# **Staircase Problem**

### <u>Problem</u>

A person can climb one, two or three stairs at a time. Find the number of ways in which he can climb n<sup>th</sup> stairs.

## Example

n = 5



### Ways:

{1, 1, 1, 1, 1}

{1, 1, 1, 2}

{1, 1, 2, 1}

{1, 2, 1, 1}

{2, 1, 1, 1}

{1, 2, 2}

 $\{2, 1, 2\}$ 

{2, 2, 1}

{1, 1, 3}

{1, 3, 1}

{3, 1, 1}

{2, 3}

{3, 2}

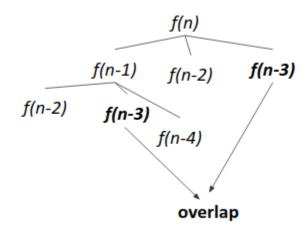
Hence total number of ways = 13.

It can be easily seen that

$$f(n) = f(n-1) + f(n-2) + f(n-3)$$

Since it can be represented as Recurrence Relation, therefore it has an optimal substructure property.

Checking whether it has overlapping subproblem property Making recursion tree



Since f(n-3) repeats, it follows overlapping subproblem property.

Approach 1 (Memoization)

- 1. Write the recursive solution.
- 2. Memoize it.

Approach 2 (Tabulation)

- 1. Initialize f(0)=1, f(1)=1, f(2)=2.
- 2. Iterate from i=3 to i=n, and keep applying f(i) = f(i-1) + f(i-2) + f(i-3).
- 3. Output *f*(*n*).

### <u>Code</u>

```
void solve()
{
    int n;
    cin >> n;

    vi dp(n+1);

    dp[0] = 1;
    dp[1] = 1;
    dp[2] = 2;

    rep(i,3,n+1)
    {
        dp[i] = dp[i-1] + dp[i-2] + dp[i-3];
    }

    cout << dp[n] << endl;
}</pre>
```