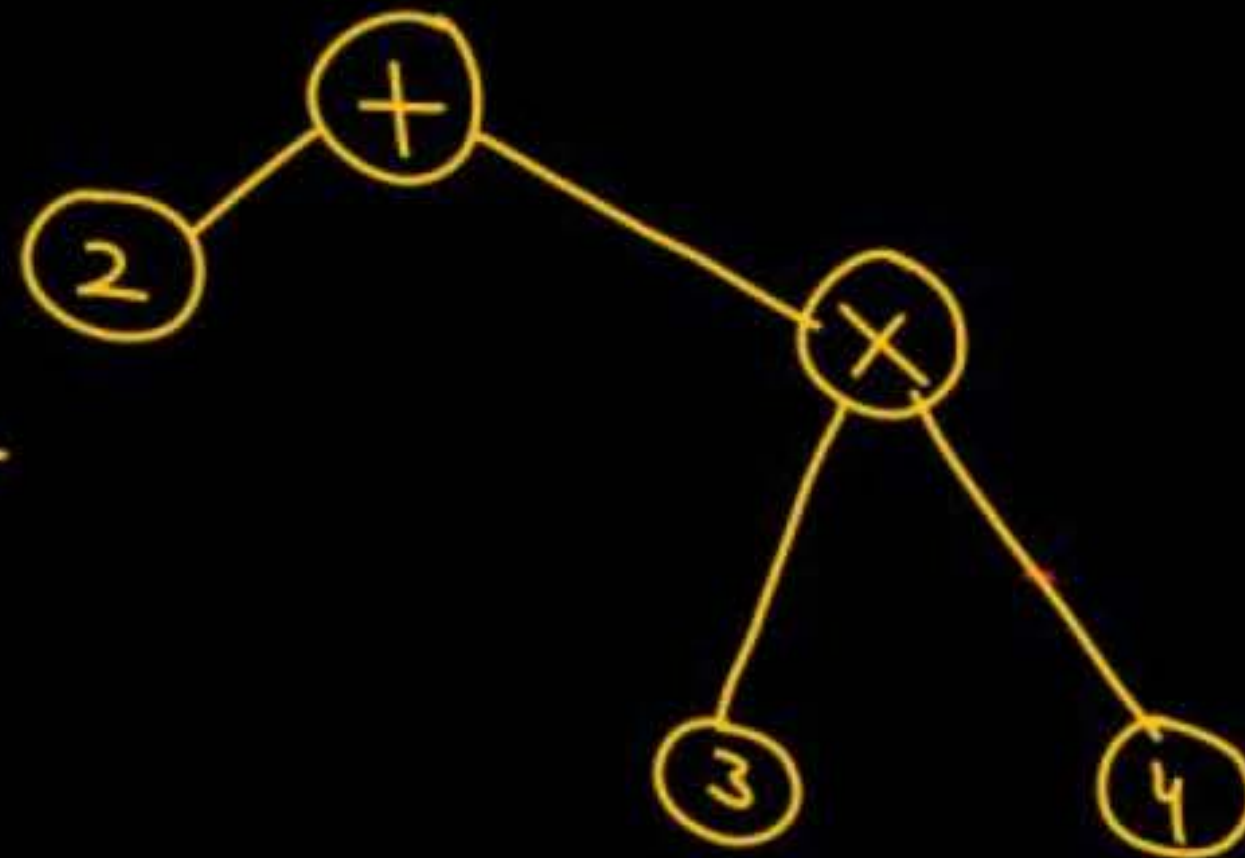
Reverse: $43 \times 2+$



Inorder: $2+3 \times 4$

Preorder: $+2 \times 34$

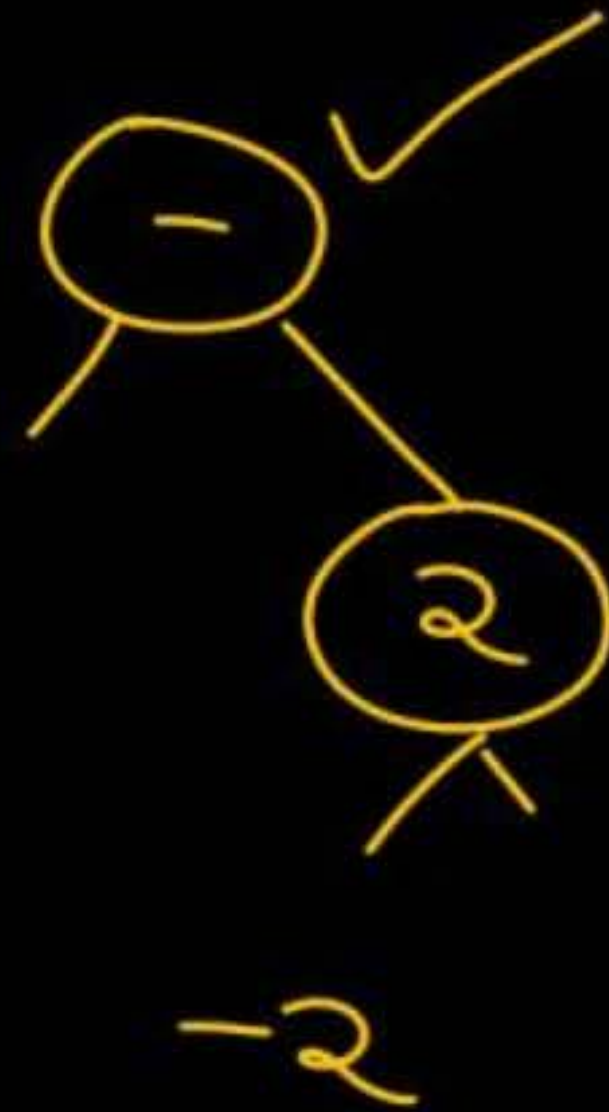
Postorder: $234 \times +$



{ Unary operator } -2

Fail

exp: -2



infix: $3 \times \log(x+1)$

Postfix:

programming

$$3 \times \log(\underbrace{x+1}_{\textcircled{1}})$$

$$3 \times \log(\underbrace{[x \ 1 +]}_{\text{operand}})$$

operator

$$\underset{\text{Op1}}{3} \times \underbrace{[x \ 1 + \log]}_{\text{Op2}}$$

Postfix : $3 \ x \ 1 + \log \ x$

Tree

- 1.) Binary tree
- 2.) Complete binary tree
- 3.) K-ary tree: Every internal node \Rightarrow K child

$L + I = K \times I + 1$
$L = (K - 1)I + 1$

- 4.) Full binary tree

5.) $n_{\max} = 2^{h+1} - 1$

$n_{\min} = h + 1$

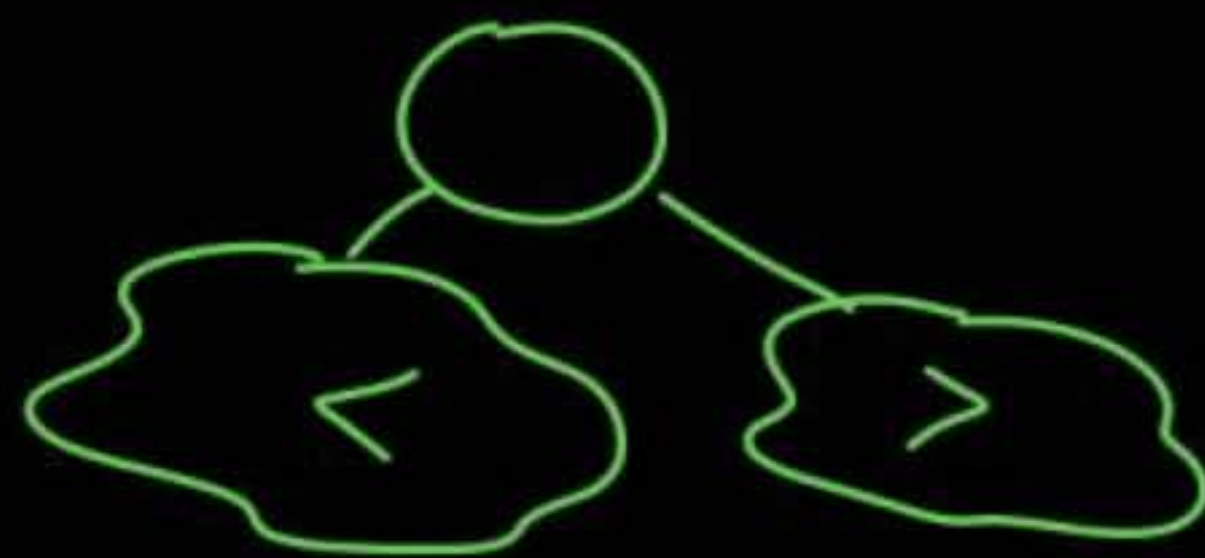
6.) $n_{\max} \Rightarrow 2^{h+1} - 1$ CBT, BT, BST, AVL tree

$n_{\min} \Rightarrow 2^h$ CBT

$n_{\min} \Rightarrow$ AVL

$$n(h) = 1 + n(h-1) + n(h-2)$$

- 7.) BST : Inorder : Asc. order of keys.



8.) # unlabelled binary tree with n nodes = $\frac{2^n C_n}{n+1}$

labelled binary tree with n nodes
 & n distinct keys = $\frac{2^n C_n}{n+1} \times n!$

BST with n keys = $\frac{2^n C_n}{n+1}$

Given a ^{BT} structure with n nodes & given n distinct keys
 BST $\Rightarrow 1$

q. # Binary tree with a given preorder of length $n = \frac{2^n C_n}{n+1}$
 " " " Inorder " $= \frac{2^n C_n}{n+1}$
 " " " Postorder " $= \frac{2^n C_n}{n+1}$

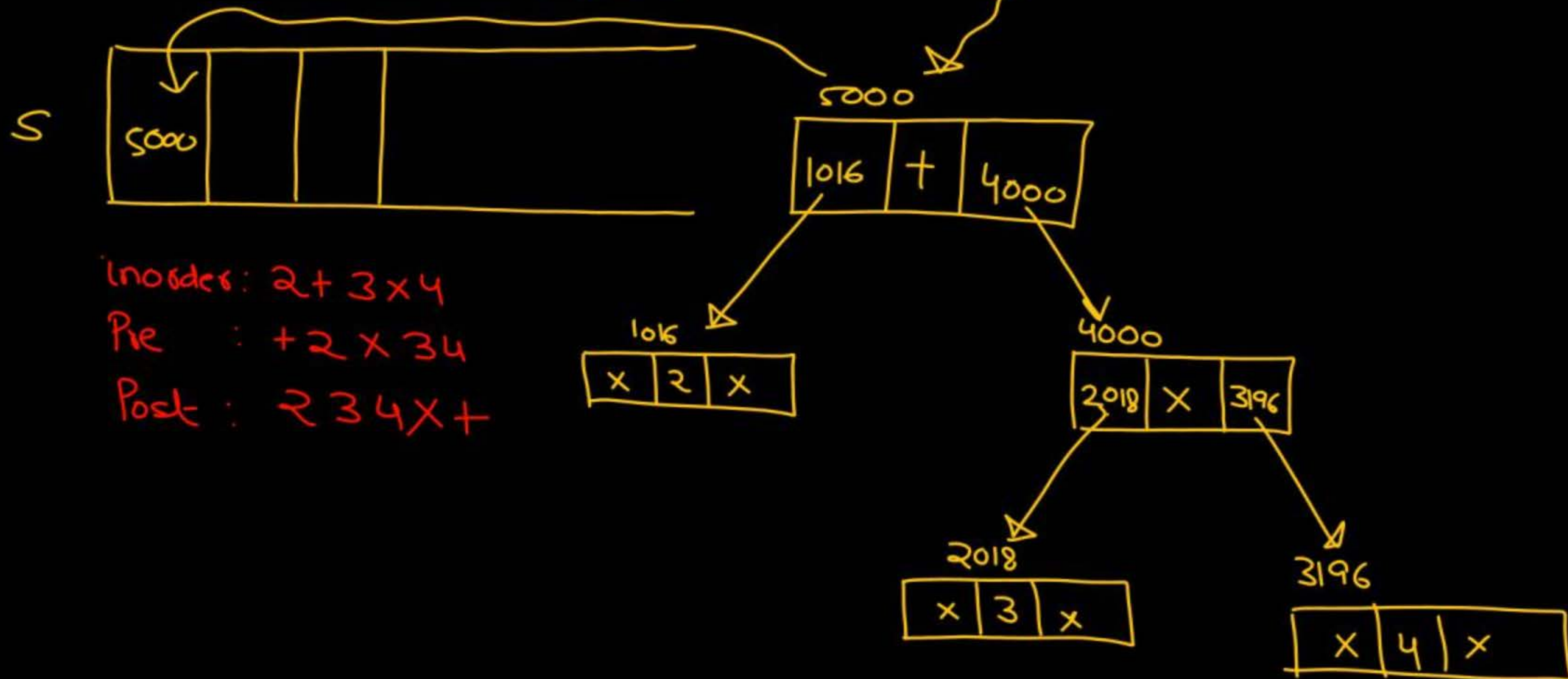
Shortcut / long }
 In + Pre \Rightarrow tree
 In + Post \Rightarrow tree

BST \rightarrow skewed



infix: $2 + 3 \times 4$

Postfix: $\checkmark 2 \checkmark 3 \checkmark 4 \checkmark \times \checkmark + \underline{\underline{\text{End}}}$



Inorder: $2 + 3 \times 4$

Pre : $+ 2 \times 3 4$

Post : $2 3 4 \times +$

