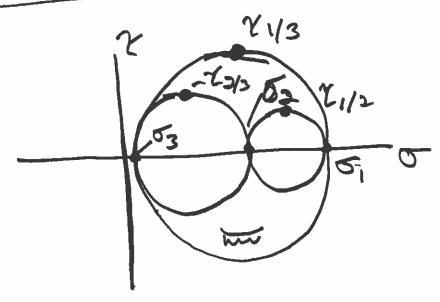
EME 150A Lecture notes Oct 17, 2015 Triaxial State of Stress

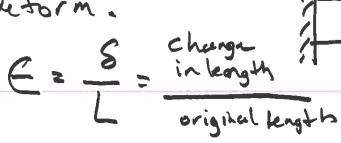
03-(5x+5y+5z)=+(5xey+5xoz+5yoz+
-2xyy-2yz-7xz)=-(5x5y5z+
2xxy7y=2xz-5xz-5xz-5xz-5z5xz)=0

3D Mohr's Circle



Elastic Strain

Under an applied load a structural member will deform.



Stress => nearly impossible to measure Strain => measurable

LA direction and intensity of deformation

Normal Strain

$$E_{x} = \frac{6x}{Lx}, E_{y} = \frac{6x}{Lx}$$

led longitudihed strain

Shear Strain

A Single Single

$$\gamma_{xy} = \frac{2s_x}{2y} + \frac{2s_y}{L_x} \Rightarrow \frac{s_x}{2} = \frac{s_x}{L_y} + \frac{s_y}{L_x}$$

Angular distortion due to shear Stress. Assume small angles.

Strain Tensor

Principal Strains (plane strain)

$$E_{1,2} = \frac{\epsilon_x + \epsilon_y + \left[(\epsilon_x - \epsilon_y)\right]^2 + \left(\frac{\epsilon_x + \epsilon_y}{2}\right)^2}{2}$$

$$\left(\frac{\chi}{2}\right) = \frac{\epsilon_1 - \epsilon_2}{2}$$

max

Hooke's Law

relates stress & strain

Elasticity: material recovers its
Original shape once load is removed

E: modulus of elasticity (Young's module)

G: sher modulus of elasticity

D: poisson's ratio

$$E_{x} = \frac{1}{E} \left[\sigma_{x} - \mathcal{V}(\sigma_{y} + \sigma_{z}) \right] \quad \text{Hooke's}$$

$$E_{y} = \frac{1}{E} \left[\sigma_{y} - \mathcal{V}(\sigma_{y} + \sigma_{z}) \right] \quad \text{Hooke's}$$

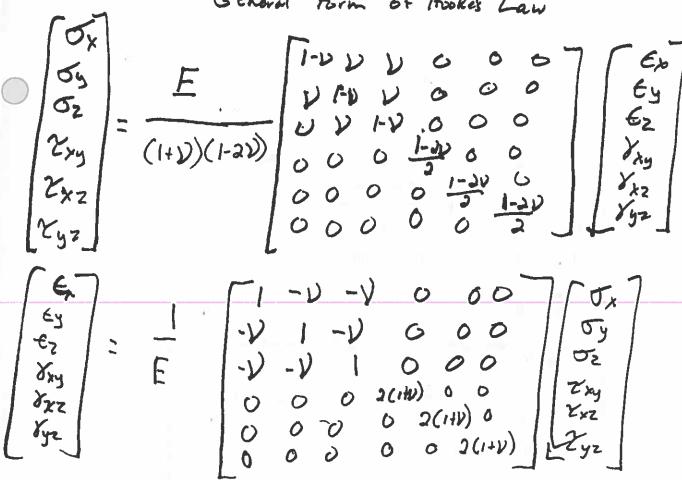
$$E_{z} = \frac{1}{E} \left[\sigma_{z} - \mathcal{V}(\sigma_{x} + \sigma_{y}) \right] \quad \text{Hooke's}$$

$$V_{xy} = \frac{1}{G} \mathcal{V}_{xy} \quad V_{xz} = \frac{1}{G} \mathcal{V}_{xz}$$

$$V_{yz} = \frac{1}{G} \mathcal{V}_{yz}$$

$$\sigma_1 = \frac{E \in (1-\nu) + \nu E (\epsilon_2 + \epsilon_3)}{1-\nu - 2\nu^2}$$

General Form of Hooke's Law



Show old table 2-1

Strain Gauges

- Change in electrical resistance to measure Strain. Change in resistance proportion to change in Strain

Garge Factor

GF = DR

RG

E

DR: change in resistance

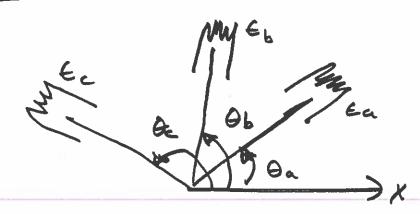
RG: nominal resistance

6: Strain

Plane Strain Measurment

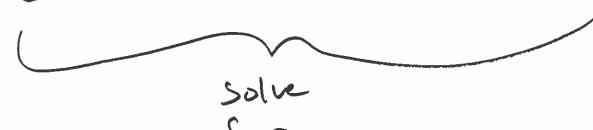
Strain

Rosettes



Eu = Ex cos = Out Ey sin = a + 8xy sin Ba cos Ba

EE = Ex cos de + Ey sin de + 8xy sin de cos de

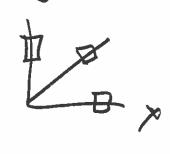


Ex, Ey, 8xy

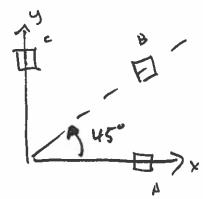
$$E_x = E_a$$

$$E_y = E_b C$$

$$\delta_{xy} = 2E_b - (E_a + E_c)$$



Example



What are the principal strains ist strain games readings are $E_a = 60E-6$, $E_b = -75E-6$, $E_c = 232E-6$?

State of strain $E_x = 60E-6$

 $E_y = 232E-6$ $Y_{xy} = 2(-75E-6) - (60E-6 + 332E-6) = -0.0004#2$ = -442E-6

COOLEGE Principal Strains

$$E_{1,2} = \frac{c_{x} + \epsilon_{y}}{2} + \sqrt{\left(\frac{c_{x} - \epsilon_{y}}{2}\right)^{2} + \left(\frac{a_{xy}}{2}\right)^{2}}$$

Mildela

E1,2= 6=383E-6 6=-91E-6

Principal stresses
$$\overline{J_1} = \underbrace{E(E_1 + UE_2)}_{1-W^2} = 78MPa$$

$$\overline{J_2} = \underbrace{E(E_2 + UE_1)}_{1-W^2} = \underbrace{5MPa}_{1-W^2}$$