

ASSIGNMENT- MATRICES

Abstract:

This manual explains the foot of the perpendicular from a point to the given line using matrices.

Problem:

Find the coordinates of the foot of perpendicular from the point $(-1,3)$ to the line $3x - 4y - 16 = 0$.

solution:

Let the given line equation be a normal vector to a plane where the given point $P(-1,3)$ lies. The intersection of the plane and line equations gives the coordinates of foot of the perpendicular from point p.

The parametric equation of a line is given by

$$x = A + \lambda m \quad (1)$$

The equation of the line perpendicular to normal of a plane and passing through the point \vec{P} is given by

$$m^\top (x - P) = 0 \quad (2)$$

Solving both the equations gives us the

intersection point 'Q'.

$$Q = A + \frac{m^\top (P - A)}{m^\top m} m \quad (3)$$

Further solving the equation with

$A = \begin{pmatrix} 0 \\ -4 \end{pmatrix}$, $P = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$, $m = \begin{pmatrix} 4 \\ 3 \end{pmatrix}$ gives us the foot of the perpendicular

$$Q = \begin{pmatrix} 2.72 \\ -1.96 \end{pmatrix} \quad (4)$$

<https://github.com/reshma0639/FWC-Assignment-1/blob/main/avrgcc/codes/main.c>

4. Now by taking different combination of inputs, check the output being 0 or 1 in regard with the LED off and on respectively.

Table 1: Truth table

5. Cross check the output with the above mentioned truth table for the corresponding input combination(X,Y,Z).

$$FN = (X + Y')(Y' + Z)(X' + Y + Z')$$