# Solution to Assignment 4: Spreadsheet Simulation Using @Risk

There are three questions (15 total points) in this assignment. All relevant Excel files can be found on Sakai. Solve these questions in Excel and fill in the solution template provided below.

#### **Question 1: Investing for retirement (Retirement.xlsx)**

Consider a variation of the investing for retirement example we discussed in class and implement the following strategy:

- invest at mean 8%, standard deviation 25% if balance is < \$700,000;
- invest at mean 5%, standard deviation 15% if balance is  $\geq$  \$700,000 and < \$1,000,000;
- stop investing if balance is  $\geq$ = \$1,000,000.

a. Specify the following @Risk Model in Excel: Personal Worth Analysis 2 Strategy: invest at mean 8%, standard deviation 25% if balance is < \$700,000: 8000 Initial yearly investment invest at mean 5%, standard deviation 15% if balance is >= \$700,000 and < \$1,000,000; Annual increase in investment stop investing if balance is >= \$1,000,000. Annual return on investment (normal dist. Mean 0.08 Mean 0.05 St. dev. Target 1000000 10 Target 700000 11 12 Ending 13 invested balance baland 14 =B3 =IF(C14<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C14<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C14\*(1+D14) =B14\*(1+\$B\$4) =C15\*(1+D15) 15 2 =E14+B15 =IF(C15<\$B\$10.RiskNormal(\$B\$7,\$B\$8),IF(C15<\$E\$10.RiskNormal(\$E\$7,\$E\$8),0)) =B15\*(1+\$B\$4) =E15+B16 =IF(C16<\$B\$10 RiskNormal(\$B\$7 \$B\$8) IF(C16<\$E\$10 RiskNormal(\$E\$7 \$E\$8) 0)) =C16\*(1+D16) 16 3 17 4 =B16\*(1+\$B\$4) =E16+B17 =IF(C17<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C17<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C17\*(1+D17) 18 5 =B17\*(1+\$B\$4) =E17+B18 =IF(C18<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C18<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C18\*(1+D18) =B18\*(1+\$B\$4) =E18+B19 =IF(C19<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C19<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C19\*(1+D19) 19 6 =E19+B20 =IF(C20<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C20<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) 20 =B19\*(1+\$B\$4) =C20\*(1+D20) 21 8 =B20\*(1+\$B\$4) =E20+B21 =IF(C21<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C21<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C21\*(1+D21) 22 9 =B21\*(1+\$B\$4) =E21+B22 =IF(C22<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C22<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C22\*(1+D22) 23 10 =B22\*(1+\$B\$4) =E22+B23 =IF(C23<\$B\$10.RiskNormal(\$B\$7.\$B\$8).IF(C23<\$E\$10.RiskNormal(\$E\$7.\$E\$8).0)) =C23\*(1+D23) 24 11 =B23\*(1+\$B\$4) =E23+B24 =IF(C24<\$B\$10.RiskNormal(\$B\$7.\$B\$8).IF(C24<\$E\$10.RiskNormal(\$E\$7.\$E\$8).0)) =C24\*(1+D24) 25 12 =B24\*(1+\$B\$4) =E24+B25 |=IF(C25<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C25<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C25\*(1+D25) 26 13 =B25\*(1+\$B\$4) =E25+B26 =IF(C26<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C26<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C26\*(1+D26) 27 14 =B26\*(1+\$B\$4) =E26+B27 =IF(C27<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C27<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C27\*(1+D27) 28 15 =B27\*(1+\$B\$4) =E27+B28 =IF(C28<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C28<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C28\*(1+D28) =B28\*(1+\$B\$4) =E28+B29 =IF(C29<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C29<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C29\*(1+D29) 29 16 =B29\*(1+\$B\$4) =E29+B30 =IF(C30<\$B\$10.RiskNormal(\$B\$7.\$B\$8).IF(C30<\$E\$10.RiskNormal(\$E\$7.\$E\$8).0)) =C30\*(1+D30) 30 17 31 18 =B30\*(1+\$B\$4) =E30+B31 =IF(C31<\$B\$10.RiskNormal(\$B\$7,\$B\$8),IF(C31<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C31\*(1+D31) 32 19 =B31\*(1+\$B\$4) =E31+B32 =IF(C32<\$B\$10.RiskNormal(\$B\$7,\$B\$8),IF(C32<\$E\$10.RiskNormal(\$E\$7,\$E\$8),0)) =C32\*(1+D32) 33 20 =B32\*(1+\$B\$4) =E32+B33 =IF(C33<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C33<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C33\*(1+D33) 34 21 =B33\*(1+\$B\$4) =E33+B34 =IF(C34<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C34<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C34\*(1+D34) 35 22 =B34\*(1+\$B\$4) =E34+B35 =IF(C35<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C35<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C35\*(1+D35) 36 23 =B35\*(1+\$B\$4) =E35+B36 =IF(C36<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C36<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C36\*(1+D36) 37 24 =B36\*(1+\$B\$4) =E36+B37 =IF(C37<\$B\$10.RiskNormal(\$B\$7.\$B\$8),IF(C37<\$E\$10.RiskNormal(\$E\$7.\$E\$8),0)) =C37\*(1+D37) 38 25 =B37\*(1+\$B\$4) =E37+B38 =IF(C38<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C38<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C38\*(1+D38) 39 26 =B38\*(1+\$B\$4) =E38+B39 =IF(C39<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C39<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C39\*(1+D39) 40 27 =B39\*(1+\$B\$4) =E39+B40 =IF(C40<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C40<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C40\*(1+D40) 41 28 =B40\*(1+\$B\$4) =E40+B41 =IF(C41<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C41<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =C41\*(1+D41) 42 29 =B41\*(1+\$B\$4) =E41+B42 =IF(C42<\$B\$10.RiskNormal(\$B\$7.\$B\$8).IF(C42<\$E\$10.RiskNormal(\$E\$7.\$E\$8).0)) =C42\*(1+D42) 43 30 =B42\*(1+\$B\$4) |=E42+B43 |=IF(C43<\$B\$10,RiskNormal(\$B\$7,\$B\$8),IF(C43<\$E\$10,RiskNormal(\$E\$7,\$E\$8),0)) =RiskOutput("Final Balance")+C43\*(1+D43) b. Report the mean and standard deviation of the ending balance after 30 years.

Mean =  $\frac{\$877,373}{\$}$ Standard deviation =  $\frac{\$360,291}{\$}$ 

c. What is the probability that the ending balance is >= \$1,000,000? (You get the probability by looking at the detailed statistics output and typing in 1,000,000 into a "target value" cell in the column corresponding to the ending balance. See page 593-594 of the text.)

Prob (the ending balance  $>= \$1,000,000) = \underline{51.5\%}$ 

d. Compare the strategy you analyzed in this problem to the strategy we discussed in class (Model 3: invest at 8% if balance is <\$1,000,000 and stop investing if balance is >=\$1,000,000). Suppose Amanda's investment target is to achieve an ending balance of \$1,000,000. Which strategy would you recommend? Why?

The strategy (Model 3) we discussed in class should be recommended because it gives Amanda a higher chance to achieve an ending balance of \$1,000,000 than the strategy analyzed in this problem.

### **Question 2: Doubling strategy in Roulette (Roulette.xlsx)**

Suppose you have \$100 at the beginning and you decide to bet on Red in Roulette.

Simulate the following *doubling* strategy. You begin by betting \$1. Each subsequent bet is decided as follows: If you won the last bet, you again bet \$1. If you lost the last bet, you bet twice the previous bet, if you have enough money. Otherwise, you return to betting \$1 unless you've run out.

a. Specify the following @Risk Model in Excel:

4	Α	В	С	D E	F	G	Н	I	J
1 5	1 Simulating Roulette Strategies								
2									
3		<b>Doubling strategy</b>							
4 (	Outcome		Prob.	Total b	ank	Bet #	Bet size	Spin result	Winnings
5 1	1	(your chosen color)	=18/38	100		0			=E5
6 2	2		=1-C5			1	1	=RiskDiscrete(A\$5:A\$6,C\$5:C\$6)	=IF(I6=1,J5+H6,J5-H6)
7						2	=IF(I6=1,MIN(1,J6),IF(J6>=2*H6,2*H6,MIN(1,J6)))	=RiskDiscrete(A\$5:A\$6,C\$5:C\$6)	=IF(I7=1,J6+H7,J6-H7)
8						3	=IF(I7=1,MIN(1,J7),IF(J7>=2*H7,2*H7,MIN(1,J7)))	=RiskDiscrete(A\$5:A\$6,C\$5:C\$6)	=IF(I8=1,J7+H8,J7-H8)
9						4	=IF(I8=1,MIN(1,J8),IF(J8>=2*H8,2*H8,MIN(1,J8)))	=RiskDiscrete(A\$5:A\$6,C\$5:C\$6)	=IF(I9=1,J8+H9,J8-H9)
10						5	=IF(I9=1,MIN(1,J9),IF(J9>=2*H9,2*H9,MIN(1,J9)))	=RiskDiscrete(A\$5:A\$6,C\$5:C\$6)	=IF(I10=1,J9+H10,J9-H10)

. . .

b. Define *Final Winning* as the winning after 100 rounds of betting. If your money runs out before 100 rounds, then the winnings remain zero.

What's the probability of losing all your initial \$100?

Prob(Final Winning = 0) = Prob(Final Winning  $\leq 0$ ) = 18.54%

What's the probability of getting a final winning of \$150 or more?

Prob(Final Winning  $\geq 150$ ) = 1 - Prob(Final Winning  $\leq 149$ ) = 1 - 82.05% = 17.95%

### **Question 3: When to pull the goalie in hockey (Hockey.xlsx)**

Consider a variation of the hockey example we discussed in class and implement the following strategy: Pull your goalie if you are behind at any point in the last *three minutes* of the game; put him back in if you tie the score.

a. Specify the following @Risk Model in Excel:

	ie jouo wing	C I ttbit In	ouei in Exect.		
A	В	С	D	E	F
1 When to pull the goalie in hockey					
2				Possible strategies (seconds left when goalie	is pulled)
3 Seconds left when goalie is pulled	=RiskSimtable(D3:F3)		60	120	180
4					
5 Inputs					
6 Prob of goal full-strength	=0.05/6				
7 Prob of our goal (our goalie pulled)	=0.08/6				
8 Prob of their goal (our goalie pulled)	=0.12/6				
9					
10 Current score (ours minus theirs)	-1				
11	1				
12 Simulation					
13 Time left (seconds)	Our score minus theirs	Are we behind?	Goalie Pulled?	We score?	They score?
14 180	=B10	=IF(B14<0,1,0)	=IF(AND(C14=1,A14<=\$B\$3),1,0)	=IF(D14=1.RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D14=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
15 170	=B14+E14-F14	=IF(B15<0,1,0)	=IF(AND(C15=1,A15<=\$B\$3),1,0)	=IF(D15=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D15=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
16 160	=B15+E15-F15	=IF(B16<0,1,0)	=IF(AND(C16=1,A16<=\$B\$3),1,0)	=IF(D16=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D16=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
17 150	=B16+E16-F16	=IF(B17<0,1,0)	=IF(AND(C17=1,A17<=\$B\$3),1,0)	=IF(D17=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D17=1,RiskBinomial(1,\$B\$6),RiskBinomial(1,\$B\$6))
18 140	=B17+E17-F17	=IF(B18<0,1,0)	=IF(AND(C18=1,A18<=\$B\$3),1,0)	=IF(D18=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D18=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
19 130	=B18+E18-F18	=IF(B19<0,1,0)	=IF(AND(C19=1,A19<=\$B\$3),1,0)	=IF(D19=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D19=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
20 120	=B19+E19-F19	=IF(B20<0,1,0)	=IF(AND(C20=1,A20<=\$B\$3),1,0)	=IF(D20=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D20=1,RiskBinomial(1,\$B\$6),RiskBinomial(1,\$B\$6))
21 110	=B20+E20-F20	=IF(B21<0,1,0)	=IF(AND(C21=1,A21<=\$B\$3),1,0)	=IF(D21=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D21=1,RiskBinomial(1,\$B\$6),RiskBinomial(1,\$B\$6))
22 100	=B21+E21-F21	=IF(B22<0,1,0)	=IF(AND(C22=1,A22<=\$B\$3),1,0)	=IF(D22=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D22=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
23 90	=B22+E22-F22	=IF(B23<0,1,0)	=IF(AND(C23=1,A23<=\$B\$3),1,0)	=IF(D23=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D23=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
24 80	=B23+E23-F23	=IF(B24<0,1,0)	=IF(AND(C24=1,A24<=\$B\$3),1,0)	=IF(D24=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D24=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
25 70	=B24+E24-F24	=IF(B25<0,1,0)	=IF(AND(C25=1,A25<=\$B\$3),1,0)	=IF(D25=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D25=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
26 60	=B25+E25-F25	=IF(B26<0,1,0)	=IF(AND(C26=1,A26<=\$B\$3),1,0)	=IF(D26=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D26=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
27 50	=B26+E26-F26	=IF(B27<0,1,0)	=IF(AND(C27=1,A27<=\$B\$3),1,0)	=IF(D27=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D27=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
28 40	=B27+E27-F27	=IF(B28<0,1,0)	=IF(AND(C28=1,A28<=\$B\$3),1,0)	=IF(D28=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D28=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
29 30	=B28+E28-F28	=IF(B29<0,1,0)	=IF(AND(C29=1,A29<=\$B\$3),1,0)	=IF(D29=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D29=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
30 20	=B29+E29-F29	=IF(B30<0,1,0)	=IF(AND(C30=1,A30<=\$B\$3),1,0)	=IF(D30=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D30=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
31 10	=B30+E30-F30	=IF(B31<0,1,0)	=IF(AND(C31=1,A31<=\$B\$3),1,0)	=IF(D31=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D31=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
32 0	=B31+E31-F31	=IF(B32<0,1,0)	=IF(AND(C32=1,A32<=\$B\$3),1,0)	=IF(D32=1,RiskBinomial(1,\$B\$7),RiskBinomial(1,\$B\$6))	=IF(D32=1,RiskBinomial(1,\$B\$8),RiskBinomial(1,\$B\$6))
33		,.,,	, , , , , , , , , , , , , , , , , , , ,	, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
34 We win or tie?	=IF(B32>=0,1,0)				
35	-,-,-,				
36 Selected summary measures from (	@RISK				
37	<u> </u>	Prob(we win	or tie)		
38 Strategy	1 minute				
39 Mean	=RiskMean(B34.1)		=RiskMean(B34,3)		
55 Modii	reservican(DJT,1)	reservican(D34,2)	(נ,דנע)וווויוווווווווווווווווווווווווווווווו	1	

## b. What's the probability that we win or tie?

Selected summary measures from @RISK							
	Prob(we win or tie)						
Strategy	1 minute	2 minutes	3 minutes				
Mean	0.1428	0.1589	0.172				