

3. Smith Chart and impedance matching

1. Reflection coefficient calculations

Exercise #1 : Analytical calculations versus Smith chart ([tutorial n1 Smith chart.pptx](#))

An air line, with a characteristic impedance of $Z_C = 250 \Omega$, is powered at the frequency $f_0 = 500$ MHz.

It is 2m long and ends at an impedance Z_L . The SWR along the line is $s = 5$ and the first maximum voltage is at $d = 12$ cm from the load.

- Calculate $|\rho_L|$, ρ_L module and argument of the reflection coefficient on the load.
- Calculate Z_L .
- The input voltage is 10V. What is the value of the voltage at the load terminals. Give V_{\max} and V_{\min} on the line.

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Exercise #2 : Graphical calculations on Smith chart ([tutorial #2 Smith chart](#))

An air line, with a characteristic impedance of $Z_C = 20 \Omega$, is loaded at its end on an impedance $Z_L = R_L + j X_L = (24 + j 36) \Omega$. At the frequency of $f_0 = 3$ GHz, the length of the line is $\ell = \lambda_0 / 4$.

- 1) Give, using the Smith chart:
 - The reflection coefficient ρ_L , the SWR s_L on the load Z_L .
 - The reflection coefficient ρ_{in} , the SWR s_{in} and the impedance Z_{in} at the distance ℓ , for $f_0 = 3$ GHz and $f_1 = 4$ GHz

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Exercise #2 : Graphical calculations on Smith chart

2) A line of length ℓ_1 , with a characteristic impedance $Z_C = 20 \Omega$, short-circuited at one end, is placed in parallel on the previous load admittance $Y_L = 1 / Z_L$.

Let :

- Y_a the input admittance of this line with ℓ_1 length
- $Y_t = Y_a + Y_L$ the total admittance in $x = 0$

ℓ_1 is selected to obtain a real Y_t named R_t . Use Smith chart to give ℓ_1 and R_t at $f = 3 \text{ GHz}$.

