

Part I (Error Control Codes)

1). Given,  $G = \begin{bmatrix} 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 \end{bmatrix}$

a)  $N = 9, K = 2$

No. of possible codewords =  $2^K = 2^2 = 4$  possible codewords.

0 0 0 0 0 0 0 0 0		dmin.	dmin = 6 //
1 1 0 1 1 0 1 1 0		6	
1 0 1 1 0 1 1 0 1		6	
0 1 1 0 1 1 0 1 1		6	

Correct  $G$  or in systematic shape.

$$G = \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 \end{bmatrix}$$

Thus, the generator polynomial is  $1 - 0^7 1^6 1^5 0^4 1^3 0^2 1^1 1^0$

$$g(D) = \underline{\underline{D^7 + D^6 + D^4 + D^3 + D^1 + 1}}$$

To check cyclic code. =  $\frac{D^N + 1}{g(D)}$

$$\begin{array}{r} D^7 + D^6 + D^4 + D^3 + D + 1 \\ \overline{D^2 + D + 1} \\ \hline D^9 + 0 + 0 + 0 + 0 + 0 + 0 + 0 + 1 \\ D^9 + D^8 + 0 + D^6 + D^5 + 0 + D^3 + D^2 \\ \hline D^8 + 0 + D^6 + D^5 + 0 + D^3 + D^2 + 0 + 1 \\ D^8 + D^7 + 0 + D^5 + D^4 + 0 + D^2 + D + 0 \\ \hline D^7 + D^6 + 0 + D^4 + D^3 + 0 + D + 1 \\ D^7 + D^6 + 0 + D^4 + D^3 + 0 + D + 1 \\ \hline 0 \end{array}$$

// The remainder is 0, so,

It is cyclic code