

TABLE 5.2 Chebyshev Transformer Design

Z_L/Z_0	$N = 2$				$N = 3$					
	$\Gamma_m = 0.05$		$\Gamma_m = 0.20$		$\Gamma_m = 0.05$			$\Gamma_m = 0.20$		
	Z_1/Z_0	Z_2/Z_0	Z_1/Z_0	Z_2/Z_0	Z_1/Z_0	Z_2/Z_0	Z_3/Z_0	Z_1/Z_0	Z_2/Z_0	Z_3/Z_0
1.0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
1.5	1.1347	1.3219	1.2247	1.2247	1.1029	1.2247	1.3601	1.2247	1.2247	1.2247
2.0	1.2193	1.6402	1.3161	1.5197	1.1475	1.4142	1.7429	1.2855	1.4142	1.5558
3.0	1.3494	2.2232	1.4565	2.0598	1.2171	1.7321	2.4649	1.3743	1.7321	2.1829
4.0	1.4500	2.7585	1.5651	2.5558	1.2662	2.0000	3.1591	1.4333	2.0000	2.7908
6.0	1.6047	3.7389	1.7321	3.4641	1.3383	2.4495	4.4833	1.5193	2.4495	3.9492
8.0	1.7244	4.6393	1.8612	4.2983	1.3944	2.8284	5.7372	1.5766	2.8284	5.0742
10.0	1.8233	5.4845	1.9680	5.0813	1.4385	3.1623	6.9517	1.6415	3.1623	6.0920

$N = 4$

Z_L/Z_0	$\Gamma_m = 0.05$				$\Gamma_m = 0.20$			
	Z_1/Z_0	Z_2/Z_0	Z_3/Z_0	Z_4/Z_0	Z_1/Z_0	Z_2/Z_0	Z_3/Z_0	Z_4/Z_0
1.0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
1.5	1.0892	1.1742	1.2775	1.3772	1.2247	1.2247	1.2247	1.2247
2.0	1.1201	1.2979	1.5409	1.7855	1.2727	1.3634	1.4669	1.5715
3.0	1.1586	1.4876	2.0167	2.5893	1.4879	1.5819	1.8965	2.0163
4.0	1.1906	1.6414	2.4369	3.3597	1.3692	1.7490	2.2870	2.9214
6.0	1.2290	1.8773	3.1961	4.8820	1.4415	2.0231	2.9657	4.1623
8.0	1.2583	2.0657	3.8728	6.3578	1.4914	2.2428	3.5670	5.3641
10.0	1.2832	2.2268	4.4907	7.7930	1.5163	2.4210	4.1305	6.5950

Equating similar terms in $\cos n\theta$ gives the following results:

$$\begin{aligned}\cos 3\theta: \quad 2\Gamma_0 &= A \sec^3 \theta_m, \\ \Gamma_0 &= 0.0698; \\ \cos \theta: \quad 2\Gamma_1 &= 3A(\sec^3 \theta_m - \sec \theta_m), \\ \Gamma_1 &= 0.1037.\end{aligned}$$

From symmetry we also have that

$$\begin{aligned}\Gamma_3 &= \Gamma_0 = 0.0698, \\ \Gamma_2 &= \Gamma_1 = 0.1037.\end{aligned}$$

Then the characteristic impedances are:

$$\begin{aligned}n = 0: \quad \ln Z_1 &= \ln Z_0 + 2\Gamma_0 \\ &= \ln 50 + 2(0.0698) = 4.051 \\ Z_1 &= 57.5 \, \Omega; \\ n = 1: \quad \ln Z_2 &= \ln Z_1 + 2\Gamma_1 \\ &= \ln 57.5 + 2(0.1037) = 4.259 \\ Z_2 &= 70.7 \, \Omega; \\ n = 2: \quad \ln Z_3 &= \ln Z_2 + 2\Gamma_2 \\ &= \ln 70.7 + 2(0.1037) = 4.466 \\ Z_3 &= 87.0 \, \Omega.\end{aligned}$$