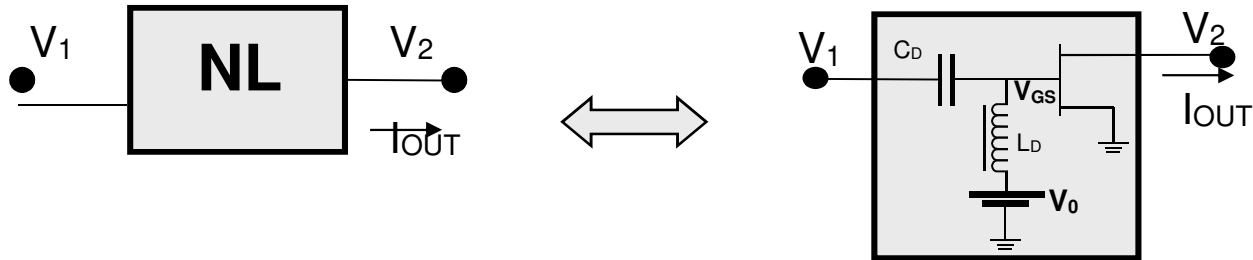


### Tutorial (SEM cold-FET Mixer)

The following cold-FET mixer (biased @  $V_{DS0}=0$  V) is used to design a SEM up-converter where the LO signal  $V_1$  is applied to the gate, which is biased @ ( $V_{GS0}=V_0$ ) while the IF input signal is applied to the drain using a low-pass filter and the output signal is extracted at the drain port using a high-pass filter.



The nonlinear operation of the cold-FET (NL) is expressed by the 2 following equations that give the output current  $I_{OUT}$  as a function of input and output control voltages  $V_1$  and  $V_2$ :

$$V_{GS} = V_0 + V_1 \quad (\text{eq1})$$

where  $V_0$  is a constant (gate bias voltage)

$$I_{OUT} = p V_2 - q V_2 V_{GS}^2 + r V_1 \quad (\text{eq2})$$

where  $p$ ,  $q$  and  $r$  are constants

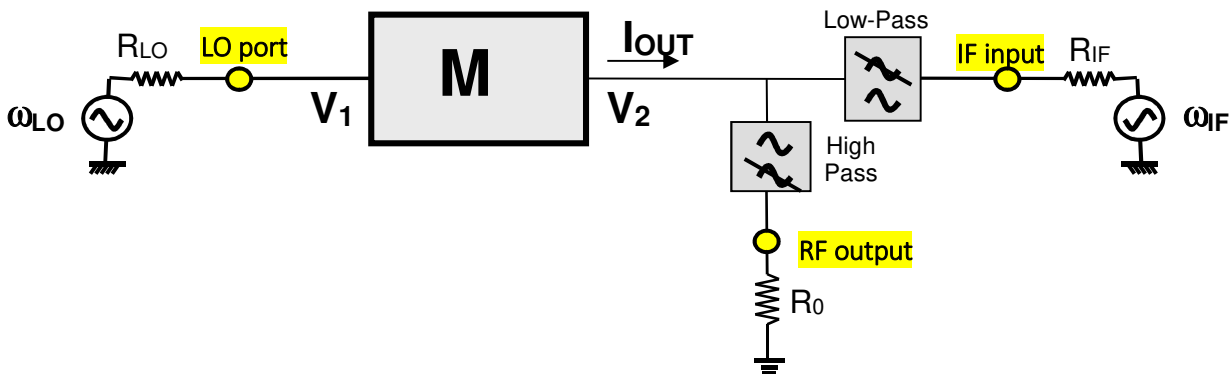
The SEM cold-FET mixer is shown below and the main frequencies are :

$$f_{LO} = 9 \text{ GHz}, \quad f_{IF} = 0.5 \text{ GHz} \text{ et } f_{RF} = f_{LO} + f_{IF} = 9.5 \text{ GHz} \quad (\omega_{RF} = \omega_{LO} + \omega_{IF}).$$

The two control voltages  $V_1$  and  $V_2$  of the FET mixer are :

$$\text{LO voltage at gate port : } V_1 = V_{LO} \cos(\omega_{LO} t) \quad (\text{eq3})$$

$$\text{IF voltage at drain port : } V_2 = V_{IF} \cos(\omega_{IF} t) \quad (\text{eq4})$$



- Using equations 1 to 4, express the output current  $I_{OUT}$  as a function of signal magnitudes ( $V_{LO}$ ,  $V_{IF}$ ), nonlinearity constants ( $p$ ,  $q$ ,  $r$ ), gate bias  $V_0$  and the mixing frequencies. The following notations can be used for mixing frequencies:  $\omega_{IM} = (\omega_{LO} - \omega_{IF})$  ;  $\omega_1 = (2\omega_{LO} - \omega_{IF})$  ;  $\omega_2 = (2\omega_{LO} + \omega_{IF})$
- The high-pass filter is designed to reject frequencies lower than 5GHz while the low-pass frequency is designed to cut frequencies greater than 5GHz. Therefore, what are the mixing frequencies at the RF output port?
- Determine the expression of the voltage conversion gain  $G_{CV}$ .
- If the LO port is assumed to be matched to  $R_{LO}$ ,
  - express the LO power applied at the LO port
  - express the LO power at the RF output port
  - express in dB the LO-to-RF isolation
  - what is the LO-to-IF isolation ?
  - express the equivalent impedance  $Z_{IN}$  seen by the IF generator @  $\omega_{IF}$  at the IF input port