

### **Exercise 1 : propagation of LP modes in step index fibers**

**Data and curves likely to be used in this exercise are given at the end .**

Step index fibers are constituted of a cylindrical core (refractive index  $n_1(\lambda)$  ), surrounded by a cladding (refractive index  $n_2(\lambda)$ ). Most of the time, the cladding is made of pure silica and the core is made of silica doped with germanium.

- 1/ a- what is the meaning of the expression "step index" ?
- b- what is the role of germanium in the core ?
- c- in what range of wavelengths are optical fibers used for telecommunication systems? Why ?

A manufacturer of silica fibers receives an order for a step index fiber which must fulfill the three following conditions:

- c 1 : the numerical aperture, which is assumed to be independent of the wavelength, must be equal to  $NA = 0.12$  ;
- c 2 : the fiber must be single mode @  $\lambda = 800$  nm ;
- c 3 : the fiber must be able to guide at least two LP modes @  $\lambda = 750$  nm

This manufacturer has 5 different fibers described in the following table:

	Fiber 1	Fiber 2	Fiber 3	Fiber 4	Fiber 5
index $n_1$ (@ 800 nm)	1.456	1.456	1.458	1.458	1.46
Core diameter ( $\mu\text{m}$ )	5	6	5	6	5

- 2/ a- verify that the weak guidance approximation can be used for these fibers. What kind of transverse modes can be considered in this case ?

- b- what are the two fibers which fulfill the condition c1?
- c- determine the limit values of the diameter of the core (maximal value and minimal value) imposed by the conditions c 2 and c 3. Deduce that the Fiber 3 only fulfills all the conditions required by the customer.

- 3/ A blue light beam from an argon laser emitting @  $\lambda_A = 457$  nm is launched in a piece of Fiber 3.
  - a- what are the LP modes able to propagate in the fiber at this wavelength ?
  - b- sketch a schematic representation of the energy distribution in each of these modes;
  - c- with any injection conditions, what can we observe on a screen set in front of the output face of the fiber ?
  - d- Fibre 3 is spliced to a fiber  $F_M$ , single mode @  $\lambda_A$ , and one measures the power at the output of this second fiber. What do we note if we handle the Fiber 3 ? Justify your answer. What do we note if we handle the Fiber  $F_M$ , without touching Fiber 3 ? Justify your answer.

- 4/ We now work with the Fibre 3 only (Fiber  $F_M$  is removed), @  $\lambda_T = 800$  nm.

- a- Using the provided information, evaluate the propagation constant  $\beta$  of the fundamental LP mode @  $\lambda_T$ .
- b- deduce the phase velocity of a continuous wave carried by this fundamental mode.
- c- why is the velocity of a pulse propagating in the fiber lower than this phase velocity ?

5/ In fact, the core of the fiber is elliptical, the axis of the ellipse being oriented along two perpendicular directions x and y. The modes  $HE_{11x}$  and  $HE_{11y}$  composing the  $LP_{01}$  mode, respectively polarized along x and y, are no longer degenerated.

- What does this expression means : " the modes  $HE_{11x}$  and  $HE_{11y}$  are no longer degenerated " ?
- At the wavelength  $\lambda_T$ , the effective indices of the two modes are  $n_{ex}=1.45549$  for the  $HE_{11x}$  mode and  $n_{ey}=1.45551$  for the  $HE_{11y}$  mode. Show that, at this wavelength, the two modes in phase periodically along their propagation, every 4 cm (= spatial period).
- What precaution should we take to ensure that a linearly polarized wave, launched at the input of a few meter long piece of fiber, remains linearly polarized at the output ?

### Data and curves likely to be useful for the exercise

$\pi=3,14159$        $V = k_0 \cdot a \cdot NA$  is the normalized spatial frequency

Relative index difference :  $\Delta = \frac{n_1^2 - n_2^2}{2 \cdot n_1^2}$

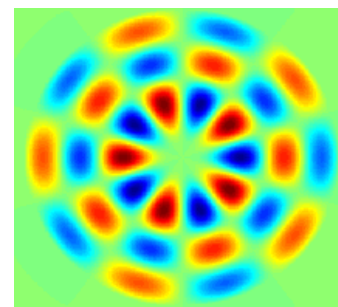
Group velocity :  $v_g = \frac{d\omega}{d\beta}$

Group index :  $n_g = n_e - \lambda \frac{dn_e}{d\lambda}$

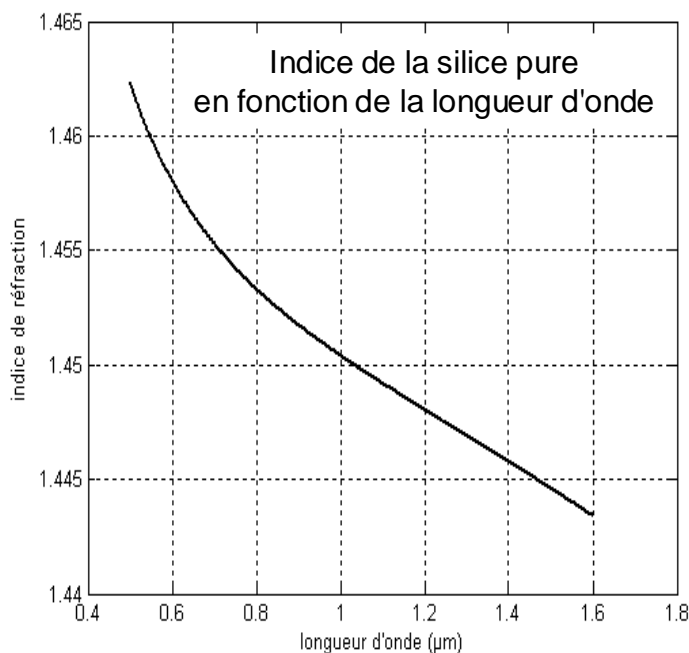
Normalized propagation constant of a given mode :  $B = \frac{\beta^2 - k_0^2 \cdot n_2^2}{k_0^2 \cdot (n_1^2 - n_2^2)}$  ( $\beta$  is the propagation constant of the mode)

Fonction →	$J_0(x)$	$J_1(x)$	$J_2(x)$	$J_3(x)$	$J_4(x)$
First zero for x =	2,405	0	0	0	0
Second zero for x =	5,52	3,83	5,14	6,38	7,59
Third zero for x =	8,65	7,01	8,42	9,76	11,06

*First zeros of the first Bessel functions of first order (including the zero at the origin if there is)*



*Distribution of the linearly polarized field in the  $LP_{5,3}$  mode :*



Curve of  $n_{sil} = f(\lambda)$  where  $n_{sil}$  is the refractive index of the pure silica

Curves  $B=f(V)$  for the first LP modes (modes of lowest orders), where  $V$  is the normalized spatial frequency, and  $B = \frac{\beta^2 - k_0^2 n_2^2}{k_0^2 (n_1^2 - n_2^2)}$ ,  $\beta$  being the propagation constant of the considered mode.

