



Position	level		
	- l3 c1 - l4		
-6x	ên + loy êz	= 0	
1, (CO1)+	ℓ2 (cθ12 sq12)		
- (3 (E.c.)	2) - 14 (C4)		
	-(ox) = (
,	Forward	Inve	rse
Known	01, 92	82,9	2
Unknown	02,42	01,	41-

Velocity level

$$\ell_1 \dot{\theta}_1 \begin{pmatrix} -s_{\theta_1} \\ c_{\theta_1} \end{pmatrix} + \ell_2 \begin{pmatrix} \dot{\theta}_1 + \dot{\theta}_2 \end{pmatrix} \begin{pmatrix} -s_{\theta_{12}} \\ c_{\theta_{12}} \end{pmatrix} - \ell_3 \begin{pmatrix} \dot{q}_1 + \dot{q}_2 \end{pmatrix} \begin{pmatrix} -s_{q_1} \\ c_{q_2} \end{pmatrix} - \ell_4 \dot{q}_1 \begin{pmatrix} -s_{q_1} \\ c_{q_1} \end{pmatrix} = 0$$

	Forward	Inverse
Known	θ1, Ψ,	θ_2 , φ_2
Unknown	$\dot{\theta}_2, \dot{\varphi}_2$	ð, , ė,

Acceleration level

$$\begin{aligned} &\ell_{1} \stackrel{\cdot}{\theta}_{1} \begin{pmatrix} -s_{\theta_{1}} \\ c_{\theta_{1}} \end{pmatrix} - \ell_{1} \stackrel{\circ}{\theta}_{1}^{2} \begin{pmatrix} c_{\theta_{1}} \\ s_{\theta_{1}} \end{pmatrix} + \ell_{2} \begin{pmatrix} \ddot{\theta}_{1} + \ddot{\theta}_{2} \end{pmatrix} \begin{pmatrix} -s_{\theta_{12}} \\ c_{\theta_{12}} \end{pmatrix} - \ell_{2} \begin{pmatrix} \ddot{\theta}_{1} + \ddot{\theta}_{2} \end{pmatrix}^{2} \begin{pmatrix} c_{\theta_{12}} \\ s_{\theta_{12}} \end{pmatrix} \\ &- \ell_{3} \begin{pmatrix} \ddot{\varphi}_{1} + \ddot{\varphi}_{2} \end{pmatrix} \begin{pmatrix} -s_{\varphi_{12}} \\ c_{\varphi_{12}} \end{pmatrix} + \ell_{3} \begin{pmatrix} \ddot{\varphi}_{1} + \ddot{\varphi}_{2} \end{pmatrix}^{2} \begin{pmatrix} c_{\varphi_{12}} \\ s_{\varphi_{12}} \end{pmatrix} - \ell_{4} \stackrel{\circ}{\varphi}_{1} \begin{pmatrix} -s_{\varphi_{1}} \\ c_{\varphi_{1}} \end{pmatrix} + \ell_{4} \stackrel{\circ}{\varphi}_{1}^{2} \begin{pmatrix} c_{\varphi_{1}} \\ s_{\varphi_{1}} \end{pmatrix} = 0 \end{aligned}$$

Known	Forward θ_1, θ_1	Inverse	
Unknown	õ, Ÿ	ö,, e,	