

CHAPTER 6

POWER COUPLING AT FIBERS CONNECTIONS

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Introduction

Introduction

Connections between fibers will induce losses and power coupling between transmitted modes

- Need to identify coupling conditions
- Model of power coupling between fiber modes at connections

Aim of the chapter 6

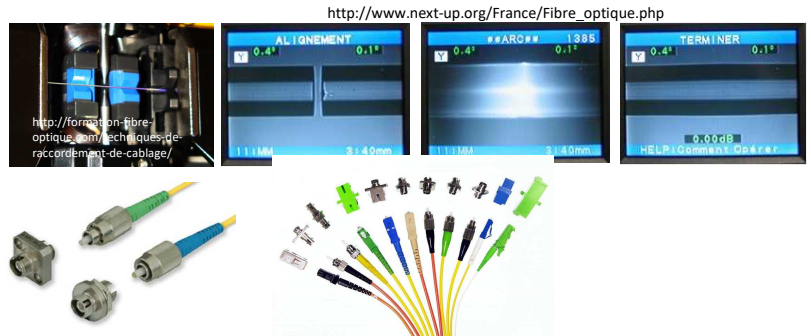
- Connections geometric defects definition
- Power transfert between optical fibers
- Connection losses in singlemode fibers (gaussian mode approximation)
- Modal coupling at misaligned multimode fibers connections

Fiber connections

- Aims
 - Increasing the length of a fiber link
 - Allowing fiber network flexibility
 - Low loss
 - Reliability

- Technologies

- Permanent link :
Electrical arc fusion splices



- Non-permanent link :
Fiber connectors

Linear propagation in optical fibers

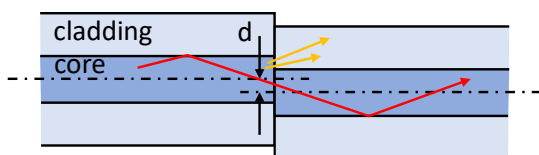
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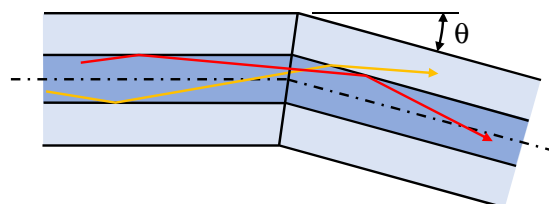
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Fiber connections loss causes (1)

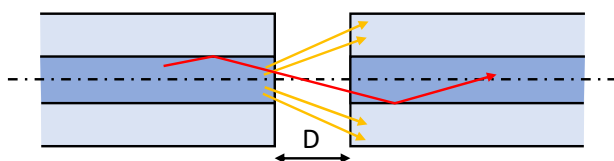
- Mechanical misalignments
 - Transversal offset d



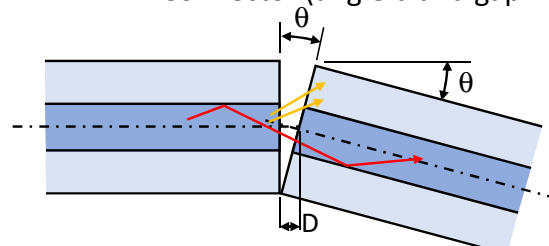
- Angular offset
 - Fusion splice (angle θ only)



- Longitudinal gap D



- Connector (angle θ and gap D)



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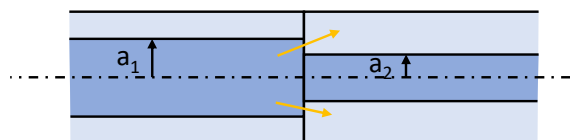
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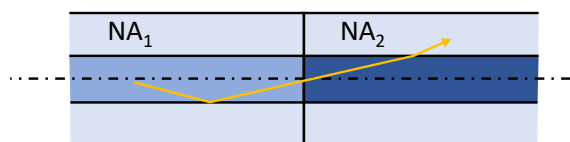
Fiber connections loss causes (2)

• Opto-geometrical mismatches

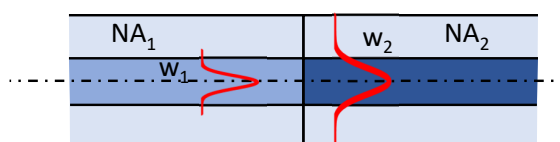
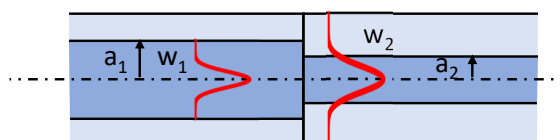
- Core size mismatch
(Multimode fiber)



Numerical Aperture mismatch (Multimode fiber)



- Mode field diameter mismatch
(Singlemode fiber)



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Power flow in optical fiber (1)

• Complex fields

$$\vec{\mathcal{E}}(x, y, z, t) = \vec{E}(x, y)e^{j(\omega t - \beta z)} = \vec{E}(x, y)e^{j\phi(z, t)}$$

$$\vec{\mathcal{H}}(x, y, z, t) = \vec{H}(x, y)e^{j(\omega t - \beta z)} = \vec{H}(x, y)e^{j\phi(z, t)}$$

• Poynting vector

$$\vec{S} = \text{Re}(\vec{\mathcal{E}}) \wedge \text{Re}(\vec{\mathcal{H}}) = \frac{1}{2}(\vec{\mathcal{E}} + \vec{\mathcal{E}}^*) \wedge \frac{1}{2}(\vec{\mathcal{H}} + \vec{\mathcal{H}}^*)$$

$$\vec{S} = \frac{1}{4}(\vec{E} \wedge \vec{H}^* + \vec{E}^* \wedge \vec{H} + \vec{E} \wedge \vec{H}e^{j2\phi(z, t)} + \vec{E}^* \wedge \vec{H}^*e^{-j2\phi(z, t)})$$

• Time averaged Poynting vector

$$\langle \vec{S} \rangle = \frac{1}{T} \int_0^T \vec{S} dt = \frac{1}{4}(\vec{E} \wedge \vec{H}^* + \vec{E}^* \wedge \vec{H}) = \frac{1}{2} \text{Re}(\underbrace{\vec{E}(x, y)}_{V m^{-1}} \wedge \underbrace{\vec{H}^*(x, y)}_{A m^{-1}})$$

$W m^{-2}$ Surfacic power density

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Power flow in optical fiber (2)

- Power flow across the fiber section



$$\langle \vec{S} \rangle = \begin{pmatrix} S_r \\ S_\theta \\ S_z \end{pmatrix}$$

The mean guided power

$$\bar{P} = \iint_{-\infty}^{+\infty} \langle \vec{S} \rangle \cdot \vec{ds} = \iint_{-\infty}^{+\infty} S_z dx dy = \iint_{-\infty}^{+\infty} \frac{n}{2} \sqrt{\frac{\epsilon_0}{\mu_0}} |E(x, y)|^2 dx dy$$

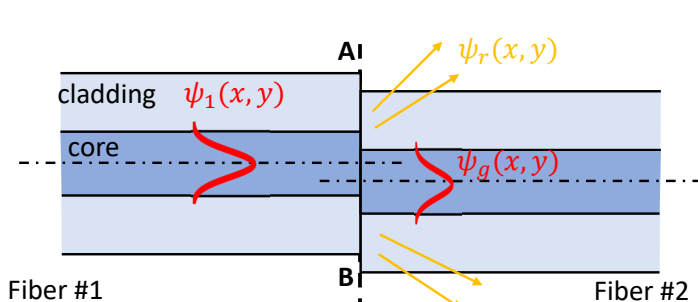
We define $|\psi(x, y)|^2 = S_z = \frac{n}{2} \sqrt{\frac{\epsilon_0}{\mu_0}} |E(x, y)|^2$

$$\bar{P} = \iint_{-\infty}^{+\infty} |\psi(x, y)|^2 dx dy$$

Fields overlap integral (1)

- Fields at the connection (plane AB)

- Incident optical wave field : $\psi_1(x, y)$ carrying a mean power $P_1 = \iint_{-\infty}^{+\infty} |\psi_1(x, y)|^2 dx dy$
- Output mode field : $\psi_2(x, y)$ with unknown amplitude and power
- Guided output field : $\psi_g(x, y) = \epsilon \psi_2(x, y)$ carrying a power $P_g = |\epsilon|^2 \iint_{-\infty}^{+\infty} |\psi_2(x, y)|^2 dx dy$
- Radiative (unguided) field : $\psi_r(x, y)$ carrying a mean power $P_r = \iint_{-\infty}^{+\infty} |\psi_r(x, y)|^2 dx dy$



In AB plane

$$\psi_1(x, y) = \psi_g(x, y) + \psi_r(x, y)$$

$$= \epsilon \psi_2(x, y) + \psi_r(x, y) \quad (\text{Eqn 1})$$

Fields overlap integral (2)

• Energy conservation

- The total output power is equal to the input power : $P_{output} = P_1 = P_g + P_r$

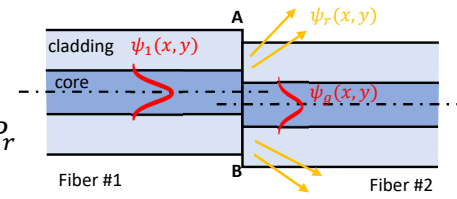
$$\iint_{-\infty}^{+\infty} |\psi_1(x, y)|^2 dx dy = |\varepsilon|^2 \iint_{-\infty}^{+\infty} |\psi_2(x, y)|^2 dx dy + \iint_{-\infty}^{+\infty} |\psi_r(x, y)|^2 dx dy$$

- From equation 1 $\psi_1(x, y) = \psi_g(x, y) + \psi_r(x, y) = \varepsilon \psi_2(x, y) + \psi_r(x, y)$

$$\begin{aligned} \iint_{-\infty}^{+\infty} |\psi_1(x, y)|^2 dx dy &= \iint_{-\infty}^{+\infty} |\varepsilon \psi_2(x, y) + \psi_r(x, y)|^2 dx dy \\ &= |\varepsilon|^2 \iint_{-\infty}^{+\infty} |\psi_2(x, y)|^2 dx dy + \iint_{-\infty}^{+\infty} |\psi_r(x, y)|^2 dx dy + \underbrace{\varepsilon \iint_{-\infty}^{+\infty} \psi_2(x, y) \psi_r^*(x, y) dx dy + \varepsilon^* \iint_{-\infty}^{+\infty} \psi_2^*(x, y) \psi_r(x, y) dx dy}_{=0} \end{aligned}$$

$$\Leftrightarrow \iint_{-\infty}^{+\infty} \psi_2(x, y) \psi_r^*(x, y) dx dy = 0$$

$\Leftrightarrow \psi_2(x, y)$ and $\psi_r(x, y)$ are orthogonal fields
Guided and radiative modes are orthogonal



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Fields overlap integral (3)

• Power transfer

- Coupling power coefficient definition

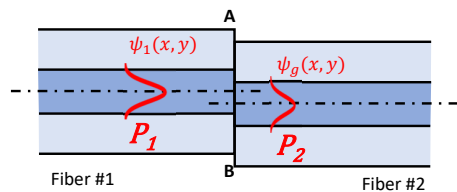
$$\alpha^2 = \frac{P_g}{P_1} = \frac{P_2}{P_1} = \frac{|\varepsilon|^2 \iint_{-\infty}^{+\infty} |\psi_2(x, y)|^2 dx dy}{\iint_{-\infty}^{+\infty} |\psi_1(x, y)|^2 dx dy}$$

- Value of ε

Multiplying by $\psi_2^*(x, y)$ and integrating eqn. 1 $\psi_1(x, y) = \varepsilon \psi_2(x, y) + \psi_r(x, y)$

$$\begin{aligned} \Leftrightarrow \iint_{-\infty}^{+\infty} \psi_1(x, y) \psi_2^*(x, y) dx dy &= \varepsilon \iint_{-\infty}^{+\infty} |\psi_2(x, y)|^2 dx dy + \underbrace{\iint_{-\infty}^{+\infty} \psi_r(x, y) \psi_2^*(x, y) dx dy}_{=0} \\ \Leftrightarrow \varepsilon &= \frac{\iint_{-\infty}^{+\infty} \psi_1(x, y) \psi_2^*(x, y) dx dy}{\iint_{-\infty}^{+\infty} |\psi_2(x, y)|^2 dx dy} \end{aligned}$$

By introducing this expression in Eqn(2)
we get the final expression of α^2



Eqn(2)

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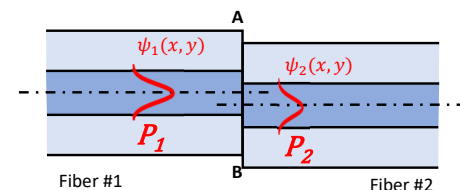
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Fields overlap integral (4)

• Power transfer

- Coupling power coefficient – Fields overlap integral



$$\alpha^2 = \frac{P_2}{P_1} = \frac{\left| \iint_{-\infty}^{+\infty} \psi_1(x, y) \psi_2^*(x, y) dx dy \right|^2}{\iint_{-\infty}^{+\infty} |\psi_1(x, y)|^2 dx dy \iint_{-\infty}^{+\infty} |\psi_2(x, y)|^2 dx dy}$$

**Fields
overlap integral**

Power normalization
terms

Fields are expressed in the plane AB and in the same coordinates axes

For normalized fields

$$\iint_{-\infty}^{+\infty} |\psi_1(x, y)|^2 dx dy = 1 \quad \text{and} \quad \iint_{-\infty}^{+\infty} |\psi_2(x, y)|^2 dx dy = 1$$

$$\alpha^2 = \frac{P_2}{P_1} = \left| \iint_{-\infty}^{+\infty} \psi_1(x, y) \psi_2^*(x, y) dx dy \right|^2$$

**Normalized fields
overlap integral**

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Fields overlap integral (5)

• Power transfer

- Between fibers

- Identical singlemode fibers :

mode of fiber #1 : $\psi_1(x, y)$

with (x,y) coordinates of the fiber #1

mode of fiber #2 : $\psi_2(x', y') = \psi_1(x', y')$

with (x',y') coordinates of the fiber #2

- Non – identical singlemode fibers

mode of fiber #1 : $\psi_1(x, y)$

mode of fiber #2 : $\psi_2(x', y')$

- Multimodes fibers

mode #i of fiber #1 : $\psi_1(x, y) = \psi_i(x, y)$

mode #j of fiber #2 : $\psi_2(x', y') = \psi_j(x', y')$

- At fiber input face

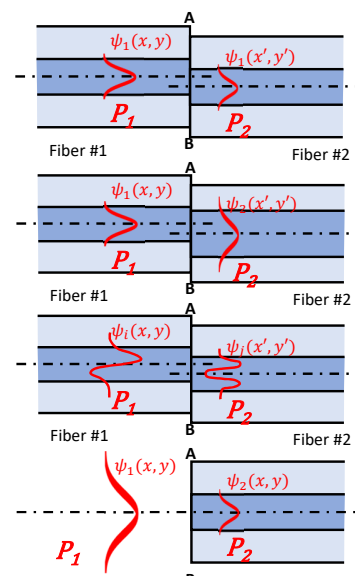
- Power injection in fiber

input field : $\psi_1(x, y)$

with (x,y) coordinates of the fiber

mode of fiber : $\psi_2(x, y) = \psi_j(x, y)$

$$P_2 = \alpha^2 P_1$$



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Fields overlap integral (6)

• Power transfer

- If $\psi_1(x, y) = \psi_2(x, y)$ then

$$\alpha^2 = 1 \Leftrightarrow P_2 = P_1 : \text{no coupling loss}$$

- If $\psi_2(x, y)$ is orthogonal to $\psi_1(x, y)$ (guided or radiative modes)

$$\alpha^2 = 0 \Leftrightarrow P_2 = 0 : \text{no coupled power to the second fiber mode } \psi_2$$

- Schwarz inequality

$$0 \leq \left| \iint_{-\infty}^{+\infty} \psi_1(x, y) \psi_2^*(x, y) dx dy \right|^2 \leq \iint_{-\infty}^{+\infty} |\psi_1(x, y)|^2 dx dy \iint_{-\infty}^{+\infty} |\psi_2(x, y)|^2 dx dy$$

$$\Leftrightarrow 0 \leq \alpha^2 \leq 1 \quad \Leftrightarrow P_2 \leq P_1$$

- Independence of propagation direction (from fiber #1 to #2 or #2 to #1)

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Connexion losses between singlemode fibers (1)

• Gaussian guided mode fields :

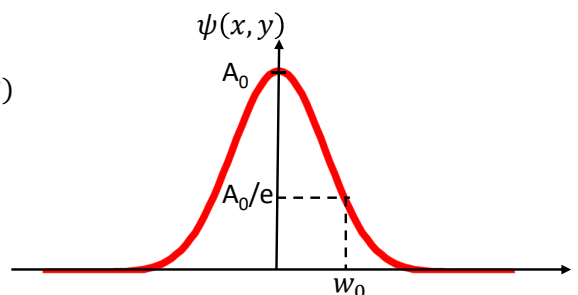
$$\psi(x, y) = A_0 e^{-\frac{x^2+y^2}{w_0^2}} = A_0 e^{-\frac{r^2}{w_0^2}}$$

w_0 is the mode field radius @ $1/e$ of the maximal amplitude ($1/e^2$ of the maximal intensity)

$$w_0 \approx a (0.65 + 1.619 V^{-\frac{3}{2}} + 2.879 V^{-6})$$

$$\text{with } V = k a \sqrt{n_1^2 - n_2^2}$$

$$\text{For } 1.2 \leq V \leq 4$$



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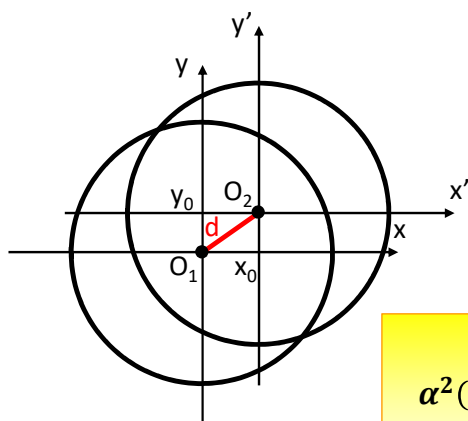
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Connexion losses between singlemode fibers (2)

• Transversal offset (1)



$$\psi_1(x, y) = \psi(x, y)$$

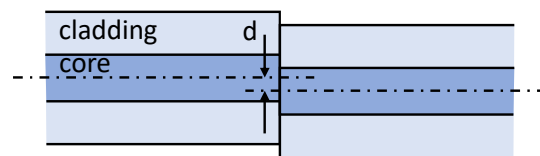
$$\psi_2(x, y) = \psi(x - x_0, y - y_0)$$

are real fields

$$d = \sqrt{x_0^2 + y_0^2}$$

$$\alpha^2 = \frac{P_2}{P_1} = \frac{\left| \iint_{-\infty}^{+\infty} \psi(x, y) \psi(x - x_0, y - y_0) dx dy \right|^2}{\iint_{-\infty}^{+\infty} |\psi(x, y)|^2 dx dy \iint_{-\infty}^{+\infty} |\psi(x - x_0, y - y_0)|^2 dx dy}$$

$$\alpha^2(x_0, y_0) = \frac{(\psi(x, y) * \psi(x, y))_{x_0, y_0}^2}{(\psi(x, y) * \psi(x, y))_{0,0}^2}$$



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Connexion losses between singlemode fibers (3)

• Transversal offset (2)

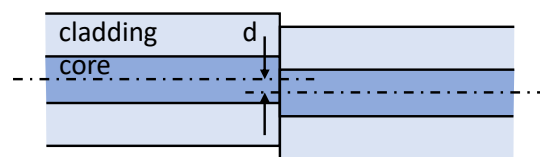
with

$$e^{-\pi x^2} \Rightarrow e^{-\pi u^2}$$

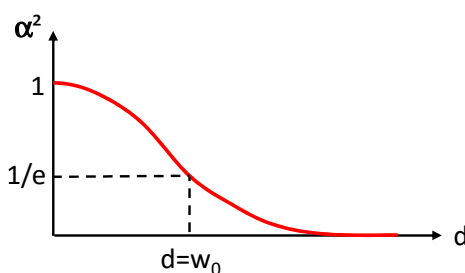
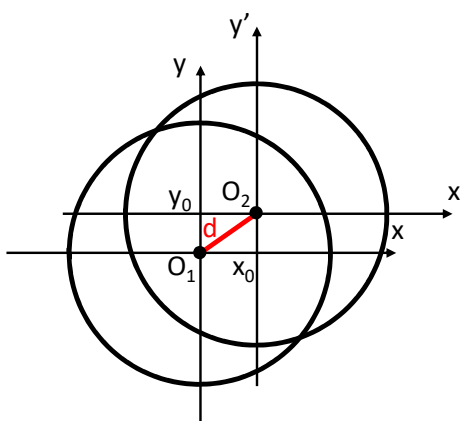
$$f(ax) \Rightarrow \frac{1}{|a|} F\left(\frac{u}{a}\right)$$

$$(\psi(x, y) * \psi(x, y))_{x_0, y_0}^2 = \frac{\pi w_0^2}{2} e^{-\frac{x_0^2 + y_0^2}{w_0^2}}$$

$$(\psi(x, y) * \psi(x, y))_{0,0}^2 = \frac{\pi w_0^2}{2}$$



$$\alpha^2(x_0, y_0) = \frac{P_2}{P_1} = e^{-\frac{x_0^2 + y_0^2}{w_0^2}} = e^{-\frac{d^2}{w_0^2}}$$



Offset $\frac{d}{w_0}$	Case $w_0 = 4.75 \mu\text{m}$	Losses (dB)
0.1	0.95 μm	0.04
0.15	1.4 μm	0.1
0.2	1.9 μm	0.17
0.3	2.85 μm	0.4
0.5	4.75 μm	1

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Connexion losses between singlemode fibers (4)

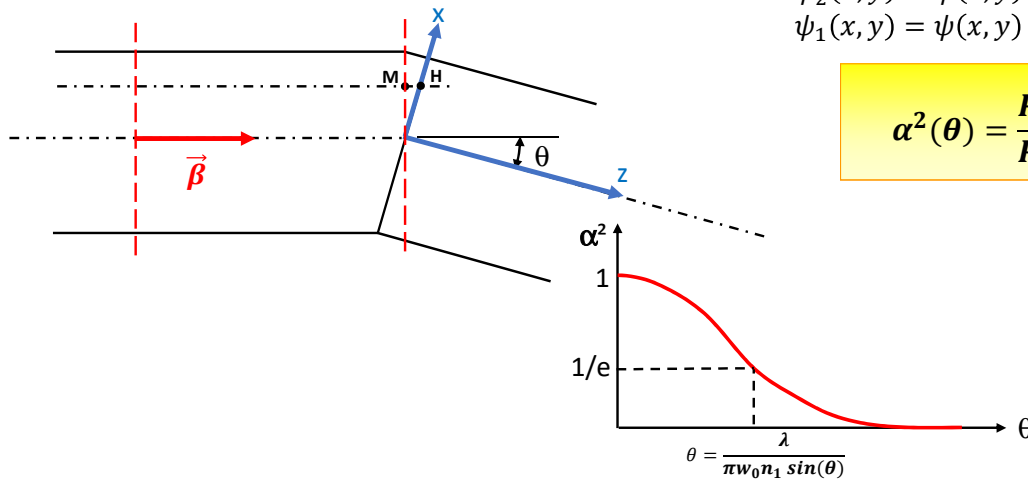
• Angular offset

In the coordinates axes of fiber #2 :

$$\psi_2(x, y) = \psi(x, y) = \psi_2^*(x, y) \text{ because is real}$$

$$\psi_1(x, y) = \psi(x, y) e^{j\beta z(x, y)} \text{ with } z(x, y) = HM$$

$$\alpha^2(\theta) = \frac{P_2}{P_1} = e^{-\left(\frac{\pi w_0 n_1 \sin(\theta)}{\lambda}\right)^2}$$



θ (deg) $w_0=4.75\mu\text{m}$ $L=1.55\mu\text{m}, n_1=1.45$	Losses (dB)
0.1	0.0025
0.2	0.01
0.5	0.06
1	0.27
2	0.92

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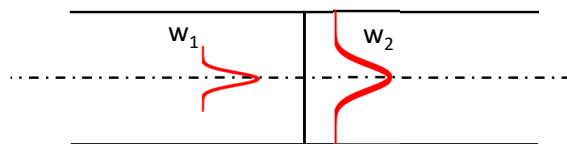
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Connexion losses between singlemode fibers (5)

• Mode field diameter mismatch



In fiber #1

$$\psi_1(x, y) = A_0 e^{-\frac{x^2+y^2}{w_1^2}}$$

In fiber #2

$$\psi_2(x, y) = A_0 e^{-\frac{x^2+y^2}{w_2^2}}$$

$$\alpha^2 = \frac{P_2}{P_1} = \left(\frac{2w_1w_2}{w_1^2 + w_2^2}\right)^2$$

$\frac{w_2}{w_1}$	Losses (dB)
1.1	0.04
1.3	0.3
1.63	1
2	2

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Connexion losses between singlemode fibers (6)

- Triple defects connection (transversal+angular+mode mismatch)

$$\alpha^2(d, \theta, w_1, w_2) = \frac{P_2}{P_1} = \left(\frac{2w_1 w_2}{w_1^2 + w_2^2} \right)^2 e^{-\left(\frac{\pi w_0 n_1 \sin(\theta)}{\lambda} \right)^2} e^{-\frac{d^2}{w_m^2}}$$

With

$$w_m^2 = \frac{w_1^2 + w_2^2}{2}$$

$$w_0^2 = \frac{2w_1^2 w_2^2}{w_1^2 + w_2^2}$$

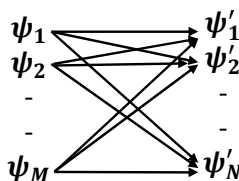
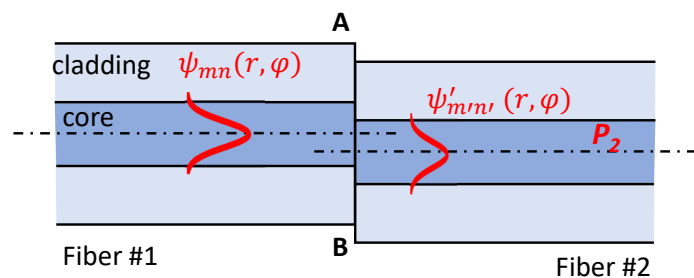
Connexion losses between multimode fibers (1)

- Power transfer at connection

- Multimode fibers connection

- M LP_{m,n} modes guided in fiber #1
 $\psi_{mn}(r, \varphi)$
- N LP_{m',n'} modes guided in fiber #2
 $\psi'_{m'n'}(r, \varphi)$

- MxN power coupling coefficients



$$(\alpha_{mn}^{m'n'})^2 = \frac{P_{m'n'}}{P_{mn}} = \left| \iint_{-\infty}^{+\infty} \psi_{mn}(r, \varphi) \psi'^*_{m'n'}(r, \varphi) r dr d\varphi \right|^2$$

$$P_2 = \sum_{j=1}^N P_{m'n'} = \sum_{i=1}^M \sum_{j=1}^N (\alpha_{mn}^{m'n'})^2 P_{mn}$$

Connexion losses between multimode fibers (3)

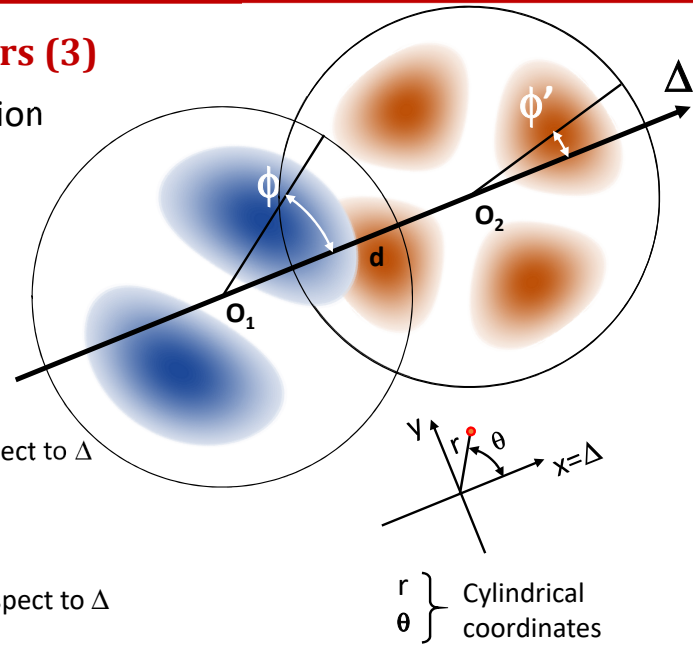
Power coupling at transversally misaligned connection

Connection description

- $d = O_1 O_2$
- Δ : axis of the transversal misalignment
- ϕ : azimuthal orientation of mode LP_{mn} (fiber #1) with respect to Δ
- ϕ' : azimuthal orientation of mode $LP_{m'n'}$ (fiber #2) with respect to Δ

$$\Psi_{mn} = R(r) \cdot \cos(m(\theta - \phi))$$

$$\Psi'_{m'n'} = R'(r) \cdot \cos(m'(\theta - \phi'))$$



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Connexion losses between multimode fibers (3)

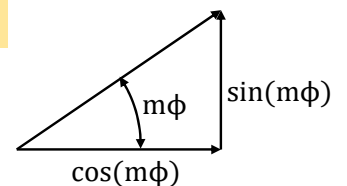
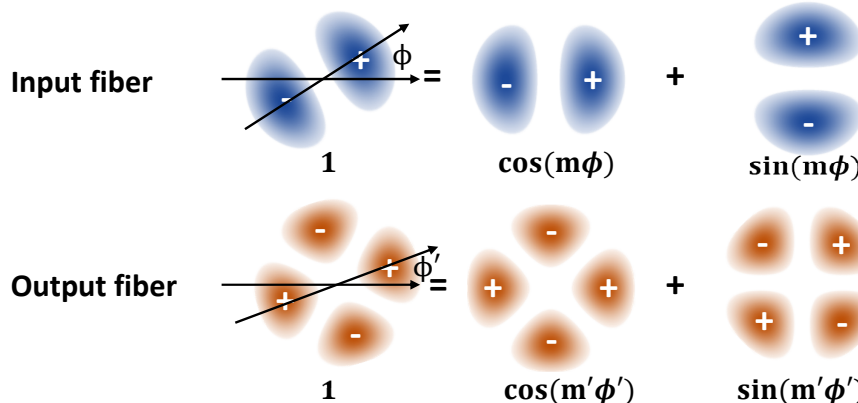
Fields decomposition

$$\Psi_{mn} = R(r) \cdot \left(\cos(m\theta) \cos(m\phi) + \sin(m\theta) \sin(m\phi) \right)$$

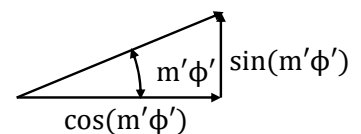
$$\Psi_{m'n'} = R'(r) \cdot \left(\cos(m'\theta) \cos(m'\phi') + \sin(m'\theta) \sin(m'\phi') \right)$$

Even modes

Odd modes



Fresnel representation



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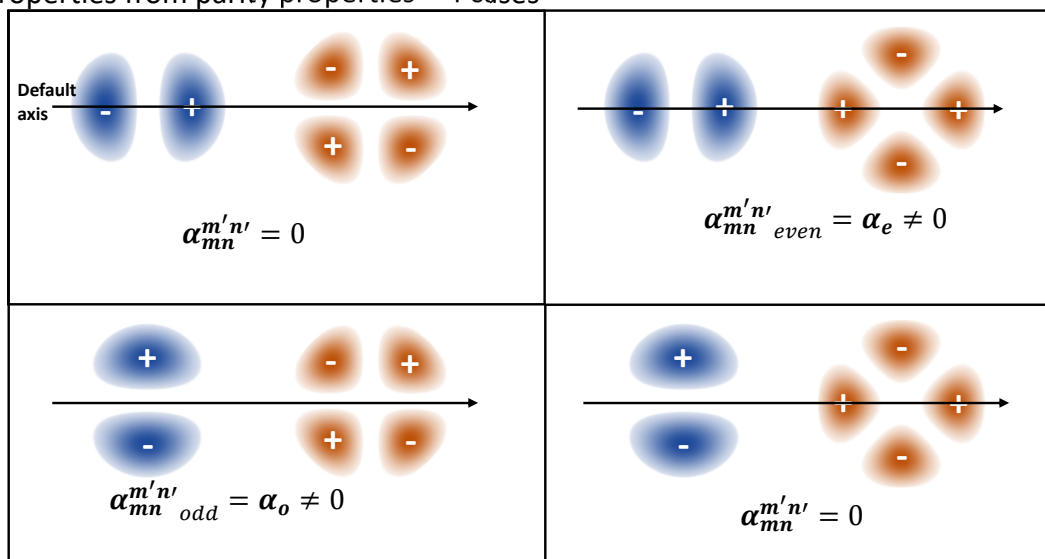
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Connexion losses between multimode fibers (4)

$$\alpha^2 = \frac{P_2}{P_1} = \left| \iint_{-\infty}^{+\infty} \psi_1(x, y) \psi_2^*(x, y) dx dy \right|^2$$

- Coupling properties from parity properties – 4 cases



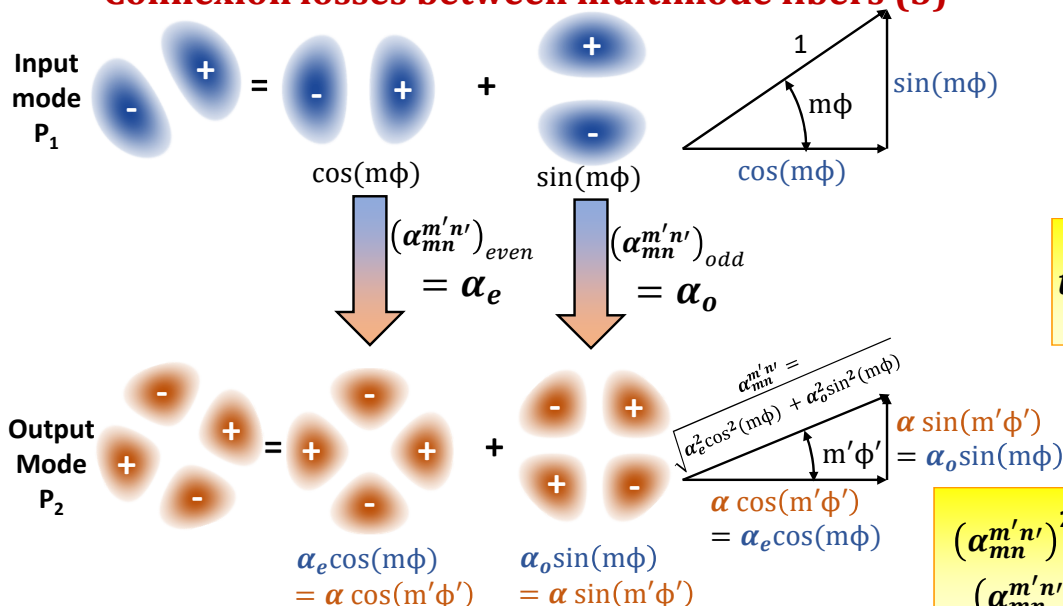
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Connexion losses between multimode fibers (5)



$$P_2 = (\alpha_{mn}^{m'n'})^2 P_1$$

$$\tan(m'\phi') = \frac{\alpha_o}{\alpha_e} \tan(m\phi)$$

The « tangents law »

$$(\alpha_{mn}^{m'n'})^2 = \alpha_e^2 \cos^2(m\phi) + \alpha_o^2 \sin^2(m\phi)$$

$$(\alpha_{mn}^{m'n'})^2 = \alpha_o^2 + (\alpha_e^2 - \alpha_o^2) \cos^2(m\phi)$$

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