

# Fundamentals on coherent optics: linear propagation in optical waveguides

## exercice 4 : correction

$$1) a, \quad N_g = \frac{L}{t_g} \text{ and } v_g = \frac{c}{N_g} \Rightarrow \frac{L}{t_g} = \frac{c}{N_g} \Rightarrow \underline{\underline{t_g = \frac{L}{c} N_g}}$$

$$b) \quad \mathcal{E} = \left| \frac{dt_g}{dL} \right| \Delta L$$

$$2) \quad D_m = \frac{\mathcal{E}}{\Delta L L} = \frac{1}{\Delta L L} \frac{dt_g}{dL} \Delta L = \frac{1}{L} \frac{d}{dL} \left( \frac{L}{c} N_g \right) = \frac{1}{c} \frac{dN_g}{dL}$$

$$a \quad \frac{dN_g}{dL} = \frac{d}{dL} \left( m - L \frac{dm}{dL} \right) = \frac{dm}{dL} - L \frac{d^2 m}{dL^2} - 1 \times \frac{dm}{dL} = -L \frac{d^2 m}{dL^2}$$

$$\text{thus } D_m = -\frac{1}{c} \frac{d^2 m}{dL^2}$$

$$3) \quad D_m = -\frac{1}{c} \frac{d^2 m_1}{dL^2}$$

$$\frac{dm_1}{dL} = -K A_1 e^{-LK}$$

$$\frac{d^2 m_1}{dL^2} = +K^2 A_1 e^{-LK}$$

$$\text{AN: } D_m = -\frac{0,8 \cdot 10^{-6}}{3 \cdot 10^8} \times (1,63 \cdot 10^6)^2 \times 0,0402 e^{-(0,85 \times 1,63)} \quad 4/4$$

$$= -7,6 \cdot 10^{-5} \text{ ps/(mm.km)} = \underline{\underline{-76 \text{ ps/(mm.km)}}}$$

$$4) \quad D_c = D_m + D_g \quad \text{et } |D_c| = \frac{181}{0,01 \times 100} = \frac{200}{0,01 \times 100} = 200 \text{ ps/(mm.km)}$$

$$\text{if } D_c = -200 \text{ ps/(mm.km)} \rightarrow D_g = \underline{\underline{-184 \text{ ps/(mm.km)}}}$$

$$\text{if } D_c = +200 \text{ ps/(mm.km)} \rightarrow D_g = \underline{\underline{+276 \text{ ps/(mm.km)}}}$$