

# Scale-Free Intermittent Flow in Crystal Plasticity

Dennis M. Dimiduk,<sup>1\*</sup> Chris Woodward,<sup>2</sup> Richard LeSar,<sup>3</sup> Michael D. Uchic<sup>1</sup>

Under stress, crystals irreversibly deform through complex dislocation processes that intermittently change the microscopic material shape through isolated slip events. These underlying processes can be revealed in the statistics of the discrete changes. Through ultraprecise nanoscale measurements on nickel microcrystals, we directly determined the size of discrete slip events. The sizes ranged over nearly three orders of magnitude and exhibited a shock-and-aftershock, earthquake-like behavior over time. Analysis of the events reveals power-law scaling between the number of events and their magnitude, or scale-free flow. We show that dislocated crystals are a model system for studying scale-free behavior as observed in many macroscopic systems. In analogy to plate tectonics, smooth macroscopic-scale crystalline glide arises from the spatial and time averages of disruptive earthquake-like events at the nanometer scale.

The vivid images of radiant-hot metal being forged on a blacksmith's anvil, or being formed between rolls and dies, support a view of crystal deformation as analogous to viscous fluid flow. Such deformation is often described via a set of continuum-level parameters, which, in contrast to those describing fluids, evolve with deformation to reflect the increasing resistance to flow that occurs with increasing distortion (work hardening). Although continuum approaches are selectively useful for describing deformation, especially at high temperatures, they completely fail to account for well-known intermittent deformation phenomena such as the spatial localization of dislocation flow into "slip bands" [described in 1900 (1)] and the temporal fluctuations in load-versus-time curves (the Portevin–Le Chatelier effect first reported in the 1920s) (2, 3).

From the late 1950s to the 1970s, numerous investigators sought to account for the heterogeneous nature of crystal deformation. Studies ranged from examining the motion of individual dislocations to describing the development and propagation of dislocation aggregates to form deformation bands (4). Those studies demonstrated the importance of both topological (crystallographic) constraints and the complex, long-range interactions between dislocations that determine collective dislocation motion, thus distinguishing crystal plasticity from continuum flow. For example, Pond convincingly showed that crystal slip in metals can be intermittent and heterogeneous at multiple length and time scales through cinematographic stud-

ies of deformation band formation and growth (5). Studies of dislocation motion, slip-line formation, and the collective intermittent nature of slip continued, providing a detailed view of dislocation motion and crystal glide (6–8). Despite much effort, a quantitative understanding of intermittency and collective dislocation flow has remained elusive. As a consequence, our ability to predict critical deformation behavior is often limited, impeding our understanding of such phenomena as work hardening (9–11).

Recent studies of intermittency in crystal plasticity were based on measurements of acoustic emissions that arise from the motion of dislocations through large (tens to hundreds of mm) ice crystals (12–16). The essence of the technique is the detection of the acoustic waves that are generated by dislocation glide and their subsequent analysis based on models of dislocation motion. Under some conditions, it has been argued that the amplitudes of the acoustic signals are related to the area swept by the fast-moving dislocations and hence to the energy dissipated during deformation events. These results were used to suggest intermittency of flow (12), scale-free dissipation processes (13), spatial clustering of flow avalanches (14), and, most recently, conditions for "supercritical" flow in polycrystalline ice (15, 16). However, the results from these measurements can only be interpreted via models and under certain key assumptions about the deformation processes. Other reports also show the characteristics of scale-free flow for crystals through simulation (17–19) and models of dislocation glide at low temperature (20, 21). These studies conclude that deformation of crystals having highly mobile dislocations exhibits the attributes of a self-organized critical (SOC) process.

We report the direct measurement of scale-free intermittent flow within micrometer-scale

pure metal crystals loaded above the elastic-plastic transition. Using the ultrahigh displacement resolution offered by modern nanoindentation systems (effectively a nanoscale seismometer), we examined the frequency of displacement events as a function of their magnitude for several sample sizes and applied loads. The results were analyzed following the suggestion that dislocations form a SOC system, as briefly reviewed in (22, 23). Bak *et al.* (24) introduced this concept to describe dynamical systems that arrange themselves such that they are always at a critical point irrespective of their initial state, that is, they self-organize to the critical point of the system (25). An important aspect of SOC behavior is that it is self-similar or scale-free. That is, structures at one scale appear the same (at least in a statistical sense) as structures at other scales. If dislocations are indeed self-organized critical systems, then the statistics that describe these ensembles can be used to develop homogenization schemes for mapping between groups of dislocations and macroscopic deformation.

The experimental techniques used for this study were reported in (26–28) [see also (29)]. Microcrystals of pure Ni were prepared by isolating cylindrical columns via focused ion-beam machining, with one end of each column attached to the bulk material, within the surface of an electropolished macroscopic crystal. The microcrystals were transferred to a nanoindenter and aligned for axial compression testing. Samples ranging in diameter from 18 to 30.7  $\mu\text{m}$ , with length-to-diameter ratios ranging from  $\sim 1.9:1$  to  $2.8:1$ , were loaded via a flattened diamond tip platen at a nominal axial strain rate of  $10^{-4}/\text{s}$  at room temperature. For each sample a variety of parameters were measured, including load ( $\pm 50$  nN) and displacement ( $\pm 0.02$  nm), and digitally stored at a frequency of 5 Hz. The displacement-versus-time data were differentiated by a simple two-point forward-derivative method. The resultant loading platen velocity profiles were correlated with the displacement-versus-time data to identify displacement events larger than a chosen "noise threshold." The shear-stress versus shear-strain curves measured for the present experiments and a typical plot of detected displacements versus time are shown in Fig. 1, A and B. Note that the displacements reflect dissipated energy and are intermittent in both space and time, despite the programmed continuous loading rate.

For the scaling analysis, a noise threshold for detecting displacements was established for each test by monitoring the standard deviation from ideal of the detected displacements during the unloading portion of the test. For these tests, the noise values ranged from 0.13 to 0.68 nm. Thus, for Ni crystals with  $\langle -2, 6, 9 \rangle$  orientation, a typical minimum detected event corresponds to  $\sim 0.3$  nm or  $\sim 4$  dislocations leaving the crys-

<sup>1</sup>Air Force Research Laboratory, Materials and Manufacturing Directorate, AFRL/MLLM, Wright-Patterson AFB, OH 45433, USA. <sup>2</sup>Department of Materials Science and Engineering, Northwestern University, Evanston, IL 60208, USA. <sup>3</sup>Theoretical Division, Los Alamos National Laboratory, Los Alamos, NM 87545, USA.

\*To whom correspondence should be addressed. E-mail: dennis.dimiduk@wpafb.af.mil

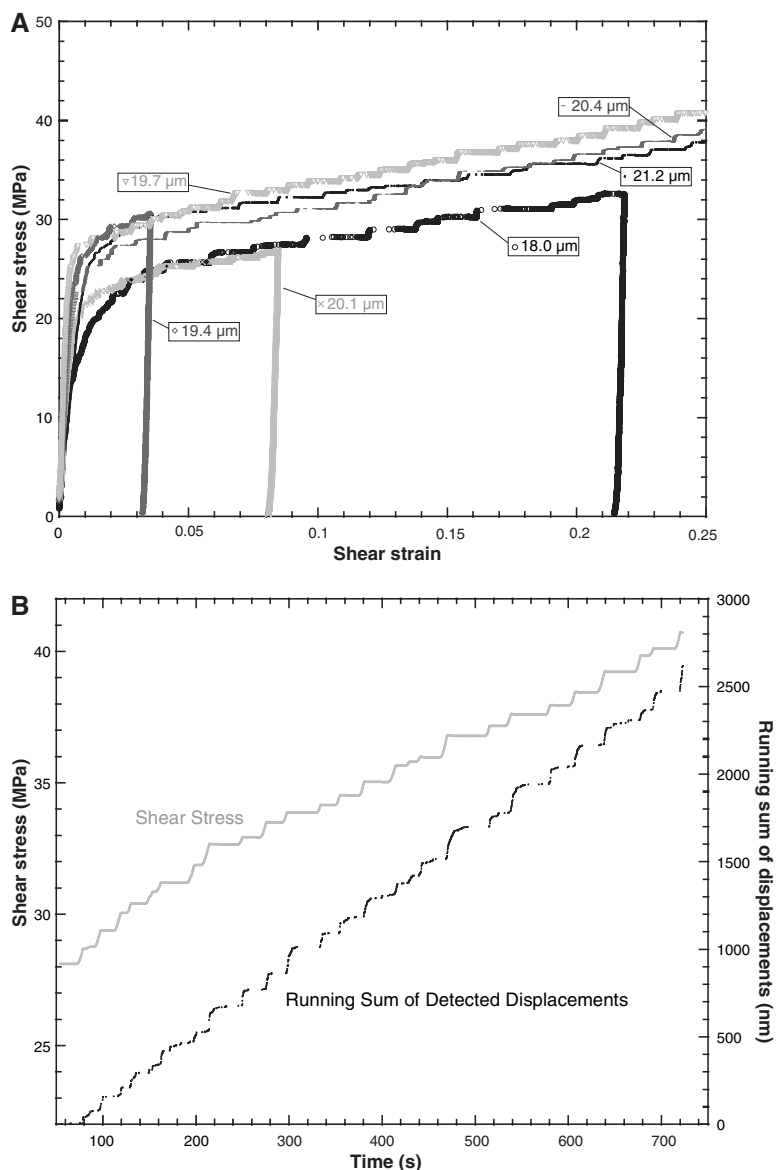
tal. For events exceeding the noise threshold, the displacement magnitude was recorded and sorted into bins for each sample as well as for the collective set of samples. A plot of the number of events at a given displacement magnitude,  $n(x)$ , versus magnitude  $x$  (in nm) for events isolated from a single sample (Fig. 2) reveals that a linear regime exists in which the probability of observing a displacement event of a given magnitude decreases as the event size increases. Also shown in Fig. 2 are the displacements for all of the samples analyzed collectively. Both data sets demonstrate power-law scaling. The data were fit to a power-law expression  $n(x) = Cx^{-\alpha}$ , producing a measured value of  $\alpha = \sim 1.5$  where  $C$  is a constant. This scale-free flow was observed over a range of

displacements from  $\sim 0.5$  nm to more than  $\sim 150$  nm per event—more than two orders of magnitude. Values for  $\alpha$  derived from log-log plots are known to underestimate this parameter. Using alternative approaches as suggested by Newman (25), we estimated a power-law slope of  $1.60 \pm 0.02$  by a bootstrap method (29). Note that the value of 1.6 is identical to that found through acoustic emission experiments (13) and from theory (19). Further, the scaling relationship is independent of sample size over the range examined as well as the gradually increasing stress over the range of the test (i.e., there is no work-hardening effect for single slip-plane flow).

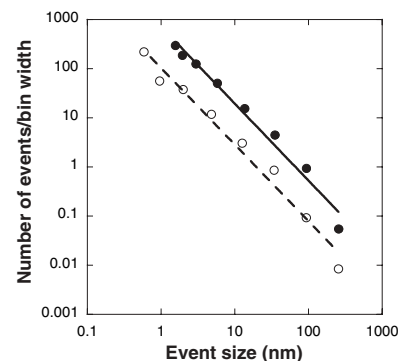
Closer inspection of a typical sequence of events (Fig. 3) shows several important

features of the data. First, the individual events take place at a rate that is much faster than the programmed displacement rate of the test. This demonstrates that dissipation is much faster than the rate of change of the driving force. Second, the largest displacement events typically occur after an increment of the remote stress. Note that the magnitude of a stress increment is a vanishingly small percentage of the total applied stress. This observation of “large” events (displacement shocks) after a small change of driving force indicates that the system is near critical. Third, these large events are frequently followed by a succession of additional displacement events of much smaller magnitude (aftershocks) that occur in the absence of further detectable remote stress rise; this suggests self-organization back to a critical state. Fourth, a post mortem examination of the deformed samples by transmission electron microscopy (TEM) (Fig. 4) shows a substructure containing many dislocations that is characteristic of those seen after similar deformation of large Ni crystals (28, 30, 31). Finally, the displacement-versus-time plots show intervals having a small positive slope that indicates additional displacements not accounted for within the detected bursts. These extra displacements occur even under conditions of no increase in the applied load, consistent with these samples exhibiting creep at or near criticality.

Our data and analysis explicitly show that crystalline glide in metals exhibits the characteristic attributes of self-organized criticality under the appropriate control of the driving force (in this case an applied displacement rate or load). These results support an emerging view that a statistical framework that creates a coarse-grained description of dislocation response is needed to bridge the



**Fig. 1.** (A) Selected shear-stress versus shear-strain curves for Ni samples with  $\langle -2, 6, 9 \rangle$  orientation,  $\sim 20$   $\mu\text{m}$  in diameter, showing intermittency of strain and stress. (B) Plot of shear stress and the cumulative sum of detected displacements as functions of time for a single sample  $19.7 \mu\text{m}$  in diameter. See (29) for additional sample data from these and from samples  $\sim 30 \mu\text{m}$  in diameter.

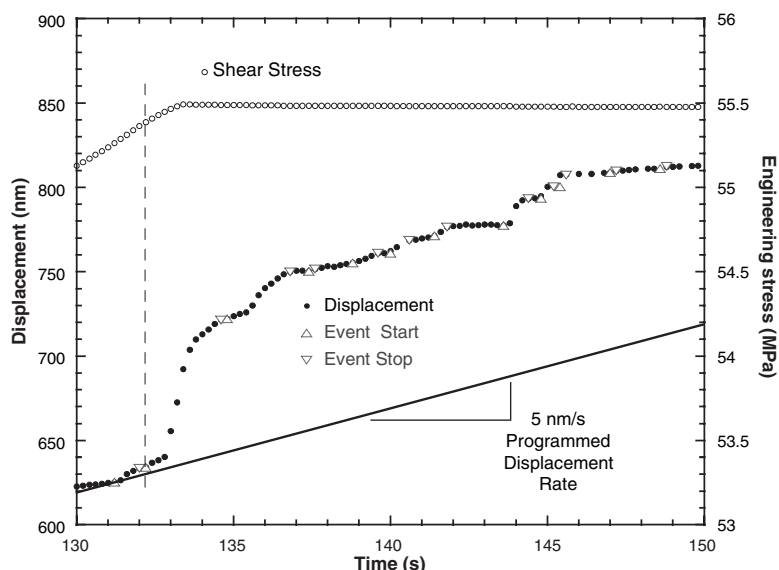


**Fig. 2.** Event frequency distribution showing the number of slip events of a certain size,  $n(x)$ , versus event size,  $x$ , plotted on logarithmic scales. Power-law scaling over more than two orders of magnitude is exhibited for both a single sample  $\sim 20 \mu\text{m}$  in diameter (open circles and dashed line fit) and the aggregate data from several samples (solid circles and solid line fit).

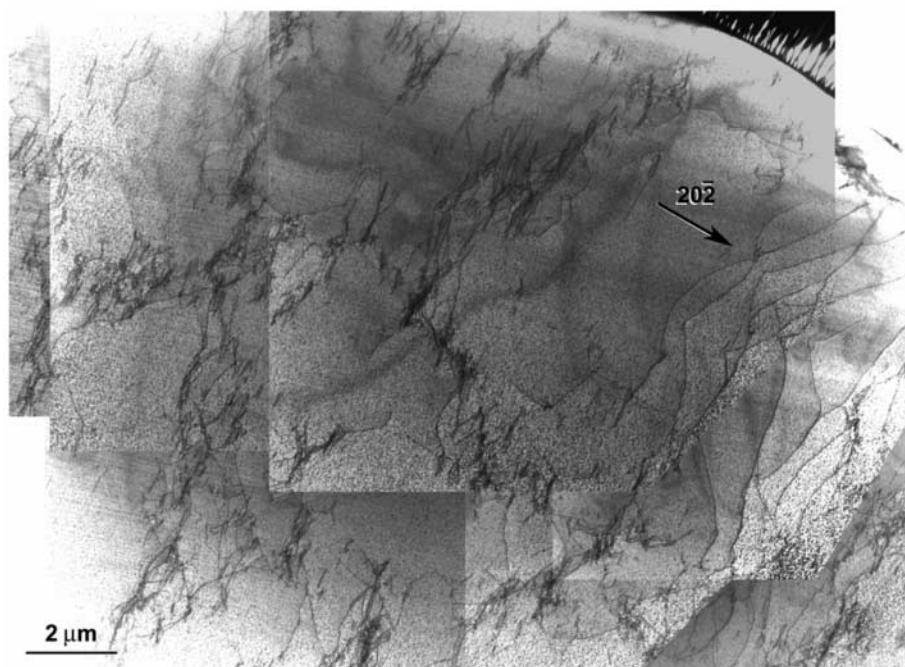
gap between the behavior of individual dislocations and the ensemble of dislocations that govern macroscopic metal plasticity. Further, the existence of a scale-free set of variables that describe deformation suggests that such a coarse-graining variable set exists

(23). This assessment puts dislocation motion in the same class as earthquakes, sand pile avalanches, magnetic domain dynamics, and a wide variety of other dynamical systems. The picture that emerges is that crystal deformation has more in common with plate

tectonics than with viscous fluid flow, at least in selected commonly experienced regimes.



**Fig. 3.** A detailed example of the stress-versus-time and displacement-versus-time curves taken from the data for the sample 30.7  $\mu\text{m}$  in diameter. The displacement curve shows superimposed markers for detected event start and stop times. Note that the large event beginning at the vertical dashed line occurs as a shock under a rising stress but continues under constant stress, as do the vast number of aftershocks at smaller magnitudes.



**Fig. 4.** Bright-field TEM image showing the dislocation structure for the sample 20.1  $\mu\text{m}$  in diameter after 8.1% plastic shear strain. The plane of view is parallel to the  $\{111\}$  slip planes, and the field of view includes most of the sample cross section. The crystallographic direction marker indicates both the imaging vector and the direction of the dislocation Burgers vector. The montage image was digitally assembled from seven individually leveled micrographs, the edges of which can be seen.

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Materials and Methods

Figs. S1 to S4

Tables S1 and S2

References

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