

The sum of the digits in the unit place of all numbers formed with the help of $a_1, a_2, a_3, \dots, a_n$ taken all at a time is
$$= (n-1)! (a_1 + a_2 + \dots + a_n)$$
 repetition of digits not allowed

The sum of all digit numbers that can be formed using the digits a_1, a_2, \dots, a_n taken all at a time is
$$= (n-1)! (a_1 + a_2 + \dots + a_n) \frac{10^n - 1}{9}$$
 repetition of digits not allowed.

Out of n non-concurrent and non-parallel straight lines points of intersection are
$$\binom{n}{2}$$

Out of n points, the number of straight lines are (when no 3 are collinear)
$$\binom{n}{2}$$

If out of n points m are collinear, then number of st. lines
$$\binom{n}{2} - \binom{m}{2} + 1$$

In a polygon the total no. of diagonals of n points (no 3 are collinear)
$$\frac{n(n-3)}{2}$$

No. of triangles formed out of n points

No. of triangles out of n points
in which m are collinear $\binom{n}{3} - \binom{m}{3}$

No. of parallelograms in 'Two sets' of parallel lines (when 1st set contains m parallel lines and 2nd set n parallel lines) = $\binom{n}{2} \cdot \binom{m}{2}$

No of squares in two sys^m of 1^2 parallel lines (

$$) = \sum_{n=1}^{m-1} (m-n)(n-1) ; (m \geq 2)$$

No. of ways of selecting 1 or more items from a group of n distinct items is $2^n - 1$

The total no. of ways of selecting one or more items from p identical items of one kind, q identical items of second kind, r identical items of 3rd kind and n different items is $(p+1)(q+1)(r+1)2^n - 1$.

Suppose $n = p_1^{n_1} p_2^{n_2} \dots p_k^{n_k}$

Then divisors of $n = (n_1+1) \dots (n_k+1)$

" " n (other than 1 and n) = $[(n_1+1) \dots (n_k+1) - 2]$

Sum of the divisors = $\left(\frac{p_1^{n_1+1} - 1}{p_1 - 1} \right) \dots \left(\frac{p_k^{n_k+1} - 1}{p_k - 1} \right)$

No. of ways in which n can be resolved as a product of two factors is $\frac{1}{2} (n_1+1)(n_2+1) \dots (n_k+1)$ if n is not a perfect square

No. of ways in which

$\frac{1}{2} [(n_1+1)(n_2+1) \dots (n_k+1) + 1]$ if n is a perfect square

If n pigeons are assigned to m pigeonholes and $m < n$. Then one of the pigeonholes must contain at least $\left\lceil \frac{n-1}{m} \right\rceil + 1$ pigeons.

If $p_1 + p_2 + p_3$ things are \exists p_1 things are alike and p_2 things are alike and p_3 things are all different. Then number of selections of r things out of $p_1 + p_2 + p_3$ things
 = coefficient of x^r in $(1+x+\dots+x^{p_1})(1+x+\dots+x^{p_2})(1+x+\dots+x^{p_3})$