

Microwave Engineering

10/01/17

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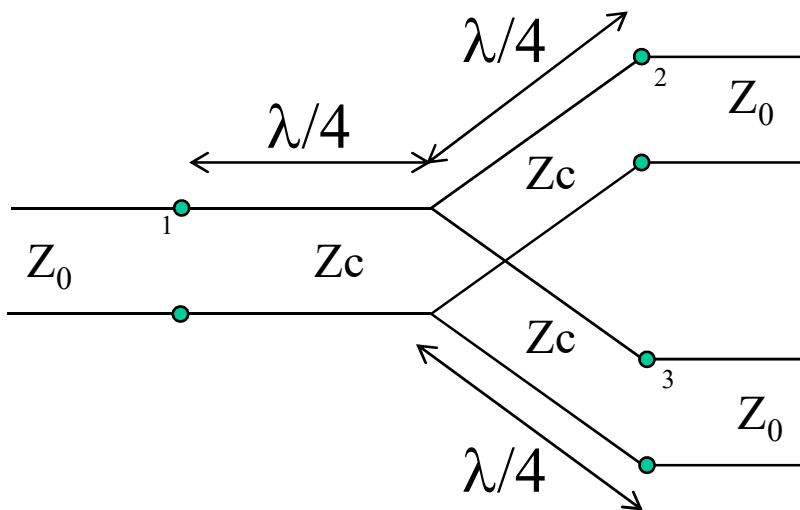
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Exercise 1

a) Discuss the properties of the scattering matrix of the three port network described in the figure.

Is it a symmetric matrix? Is it a unitary matrix?

b) Compute the scattering matrix of the three port network described in the figure ($Z_0 = 50 \Omega$, $Z_c = \sqrt{2}Z_0$).



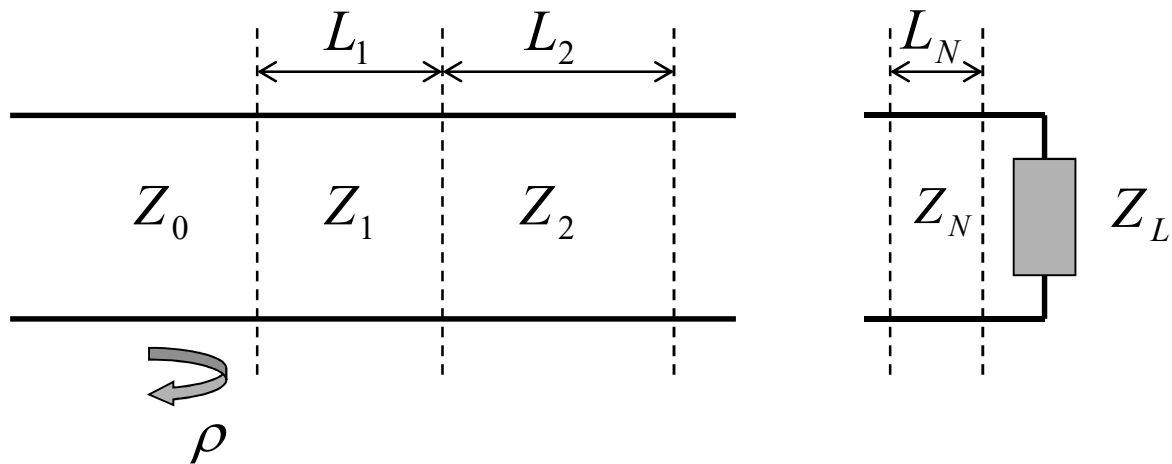
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Exercise 2

a) Consider the transmission line described in the figure.



Explain how to compute the reflection coefficient using the theory of small reflections.

b) Using $Z_0=50\ \Omega$, $Z_L=90\ \Omega$ and $Z_1=75\ \Omega$ (with $L_1=20\text{ cm}$), and assuming a phase velocity equal to the phase velocity in vacuum, compute the reflection coefficient at input for an operating frequency $f=3\text{ GHz}$.

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Exercise 3

Consider a plane wave normally incident on a half space of copper. If the wave frequency $f=5$ GHz, compute the propagation constant, the intrinsic impedance, and the skin depth for the conductor. Also compute the reflection and transmission coefficients.

Hint: for copper, $\sigma=5.813 \times 10^7$ S/m.

Also, the free space magnetic permeability $\mu=4\pi \times 10^{-7}$ H/m

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Exercise 4

A microwave antenna feed network operating at 5 GHz requires a 50Ω printed transmission line that is 16λ long. Possible choices are:

- 1) copper microstrip, with $d=0.16$ cm, $\epsilon_r=2.20$, and $\tan\delta=0.001$, or
- 2) copper stripline, with $b=0.32$ cm, $\epsilon_r=2.20$, $t=0.01$ mm, and $\tan\delta=0.001$. Which line should be used if attenuation is to be minimized?

•Background formulas for microstrip lines:

The effective dielectric constant of a microstrip line is given approximately by

$$\epsilon_e = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \frac{1}{\sqrt{1 + 12d/W}}. \quad (3.195)$$

The effective dielectric constant can be interpreted as the dielectric constant of a homogeneous medium that equivalently replaces the air and dielectric regions of the microstrip line, as shown in Figure 3.26. The phase velocity and propagation constant are then given by (3.193) and (3.194).

Given the dimensions of the microstrip line, the characteristic impedance can be calculated as

$$Z_0 = \begin{cases} \frac{60}{\sqrt{\epsilon_e}} \ln \left(\frac{8d}{W} + \frac{W}{4d} \right) & \text{for } W/d \leq 1 \\ \frac{120\pi}{\sqrt{\epsilon_e} [W/d + 1.393 + 0.667 \ln(W/d + 1.444)]} & \text{for } W/d \geq 1. \end{cases} \quad (3.196)$$

For a given characteristic impedance Z_0 and dielectric constant ϵ_r , the W/d ratio can be found as

$$\frac{W}{d} = \begin{cases} \frac{8e^A}{e^{2A} - 2} & \text{for } W/d < 2 \\ \frac{2}{\pi} \left[B - 1 - \ln(2B - 1) + \frac{\epsilon_r - 1}{2\epsilon_r} \left\{ \ln(B - 1) + 0.39 - \frac{0.61}{\epsilon_r} \right\} \right] & \text{for } W/d > 2, \end{cases} \quad (3.197)$$

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Exercise 4 (continued)

where

$$A = \frac{Z_0}{60} \sqrt{\frac{\epsilon_r + 1}{2}} + \frac{\epsilon_r - 1}{\epsilon_r + 1} \left(0.23 + \frac{0.11}{\epsilon_r} \right)$$
$$B = \frac{377\pi}{2Z_0\sqrt{\epsilon_r}}.$$

Considering a microstrip line as a quasi-TEM line, we can determine the attenuation due to dielectric loss as

$$\alpha_d = \frac{k_0 \epsilon_r (\epsilon_e - 1) \tan \delta}{2\sqrt{\epsilon_e} (\epsilon_r - 1)} \text{ Np/m}, \quad (3.198)$$

where $\tan \delta$ is the loss tangent of the dielectric. This result is derived from (3.30) by multiplying by a “filling factor,”

$$\frac{\epsilon_r (\epsilon_e - 1)}{\epsilon_e (\epsilon_r - 1)},$$

which accounts for the fact that the fields around the microstrip line are partly in air (lossless) and partly in the dielectric (lossy). The attenuation due to conductor loss is given approximately by [8]

$$\alpha_c = \frac{R_s}{Z_0 W} \text{ Np/m}, \quad (3.199)$$

where $R_s = \sqrt{\omega\mu_0/2\sigma}$ is the surface resistivity of the conductor. For most microstrip substrates, conductor loss is more significant than dielectric loss; exceptions may occur, however, with some semiconductor substrates.

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Exercise 4 (continued)

- Background formulas for strip lines:

When designing stripline circuits one usually needs to find the strip width, given the characteristic impedance (and height b and relative permittivity ϵ_r), which requires the inverse of the formulas in (3.179). Such formulas have been derived as

$$\frac{W}{b} = \begin{cases} x & \text{for } \sqrt{\epsilon_r} Z_0 < 120 \, \Omega \\ 0.85 - \sqrt{0.6 - x} & \text{for } \sqrt{\epsilon_r} Z_0 > 120 \, \Omega, \end{cases} \quad (3.180a)$$

where

$$x = \frac{30\pi}{\sqrt{\epsilon_r} Z_0} - 0.441. \quad (3.180b)$$

Since stripline is a TEM line, the attenuation due to dielectric loss is of the same form as that for other TEM lines and is given in (3.30). The attenuation due to conductor loss can be found by the perturbation method or Wheeler's incremental inductance rule. An approximate result is

$$\alpha_c = \begin{cases} \frac{2.7 \times 10^{-3} R_s \epsilon_r Z_0}{30\pi(b-t)} A & \text{for } \sqrt{\epsilon_r} Z_0 < 120 \, \Omega \\ \frac{0.16 R_s}{Z_0 b} B & \text{for } \sqrt{\epsilon_r} Z_0 > 120 \, \Omega \end{cases} \quad \text{Np/m}, \quad (3.181)$$

with

$$A = 1 + \frac{2W}{b-t} + \frac{1}{\pi} \frac{b+t}{b-t} \ln \left(\frac{2b-t}{t} \right),$$
$$B = 1 + \frac{b}{(0.5W + 0.7t)} \left(0.5 + \frac{0.414t}{W} + \frac{1}{2\pi} \ln \frac{4\pi W}{t} \right),$$

where t is the thickness of the strip.