

# CS & IT ENGINEERING

Theory of Computation

Push Down Automata

**DPP 03** Discussion Notes



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# TOPICS TO BE COVERED

01 Question

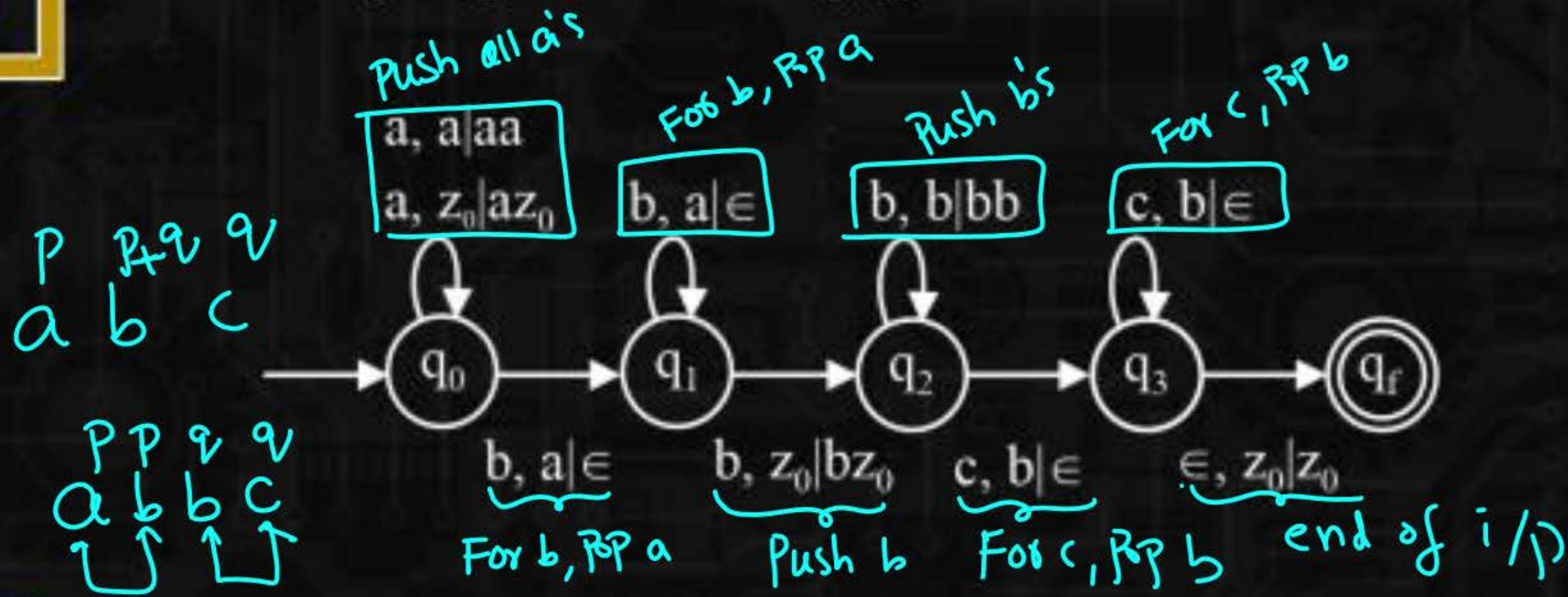
02 Discussion



Q.1

The language derived by given PDA is

[MCQ]



A.

$$L = \{a^n b^m c^k \mid n = m + k, m, n, k \geq 0\}.$$

B.

$$L = \{a^m b^n c^k \mid k = m + n, m, n, k \geq 1\}.$$

C.

$$L = \{a^m b^n c^k \mid k = m + n, m, n, k \geq 0\}.$$

D.

$$L = \{a^m b^n c^k \mid n = m + k, m, n, k \geq 1\}.$$



Q.2

[NAT]



Consider the following statements:

- (i) For every NFA  $N$  there exists a minimal DFA  $(N)$  such that  $L(N) = L(M)$ . ✓
- (ii) For every DFA  $M$  there exists a DPDA  $P$  such that  $L(M) = L(P)$ . ✓
- (iii) For every DPDA  $P$  there exists a NPDA  $N$  such that  $L(P) = L(N)$ . ✓
- ~~(iv)~~ For every NPDA ' $N$ ' there exists a DPDA ' $P$ ' such that  $L(N) = L(P)$ .

The number of correct statements is 3.

Q.3

Let  $r_1 = (01^*)^*$  is any regular expression. Then which of the following regular expression represents  $r_2$  such that  $L(r_1) = L(r_2)$ .



[MCQ]

☒ A.

$(10^*)^*$

$\begin{matrix} \epsilon \checkmark \\ 0 \times \end{matrix}$

☒ B.

$(1^* + 01^*1)^*$

$\begin{matrix} \epsilon \checkmark \\ 0 \checkmark \\ 00 \times \end{matrix}$

☒ C.

$(0^* + 01^*1)^*$

$\begin{matrix} \epsilon \checkmark \\ 0 \checkmark \\ 00 \checkmark \\ 01 \checkmark \end{matrix}$

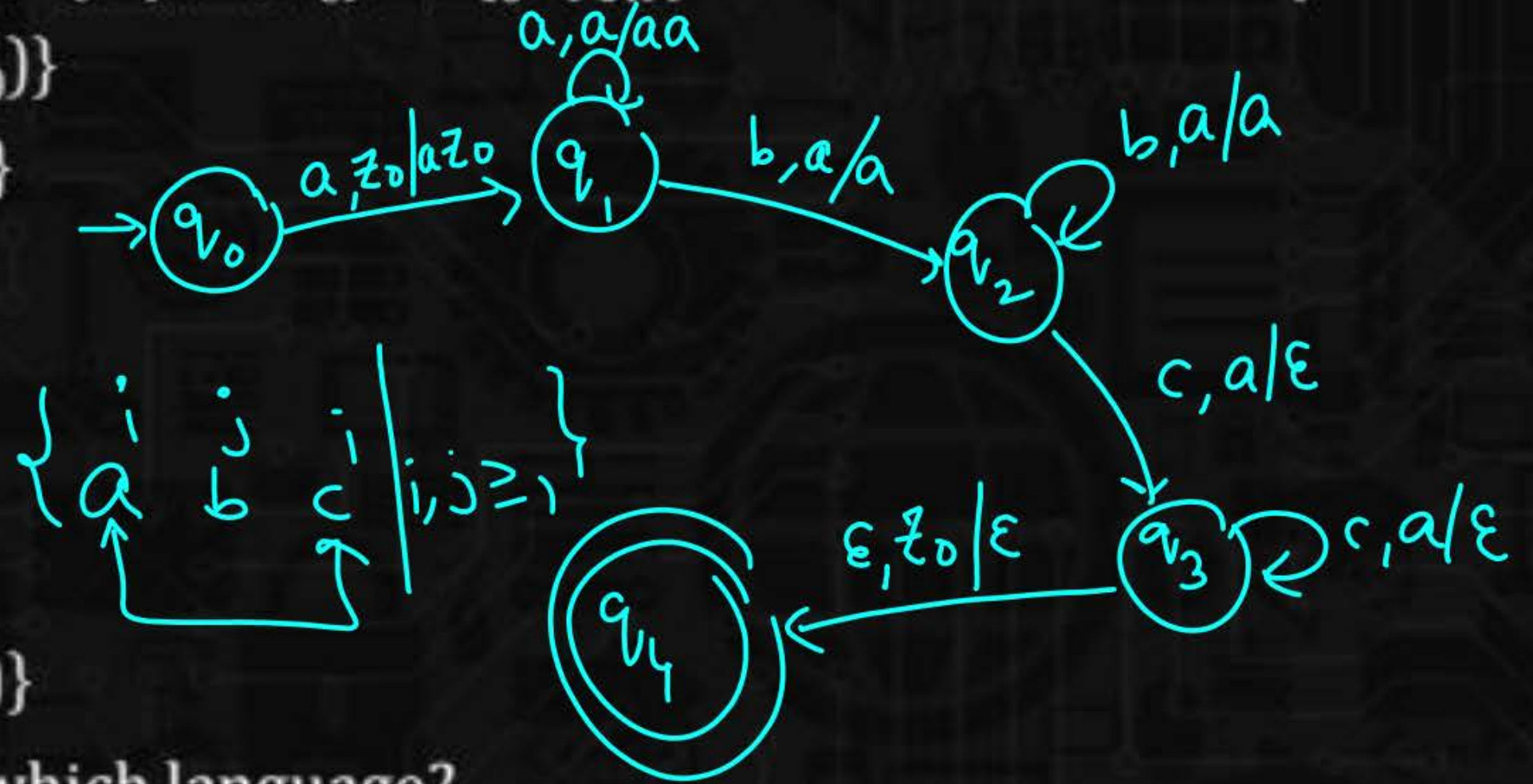
☐ D.

None

$$r_1 = (01^*)^*$$

$$L(r_1) = \{ \epsilon, 0, 00, 01, \cancel{1}, \cancel{01}, \dots \}$$
$$= \epsilon + 0 \times$$



**Q.4**Consider a PDA  $M$  as defined below:**[MCQ]**
 $M = \{\{q_0, q_1, q_2, q_3, q_4\}, \{a, b\}, \{a, b, z_0\}, \delta, q_0, \{q_4\}\}$  where  $\delta$  is defined by
Push  $a$ :  $\delta(q_0, a, z_0) = \{(q_1, az_0)\}$ Push  $a$ :  $\delta(q_1, a, a) = \{(q_1, aa)\}$ Skip  $b$ :  $\delta(q_1, b, a) = \{(q_2, a)\}$ Skip  $b$ :  $\delta(q_2, b, a) = \{(q_2, a)\}$ Pop  $a$ :  $\delta(q_2, c, a) = \{(q_3, \epsilon)\}$ Pop  $a$ :  $\delta(q_3, c, a) = \{(q_3, \epsilon)\}$  $\delta(q_3, \epsilon, z_0) = \{(q_4, \epsilon)\}$ 

The above PDA accepts which language?

A.

 $L(M) = \{a^n b^n c^m \mid n \geq 1, m \geq 0\}$ 

C.

 $L(M) = \{a^n b^m c^m \mid n \geq 1, m \geq 0\}$ 

B.

 $L(M) = \{a^n b^m c^n \mid n \geq 1, m \geq 0\}$ 

D.

 $L(M) = \{a^n b^m c^n \mid n \geq 1, m \geq 1\}$



Q.5

[MCQ]



Consider the following grammar G:  
G:

$$S \rightarrow SS \mid S$$

$$A \rightarrow aA$$

}  $\Rightarrow L = \phi$

Here, S and A are variables and a is a terminal then the language generated by above grammar G is:

A.

$$L(G) = a^n$$

B.

$$L(G) = a^*$$

C.

$$L(G) = \phi$$

D.

$$L(G) = a^n b a^n$$

Q.6

Which of the following is/are context free language.

[MSQ]



☒ A.  $L = \{a^m b^m c^n \mid m \geq 1 \text{ and } n \geq 1\}$   $\rightarrow$  CFL

☐ B.  $L = \{a^m b^m c^m \mid m \geq 0\}$   $\rightarrow$  not CFL

☒ C.  $L = \{wcw^R \mid w \in (a + b)^+\}$

☒ D. All strings of balanced parenthesis



Q.7

Consider the following language L:

$$L = \{wcw^R \mid w \in (a+b)^*, c \in (a+b)\} = \{w(a+b)w^R \mid w \in \{a,b\}^*\}$$

[MCQ]



The complement of L will be \_\_\_\_.

→ CFL but not DCFL

A.

Regular

B.

DCFL but not regular

☒ C.

CFL but not DCFL

D.

None of these

---

$$\{ww^R \mid w \in \{a,b\}^*\}$$

→ CFL

Q.8

[NAT]



Suppose,  $L$  is a language accepted by PDA.

(i)  $L = \{ \underbrace{a^n b^n} \underbrace{c^m d^m} \mid n, m \geq 1 \} \rightarrow \text{DCFL}$

(ii)  $L = \{a^n \mid n \text{ is prime}\} \rightarrow \text{not CFL}$

(iii)  $L = \{ww^R \mid w \in (a+b)^+\} \rightarrow \text{CFL}$

Then how many of the following can be  $L$  2.



