

Master 1 EMIMEO - Exam of “Basics of active and nonlinear electronics” (M. Campovecchio)

A- Narrow-band power amplifier (2 stages)

Specifications:

Output Power $P_{OUT} > 2 \text{ W}$; Center frequency $f_0 = 20 \text{ GHz}$;

Total power gain $G_P > 20 \text{ dB}$; Source and Load resistors $R_G = R_L = R_{50} = 50 \Omega$

MMIC technology (0.25 μm GaAs HEMT foundry) :

Power density $PD = 1 \text{ W/mm}$; Measured maximum gain @ 20 GHz $G_{MAX(@20GHz)} = 16 \text{ dB} \approx 40$;

Maximum drain current $I_{DSmax} = 800 \text{ mA/mm}$; Limits of V_{DS} voltage ($V_{DSmin}=1 \text{ V}$ and $V_{DSmax}=11 \text{ V}$)

Optimum power resistance: $R_{OPT} = 12,5 \Omega \cdot \text{mm}$

Linear electrical model : $C_{GS} = 2,7 \text{ pF/mm}$; $C_{DS} = 0,6 \text{ pF/mm}$; $R_i = 1 \Omega \cdot \text{mm}$; $R_{DS} = 125 \Omega \cdot \text{mm}$

Selected transistor (unitary size T1 of 0.6mm) @ 20 GHz = 8x75 μm GaAs HEMT

In the problem (C_{GS1} ; C_{DS1} ; R_{i1} ; R_{IN1} ; R_{DS1} ; R_{OPT1}) stand for the values of transistor T1 = 8x75 μm = **0.6 mm**

In this problem, **each stage has to be matched to its optimum power load R_{OPTA} and R_{OPTB}**

- 1) Using scaling rules, calculate the numerical values (C_{GS1} ; C_{DS1} ; R_{i1} ; R_{DS1} ; R_{OPT1} ; R_{IN1} @ 20GHz) of T1.
- 2) Power gain :
 - $G_P(R_{OPT})$ is the power gain of a transistor T when it is loaded by its optimum power load ($L_{OPT} // R_{OPT}$).
 - $G_{MAX} = G_P(R_{DS})$ is the maximum power gain of T when it is loaded by its optimum gain load ($L_{OPT} // R_{DS}$).

In both cases, $L_{OPT} = 1 / (C_{DS} \omega^2)$.

It can be demonstrated that the power gain $G_P(R_{OPT})$ can be expressed as a function of G_{MAX} by:

$$G_P(R_{OPT}) = R_{OPT} \left[\frac{R_{DS}}{R_{DS} + R_{OPT}} \right]^2 \frac{g_m^2}{R_i C_{GS}^2 \omega^2} = 4 R_{OPT} \frac{R_{DS}}{[R_{DS} + R_{OPT}]^2} G_{MAX}$$

Using this equation and the measured value of $G_{MAX(@20GHz)} = 16 \text{ dB} = 40$, determine the expression of $G_{P1}(R_{OPT1})$ for the transistor T1 when it is matched to its optimum power load R_{OPT1} . Demonstrate that the numerical value of G_{P1} at 20GHz is $G_{P1(@20GHz)} = 13,2 = 11,2 \text{ dB}$.
- 3) Using the specifications of output power and the technological data of power density, determine the sizing of the 2-stage amplifier (**size** of each stage with numbers n_B and n_A of transistors T1 per stage / optimum load resistance required by each stage R_{LB} and R_{LA} as a function of R_{OPT1} / output power P_{OUT} of 2nd stage/ gain of 2nd stage $G_{PB} = G_{P1}$ / inter-stage power $P_{INB} = P_{OUTA}$ / gain of 1st stage $G_{PA} = G_{P1}$ / input power $P_{IN} = P_{INA}$).
- 4) On the amplifier schematic (next page), indicate the numerical values of each stage when the amplifier operates at the maximum output power of the last stage.
- 5) Input and inter-stage matching
 - a) Calculate the equivalent series input resistances R_{iA} and R_{iB} of each stage.
 - b) Calculate the equivalent parallel input resistances R_{INA} and R_{INB} of each stage at 20GHz.
- 6) Draw the electrical matching circuits (inductors and transformers) of the two-stage amplifier when matched to $R_G = R_L = 50 \Omega$ and determine the expression of matching elements **without calculating numerical values**. For the sake of simplicity, you can use the notations:

$$L_1 = 1 / (C_{GS1} \omega_0^2) \text{ and } L_2 = 1 / (C_{DS1} \omega_0^2)$$
- 7) If both stages operate in class-A, calculate the total DC power to determine the maximum PAE of the amplifier? Why is-it less than 50%?

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