



In systematic form:

$$G = \left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 1 & 0 & 1 \end{array} \right] \quad \checkmark$$

2 Errors detected :-

$$\textcircled{1} \text{ Detected error} = d_{\min} - 1 = 3 - 1 = 2.$$

$$\textcircled{2} \text{ Corrected error} \Rightarrow t = \left\lfloor \frac{d_{\min} - 1}{2} \right\rfloor = \frac{3 - 1}{2} = 1 //$$

(C) $N=7$.

$$g(D) = (D+1)(D^3+D+1) = D^4 + D^2 + D + D^3 + D + 1 = D^4 + D^3 + D^2 + 1.$$

For checking code is cyclic or not.

$$\text{Use } \frac{D^7+1}{g(D)}.$$

$$\begin{array}{r} D^4 + D^3 + D^2 + 1 \quad \overline{) \quad D^7 + 0 + 0 + 0 + 0 + 0 + 1} \\ \underline{D^7 + D^6 + D^5 + 0 + D^3} \\ D^6 + D^5 + 0 + D^3 + 0 + 0 + 1 \\ \underline{D^6 + D^5 + D^4 + 0 + D^2} \\ D^4 + D^3 + D^2 + 0 + 1 \\ \underline{D^4 + D^3 + D^2 + 0 + 1} \\ 0 // \end{array} \quad \checkmark$$

Therefore, the given block code is cyclic as there is no remainder. and even when we ^{can} shift the polynomial of generator matrix,