# PHY201: Homework 1

### Ariel Attias Matthieu Chapuy Matthieu Melennec André Renom

## $7^{th}$ November 2019

### Contents

Hor	rizontally Excited Pendulum	1
1.1	•	1
1.2		1
1.3		1
		2
		2
1.6		2
Equ	nilibrium of Two Masses	2
2.1		2
2.2		2
2.3		2
2.4		2
Sus	pended Bar	2
3.1	One Mass Only	2
	3.1.1	2
	3.1.2	2
		2
		2
		2
	316	2
		2
3 2	*****	2
0.2		$\sim$
	3.2.1	2
	1.1 1.2 1.3 1.4 1.5 1.6 Equ 2.1 2.2 2.3 2.4 Sus 3.1	1.1 1.2 1.3 1.4 1.5 1.6  Equilibrium of Two Masses 2.1 2.2 2.3 2.4  Suspended Bar 3.1 One Mass Only 3.1.1 3.1.2

### 1 Horizontally Excited Pendulum

#### 1.1

Under normal assumptions, we would write the position of the pendulum as:

$$\begin{pmatrix} x \\ z \end{pmatrix} = \begin{pmatrix} x_f + l\sin\theta \\ -l\cos\theta \end{pmatrix}$$

However for  $\theta \ll 1$ , we can use the Taylor series of the trigonometric functions to approximate  $\cos\theta \approx 1$  and  $\sin\theta \approx \theta$ . We therefore have:

$$\begin{pmatrix} x \\ z \end{pmatrix} = \begin{pmatrix} x_f + l\theta \\ -l \end{pmatrix}$$

#### 1.2

We now consider the forces in the direction of the bar at the point mass. We observe two forces: the constraint force in the bar, that acts parallel to the bar, and the force due to gravity, that acts straight down. By projecting the force due to gravity along the direction of the bar, we can write the equation

$$F_{bar} - mg \cos\theta = ma$$

with a the component of the acceleration in the direction of the bar. However we know the bar to be rigid, hence a=0, and as established before, over the studied range,  $\cos\theta=1$ . We can therefore re-write the equaiton above as

$$F_{bar} = mg$$

#### 1.3

In order to write the oscillator equation of the system, we will consider the motion of the mass in the direction of the x-axis. From our definition of the x-position of the particle in 1.1, we can derive twice to obtain the acceleration of the particle in the x-direction,  $\ddot{x} = \ddot{x}_f + l\ddot{\theta}$ .

By considering the forces on the mass, we get that:

$$F_{bar}sin\theta = ma$$
 
$$mg sin\theta = m(\ddot{x}_f + l\ddot{\theta})$$
 
$$g sin\theta = -\omega^2 x_0 sin\omega t + l\ddot{\theta}$$

From this we can write our oscillator equation:

$$l\frac{d^2\theta}{dt^2} - g\theta - \omega^2 x_0 sin\omega t = 0$$

3.2.4