## **Antennas**

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### **Exercise 1**

The far field of a short dipole is described by the following formulas (in spherical coordinates):

$$E_{g} = j\eta \frac{\beta}{4\pi} I_{0} dz \frac{e^{-j\beta r}}{r} \sin \theta$$

$$H_{\varphi} = j \frac{\beta}{4\pi} I_0 dz \frac{e^{-j\beta r}}{r} \sin \theta$$

- a) Plot the radiation pattern in a plane perpendicular to the antenna and passing through its center.
- b) Plot the radiation pattern in a plane containing the antenna itself.
- c) Calculate the directivity of the short dipole.
- d) Calculate the radiation resistance of the short dipole. Is there any difference with respect to the input resistance?

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### **Exercise 2**

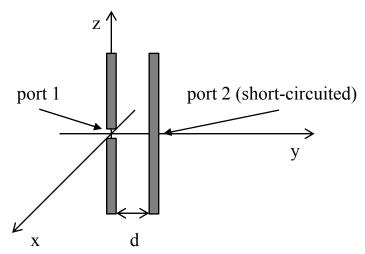
- a) Define and explain the linear polarization of the electromagnetic field. Give an example of a source emitting a linearly polarized field.
- b) Define and explain the circular polarization of the electromagnetic field. Give an example of a source emitting a circularly polarized field.
- c) Define and explain the elliptical polarization of the electromagnetic field.
- d) Starting from Maxwell's equations, prove that if the electric field is circularly polarized the magnetic field is circularly polarized, as well.

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### Exercise 3

Let us consider an array composed of 2 half-wave radiators (their separation is d=0.2  $\lambda$ ).



Their impedance matrix reads as:

$$Z = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} = \begin{bmatrix} 73 + j42 & 50 - j20 \\ 50 - j20 & 73 + j42 \end{bmatrix}$$

- a) Obtain the array complex composition factor.
- b) Calculate the maximum and minimum directions of the complex composition factor (if there is any).
- c) Calculate the null directions of the complex composition factor (if there is any).
- d) Plot the radiation pattern in the (x,y) plane.
- e) Plot the radiation pattern in the (y,z) plane.