

L-1 (10-1)Topic - 1Searching (Imp. For Final)Linear Search ( $O(n)$ )

Given value' and array  $a[]$ , find index  $i$  such that  $a[i] = \text{value}$ , or report that no such index exists

\* **Search space** = place to search in. In this case,  $a[]$  is search space

- \* Best Condition: value in first index of search  $O(1)$   $O(\approx n)$
- \* Average " : value in any index that's not in first or last  $O(n)$
- \* Worst " : value in last index of search  $O(n)$

Time Complexity: Big  $O(n)$  } Asymptotic Notation  
 "  $\Theta(n)$  }  
 "  $\Omega(n)$  } can be expressed in a number line in between 1 and  $n$ !

## Random Search

Given . . . , randomly pick index  $i$  such that . . .

\* **Exploitation**: Reduction of search space

No replace

Best Case : 1

\* Linear search is a variation of Random search

Average " :  $\approx n$

Worst " :  $n$

Replace

Best Case : 1

Average " :  ~~$\approx$~~   $n$

Worst " :  $\infty$

## Binary Search

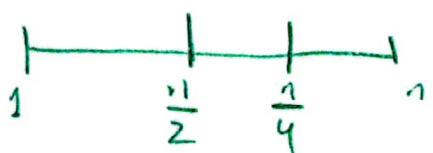
Given 'value' and Sorted array . . .

Invariant : Maintains  $a[\text{low}] \leq \text{value} \leq a[\text{high}]$

Best case : 1

Avg " :

Worst " :  $\log_2(n)$

+  until you find it

## Binary Search Algo

Bin\_search ( $A, k$ )  
     $\nearrow$  Array  
     $\searrow$  value

$low = 0$

$high = \text{size}(A) - 1$

while  $low < high$   
 $mid = \frac{low + high}{2}$

if  $A[mid] = k$ :

    return found

else if  $A[mid] > k$ :

$high = mid - 1$

else

$low = mid + 1$

return not found

\* Algorithm is code without syntax

+ Binary search in an unsorted array is the same as replacing random array

\* For best case, worst case of B.S, we trace

\* use for any sorted array

C-1 (W-1)

## Pseudocode, Algorithm, Flowchart

### \* Pseudocode:

Artificial and informal language that helps to develop algorithm. Very similar to plain/everyday English  
 (Avoid syntaxes and mathematical operation symbols)

### \* Algorithm:

Series of instructions to accomplish a task; very close to programming language; more like steps involving notations; ordered sequence of steps

- (Avoid syntaxes)

### \* Flowchart:

Graphical representation of the sequence of operations i.e. Algorithms

### Example:

write an algorithm to determine a student's final grade and indicate whether the student is passing/failing. The final grade is calculated as the average of four marks.

### Pseudocode:

1. input a set of 4 marks
2. calculate the average by summing and dividing by 4
3. If average is below 40, print fail
4. else print pass

### Algorithm:

1. input M1, M2, M3, M4
2. grade  $\leftarrow \frac{M1 + M2 + M3 + M4}{4}$
3. if grade < 40 : (no then)  
    print fail
4. else  
    print pass

### code:

```

1. cin >> M1 >> M2 >> M3 >> M4;
2. double grade = (M1 + M2 + M3 + M4) / 4.0;
3. if (grade < 40.0){
    cout << "Fail" << endl;
}
4. else{
    cout << "Pass" << endl;
}

```

\* "class theke kisu asebe na" ~ Sir "15 marks common from memory"

# From an array find minimum value:

pseudocode:

1. take min  $\infty$  as first element of array
2. run a loop for each element in array
3. if min is greater than element, change min to that element
4. else continue running the loop
5. print min.

algorithm:

1. min  $\leftarrow arr[0]$
2. while For i=0 to size of arr:  
    if  $min > arr[i]$ :  
        | min  $\leftarrow arr[i]$   
    end if  
    else  
        | end for
3. print min

code:

```
1. int min = arr[0];  
2. for (int i = 0; i < sizeof(arr); i++) {  
    if (min > arr[i]) {  
        min = arr[i];  
    }  
}  
3. cout << min << endl;
```

Selection Sort

- 1) Swap two numbers  $\rightarrow \text{swap}(A, B)$   
 Built-in C++ function
- 2) Find the minimum value from a vector of integers

Algorithm: 0.  $\text{Find\_Min}(A)$ :

1.  $n = \text{size}(A)$   $\rightarrow$  finds size of vector  
 2.  $\min = A[0]$   $\rightarrow$  considering first term to be lowest  
 3.  $\rightarrow \text{pos} = 0$   
 4. For  $i = 1$  to  $n-1$ :  
 5.   if  $A[i] < \min$ :  
 6.      $\min = A[i]$   
 7.      $\rightarrow \text{pos} = i$   
 8. end if  
 9. end for  
 10. print  $\min$   
 11.  $\rightarrow$  print  $\text{pos}$

$\rightarrow$  compare and swap find min

W

new index

20  
 29 72 98 13 87 66 52 51 36  
 20  
 0. 13 72 98 29 87 66 52 51 36

assumption of next array

1. 13 29 98 72 87 66 52 51 36

2. 13 29 36 72 87 66 52 51 98

3. 13 29 36 51 87 66 52 72 98

4. 13 29 36 51 52 66 87 72 98,

5. 13 29 36 51 52 66 87 72 98,

6. 13 29 36 51 52 66 72 87 98,

7. 13 29 36 51 52 66 72 87 98

### Algorithm Pasing

\* For  $n$  terms, sort has to be done  $n-1$  times

Pasing  $\rightarrow$  Iteration or Iteration / Tracing of

### Selection Sort Algorithm:

0. Selection - Sort(A) :

1.  $n = \text{size}(A)$

2. For  $j=0$  to  $n-2$ :

$\min = A[j]$

3.

4.      $\text{pos} = j$

5.     For  $i=j+1$  to  $n-1$ :

6.         if  $A[i] < \min$ :

7.              $\min = A[i]$

8.              $\text{pos} = i$

9.         end if

10.     end For  $\rightarrow$  do NOT use  $\min$

11.     swap  $A[\text{pos}], A[j]$

12. end For

## Complex. (min)

Best :  $n$

Avg :  $n$

Worst :  $n$

## Complexity of Algo sorting

*Selection*

Best :  $n(n-2) \approx n^2 - 2n$

Avg :  $n(n-2) = "$

Worst :  $n(n-2) = "$

C-3(W-2)

16/04/24

## Insertion & Sort

\* Insert an element into the sorted array

$$A = [10 | 15 | 20 | 25 | 30]$$

Say, we want to insert 18,

Two different ways to achieve this →

- (1) ~~Search, then shift~~ → Complexity  $(n)$ ; [number of search + no. shift]
- (2) ~~Search + Shift~~

\* Shift from last element

Search ~~then~~ Shift:

$$A = [10 | 15 | 18 | \underbrace{20 | 25 | 30}_{\uparrow}]$$

Search and Shift:

Use  $\downarrow$  to navigate

if  $insert > index$ ,  $A[index] =$

$A[index] =$

$A[index+1] = A[index] insert$

else

$A[index+1] = A[index]$

## Algorithm (Insert)

→ insert element

0. Insert( $A[\cdot], key$ ):

1.  $n = \text{size}(A)$

2.  $j = n - 1$

3. while  $j \geq 0$  and  $A[j] > key$

4.      $A[j+1] = A[j]$

5.      $j = j - 1$

6. end while

7.  $A[j+1] = key$

## Insertion Sort:

nb.	1	2	3	$n$	5	6
0	5	2	4	6	1	3

Ind(n)	0	1	2	3	4	5
0.	2	5	4	8	1	3

1.	2	4	5	6	1	3
----	---	---	---	---	---	---

2.	2	4	5	6	1	3
----	---	---	---	---	---	---

3.	1	2	4	5	6	3
----	---	---	---	---	---	---

4	1	2	3	4	5	6
---	---	---	---	---	---	---

$n-1$

## Algorithm (Insertion Sort):

0. Insertion\_Sort(A) :

1.  $n = \text{size}(A)$

2. For  $i = 1$  to  $n - 1$ : // Starts from 1 NOT 0

3.   ; key =  $A[i]$  // consider the ~~the~~  $i$ -th term to be inserted

4.   ;  $j = i - 1$  // to p to work on the prev indexes

5.   ; while  $j \geq 0$  and  $A[j] > \text{key}$ :

6.   ;   ;  $A[j+1] = A[j]$  // shift

7.   ;   ;  $j = j - 1$  // for the loop

8.   ;

9.   ; end while

10.   ;  $A[j+1] = \text{key}$  // if the location is found;  
[the elem insert element is greater than the index]

end For

Complexity:

Best :  $n$

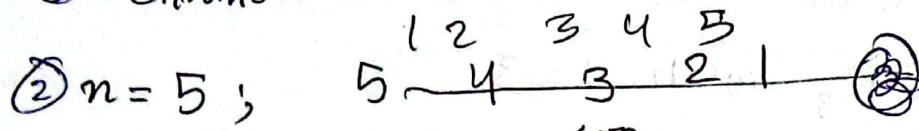
Avg :  $n^2$

Worst :  $n^2$

\* Binary search IS an improvement  
→ Do at Home (from Cut)

Recursion:

① Definition of Recursion = see the definition of Recursion

②  $n = 5$ ; 

for (int i = 0; i <= n; i++) → iterative solution

{

cout << i << " "; // do something

}

void

③ FOR (int i, int n) → recursive solution

{

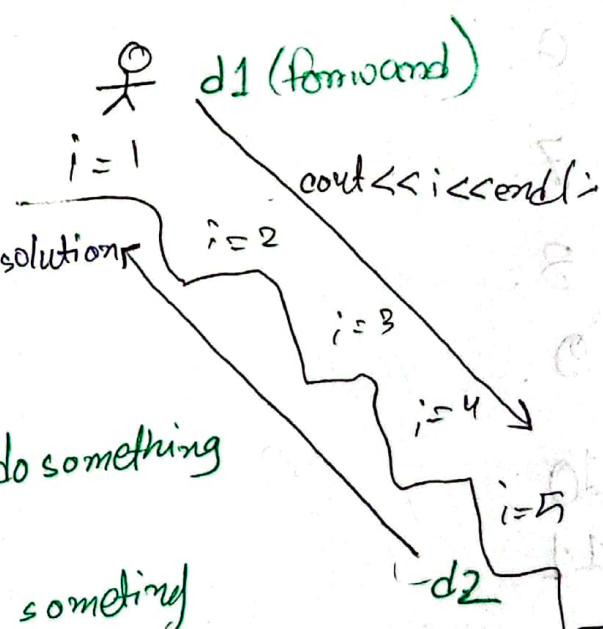
if ( $i \leq n$ )

{ → d1 cout << i << " "; // do something

FOR (i + 1, n);

{ → d2 cout << i << " "; // do something

}



\* Useful for [dynamic programming] → saves every state of the program  
 ↳ parameters become "states"

int main()

{

FOR (1, 5);

}

## Recursion Steps:

(a) 12

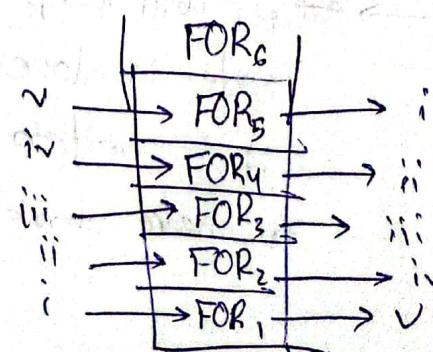
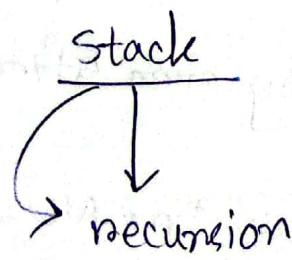
1. call  $\text{FOR}_1$  with  $i = 1$
2. . . call  $\text{FOR}_2$  with  $i = 2$
3. . . . call  $\text{FOR}_3$  with  $i = 3$
4. . . . . call  $\text{FOR}_4$  with  $i = 4$
5. . . . . . call  $\text{FOR}_5$  with  $i = 5$
6. . . . . . . call  $\text{FOR}_6$  with  $i = 6$
7. . . . . . . break; no more calls
8. . . . . . . return to  $\text{FOR}_5$
9. . . . . . . print 5
10. . . . . . . return to  $\text{FOR}_4$
11. . . . . . . print 4
12. . . . . . . return to  $\text{FOR}_3$
13. . . . . . . print 3
14. . . . . . . return to  $\text{FOR}_2$
15. . . . . . . print 2
16. . . . . . . return to  $\text{FOR}_1$
17. . . . . . . print 1
18. . . . . . . return to main

\* Reversing an array:

```
void FOR (int i, int n) // (int i, n)
{
    if (i >= 0) // (i < n)
    {
        cout << i << " ";
        FOR(i - 1 n); // (i + 1, n)
    }
}

int main()
{
    FOR(n - 1 n); // FOR(0, n - 1)
}
```

\* Memory where recursion is kept  
is called STACK MEMORY



L-3 (W-3)

## Pointers

23/04/24

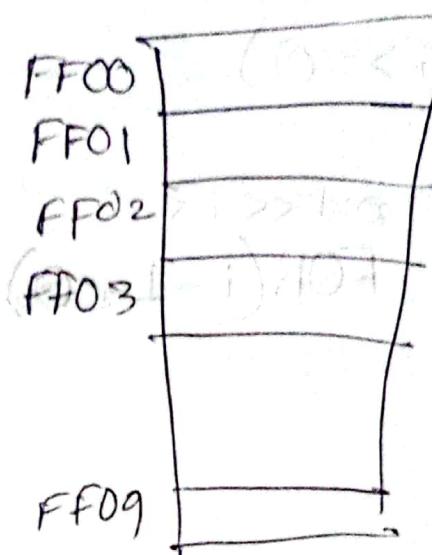
↳ important  
for linked list

int x = 5

variable : x

value : 5

Address : FF00



int x = 5

int \*p } int \*p  
p = &x }

$$*p = 25$$

$$\underline{x} + (\underline{\&x}) = 25$$

$$\underline{x} = 25$$

\*After declaring  $p = \&x$

+ int \*p = NULL }  $\rightarrow$   $p$  will keep pointing even after  
p = &x code is closed  
it is better to use  $*p = \text{NULL}$   
to make sure address is not assigned

\*  $\text{int } *p = \text{arr}; \equiv \text{int } *p = \&\text{arr}[0]$

$\text{arr} = \{ 10, 12, 18, 14, 15 \}$

$\text{arr}[0] \longrightarrow 10$

$\&\text{arr}[0] \longrightarrow \text{address of } 10$

$*(\&\text{arr}[0]) \longrightarrow 10$

$*(\&\text{arr}[0]) + 1 \longrightarrow 11 // 10 + 1$

$*(\&\text{arr}[0] + 1) \longrightarrow 12 // \text{addr. of } 10 + 1$

$\hookrightarrow$

\* Good practice to free the pointers

\* Cpp allows method/function overloading, overriding etc

\* Cpp is OOP (better than java)

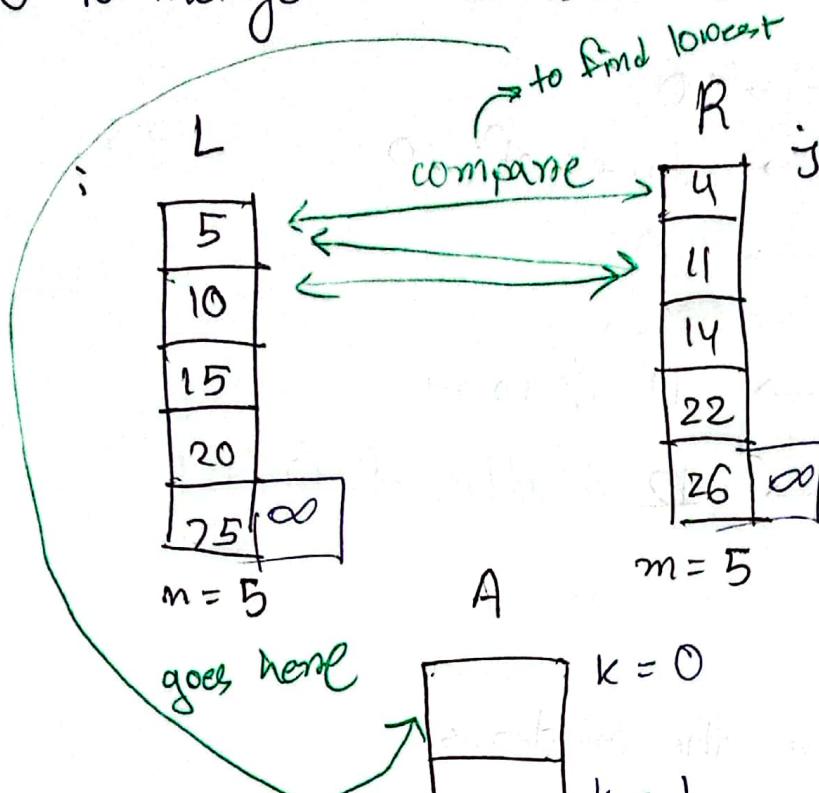
C-5(w-3)

Menge Sort : Menge

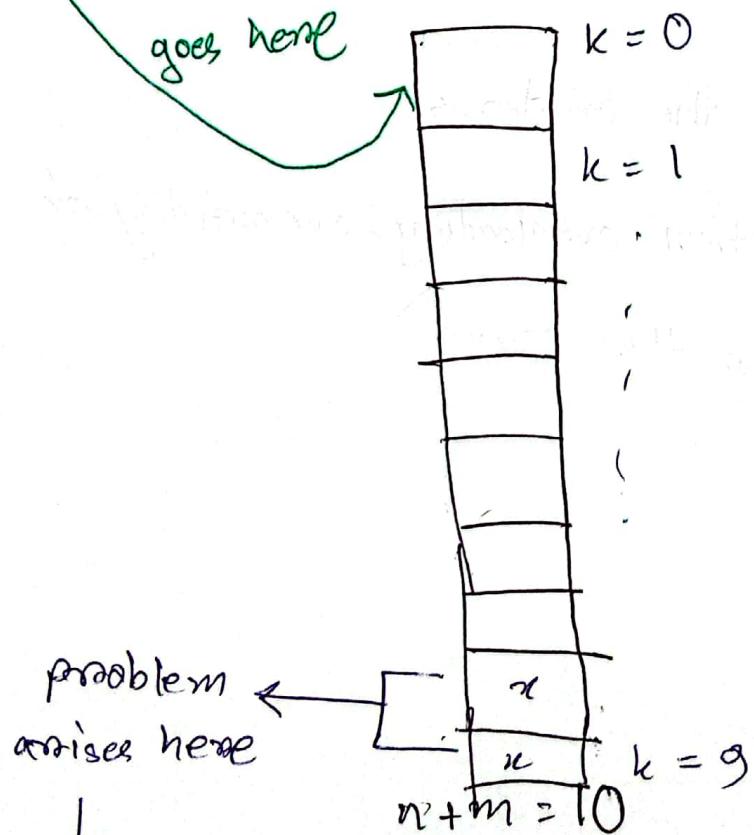
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→ conquer

\* How to merge two sorted lists into one sorted list



Comparing:  
L[i] R[j]



↳ same value  
will ~~happ~~ be placed  
here twice

↳ sol<sup>n</sup>  
add index  
+ put infinity then

## \*Algorithm for merging:

0. MERGE(L, R)

1.  $m = \text{size}(L)$

2.  $n = \text{size}(R)$

3.  $i = j = 0$     $L[m] = \infty$  // } getting adding infinity at the end

4.    $R[n] = \infty$  //

5.    $i = j = 0$

6. For  $x = 0$  to  $(m+n) - 1$ :

7.   ; if  $L[i] \leq R[j]$ :

8.   ;    $A[x] = L[i]$

9.   ;    $i = i + 1$

10.   ; end if

11.   ; else if  $R[j] < L[i]$ :

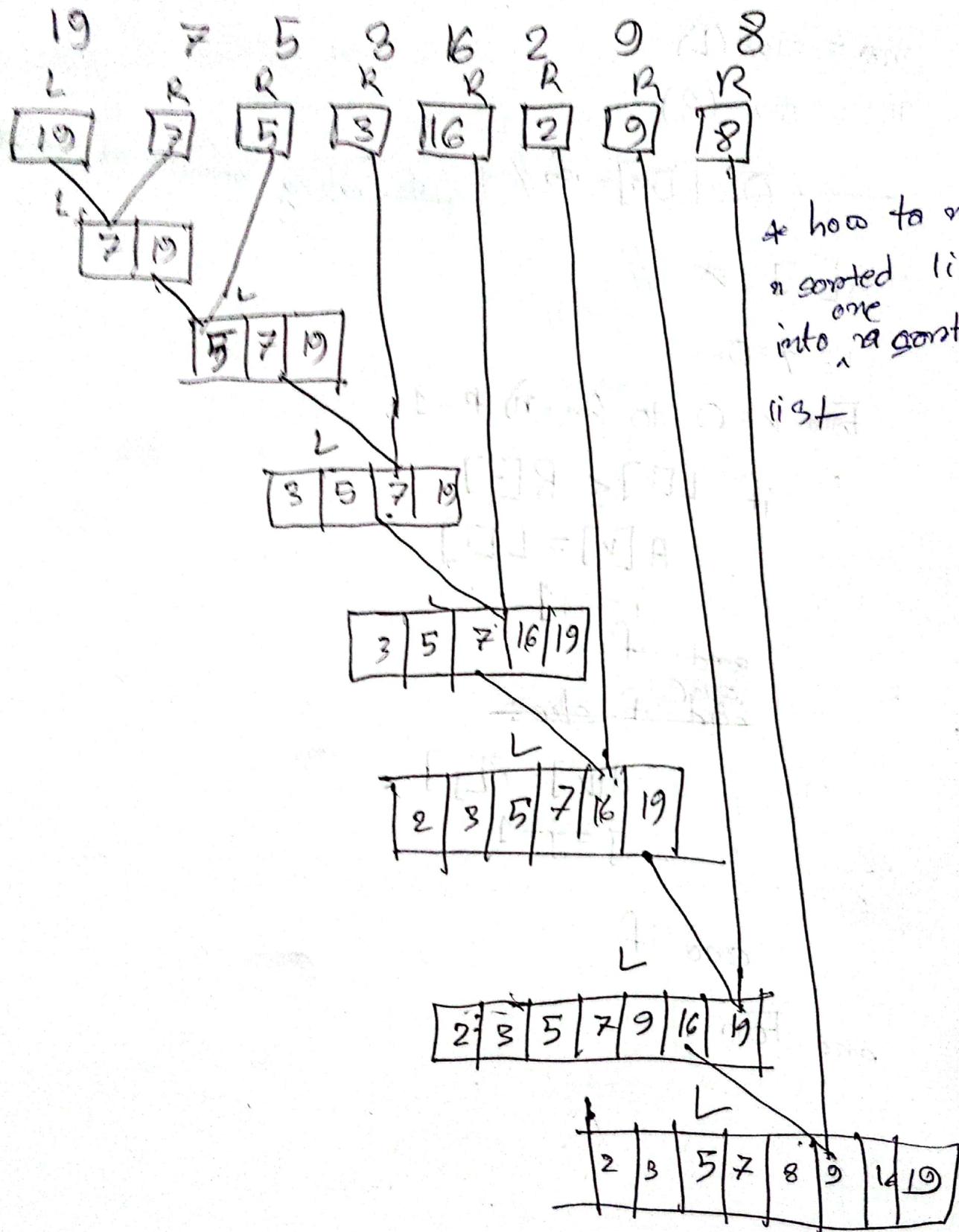
12.   ;    $A[x] = R[j]$

13.   ;    $j = j + 1$

14.   ; end if

15. end For

# MERGE SORT



+ how to merge  
sorted lists  
one  
into one sorted  
list

\* Algorithm (one ascending, one descending)

$L \rightarrow$  ascending -  $R \rightarrow$  descending

MERGE( $L, R$ )

$m = \text{size}(L)$

$n = \text{size}(R)$

$L[m] = \infty$

//  $R[n] = -\infty \rightarrow$  do not use

$i = 0$

$j = n - 1$

For  $k = 0$  to  $(m+n)-1$ :

if  $L[i] \leq R[j]$ :

$A[k] = L[i]$

$i = i + 1$

else:

$A[k] = R[j]$

$j = j + 1$

end if

end For

$j=0$	6000	6000
1	2	3
1	1	1
120	i=1	i=2
<u><math>i=1</math></u>	<u><math>m+n-1</math></u>	

4.14:

## o. MERGE(L, R):

1.

$$m = \text{size}(L)$$

2.

$$n = \text{size}(R)$$

$$k = 0$$

3.

$$i = 0$$

$$j = n - 1$$

while  $i \leq m$  and  $j \geq 0$ :

    if  $L[i] \leq R[j]$ :

$$A[k] = L[i]$$

$$i = i + 1$$

$$k = k + 1$$

    else:

$$A[k] = R[j]$$

$$j = j - 1$$

$$k = k + 1$$

    end if

end while

    while  $i < m$ :

$$A[k] = L[i]$$

$$k = k + 1$$

$$i = i + 1$$

    end while

    while  $j \geq 0$ :

$$A[k] = R[j]$$

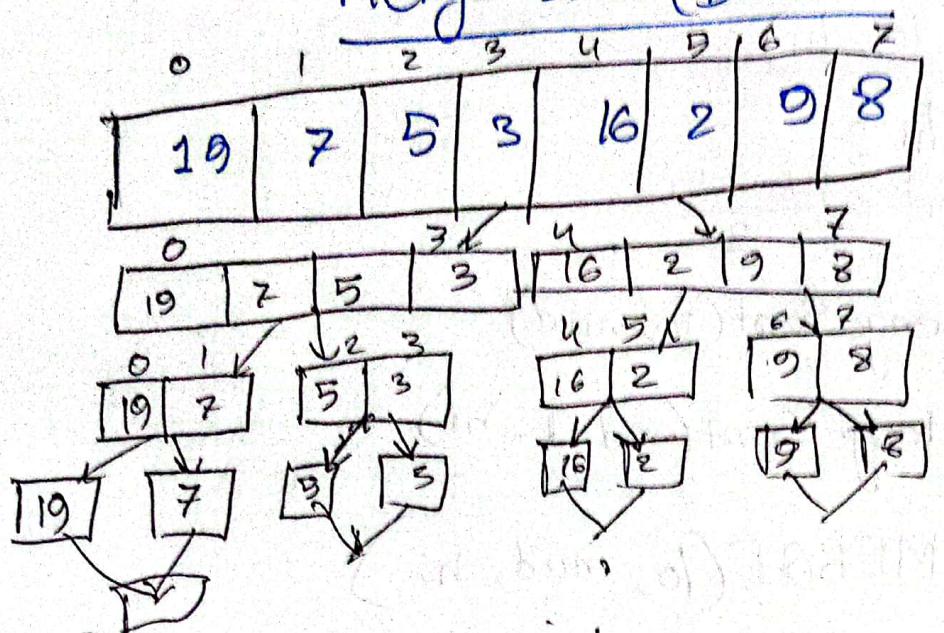
$$k = k + 1$$

$$j = j - 1$$

C-6(w-4)

29/04/24

## Merge Sort (Divide)



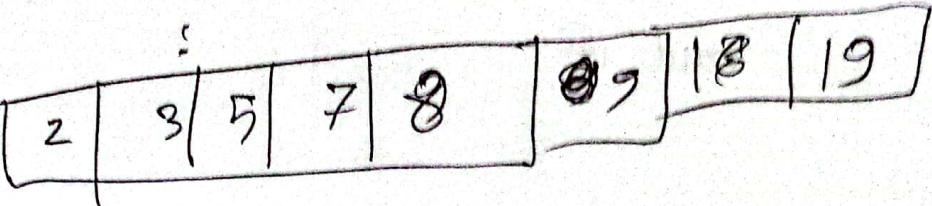
$$low = 0$$

$$hi = 7$$

$$\text{mid} = \frac{low + hi}{2}$$

$$= \frac{0 + 7}{2}$$

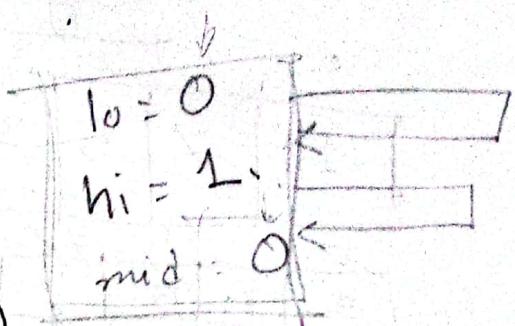
$$= 3$$



## \* Algo iarithm:

Complex:  $n \log_2 n$

0. ~~ME~~ MengeSort( $lo$ ,  $hi$ )  
if  $lo < hi$   
    mid =  $\frac{lo + hi}{2}$   
    MengeSort( $lo$ ,  $mid$ )  
    MengeSort( $mid + 1$ ,  $hi$ )  
end if MERGE( $lo$ ,  $mid$ ,  $hi$ )
- 1.
- 2.
- 3.
- 4.
- 5.
6. end if



# Q. MERGE( $l_0$ , $mid$ , $hi$ ):

1.  $m = \underline{mid - l_0 + 1}$   
 2.  $n = hi - mid$   
 3. Let,  $L[0 \dots m-1]$  and  $R[0 \dots n-1]$  be new arrays  
 4. for  $i = 0$  to  $m-1$ :  
 5.   :  $L[i] = A[l_0 + i]$   
 6. end For  
 7. For  $j = 0$  to  $n-1$ :  
 8.   :  $R[j] = A[mid + 1 + j]$   
 9. end For  
 10.  $L[m] = \infty$ ,  $R[n] = \infty$   
 11.  $i = j = 0$        $hi$   
 12. for  $k = 0$  to  $(m+n)-1$ :  
 13.   if  $L[i] \leq R[j]$ :  
 14.     :  $A[k] = L[i]$   
 15.     ~~end if else:~~  
 16.    :  $A[k] = R[j]$   
 17.    :  $j = j - 1$   
 18.   end if  
 19. end For  
 20. end For

$0 \rightarrow m+n-1$   
 $l_0 \rightarrow hi$

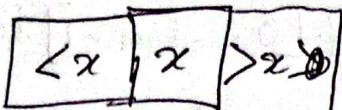
~~Q6/L-4~~

## Quick Sort

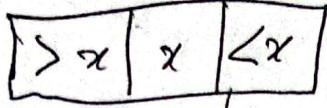
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[Online]

A number is sorted when,

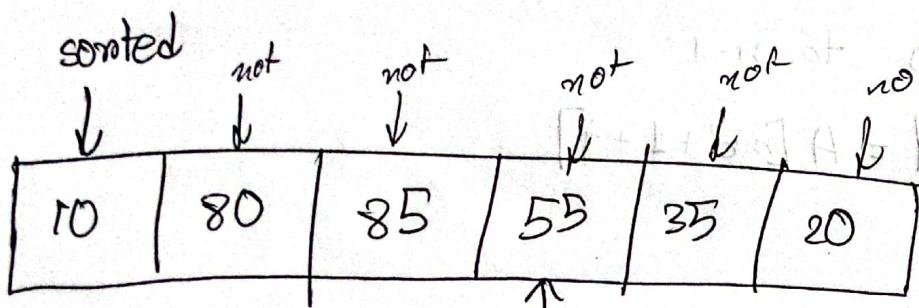


or,



all elements in  $> x$  and  $< x$  being sorted by themselves is not a requirement

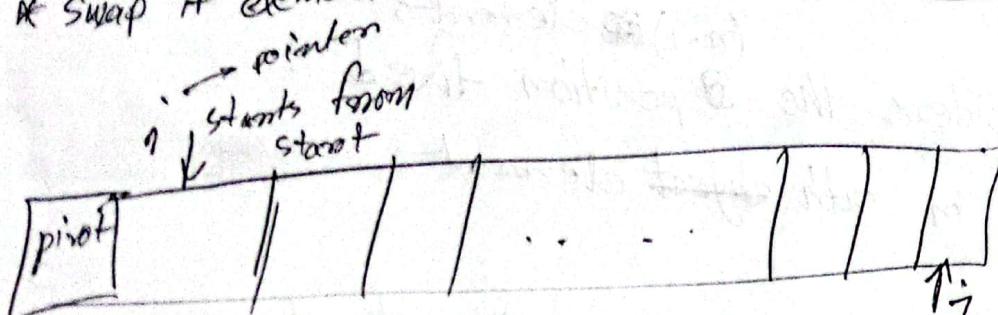
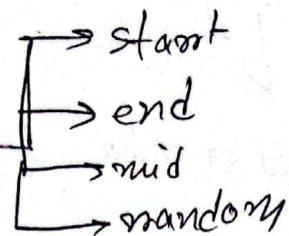
so,



might be in its position but its not correct according to the definition

\* To find the sorted position

Pivot → element in its sorted position  
can be swap if element is not in position



$p_j$  starts from end  
pointer

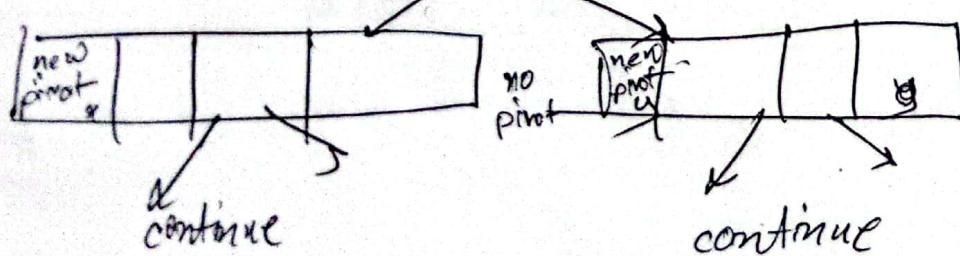
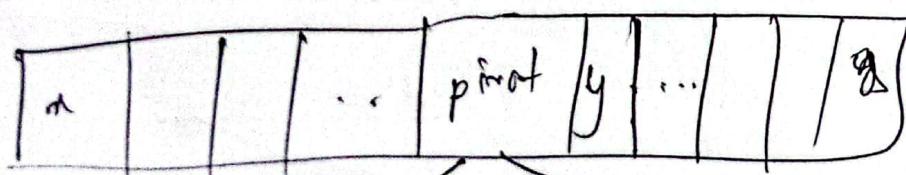
$i++$  happens when  $\leq \text{pivot}$   
until  $\geq \text{pivot}$

$j--$  happens until  $\leq \text{pivot}$   
until  $\geq \text{pivot}$

$\text{swap}(i, j)$  → swapping between small and big

when  $j < i$ ,

$\text{swap}(\text{pivot}, p_j)$  → partitioning  
swapping between ~~be~~ pivot and  $j$



\* Diff b/w merge and quick

↓  
1. based on index 1-based on pivot

Sel Sort → Considers the ~~(n-1)~~ elements  
position fixed  
Picks in nth object element

Quick Sort → Considers the nth position fixed  
Picks in (n-1) elements

## Algorithm

```
0. Partition(l0, hi):
1.   pivot = A[l0]
2.   i = l0 // starts from lowest index
3.   j = hi // " highest index
4.   while i < j: // will run until they dont cross
5.       while A[i] ≤ pivot:
6.           i = i + 1 // to find big number
7.       end while
8.       while A[j] ≥ pivot:
9.           j = j + 1 j - 1 // to find small number
10.      if i < j:
11.          swap A[i], A[j]
12.      end if
13.  end while
14. swap A[l0], A[j]
15.
16. return j
```

0. Quicksort( $l_0$ ,  $h_i$ ):

1. if  $l_0 < h_i$ :

$p = \text{Partition}(l_0, h_i)$

2. Quicksort( $l_0, p-1$ ) // left side

3. Quicksort( $p+1, h_i$ ) // right side

4.

Complexity:

Partition :  $O(n)$

Recursive Breaking Down :  $O(\log_2 n)$

$\therefore \text{Quicksort} = \cancel{\frac{\log n}{2}}$  Best :  $n \log_2 n$

Avg :  $n \log_2 n$

Worst :  $n^2$

■ Linked list can be defined as a collection of data items that can be stored in scattered memory locations. Here, data items must be linked with each others. Data items are known as ~~node~~ nodes.

\* A linear linked list (singly) is a list where there is only one way link between nodes.

\* A doubly linked list is a list where there are links in both directions between nodes.

\* A circular linked list is a list where the last node has a pointer which points to the first node.

■ Each type of linked list requires an external pointer to point the first node of the list (root).



insert

- first
- last
- anywhere

delete

- first
- last
- anywhere

traverse

- print
- search
- others,

create

- list/structure declaration
- pointer declaration

```

#include
using
struct node
{
    int data;
    * address
    node * address
};
```

```
node * root = NULL;
```

```
int main()
```

```
{
```

```
node * A, * B, * C;
```

A = new node();

B = new node();

C = new node();

A. data = 10; A → data = 10;

B. data = 20; B → data = 20;

C. data = 30; C → data = 30;

A → address = B

B → address = C

C → address = NULL

cout << A.data << B "B" << B.data << " " << C.data;

root = A;

cout << A → data << " " << A → address → data << " " \*

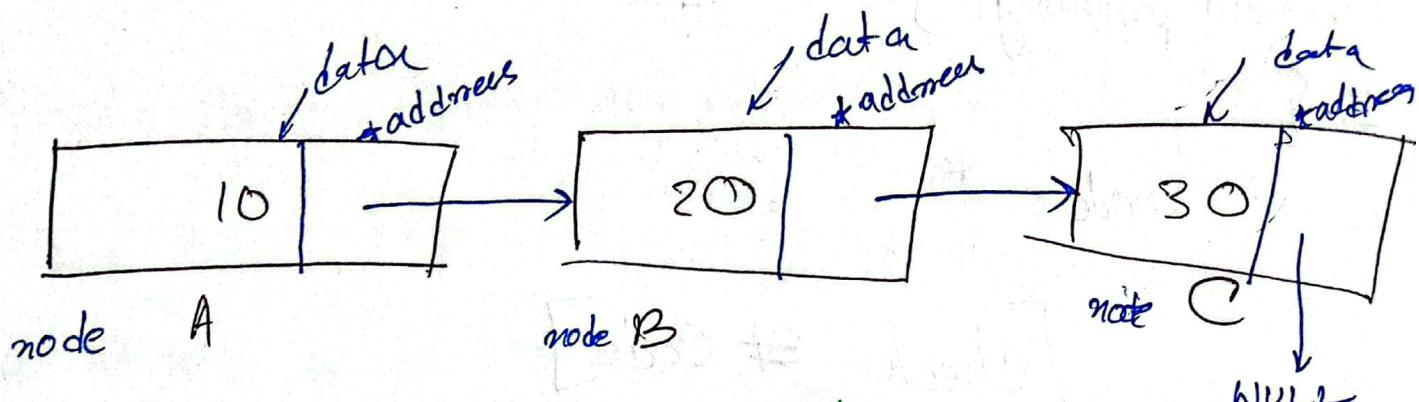
(root

<sup>root</sup>

<< A → address → address → data;

root

↳ share error



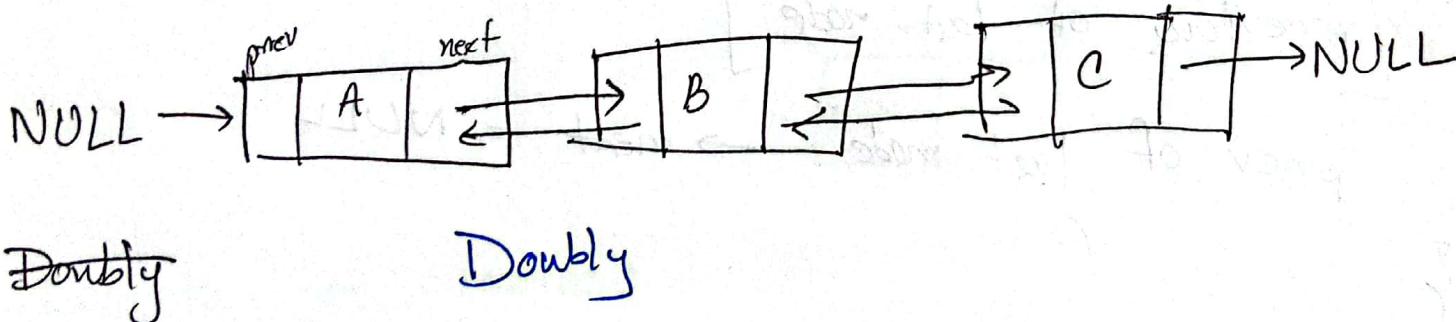
\* we want to call B and C with A

\* Not possil Does not have same sequential address

\* A will have address of B

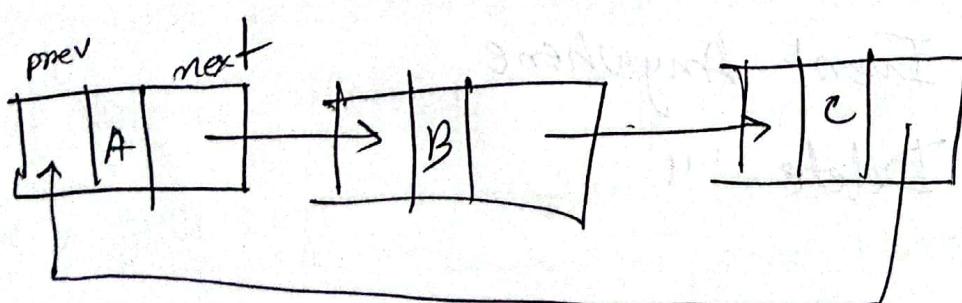
\* data type will be struct for struct pointers.

\* Cpp uses  $\rightarrow$  for pointers struct.



Doubly

Doubly



0. void printing()

1. {

2.     node \*

[Check st code]

\* Always assume list is ready

\* If inserted at first, the list is ~~then~~ automatically reversed.

void delete last()

{

[previous of last node]

prev of last node → next = NULL

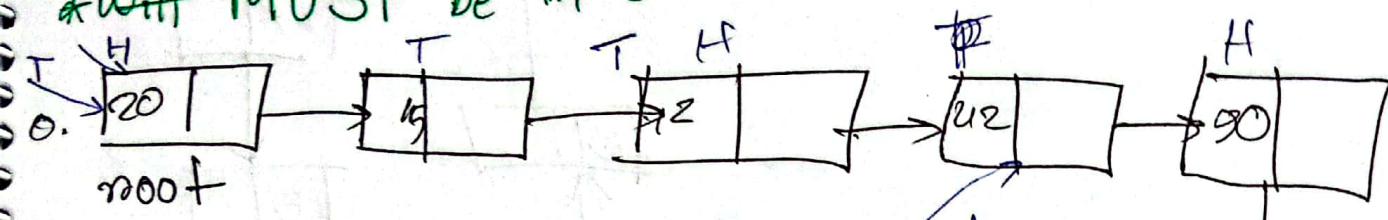
}

\* Assignment : Insert Anywhere

Delete ::

## Floyd's Cycle Finding Algorithm ('Hare and Tortoise Algorithm')

\* MUST be in exam

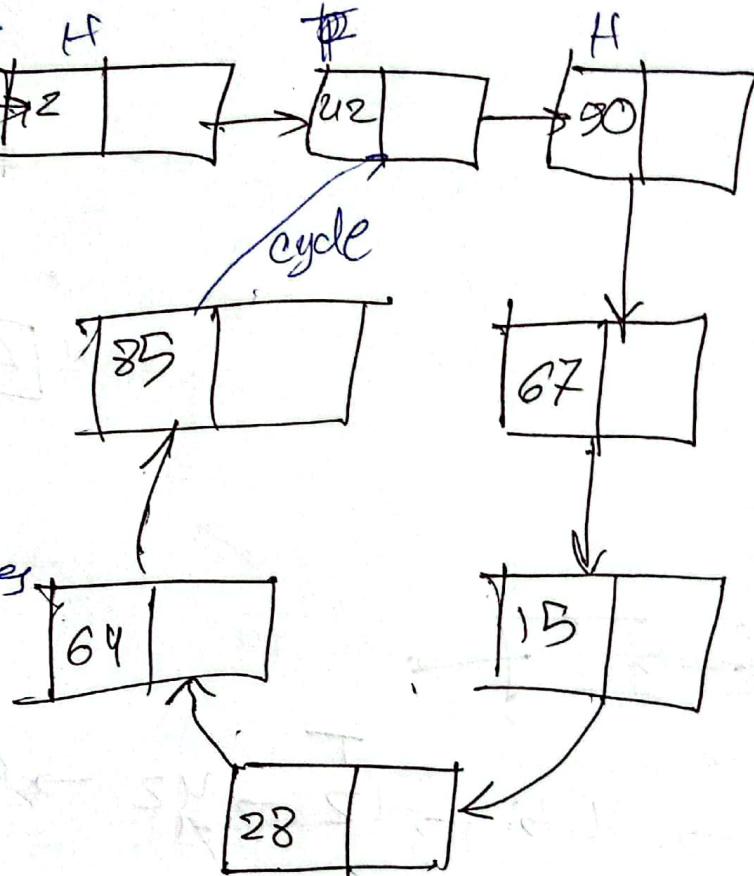


\* node \* curr

will be node \* tortoise

\* Tortoise will move 1 node

\* Hare will move 2 nodes

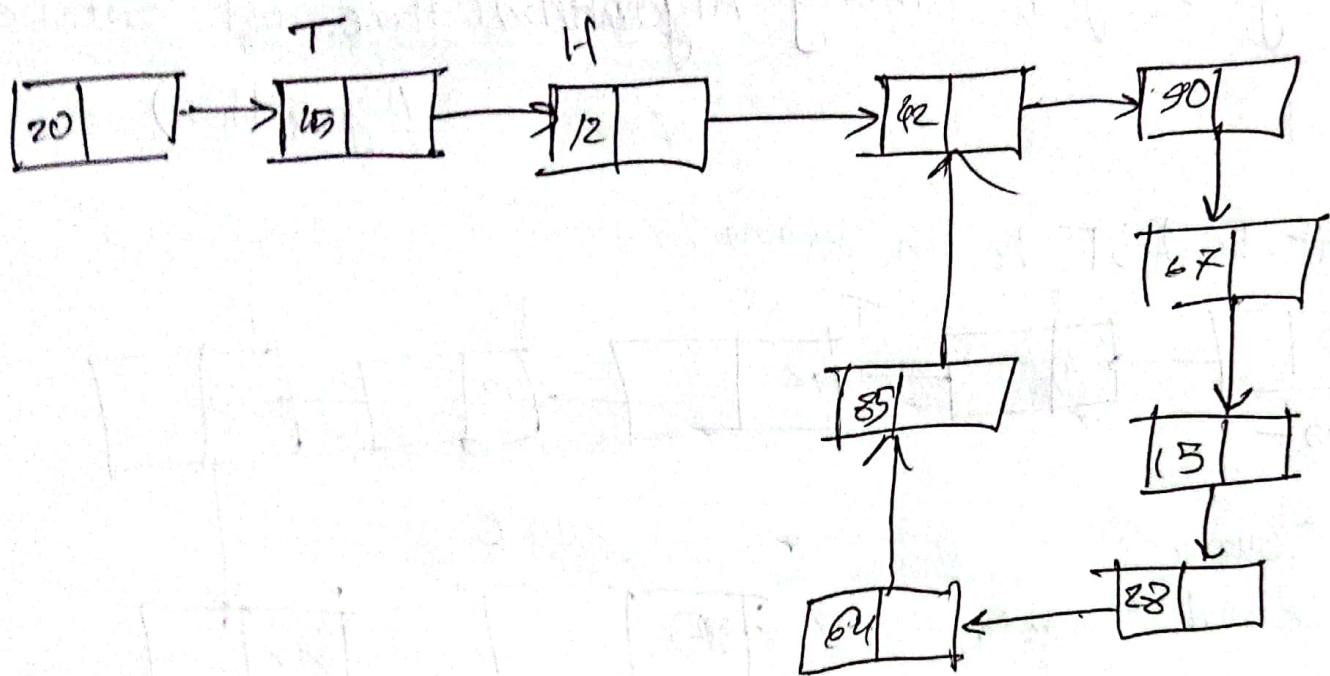


\* Imp for job interview

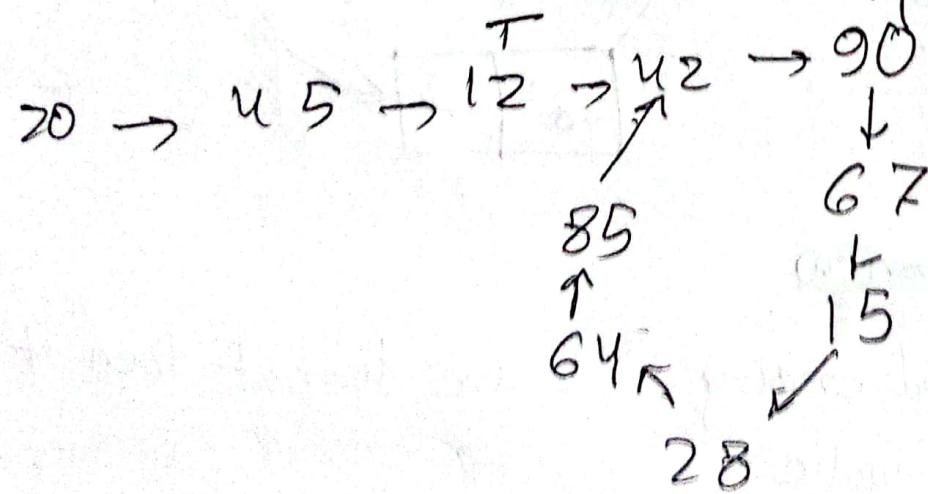
\* If starting node and ending nodes are distinct then it is a will not be cyclic

\* To check, you can → the Map nodes  
 → Compare address

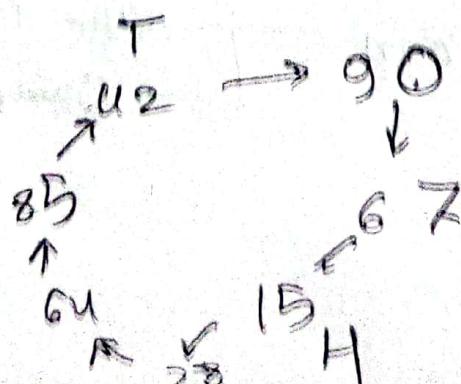
1.

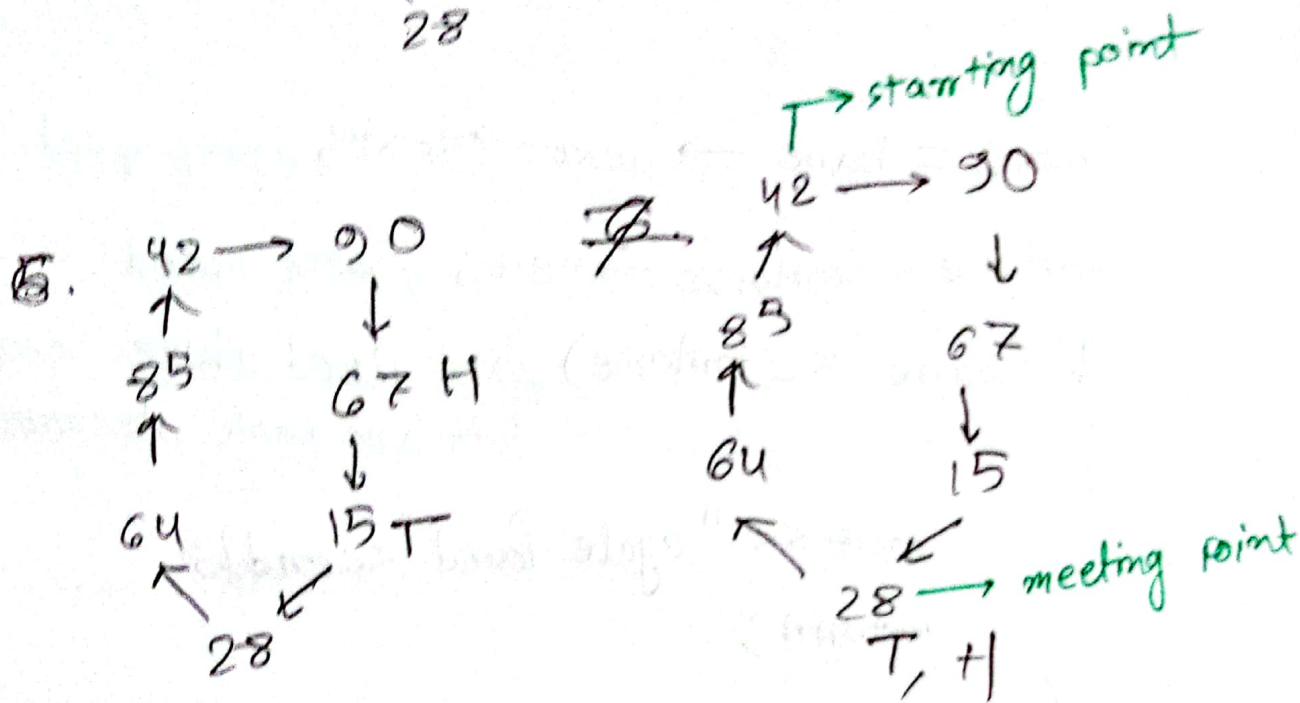
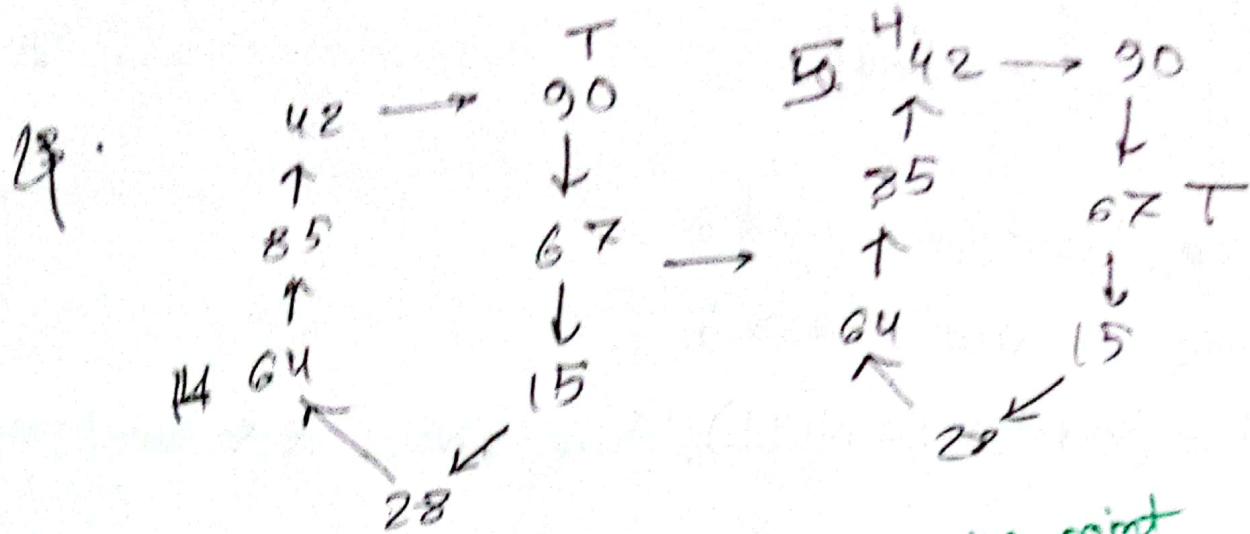


2.



20 3





$\therefore$  T and H will meet if and only if one runs  
at the other's multiple speed

void cycle → void find()

{  
node \*tortoise = root;  
node \*hare = root;

while (tortoise != NULL) // (hare != NULL && hare->next != NULL)

{

    hare = hare → next → next; // jump speed

    tortoise = tortoise → next; // move speed

    if (hare == tortoise) // Not placed above because  
        both are roots at start

{

        cout << "cycle found" << endl;  
        return;

}

{

    cout << "cycle not found" << endl;

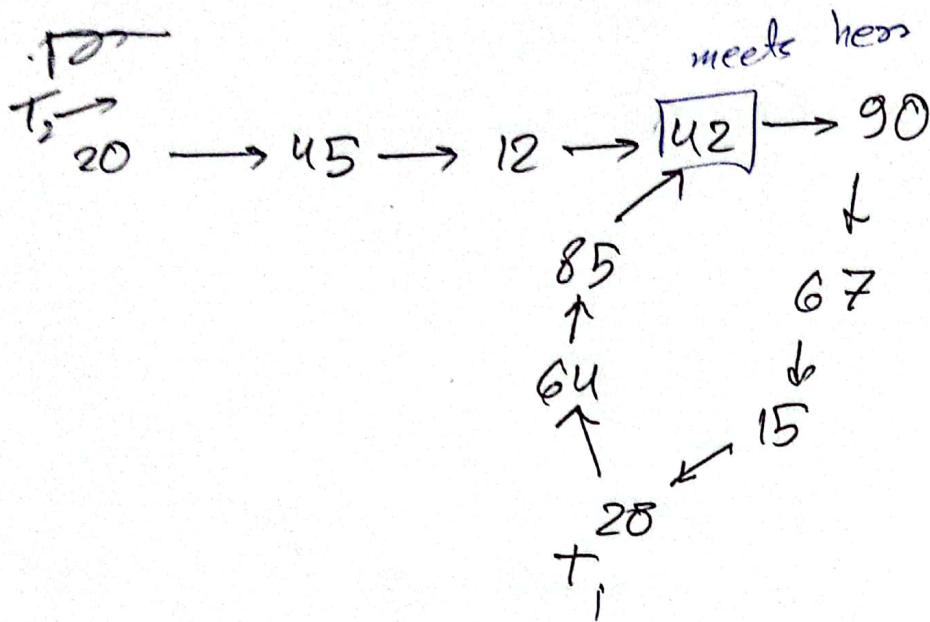
}

\* Complexity:  $O(m \times n)$

+ shafayet's planet

\* Multiple of each other

\* To find meeting point



```
void starting_node()
```

```
{ node *tortoise = root;
```

```
while( . . . )
```

```
if (hare == tortoise)  
{ cout << "cycle found" <endl;  
}
```

```
}
```

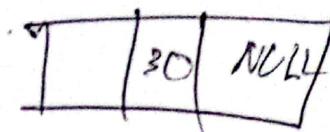
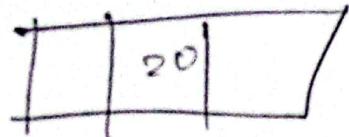
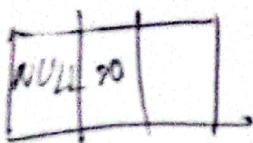
```
node *tortoise2 = root;
```

```
while(tortoise != tortoise)
```

```
{ tortoise = tortoise -> next;
```

```
& cout << tortoise -> data -> next -> next -> next << endl;
```

## Doubly Linked List



Insert anywhere:

curr\_node  $\rightarrow$  next = temp

temp  $\rightarrow$  next = poren\_node

+ do prev as well

end

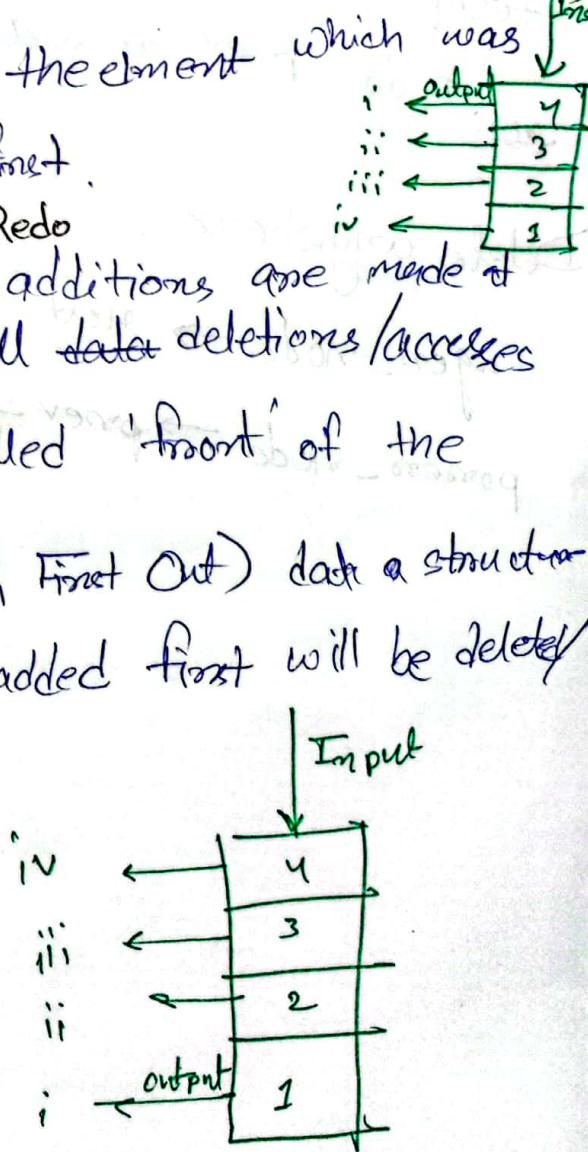
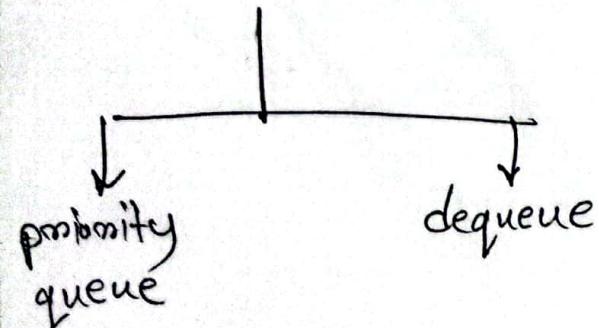
Delete anywhere:

agen\_node  $\rightarrow$  next = poren\_node

poren\_node  $\rightarrow$  prev = agen\_node

## Stack and Queue

- Stack is a linear list where any element is added at the top of the list and any element is deleted/ accessed from the top of the list. Add operation for a stack is called 'push' operation and deletion operation is called 'pop' operation. Stack is LIFO (Last In First Out) data structure. That means the element which was added will be deleted/ accessed first.
- Example: Scrolling/Browsing/ Undo + Redo
- Queue is a linear list where all additions are made at one end, called 'rear' and all deletions/ accesses are made from another end called 'front' of the list. Queue is a FIFO (First In First Out) data structure. That means the element that is added first will be deleted/ accessed first.



STL Standard template library

// include

using namespace

```
int main()
```

```
{
```

stack<int> s; // container

```
s.push(10);
```

```
s.push(20);
```

```
s.push(30);
```

```
s.push(40);
```

```
cout << s.size() << endl;
```

```
while (true) // while (!s.empty())
```

```
{ if (s.size() > 0)
```

```
    int val = s.top();
```

```
    cout << val << endl;
```

```
    s.pop();
```

```
}/
```

```
}/
```

```
}/
```



## Stack

using Linked List.

push() ——> insertFirst()

top() ——> root —> data

pop() ——> deleteFirst()

size() ——> size() // count ++

empty() ——> size() // count == 0

\* if inserted last, deleted last

## Queue

push() ——> insertLast()

front() ——> root —> data

pop() ——> deleteFirst()

size() ——> size() // count ++

empty() ——> size() // count == 0

## STL

### Queue

```
#include <queue>
```

```
using namespace std;
```

```
int main()
```

```
{
```

```
queue<int> s;
```

```
s.push(10);
```

```
s.push(20);
```

```
.
```

```
.
```

```
while (!s.empty())
```

```
{
```

```
int val = s.front();
```

```
.
```

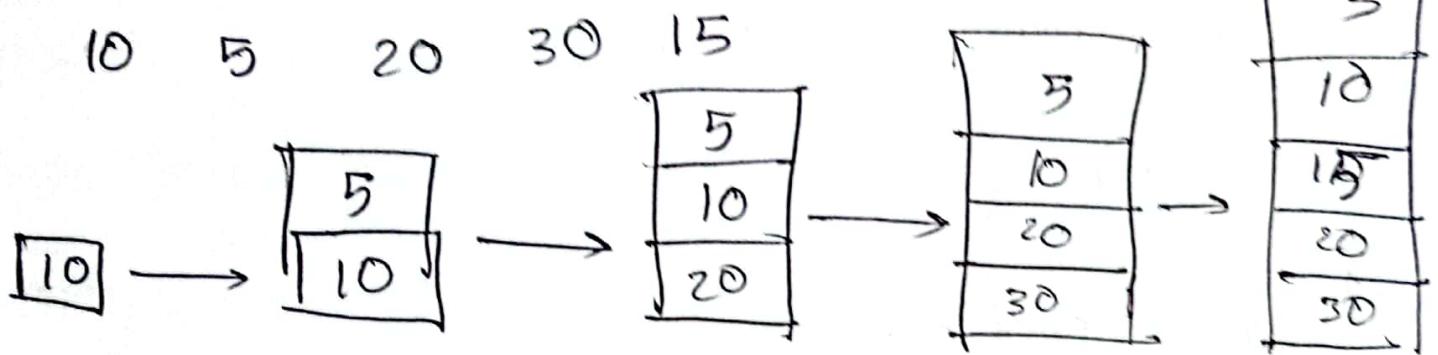
```
.
```

```
}
```

```
}
```

## \* Priority Queue

\* Setting condition for data insertion



priority - queue <int> s;

for descending

s.push(-data)

cont << -val << endl;

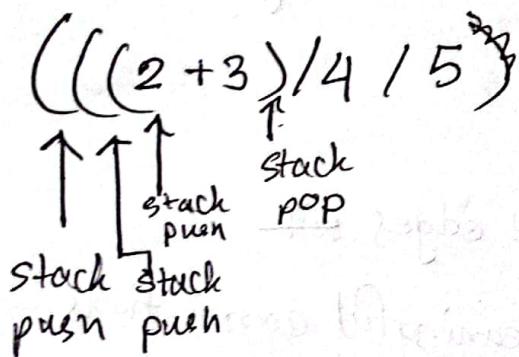
for ascending

## \* Dequeue

\* Not necessary

\* Double ended removal + addition.

## \* Balanced Parentheses Problem (Stack)



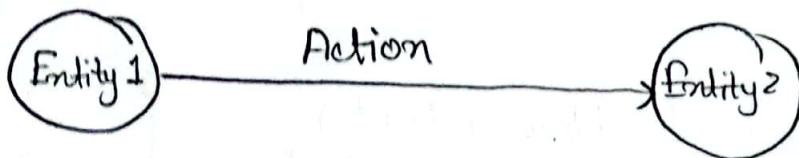
If stack size != 0, not balanced parentheses

## \* LightOg

↳ Discovering the web

stack < char > temp  
{'{', '[', '(', '}', ']', ')'}  
→

Graph  $\rightarrow$  30/100 in lab  
 $\rightarrow$  30/100 in theory



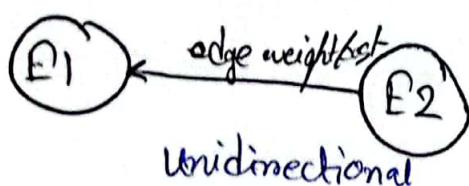
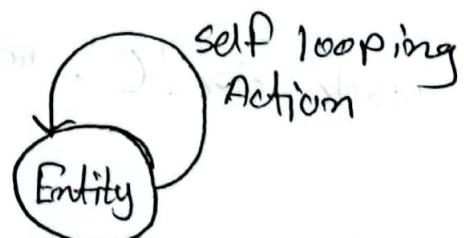
whatever Entities must have meaningful connections.

Graph: \* A group of nodes and edges with

\* Nodes will have meaningful connections

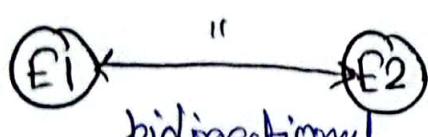
\* Connections are edges.

\* Nodes > Edges

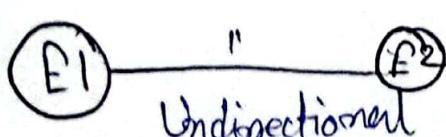


$\rightarrow$  At least 1 node is mandatory

$\rightarrow$  Edges are not mandatory



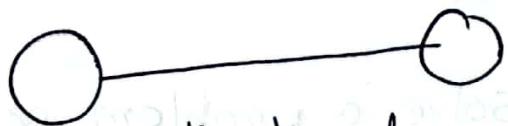
Difference:  
 bidirectional can have 2 different weight  
 unidirectional will ALWAYS have same weight



All bidirectional are unidirectional  
 but not all unidirectional are bidirectional



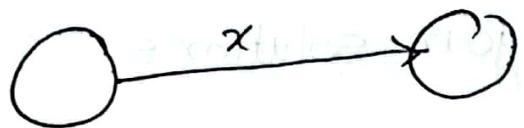
unidirectional  
unweighted graph



undirectional  
unweighted graph



bidirectional  
weighted graph



unidirectional  
weighted graph

- \* If any graph has at least one detached node, it is called disconnected graph
- \* Max edges :  $\frac{n(n-1)}{2} \cdot [\text{Undirectional}]$

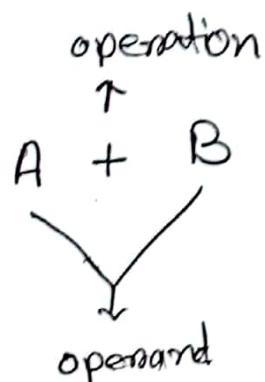
\* Max edges in unidirectional, undirectional and bidirectional?

## Expression

(Part of stack)

An arithmetic expression can be represented in various

forms such as prefix, infix or postfix. 'Pre', 'In', 'Post' refer to the relative position of the operator with respect to its operands. For example:



infix : < operand > < operator > < operand >

prefix : < operator > < operand > < operand >

postfix : < operand > < operand > < operator >

$A + B$ ; Easy for human

$+ A B$ ; Hard for computer

$6 + 2 * 7$

Precedence

Associativity

(i) (), {}, []

(ii)  $\wedge$ ,  $\neg$  R - L

(iii)  $*$ ,  $/$  L - R

(iv)  $+$ ,  $-$  L - R

Prefix:

\* A \* B + C / D

=> \*AB + C / D

=> x + C / D

=> x + /CD

=> x + y

=> + xy

=> + \*AB / CD (Ans)

$$1. a + b * c / d$$

$$2. 5 * (6+2) - (12/4)$$

$$1. a + b * c / d$$

$$\Rightarrow a + *bc / d$$

$$\Rightarrow a + x / d$$

$$\Rightarrow a + /xd$$

$$\Rightarrow a + y$$

$$\Rightarrow +ay$$

$$\Rightarrow +a / xd$$

$$= +a / *bcd \checkmark$$

$$2. 5 * (6+2) - (12/4)$$

$$\Rightarrow 5 * (+62) - (124)$$

$$\Rightarrow 5 * a - b$$

$$\Rightarrow +\cancel{5}a - b$$

$$\Rightarrow c - b$$

$$\Rightarrow -\cancel{b}cb$$

$$\Rightarrow -\cancel{\frac{5}{1}} * \cancel{ab}$$

$$\Rightarrow -\cancel{+62} / \cancel{124}$$

$$\Rightarrow - - * 5 + 62 / 124$$

## Postfix

$$* a + b * c / d$$

$$* A * B + C / D$$

$$\Rightarrow a + b c * / d$$

$$\Rightarrow A B * + C / D$$

$$\Rightarrow a + x / d$$

$$\Rightarrow x + C / D$$

$$\Rightarrow a + y z d /$$

$$\Rightarrow x + y$$

$$\Rightarrow a + y$$

$$\Rightarrow x y +$$

$$\Rightarrow a y +$$

$$\Rightarrow A B * C D / +$$

$$\Rightarrow a x d / +$$

$$d o g - <$$

$$> a b c * d / + \checkmark$$

$$p d g - <$$

$$+ 5 * (6 + 2) - (12 / 4)$$

$$+ 5 * 6 2 + - 12 4 /$$

$$= 5 * x - y$$

$$= 5 x * - y$$

$$= z - y$$

$$= z y -$$

$$= 5 x * 12 4 / -$$

$$= 5 6 2 + * 12 4 / -$$

$$* K + L - M * N / P \wedge Q$$

$$\Rightarrow K + L - M * N / \underline{Q P A}$$

$$\Rightarrow K + L - M * N / a$$

$$\Rightarrow K + L - \frac{MN*}{b} / a$$

$$\Rightarrow K + L - b / a$$

$$\Rightarrow K + L - \frac{ba}{c}$$

$$\Rightarrow K + L - c$$

$$\Rightarrow \frac{KL+}{d} - c$$

$$\Rightarrow d - c$$

$$\Rightarrow dc -$$

$$\Rightarrow KL + ba / -$$

$$\Rightarrow KL + MN * QPA / -.$$

Tower of Hanoi

- Three towers fixed
- all discs from source to destination
- at any time, no large disc on top of smaller ones.

Answer Steps:

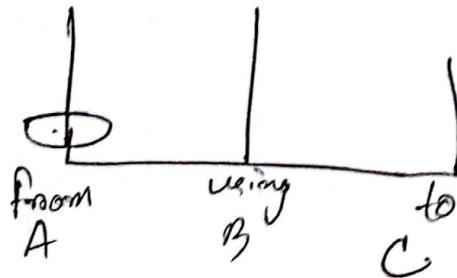
1. A to C
2. A to B
3. C to B
4. A to C
5. B to A
6. B to C
7. A to C



$$n = 3$$

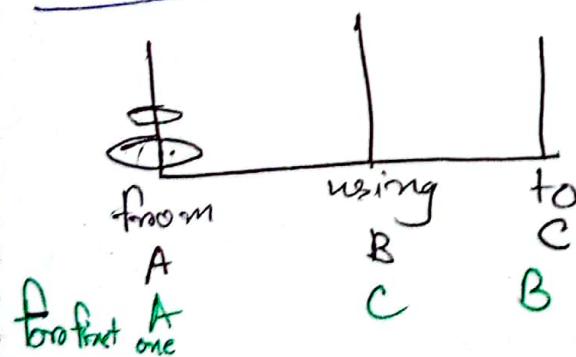
$$\begin{aligned}2^n - 1 &= 2^3 - 1 \\&= 7\end{aligned}$$

Solution for 1 disc ( $n=1$ ):



- Move a disc from A to C

Solution for 2 discs ( $n=2$ ):



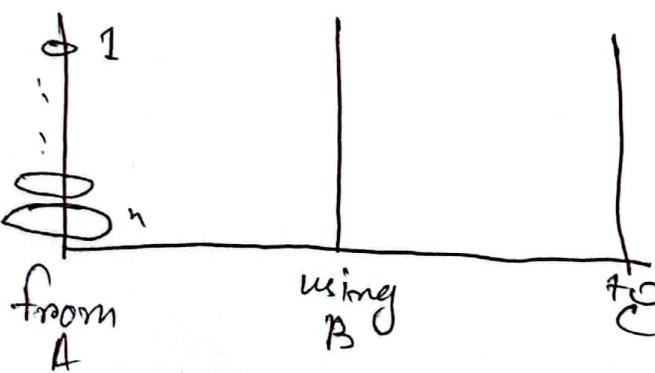
- Move <sup>1</sup> disc from A to B using C
- Move disc from A to C
- Move disc from B to C using A

Solution for 3 discs ( $n = 3$ ):



- Move 2 discs from A to B using C
- Move a disc from A to C
- Move 2 discs from B to C using A

Solution of  $n$  discs: (n)



- Move  $(n-1)$  disc from A to B using C
- Move a disc from A to C
- Move  $(n-1)$  discs from B to C using A

Code: disc no. pillars/towers  
void TOH ( $n$ ,  $\overbrace{A, B, C}^{\text{pills/towers}}$ ) // (no. of discs, from, using, to)  
{

~~TOH~~

if ( $n > 0$ )  
{

TOH ( $n - 1$ , A, C, B)

point A to C // A to C will be changed depending  
on the recursion

TOH ( $n - 1$ , B, A, C)

}

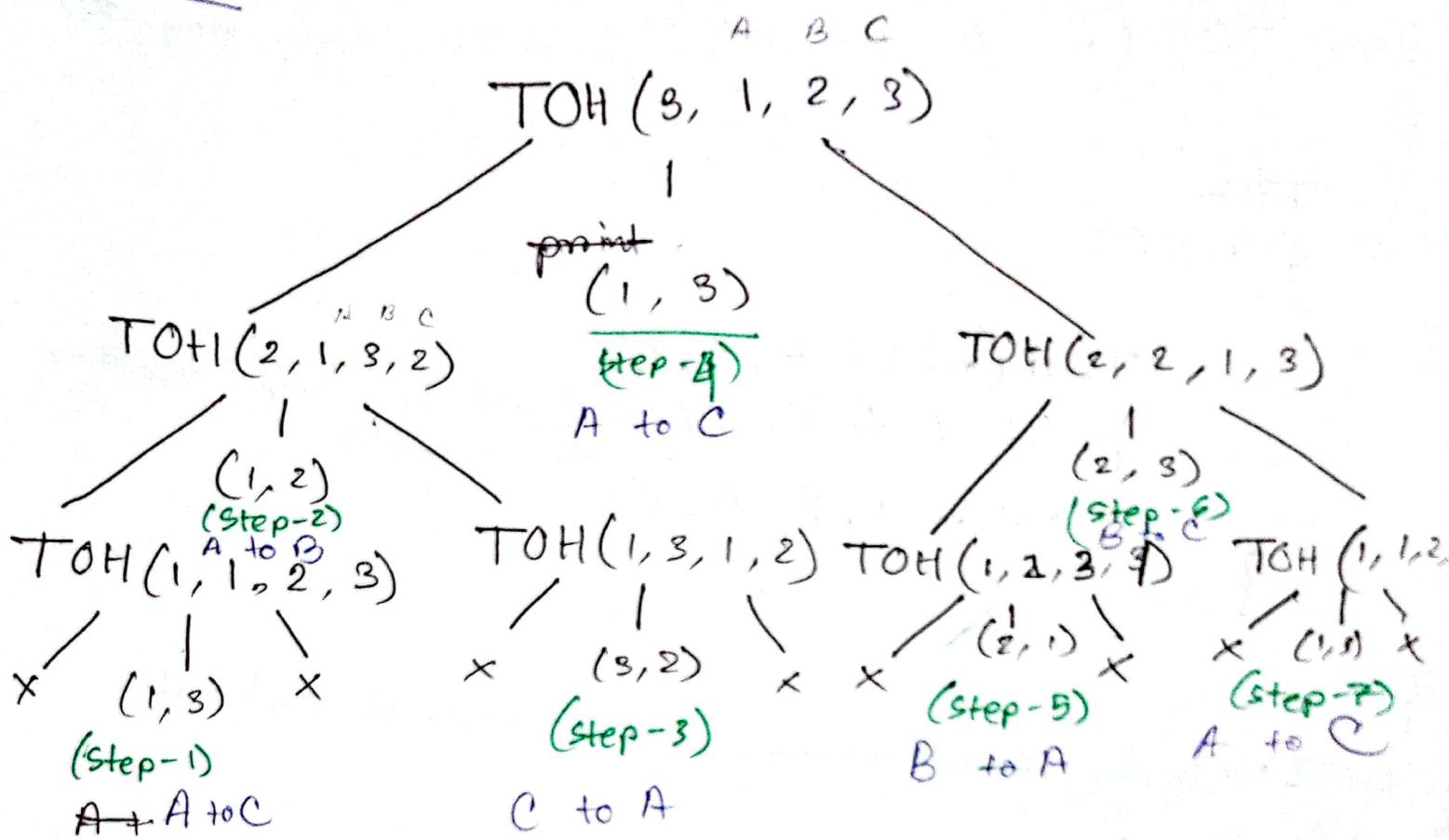
}

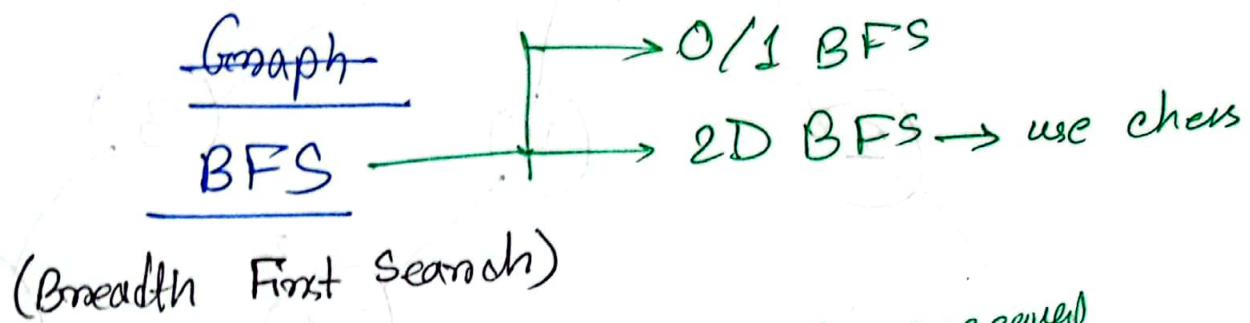
// for DMT Dynamic Programming, use an array for each state  
Complexity:  $2^n$

+ [zobayer.blogspot.com](http://zobayer.blogspot.com) - I, Me and Myself  
- Attacking Recursion

\* Do TOH for 4 towers

## Execution:





- We have a graph: unweighted // all weights are equal
- we assume that all edges have equal/same weight
- Task: We have to find the shortest path length/path itself  
from a source node to a destination node.  
// Try to find all possible paths

### BFS Procedure:

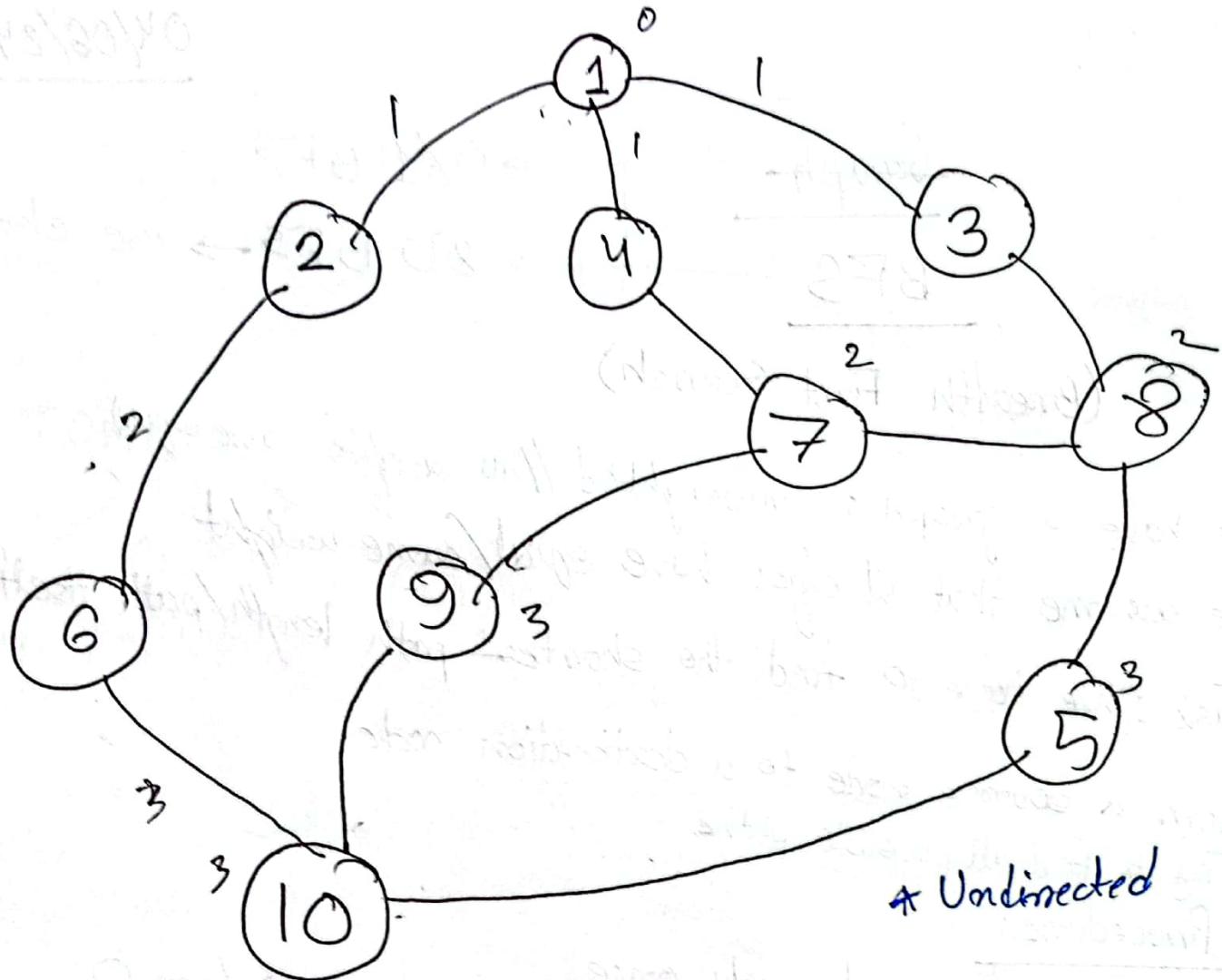
- we visit a node only once
- we assume that the source node is in level 0/gen 0
- All the nodes reachable from source nodes are in level 1;
- all the nodes reachable from level 1 are in level 2 and so on. -

\* Can find the length with path

\* Path: All nodes passed through to reach a destination

\* Considers everything other than source as destination

- Considers each path as unique



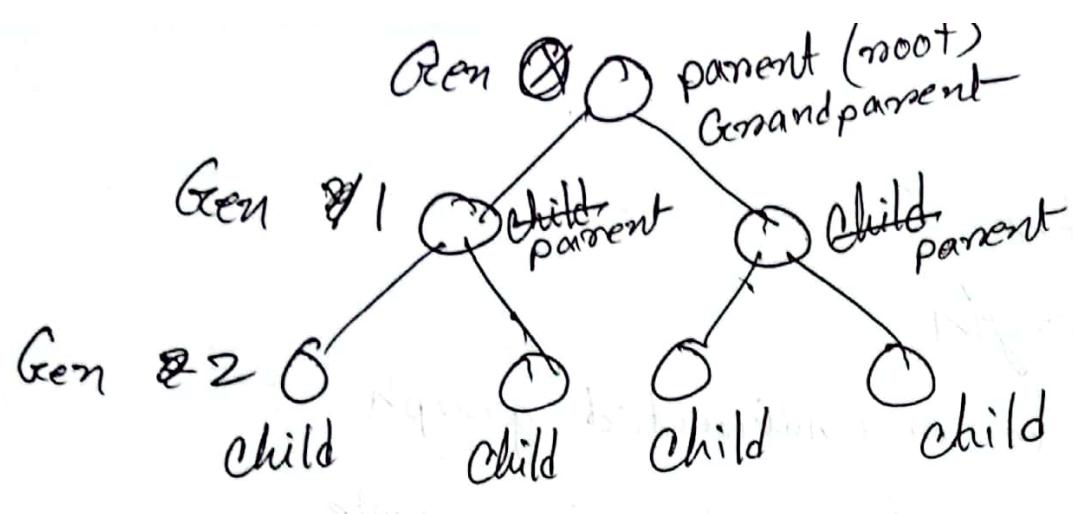
<u>Input</u>	
10	13
1	2
1	4
1	3
2	6
u	7
3	8
3	7
6	10

	9	10
9	7	8
8	5	10
5		

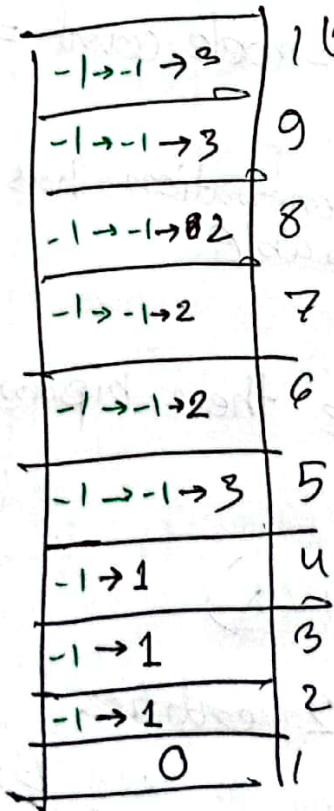
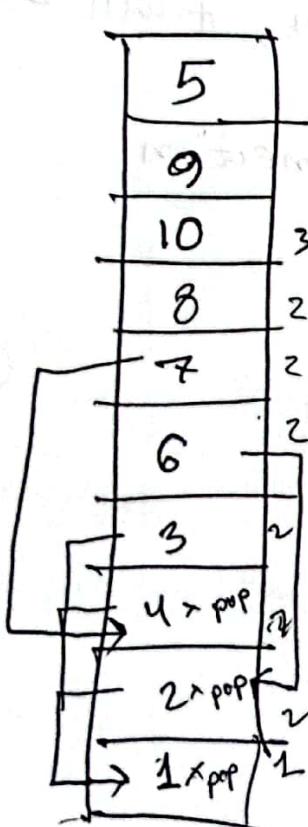
Adjacency list

---

- 1 → 2, 4, 3
- 2 → 1, 6
- 3 → 8, 1, 8, 7
- 4 → 1, 7
- 5 → 3, 10
- 6 → 10, 2, 10
- 7 → 8, 4, 3, 9, 8
- 8 → 3, 5, 7, 5
- 9 → 10, 7
- 10 → 6, 9, 5



- Find Generation
- Same generation will not have multiple parents



Queue

## \* BFS solves :

- Finds shortest path
- Finds distance length
- Cycle detection in an undirected graph
  - ↳ if edge count reduces, there is a cycle  
*(loop)*
- Bi-colorable
  - ↳ Cycle ~~→ edge count = node count in cycle~~
  - ↳ if edge count = node count = even, it will be bicolorable
  - ↳ if nodes in same generation has connection then not bicolorable
- Bi-partition
  - ↳ if bicolorable then bipartite
- Commandos (Light OJ, UVa)
- Any problem involving 2 entities
  - ↳ try to use BFS

\* MEGA MEAT MAN

\* Farthest node in a tree - (I) and (II)

\* Going Together

## Algorithm:

0. BFS (source)
1. Declare a queue
2. Enque source
3. level [source] = 0
4. while queue is not empty
5.    u = deque
6.    remove u from queue
7.    For all adjacent nodes of u: // to adjacency
8.       v = adjacent node of u // v is child, u is parent
9.       if level[v] = -1  
10.          level[v] = level[u] + 1  
11.          Enque v
12.     end if
13. end for
14. end while

Complexity:  $O(\text{node} + \text{edge}) = O(n + m)$

## Code:

Q. void

int level[72];

Q. void BFS(int source){

1. queue <int> Q;

2. Q.push(source);

3. level[source] = 0;

4. while(Q.empty()) {

5. int u = Q.front();

6. Q.pop();

7. for(int j = 0; j < NodeVec[u].size(); j++)

8. int v = NodeVec[u][j];

9. if (level[v] == -1) {

10. level[v] = level[u] + 1;

11. Q.push(v); }

}

}

}

C-10 (W-9)

04/03/24

Infix to Postfix  
using Stack

$$A * (B + C) - (D/E)$$

Pre: ~~A \* x - y~~  $A * (+BC) - (/DE)$

$$\textcircled{1} = A * x - y$$

$$= * Ax - y$$

$$= z - y$$

$$= - zy$$

$$= - * Ax y$$

$$= - * A + BC / DE$$

Post:  $A * (B + C) - (D/E)$

$$= A * (BC+) - (DE/)$$

$$= A * x - y$$

$$= Ax * - y$$

$$= z - y$$

$$= zy -$$

$$= Ax * y -$$

$$= ABC + DE / -$$

## Infix to Postfix :

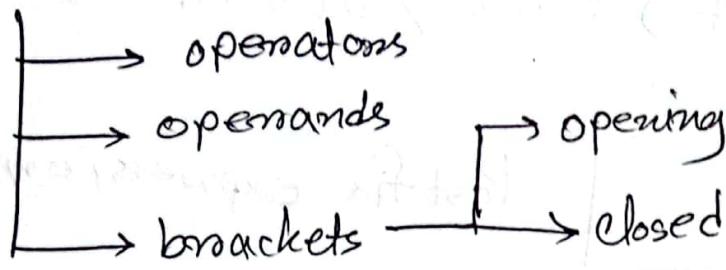
$$A * (B + C) - (D / E)$$

For negative numbers:  
convert  $-x$  to  
 $(-1)^x$

Symbol scanned	Stack	Postfix
A		A
*	*	<del>A</del> - (B + C) + D / E
(	* , (	<del>A</del>
B	* , (	<del>AB</del>
+	* , ( , +	<del>AB</del>
C	* , ( , +	<del>ABC</del>
)	* <del>POP</del>	<del>ABC +</del> → lower precedence
-	-	<del>ABC + ABC + *</del>
D	- , (	<del>ABC + *</del>
/	- , ( , /	<del>ABC + * D</del>
E	- ; ( , /	<del>ABC + * D E</del>
)	-	<del>ABC + * D E /</del> <del>ABC + * D E / -</del>

## Symbol Table

options:



Precedence

parantheses

1

\* , /

+ , -

Conversion: → Write for prefix

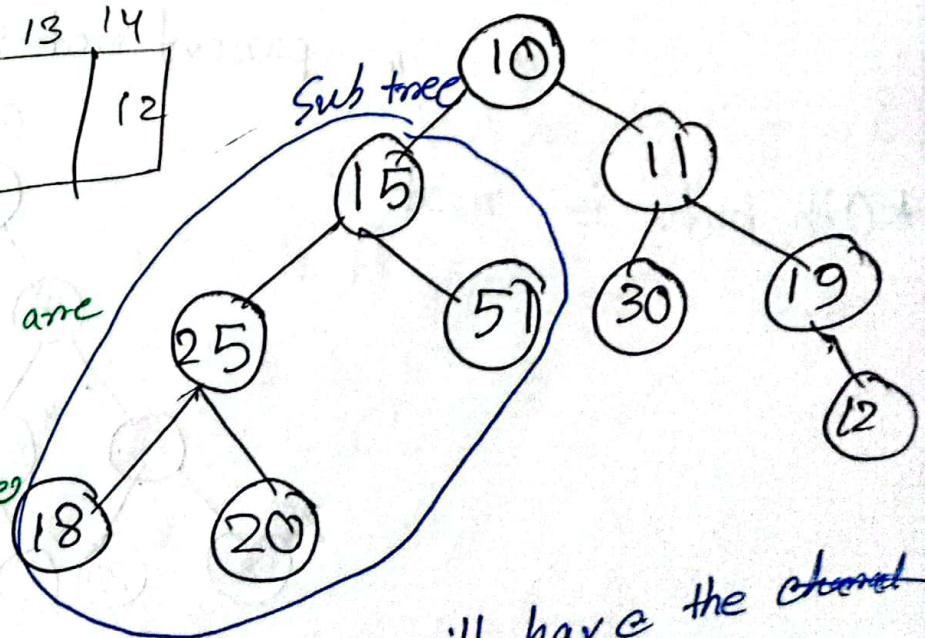
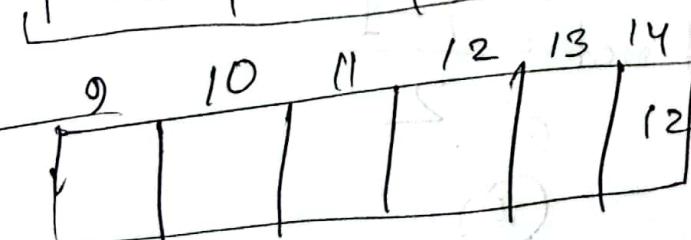
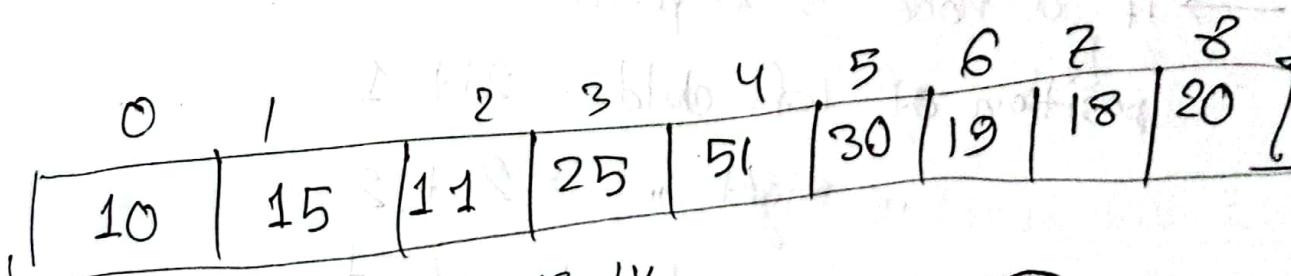
- 1) If symbol = operand, add to postfix
- 2) If symbol = '(', push to stack
- 3) If symbol = operation, check top of stack
  - i) if precedence (Symbol)  $\geq$  precedence (stack top), push symbol to stack.
  - ii) Otherwise, pop one by one from stack (operations) and add to postfix until ' $'('$ , is added to postfix'
- 4) If symbol = ')', pop one by one (Other solutions are available)

$$(A+B/C)* (D+E) - F = A BC/DE + * + F - \text{Ans}$$

Symbol	Scan	Stack	Postfix expression
(		(	
A		+ C	A ✓
+		(, +	AB ✓
B		(, +, C	ABC ✓
/		(, +, /	ABC/
C		(, +, /, C	ABC/
*		(, +, *, C	ABC/*
(		(, +, *, (	ABC/*(
-		(, +, *, (, -	ABC/*(-
D		(, +, *, (, -, D	ABC/*(-D
+		(, +, *, (, -, +	ABC/*(-+)
E		(, +, (, *, (, +	ABC/*(-+E
)		(, +, (, *, (, +	ABC/*(-+E+
-		(, +, (, *, (, +	ABC/*(-+E+*
F		(, *, (, +, (, +	ABC/*(-+E+*F
)		-	ABC/*(-+E+*F -

Tree

- \* A tree is a finite collection of nodes that reflects one to many relationship among the nodes. An ordered tree has a specially designated node called root node. The nodes of a level are connected to the nodes of the upper level. The node that has no child is called leaf node. A node with a child node is called parent node.



\* All non-leaf nodes are parent nodes

\* Basic tree = m-many trees

\* All sub trees will have the characteristics of parent tree

\*Binary Tree: A finite set of nodes with a root node and every node has at most 2 children.

In a binary tree, //For Array

→ if no. of levels = k then,

maximum number of nodes in tree,  $n = 2^k - 1$

→ if maximum no. nodes = n then,

no. of levels in tree,  $k = \lceil \log_2(n+1) \rceil$

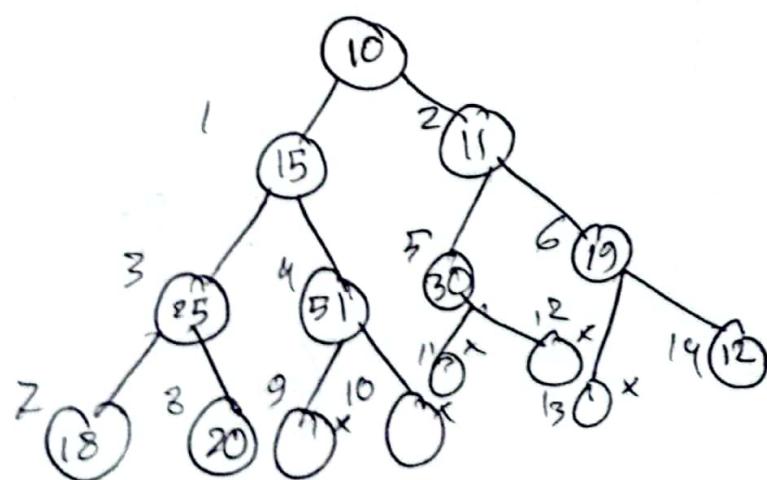
→ if a node is in position = i then,

position of left child =  $2i + 1$

" " right " =  $2i + 2$

" " parent node =  $\frac{i-1}{2}$

k0th index is root



• Doubly linked list can also make binary tree

## \* Tree Traversal Technique:

(a) Pre - Orden

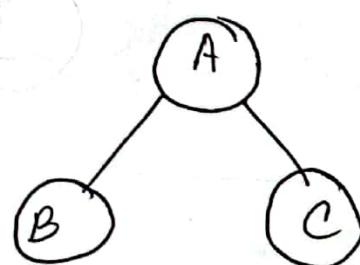
root  
left  
right

(b) In - Orden

left  
root  
right

(c) Post - Orden

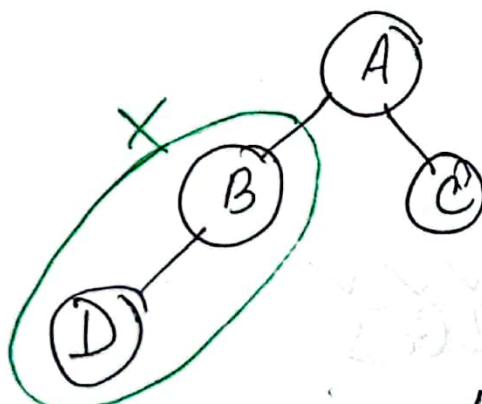
left  
right  
root



Pre : ABC

In : BAC

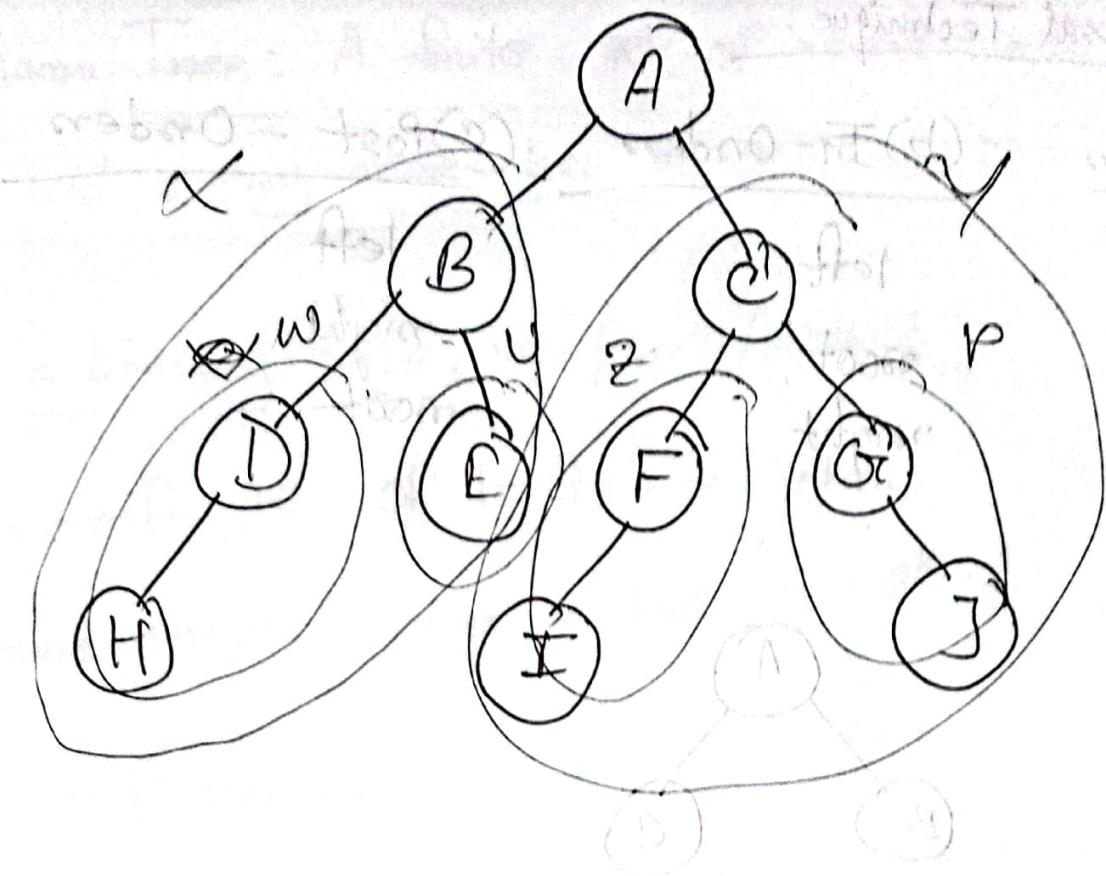
Post : BCA



Pre - orden : AXC = A BDC

In - orden :

Post - orden :



Pre : AXY

= ABWUCZP

= ~~A B D H E C F I G J~~

Post In : xAY

= WBUAZCP

= ~~H D B E A F F C G J~~

Post : XYA = ~~W U B A Z P C A~~

= ~~H D B E B I F J G C A~~

## \* Algorithm:

O. Pre-orden ( temp ) :

```
1. if temp ≠ NULL :  
2.   print temp → data // print in in-order  
3.   pre-orden (temp → left) // print in post  
4.   pre-orden (temp → right) // print in post  
5. end if
```

\* For array implementation we send index

\* Root is printed directly

Complexity:  $O(n) = \log_2(n)$

## \* Categories of Binary Tree:

(a) Rooted Binary

(a) Rooted Binary Tree:

Every binary tree is a rooted binary tree.

(b) Full Binary Tree:

A binary tree in which every node has either

- ① or 2 nodes.

(c) Perfect Binary Tree:

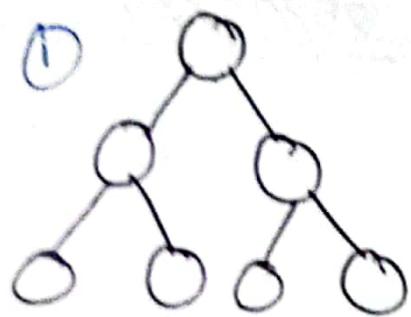
A binary tree in which all internal nodes have

2 children all leaves one

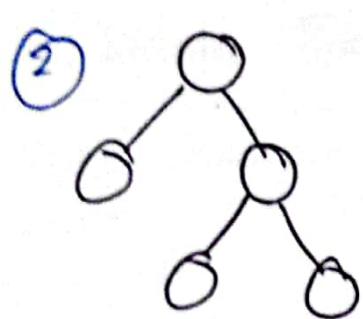
in the same level.

(d) Complete Binary Tree:

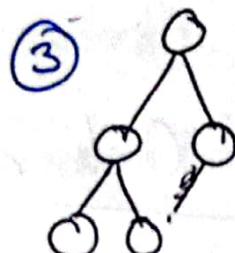
A binary tree in which every level except  
possibly the last is completely filled and nodes in  
the last level are as far LEFT as possible



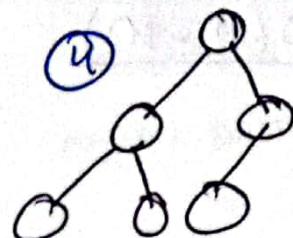
- Rooted
- Perfect
- Full
- Complete



- Rooted



- Rooted

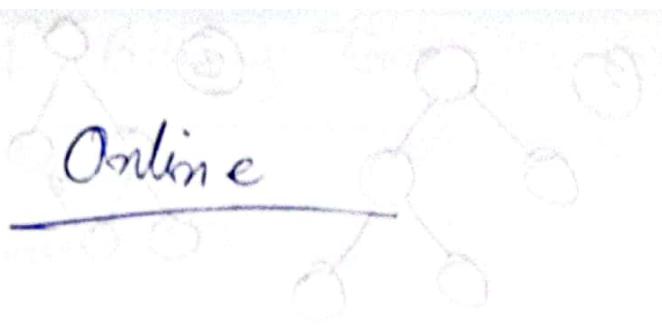


- Rooted

- Full

- Full

- Complete
- Complete



See question

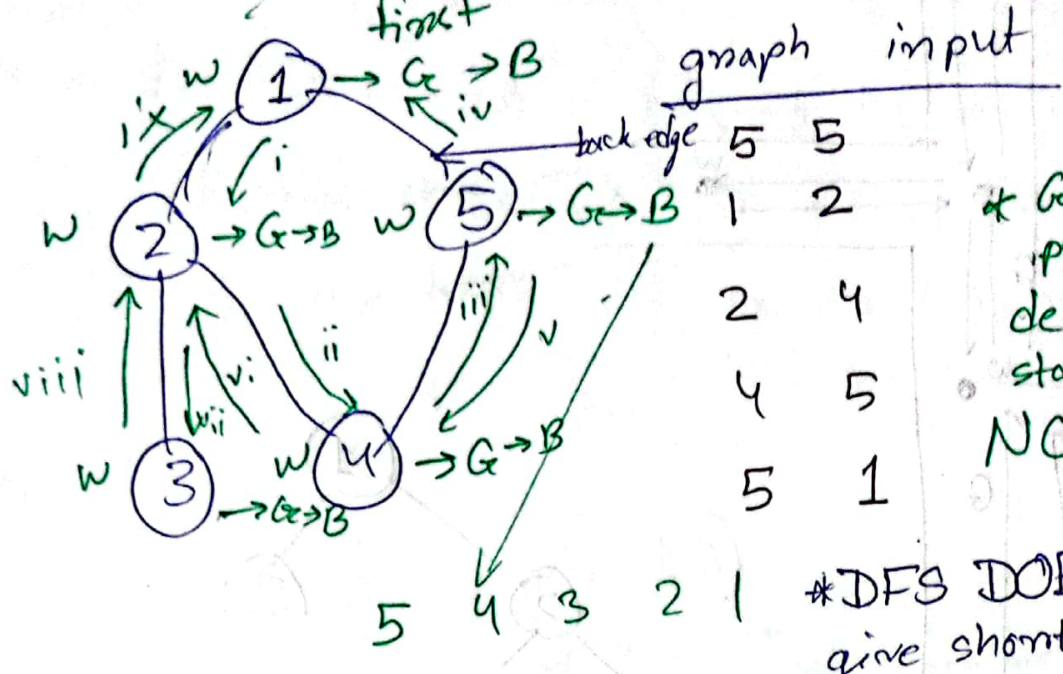
```
for (i = 1; i <= node_no; i++)  
{  
    if (level[i] == -1)  
    {  
        BFS(i);  
        cout << i << endl;  
        k++;  
    }  
}
```

HEAVILY

Depends on user input

## DFS (Depth First Search)

Use recursion to reach the deepest point first



\* DFS DOES NOT give shortest path  
\* if back edge i.

### Three Colors:

white = node not visited yet

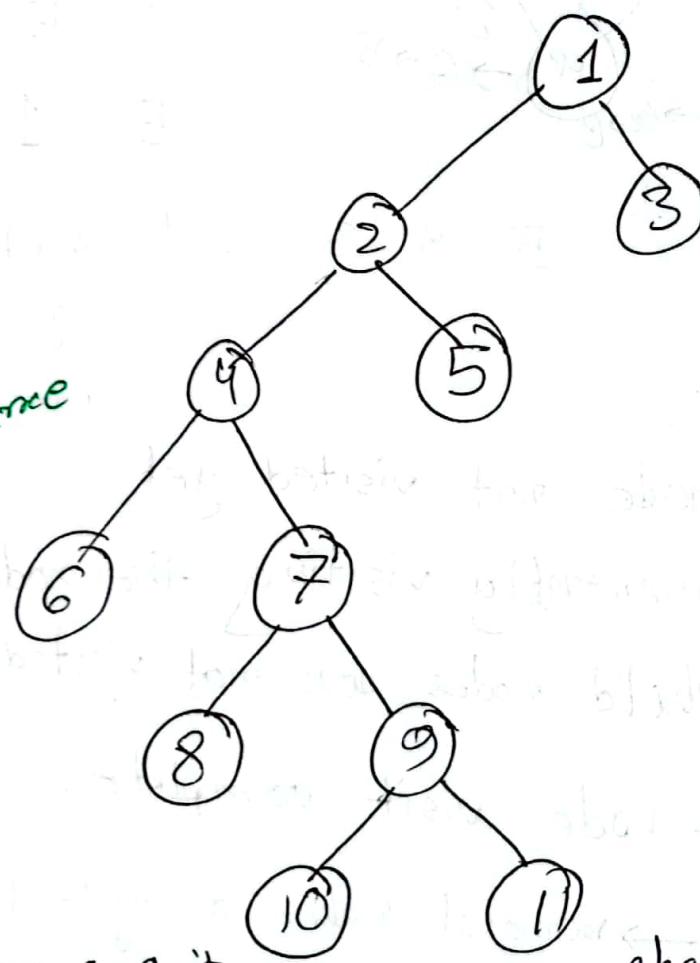
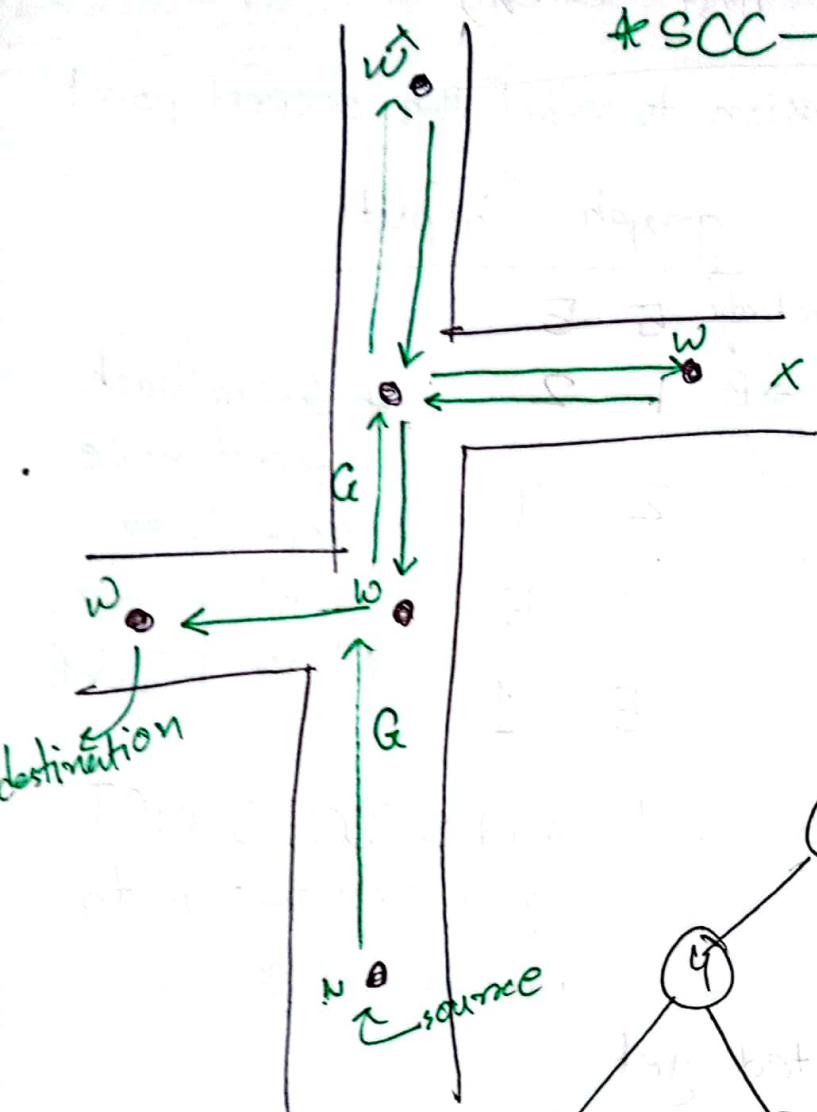
gray = currently visiting the node but all the child nodes are not visited yet

black = node visit complete.

\* back edge  $\rightarrow$  removal makes a cycle-less tree. graph/tree

\* free edge.

\* SCC → Used to find numbers of cycles.



\* graph traversal

\* cycle finding → when  $g - g$ , it has cycle

\* connected/disconnected graph finding

\* count number of components in a graph → Number of times comp BFS/DFS is run

\* Topological sort

## \*Topological Sort:

In a ~~dependent~~ <sup>directed</sup> graph, it will give a sorted

Step.

→ Multiple solutions are possible

→ Run DFS with the least in orders.

## DFS Algorithm:

```
0. DFS(u) // initial data
1. color[u] = gray // set it to gray
2. For all adjacent edges of u: {
    v = adjacent node of u
    if color[v] = white: {
        DFS(v) // recursion
    }
}
3. end if
4. end For
5.
6.
7. end
8. color[u] = black // when done make it black
```

Complexity:  $O(n + e)$

C-12 (W-II)

01/07/24

## Binary Search Tree (BST)

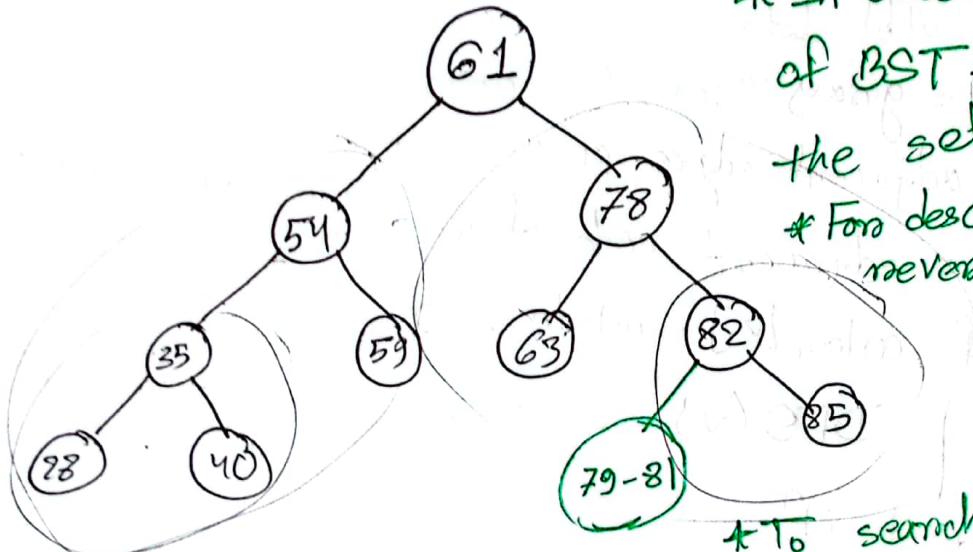
A binary search tree is a binary tree where the node values of the left sub tree are smaller than the node value of the root and all the node values of the right sub tree are greater than the node value of the node.

\* In order traversal

of BST is sorts

the set

\* For descending order, reverse the tree



Inorder: X 61 Y

= W 54 59 61 63 78 V if switch to check

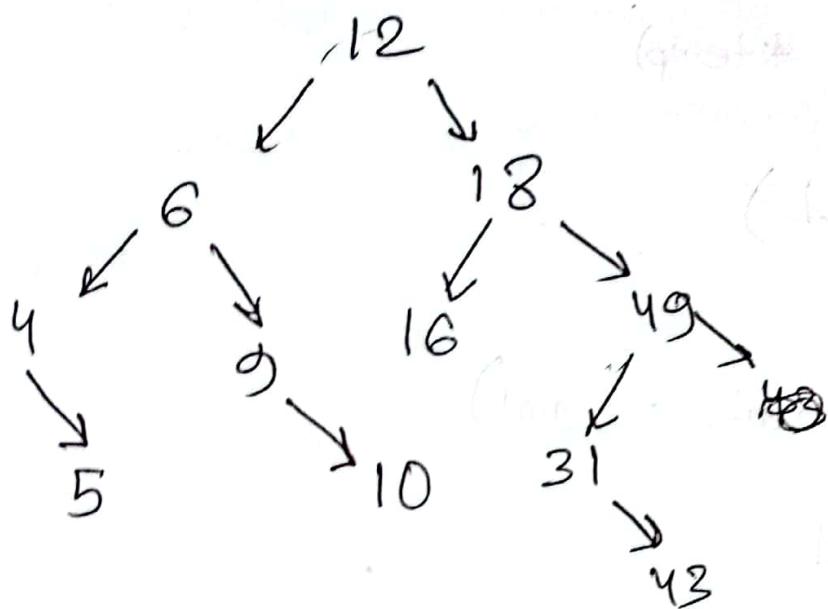
= 28 35 40 54 59 61 63 78 82 85

\* To search, use preoder algo algorithm then use

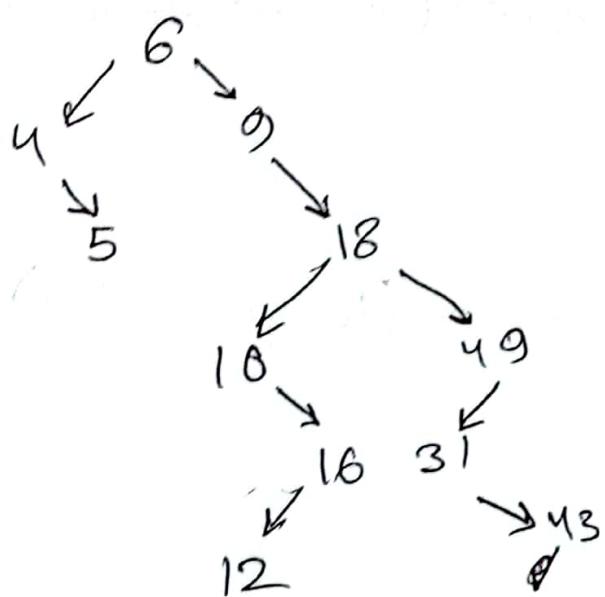
## Search Code :

```
int val, flag = 0;  
void pre_order(node *temp)  
{  
    if (temp != NULL)  
    {  
        if (temp->data == val)  
        {  
            flag = 1;  
        }  
        else if (temp->data > val)  
        {  
            pre_order (temp->left) // for small ignore  
            // greatest right this  
        }  
        else  
        {  
            pre_order (temp->right) // for smallest  
            // ignore this  
        }  
    }  
}
```

12, 6, 9, 18, 4, 10, 5, 16, 49, 31, 43



Root 12 at last,



Binary Search Tree Code: → Complexity:  $O(n) = n \log_2 n$

struct node

{  
    int data;  
    node \*left;  
    node \*right;  
};

node \*root = NULL

void BST insert(int val)

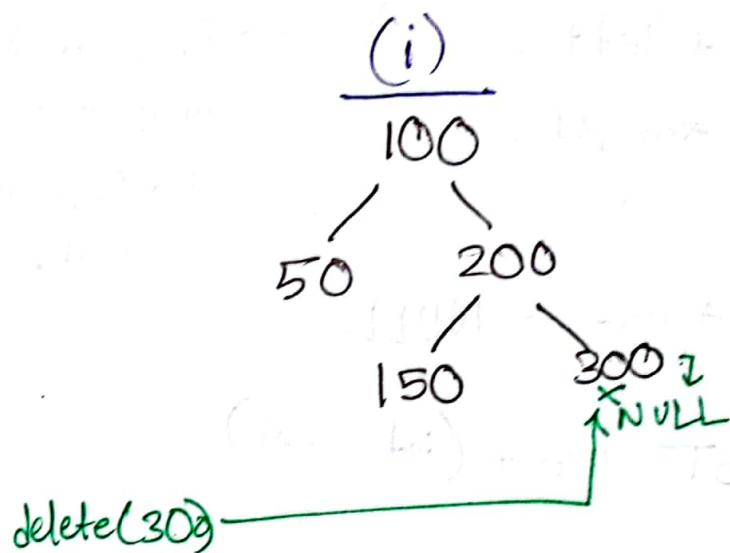
{  
    node \*temp;  
    temp = new node();  
    temp->data = val;  
    temp->left = NULL;  
    temp->right = NULL;  
    if (root == NULL) { root = temp; }  
    else  
    {  
        node \*curr\_node = root;  
        node \*prev\_node = root;  
        while (curr\_node != NULL)  
        {  
            prev\_node = curr\_node;  
            if (curr\_node->data > val) { curr\_node->left; }  
            else { curr\_node = curr\_node->right; }  
        }  
        if (prev\_node->data > val) { prev\_node->left = temp; }  
        else { prev\_node->right = temp; }  
    }  
}

Delete From a Binary Search TreeTree cases:

(i) leaf node

(ii) node with one child

(iii) node with two children



```
void delete_node(int val)
```

```
{
```

```
    node * curr_node = root;
```

```
    node * prev = root;
```

```
    while (curr_node != NULL)
```

```
{
```

```
: if (curr_node->data == val) {
```

```
        break;
```

```
        if (curr_prev
```

```
        prev = curr_node;
```

```
        if (curr_node->data < val) {
```

```
            curr_node = curr_node->right;
```

```
}
```

```
else {
```

```
    curr_node = curr_node->left;
```

```
}
```

```
}
```

```
if (curr_node == NULL) {
```

```
    return;
```

```
else {
```

```
: if (curr_node->right == NULL) && (curr_node->left
```

```
    == NULL)
```

```
{
```

```
    if (prev->right == curr_node)
```

```
    prev->right = NULL;
```

```
{
```

```
else {
```

```
    prev->left = NULL;
```

```
,
```

case (i)

on Leaf

Does not activate until  
value is found

used to navigate

If not found

else if (*curr\_node* → right == NULL || *curr\_node* → left == NULL)

}

node \*child; // temp node

if (*curr\_node* → right == NULL)

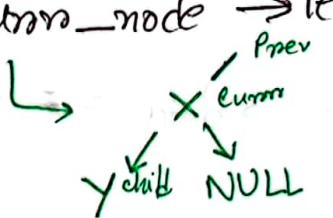
{

child = *curr\_node* → left;

{

else

{



Set child

child = *curr\_node* → right;

{

if (*prev* → right == *curr\_node*) // Find curr's parent prev

{

*prev* → right = child;

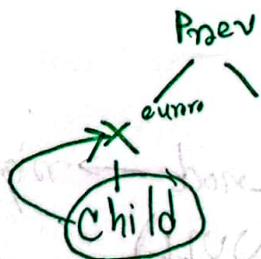
{

else

{

*prev* → left = child;

{

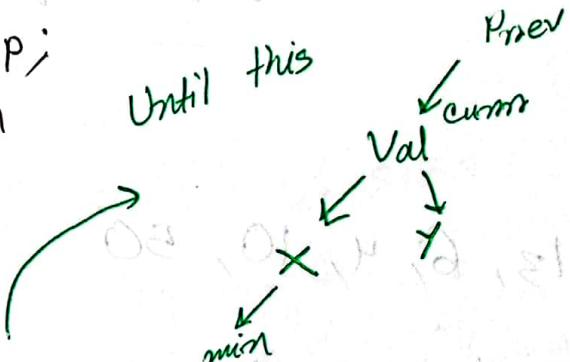


else  
 {  
 node \* min = curr\_node;  
 min = curr\_node; pprev = curr\_node;  
 while (min->left != NULL)  
 {  
 min = min->left;  
 }

# Find Do the same  
 with right min  
 value.

node \* temp;  
 temp = min

Until this

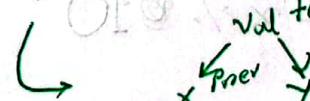


else  
 {  
 node \* temp = curr\_node;  
 pprev = curr\_node;  
 curr\_node = curr\_node->right;  
 while (curr\_node->left != NULL)

Finding minimum  
of

case  
 (ii)  
 ↓  
 two  
 children

pprev = curr\_node;  
 curr\_node = curr\_node->left;



temp->data = curr\_node->data; // swaps Val with  
 the min data

pprev if (pprev->left == curr\_node)

{  
 pprev->left = curr\_node->right;

}  
 else  
 {  
 pprev->right = curr\_node->right;



C-14 (W-13)

## Hashing (10 from here)

15/07/24

+ 10 0

Linear search -  $O(n)$

Binary Search -  $O(\log n)$

We want a search method that requires  $O(1)$  time

Different from cryptography  
Hashing is more involved with searching  
Does not give  $O(1)$  but does work better than  $O(n)$  and  $O(\log n)$

keys = 8, 3, 13, 6, 4, 10, 50

A	x	x	1	3	4	5	6	x	8	x	10	x	11	12	13	x.	x	50
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	50

$h(x) = x$

Gives  $O(1)$  but we waste memory space

key space

hashing function = hash table

$$h(x) = x \% 10$$

8  
3  
13  
6  
4  
10  
50

9	8
7	7
6	6
5	5
4	4
3	3
2	2
1	1
0	10

hash collision: conflict for space.

## hash collision

- linear probing
- quadratic probing
- separate chaining

### Linear Probing

$$h(x) = x \% \text{size}$$

$$h'(x) = [h(x) + f(i)] \% \text{size}$$

$$f(i) = i ; i = 0, 1, 2, \dots$$

\* ~~Search~~ =  $\rightarrow A[x] \rightarrow A[x+1] \rightarrow \dots$

$$h(13) = 13 \% 10 = 3 \rightarrow \text{collision}$$

$$\therefore h'(13) = (13 + 1) \% 10 = \frac{4 \% 10}{3+1} = 4 \rightarrow \text{collision}$$

$$h'(14) = (13 + 2) \% 10 = \frac{5 \% 10}{3+2} = 5 \rightarrow \text{free}$$

### Quadratic Probing

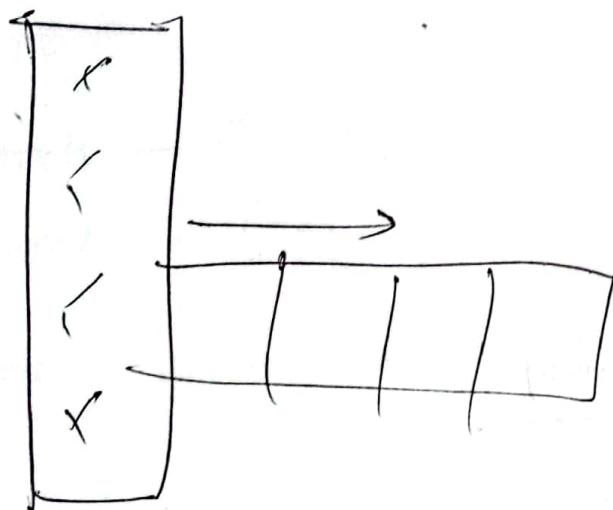
$$h(x) = x \% \text{size}$$

$$h'(x) = [h(x) + f(i)] \% \text{size}$$

$$f(i) = i^2 ; i = 0, 1, 2, \dots$$

Separate

## Separate chaining



probing works ←

+ 2D vector →

parallel storage ←

parallel works

parallel works

$$\text{size } \Delta[(0) + (0)] = O(1)$$

$$S = P \circ S + C \circ S + (I)$$

$$S = S - E + SA \leftarrow [SA] \in \text{densest}$$

$$\text{probabilities} \leftarrow S = O(1) \times S = (S)N$$

$$\text{softmax} \rightarrow P = \frac{e^S}{\sum e^S} = O(1) \times (1 + e^{-S}) \cdot (S)N$$

$$\text{softmax} \leftarrow S = O(1) \times S + O(1) \times (S + eS) = O(1)N$$

gradient estimator

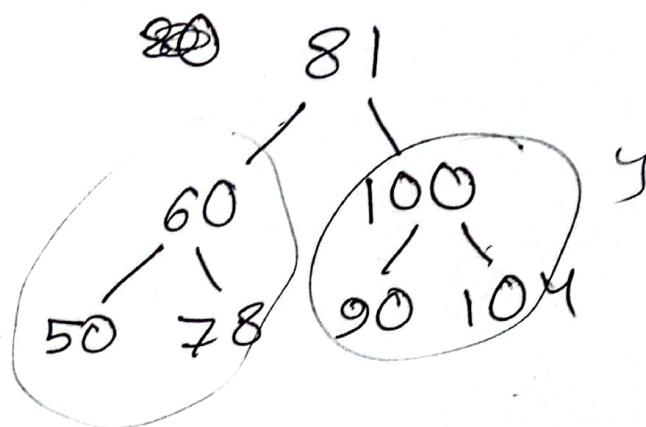
$$\text{size } \Delta \otimes = O(1)$$

$$\text{size } \Delta[(1) + (0)] = O(1)N$$

$$S = P \circ S + C \circ S = (1)P$$

17 L-10 (w-13)

17/03/24



Pre: ~~x 81 y~~ ~~81 x y~~ ~~x 81~~

= ~~81~~ ~~60~~ ~~100~~  $\rightarrow$   $\rightarrow$

= ~~81~~ ~~60~~ ~~50~~ 81 60 50 ~~78~~ 100 90 104

In: ~~x 81 y~~

= w 60 v 81 p 100 q

= 50 60 ~~78~~ 81 90 100 104

Post: ~~x y 81~~

= wv60 pq100 81

= 50 ~~78~~ 60 90 104 100 81