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Semester S1

Basics of active and non linear electronics

RF Power amplifiers (JM Nebus)

COURSE N° 5

Module Name

Module's Author

-1-

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Chapter V : Load modulated Power amplifier (Doherty power amplifier : DPA)

I] Motivations

We want to design a power amplifier having an efficiency which remains at a high value even if the input RF power decreases from the maximum input power at saturation ($V_{gs}=V_{gs_{max}}$) to a lower input power ($V_{gs}=V_{gs_{max}}/2$) .

Doing so we can have a high average efficiency for useful input modulated signal having a varying instantaneous envelope power as mentioned in chapter I .

Let us consider class B operation of a transistor.

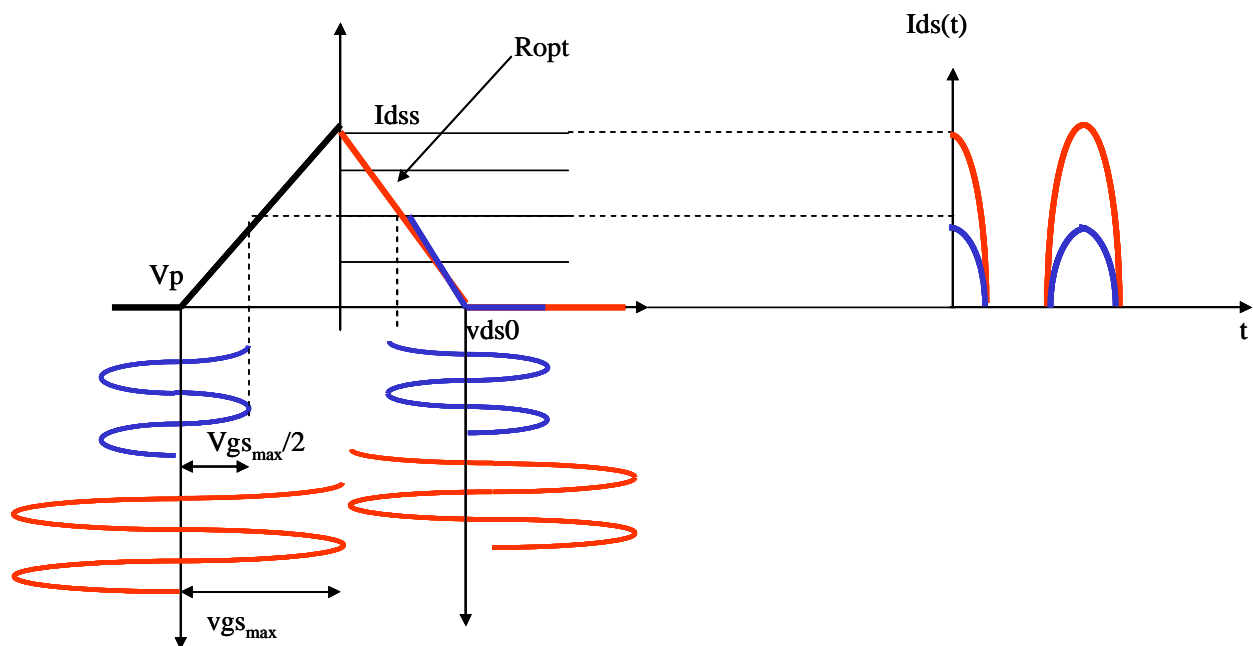


Figure 1

If the load resistance remains constant and at its optimal value (R_{opt}) for maximum output power, we can see that the RF drain voltage swing decreases if the input gate source voltage decreases as represented in Figure 1.

If we take for example, $V_{ds0}=30V$, $V_k=V_{dsmin}=5V$ and $I_{dss}=1A$

- For $V_{gs1}=V_{gsmax}=-V_p$ (high input power level)

$R_{opt} = 50\Omega$, $P_{out} = 6.25W$ and $\eta_d=65.5\%$, $V_{ds1} = 25V$ and $I_{ds1} = 0.5 A$

- For $V_{gs1}=V_{gsmax}/2$ (medium input power level)

$V_{ds1} = R_{opt} \cdot I_{dss}/4 = 12.5 V$ and $I_{ds1} = 0.25 A$

$P_{out}= 3.125W$ and $\eta_d=33\%$

The drain efficiency decreases drastically because V_{ds1} is reduced

We can plot the representative RF power and efficiency characteristics as shown in figure 2

When V_{gs} is divided by 2, the input RF power is divided by 4

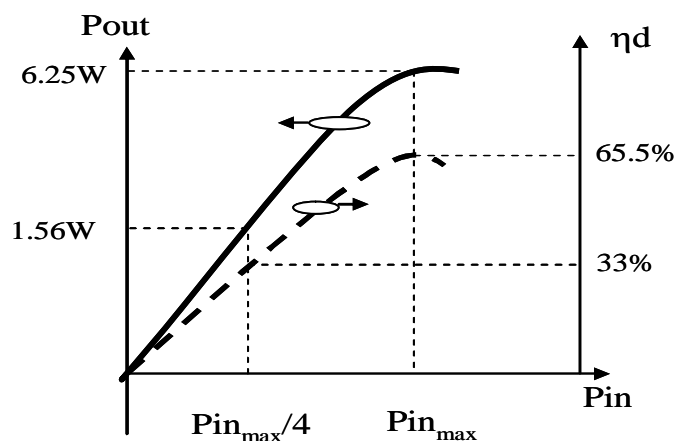


Figure 2

In order to maintain a high efficiency value when the input power decreases we can modify the optimal load resistance (R'_{opt}) to have a higher drain voltage swing V_{ds1} .

The maximum achievable value of V_{ds1} is equal to 25V

So we need to have $R'_{opt} = 2R_{opt}$ as depicted in, figure 3

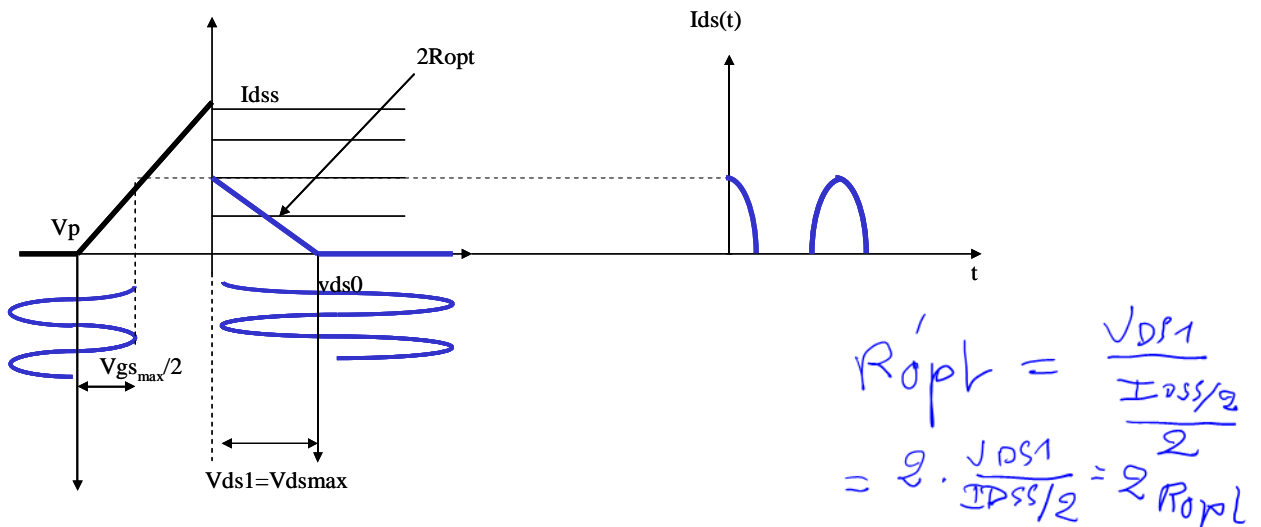


Figure 3

In this case we obtained the power characteristics plotted in figure 4.

Calculations give: $R'_{opt} = 100\Omega$, $P'_{out\ max} = 3.125W$ and $\eta'_d = 65.5\%$

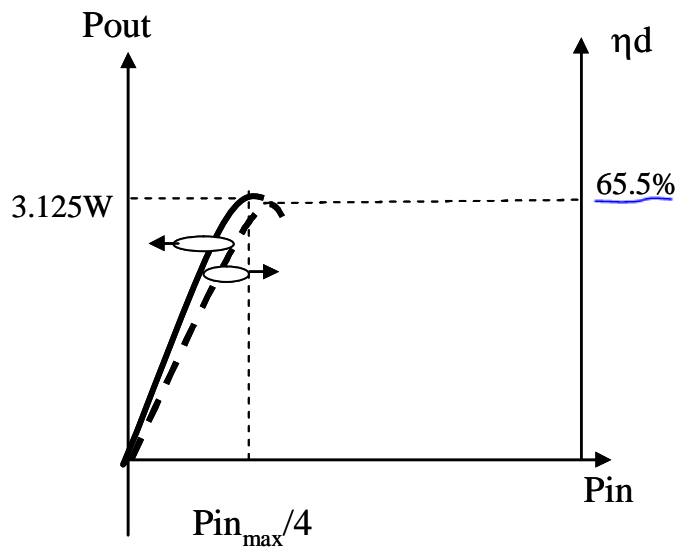


Figure 4

Consequently the aim of load modulation is to target a drain efficiency curve having the shape shown in figure 5 . For this purpose the load resistance needs to be varied from $2R_{opt}$ to R_{opt} when the input gate voltage V_{gs} varies from $V_{gsmax}/2$ up to V_{gsmax} as shown in figure 6 .

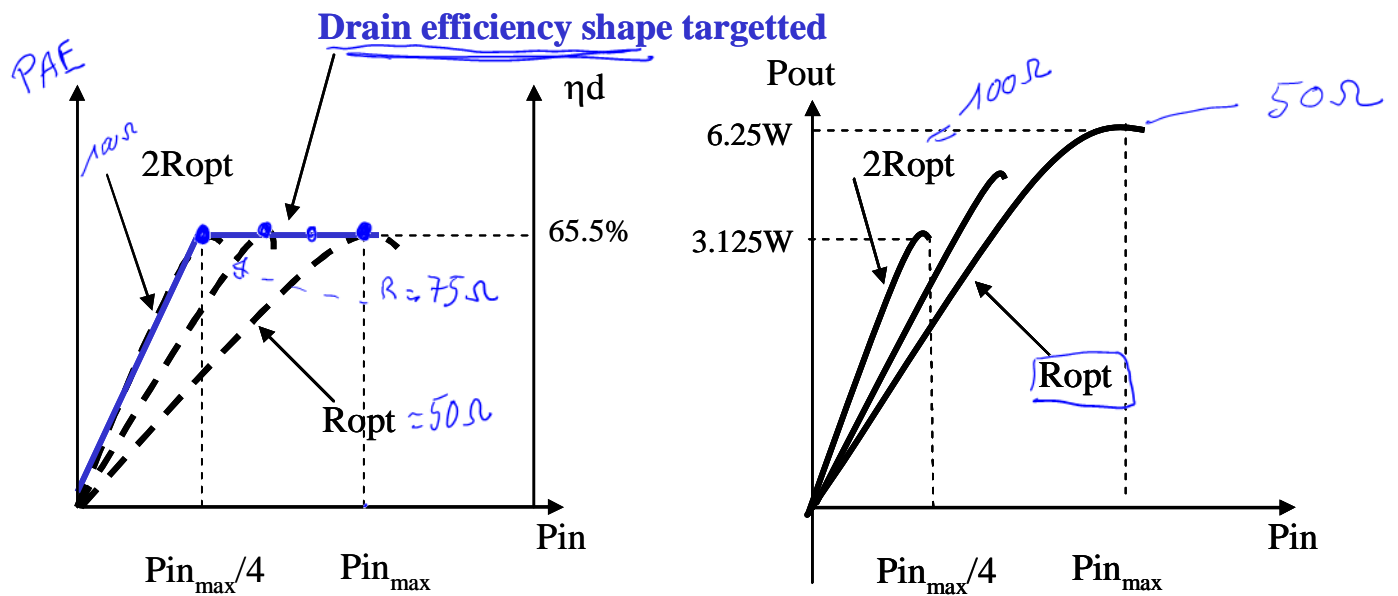


Figure 5

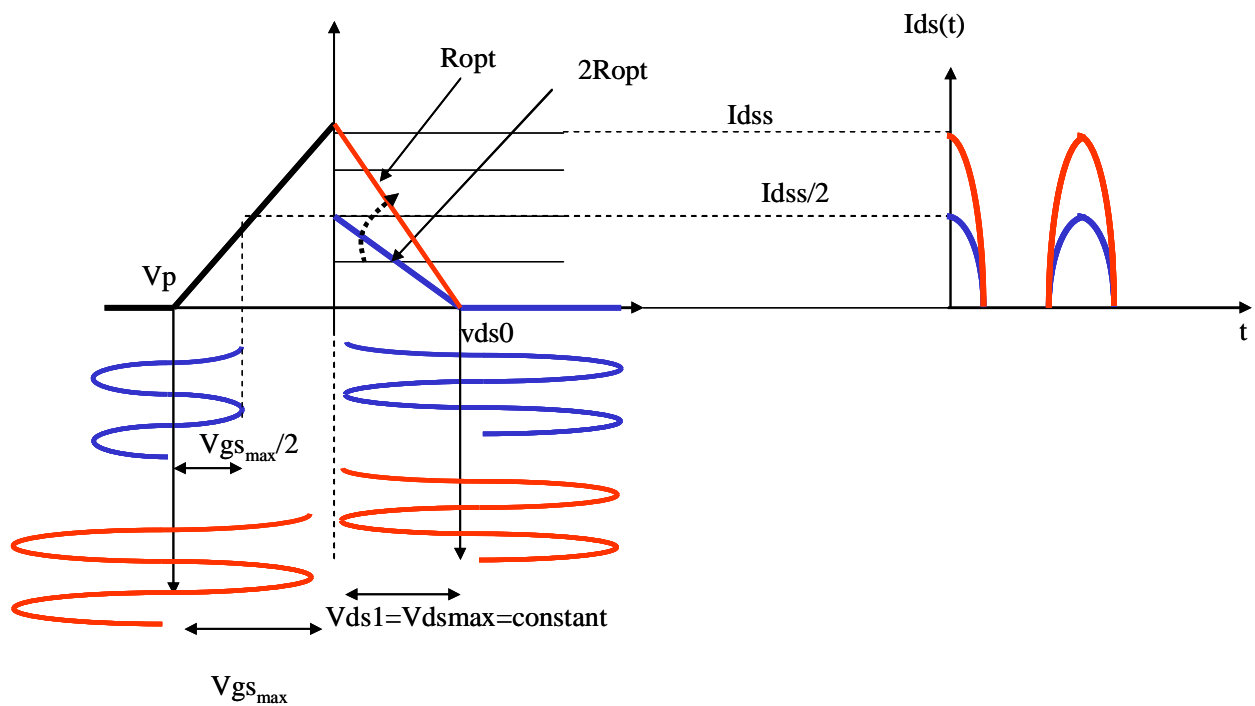


Figure 6

For V_{gs} lower than $V_{gsmax}/2$, the load resistance is kept at a fixed value of $2 R_{opt}$

II] Load modulation circuit principle (figure 7)

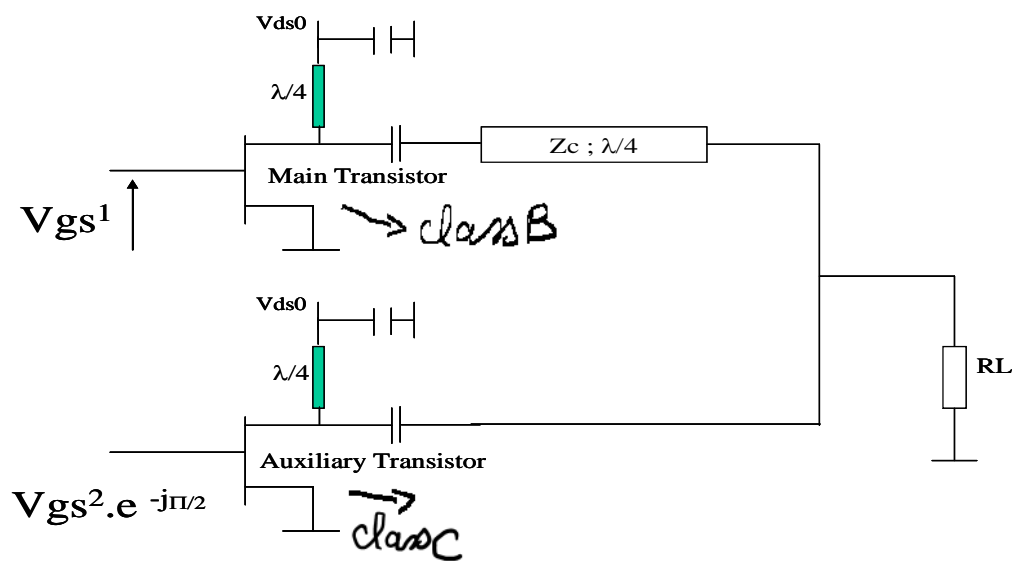


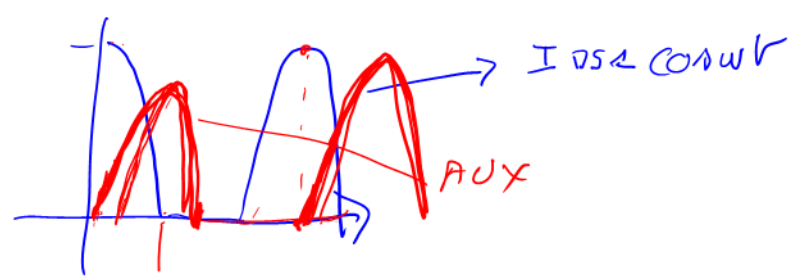
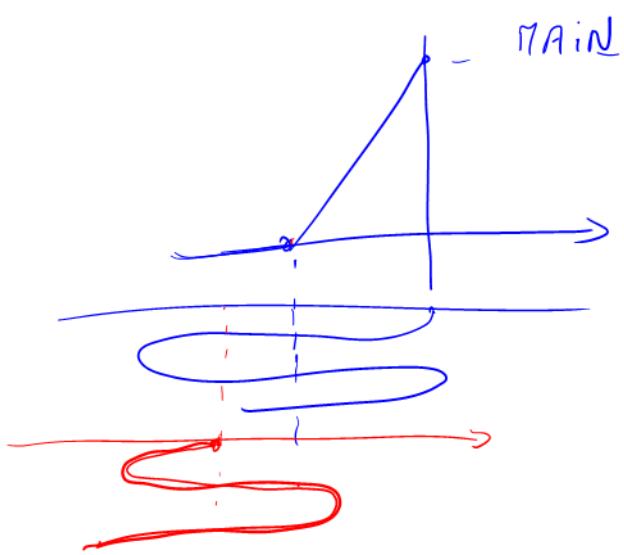
Figure 7

Using quarterwave line for the drain bias circuit, second harmonic of the drain currents are terminated into a short circuit.

We consider also that higher harmonics are small and not taken into account in the following.

The gate source voltage that drives the auxiliary transistor is applied when the gate source voltage of the main transistor is higher than $V_{gsmax}/2$. Below this value the auxiliary transistor is considered to be turned off.

This could be realised by using a Class C auxiliary transistor while the main transistor is operating in class B.



$$\cos \omega \left(t - \frac{T}{4} \right) \rightarrow$$

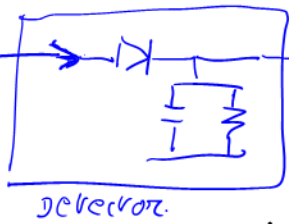
$$\cos \left(\omega t - \frac{2\pi}{T} \cdot \frac{T}{4} \right) = \cos \left(\omega t - \frac{\pi}{2} \right)$$

Principle of passive load variation technique

$R_{opt} \times 2R_{opt}$



R will not be used.



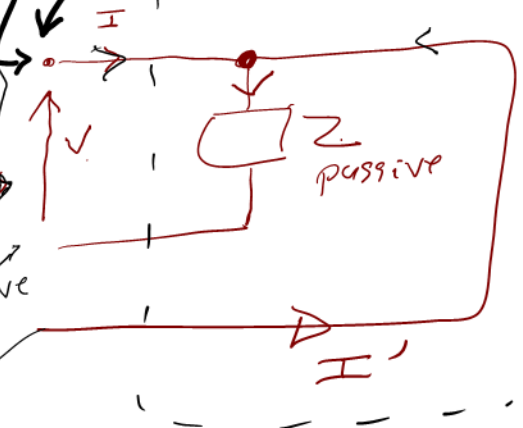
detector

Principle of active load variation technique

This technique will be used a second transistor is necessary.



$$Z = \frac{V}{I}$$



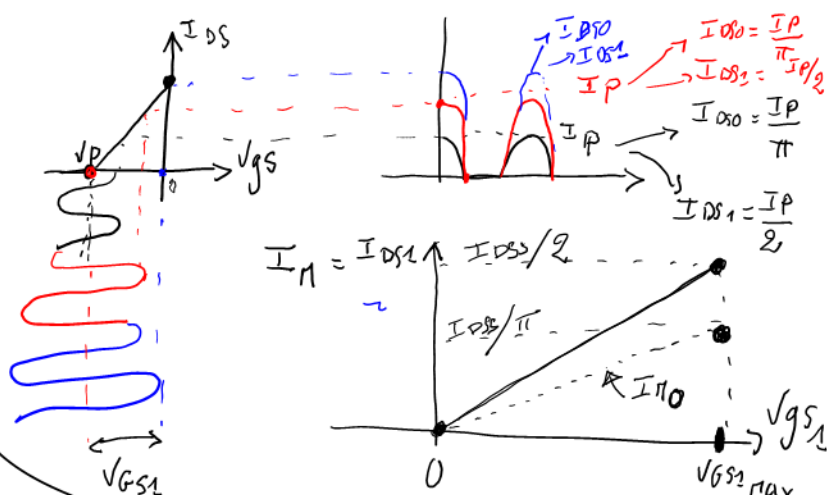
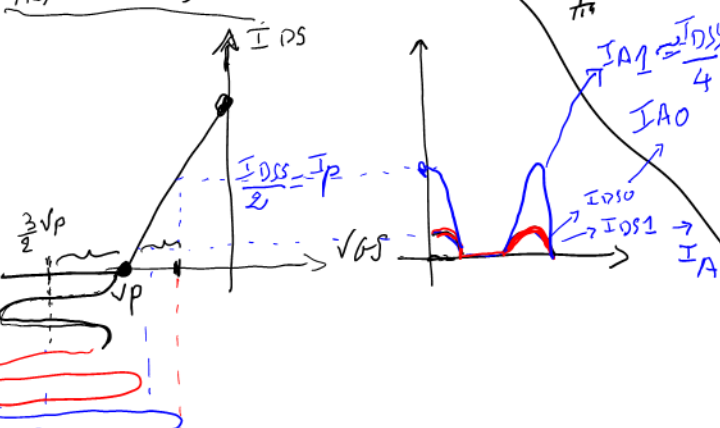
$$V = Z \times (I + I')$$

$$Z_{active} = \frac{V}{I}$$

Main Transistor:

MAIN: class B

Aux Transistor:



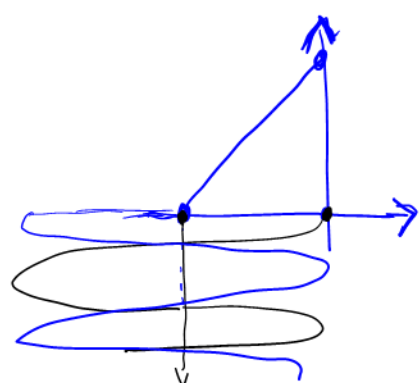
$$V_{GS0} + V_{GS1} \cos \phi = V_p$$

$$I_{DS0} + I_{DS1} \cos \omega t + I_{DS2} \cos(2\omega t)$$

$$I_{DS}(t) = I_{DS}\left(t - \frac{T}{2}\right)$$

$$I_{DS}(t) = I_{DS0} + I_{DS1} \cos \omega\left(t - \frac{T}{2}\right) + I_{DS2} \cos(2\omega\left(t - \frac{T}{2}\right))$$

$$I_{DS}(t) = I_{DS0} + I_{DS1} \cos \omega t + I_{DS2} \cos(2\omega t)$$



The equivalent circuit at the fundamental operating frequency is given in figure 8

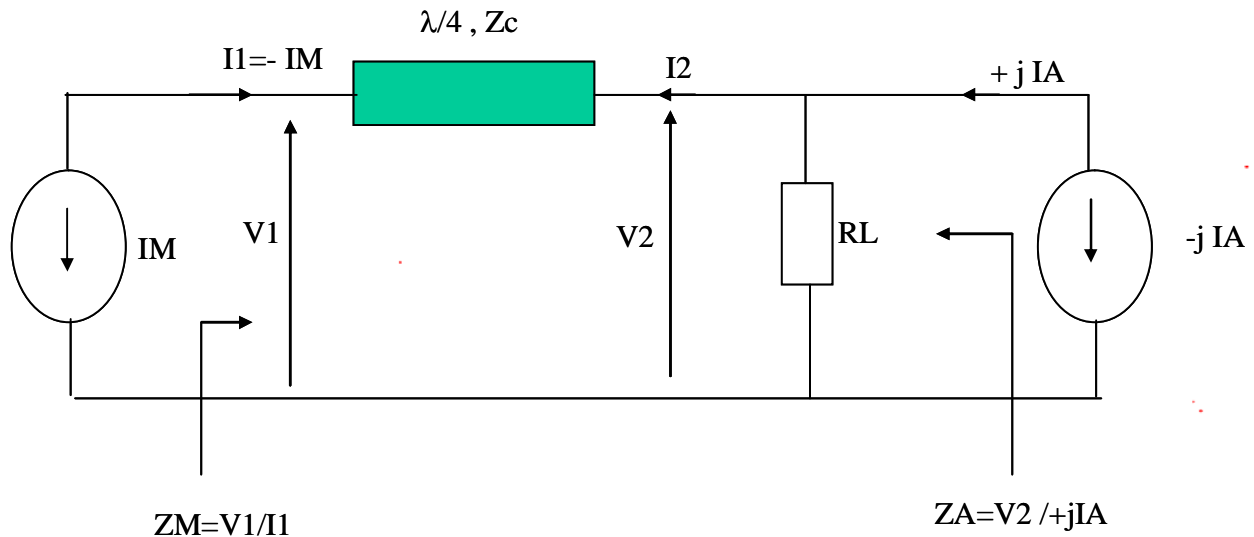


Figure 8

$$\begin{pmatrix} V_1 \\ I_1 \end{pmatrix} = \begin{pmatrix} 0 & jZ_c \\ \frac{j}{Z_c} & 0 \end{pmatrix} \cdot \begin{pmatrix} V_2 \\ -I_2 \end{pmatrix}$$

$$\begin{aligned} V_1 &= -jZ_c I_2 & I_2 &= jI_A - \frac{V_2}{R_L} \\ I_1 &= \frac{jV_2}{Z_c} & V_2 &= -jZ_c I_1 = +jZ_c I_M \end{aligned}$$

$$Z_M = \frac{V_1}{I_1} = \frac{-jZ_c(jI_A - \frac{V_2}{R_L})}{\frac{jV_2}{Z_c}} = \frac{Z_c^2}{R_L} - Z_c \frac{I_A}{I_M}$$

$$Z_A = Z_c \frac{I_M}{I_A}$$

When $I_A=0$ (auxiliary off) we want to have

$$Z_M = \frac{Z_c^2}{R_L} = 2R_{opt} \rightarrow R_L = \frac{R_{opt}}{2}$$

At maximum output power of both transistors ($I_M = I_A$) we want to have

$$Z_M = Z_A = R_{opt}$$

This leads to

$$Z_C = R_{opt}$$

$$R_L = \frac{R_{opt}}{2}$$

The variations of the currents I_M and I_A versus V_{gs}

are given in figure 9 :

(linear variations of both the fundamental and DC value for class B operation)

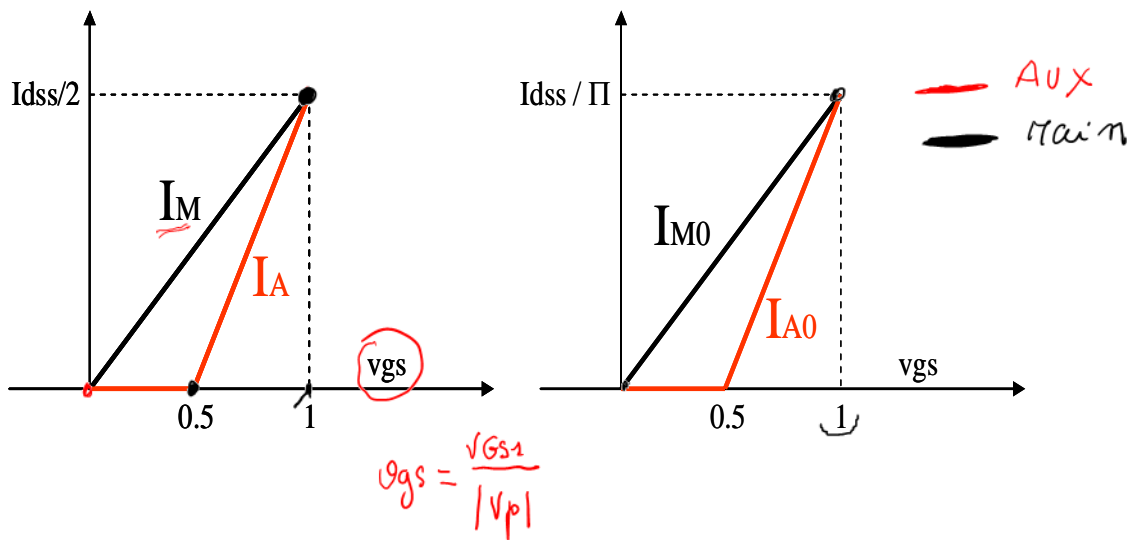


Figure 9

I_M and I_A are fundamental frequency components of currents while I_{M0} and I_{A0} are DC components of currents .

v_{gs} is here normalized to $-V_p$. It varies between 0 and 1

- Equations of current components are :

$$I_M = \frac{Id_{ss}}{2} \cdot v_{gs} \quad I_{M0} = \frac{Id_{ss}}{\pi} \cdot v_{gs} \quad \longrightarrow \quad \text{For } 0 < v_{gs} < 1$$

$$I_A = Id_{ss} \cdot v_{gs} - \frac{Id_{ss}}{2} \quad I_{A0} = \left(Id_{ss} \cdot v_{gs} - \frac{Id_{ss}}{2} \right) \cdot \frac{2}{\pi} \quad \longrightarrow \quad \text{For } 0.5 < v_{gs} < 1$$

- Equations of load impedances are :

$$Z_M = \frac{Z_C^2}{R_L} \quad Z_A = \infty$$

For $0 < v_{gs} < 0.5$

$$I_n \neq 0 \\ I_A = 0$$

$$Z_M = \frac{Z_C^2}{R_L} - Z_C \left(2 - \frac{1}{v_{gs}} \right) \quad Z_A = Z_C \cdot \left(\frac{1}{2 - \frac{1}{v_{gs}}} \right)$$

$$I_A \neq 0 \quad I_n \neq 0 \\ \text{For } 0.5 < v_{gs} < 1$$

$$\begin{aligned} Z_C = R_{opt} : \\ R_L = R_{opt}/2 \quad \rightarrow \quad v_{gs} = 0.5 \quad \rightarrow \quad Z_n = \frac{Z_C^2}{R_L} = \frac{(R_{opt})^2}{R_{opt}/2} = 2R_{opt} \\ v_{gs} = 1 \quad \rightarrow \quad Z_n = \frac{Z_C^2}{R_L} - Z_C = \frac{R_{opt}^2}{R_{opt}} - R_{opt} = R_{opt} \end{aligned}$$

Load impedance variations versus v_{gs} are plotted in figure 10

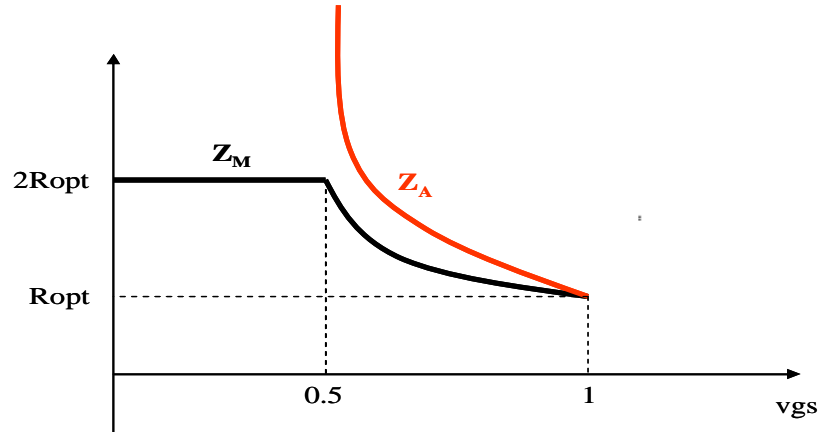


Figure 10

- Equations of Voltages are :

$$V_1 = V_M = Z_M \cdot I_M = \frac{Z_C^2 \cdot Id_{ss}}{2R_L} \cdot v_{gs}$$

$$|V_A| = Z_C \cdot I_M = \frac{R_{opt} \cdot Id_{ss}}{2} \cdot v_{gs}$$

$\nearrow = |\sqrt{2}|$

For $0 < v_{gs} < 0.5$

$$V_1 = 2\pi \cdot I_1$$

$$V_M = \frac{R_{opt} \cdot Id_{ss}}{2}$$

For $0.5 < v_{gs} < 1$

$$|V_A| = Z_C \cdot I_M = \frac{R_{opt} \cdot Id_{ss}}{2} \cdot v_{gs}$$

(initial
chain
matrix
of $\lambda/4$)

Note that as $Z_c = R_{opt}$ we have the following relationship

$$\frac{R_{opt} \cdot Id_{ss}}{2} = \underbrace{V_{ds1_{max}}}_{V_{M}} = V_{ds0} \quad \text{If we consider } V_{dsmin} = 0$$

$\downarrow V_{M} \rightarrow |V_A|$

Plots of voltages are given in figure 11

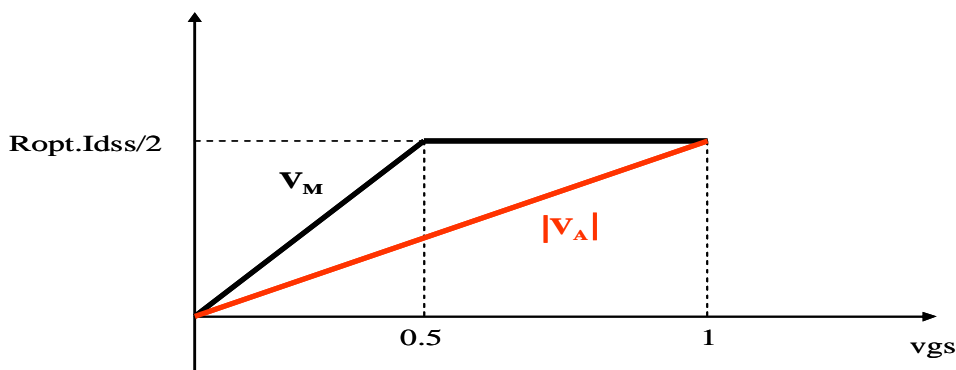


Figure 11

- Equations of RF powers are :

only the drain is ON

For $0 < v_{gs} < 0.5$

$$P_M = \frac{1}{2} \text{Real}(Z_M I_1 I_1^*) = R_{opt} \frac{Id_{ss}^2}{4} \cdot v_{gs}^2 \quad P_A = 0$$

$\downarrow V_1$
 V_M

$$P_{\text{our amplifier}} = P_M + P_A :$$

For $0.5 < v_{gs} < 1$

$$P_M = R_{opt} \frac{Id_{ss}^2}{8} \cdot v_{gs} \quad P_A = \frac{1}{2} \text{Real} \left(V_A \cdot (jI_A)^* \right) = \frac{1}{8} R_{opt} \cdot Id_{ss}^2 \cdot (2v_{gs}^2 - v_{gs})$$

And $P_{RL} = P_M + P_A$

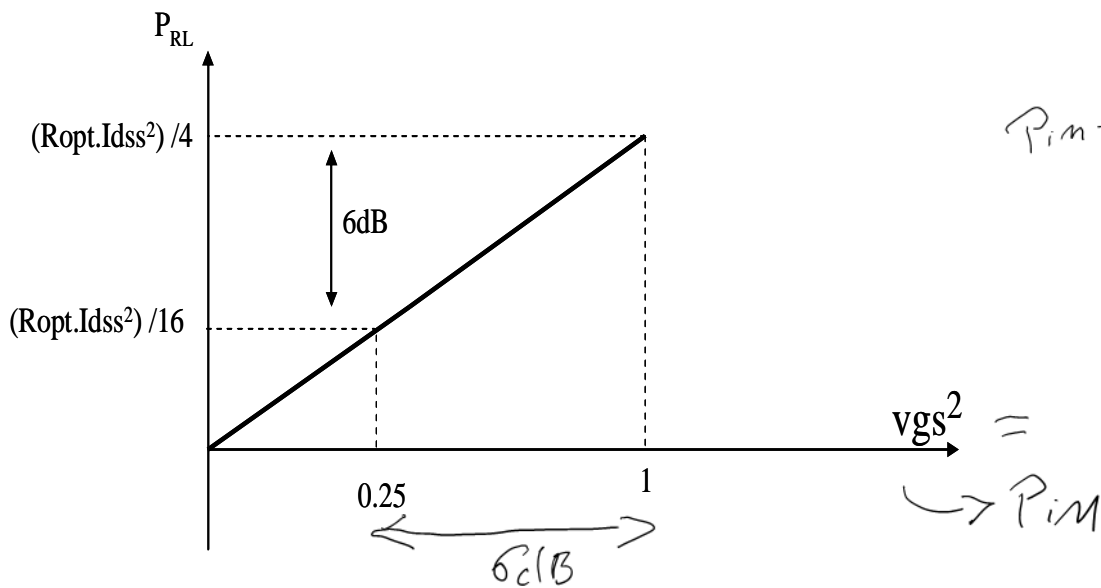


Figure 12

- Equations of Drain efficiency are :

$$\eta_d = \frac{\pi}{4} \cdot \left(\frac{R_{opt} \cdot Id_{ss}}{V_{ds0}} \right) \cdot v_{gs}$$

For $0 < v_{gs} < 0.5$

$$\eta_d = \frac{\pi}{2} \cdot \left(\frac{v_{gs}^2}{3v_{gs} - 1} \right)$$

For $0.5 < v_{gs} < 1$

$$\eta_D = \frac{P_{out}}{v_{DSS0} I_{n0} + v_{A0} I_{A0}}$$

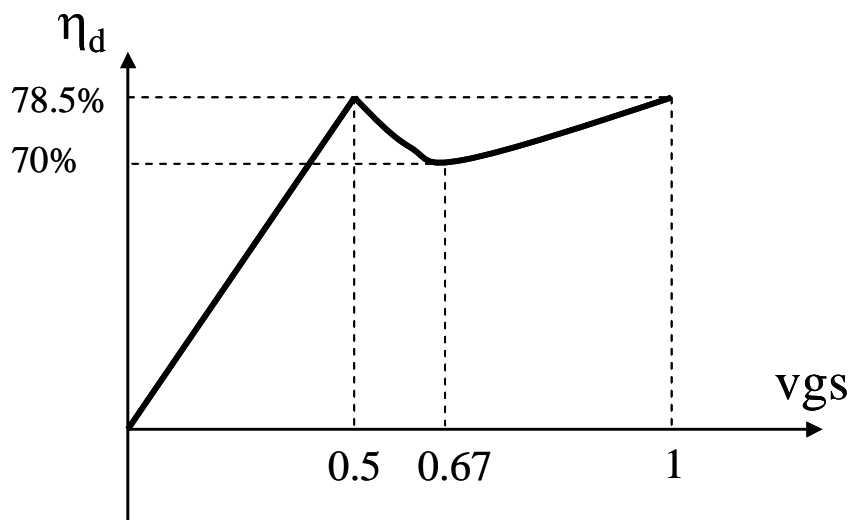


Figure 13