

Section:

5.1

Assignment : 6

Section

5.2

30. $23^{\circ}42'48''$

$$23 + \frac{42}{60} + \frac{48}{3600}$$

$$23 + 0.7 + 0.0133$$

$$23.7133 \text{ decimal degrees}$$

33. -84.64°

$$-84^{\circ}38'24''$$

$$38 + 240$$

$$R = \text{Degree} \times \frac{\pi}{180}$$

$$= \frac{240\pi}{180} \times \frac{8}{6} \times \frac{4}{3}$$

$$= \frac{4}{3}\pi$$

43. $12^{\circ}6'36''$

$$12 + 0.1 + 0.01$$
$$= 12.11$$

$$12.11 \times \frac{\pi}{180} = \frac{12.11\pi}{180}$$

48. $-\frac{7\pi}{6}$

$$R = 0 \times \frac{\pi}{180}$$

$$\frac{180R}{\pi} = 0$$

$$\frac{180(-7\pi)}{6\pi} = 0$$

$$30(-7) = \text{Degree}$$

$$-210$$

53. 2.7

$$2.7 = 0 \times \frac{\pi}{180}$$

$$\frac{426}{\pi} = 0$$

58.

$$313^{\circ} + 360 = 673^{\circ} + \text{ve}$$

$$313 - 360 = -47^{\circ} - \text{ve}$$

69. $-\frac{7\pi}{18} + 2\pi = -\frac{7\pi}{18} + \frac{36\pi}{18} = \frac{29\pi}{18}$

72. $\theta = \frac{5\pi}{6}$ $r = 4\text{m}$

$$\text{arc length} = r \times \theta$$
$$= 4 \times \frac{5\pi}{6}$$

$$= \frac{10\pi}{3}$$

$$= 10.472$$

98. arc length: $\frac{\pi}{6}$ $r = 1.2$

$$\frac{1}{2}(1.2)^2 \frac{\pi}{6}$$

$$= \frac{1.44}{2} \times \frac{\pi}{6}$$

$$= \frac{1.44\pi}{12}$$

$$= 0.37$$

108. $82^{\circ}15'3''$

$$82 + \frac{15}{60} + \frac{3}{3600}$$

$$82 + 0.25 + 0.00083$$

$$= 82.25083$$

$$82^{\circ}15'3''$$

$$82.25083$$

(a) 7.74917

(b) $180 - 82.250833 = 97.749$

13.

(a) $\sin \theta = \frac{6}{10} = \frac{3}{5}$

$$\cos \theta = \frac{8}{10} = \frac{4}{5}$$

$$\tan \theta = \frac{6}{8} = \frac{3}{4}$$

$$\operatorname{cosec} = \frac{5}{3}$$

$$\sec = \frac{5}{4}$$

$$\cot = \frac{4}{3}$$

(b) $\sin \theta = \frac{20}{12} = \frac{5}{3}$

$$\cos \theta = \frac{16}{20} = \frac{4}{5}$$

$$\tan \theta = \frac{12}{16} = \frac{3}{4}$$

$$\operatorname{cosec} \theta = \frac{3}{5}$$

$$\sec \theta = \frac{5}{4}$$

$$\cot = \frac{4}{3}$$

16. $15^2 = 8^2 + x^2$

$$225 - 64 = x^2$$

$$\sqrt{161} = x^2$$

$$\sin \theta = \frac{15}{\sqrt{161}}$$

$$\cos \theta = \frac{8}{\sqrt{161}}$$

$$\tan \theta = \frac{15}{8}$$

$$\operatorname{cosec} = \frac{\sqrt{161}}{15}$$

$$\sec = \frac{\sqrt{161}}{8}$$

$$\cot = \frac{8}{15}$$

$$20. x^2 = 9 + 225$$

$$x^2 = 234$$

$$x = \sqrt{234}$$

$$23. \tan \theta = \frac{4}{7} = \frac{p}{q}$$

$$16 + 49$$

$$= \sqrt{55} = h$$

$$\sin \theta = \frac{4}{\sqrt{55}}$$

$$\cos \theta = \frac{7}{\sqrt{55}}$$

$$\sec \theta = \frac{\sqrt{55}}{7}$$

$$\csc \theta = \frac{\sqrt{55}}{4}$$

$$\cot \theta = \frac{7}{4}$$

$$30. \cot = \frac{\sqrt{3}}{2} = \frac{B}{P}$$

$$(\sqrt{3})^2 + 4$$

$$7 = 3 + 4$$

$$7 = x^2 \quad x = \sqrt{7}$$

$$\cos \theta = \frac{B}{H} = \frac{\sqrt{3}}{\sqrt{7}}$$

45.

$$\tan \theta = \frac{11}{60} = \frac{p}{q}$$

$$= 121 + 3600$$

$$H^2 = 3721$$

$$H = 61$$

$$\sec = \frac{1}{\cos} = \boxed{\frac{61}{60}}$$

$$\cos = \frac{60}{61}$$

55.

$$\tan 75^\circ = 2 + \sqrt{3}$$

$$15 + 180 = 255$$

$$\tan 255^\circ = 2 + \sqrt{3}$$

68.



$$\cos 58^\circ = \frac{B}{10}$$

$$\cos 58^\circ = \sin 32^\circ$$

$$10 \times \cos 58^\circ = B$$

$$= 8.48 \text{ ft}$$

76.

$$\cos \frac{\pi}{12} = \frac{\sqrt{2} + \sqrt{6}}{4}$$

$$\frac{180}{12} \quad \frac{90}{6} = \frac{90}{6}$$

$$a. \sin \frac{5\pi}{12}$$

$$= \sin \frac{\pi}{12} = 1 - \left(\frac{\sqrt{2} + \sqrt{6}}{4} \right)^2$$

$$= 1 - \frac{2 + 6 + 4\sqrt{3}}{16}$$

$$= 1 - \frac{8 + 4\sqrt{3}}{16}$$

$$= 1 - \frac{2 + \sqrt{3}}{4}$$

$$= \frac{4 - 2 + \sqrt{3}}{4}$$

$$= \frac{2 + \sqrt{3}}{4}$$

$$\sin \frac{\pi}{12} = \frac{2 + \sqrt{3}}{4}$$

$$\sin \frac{\pi}{12} = \sqrt{\frac{2 + \sqrt{3}}{4}}$$

$$\sin \frac{5\pi}{12} = 5 \sqrt{\frac{2 + \sqrt{3}}{4}}$$

31. SOH CAH TOA

	Sin	Cos	Tan	Csc	Sec	Cot
30	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{3}}$	2	$\frac{2}{\sqrt{3}}$	$\sqrt{3}$
45	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$	1	$\sqrt{2}$	$\sqrt{2}$	1
60	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$	$\frac{2}{\sqrt{3}}$	2	$\frac{1}{\sqrt{3}}$

$$38. \cos^2 45^\circ + \tan^2 60^\circ$$

$$\frac{1}{2} + 3$$

$$= \frac{7}{2}$$

42.

$$\sin \theta = \frac{8}{17} = \frac{p}{H}$$

$$17^2 = x^2 + 8^2$$

$$289 = x^2 + 64$$

$$B = 15$$

$$\cos \theta = \boxed{\frac{15}{17}}$$

5.3

$$15. 5, -12$$

$$\sin \theta = \frac{-12}{13} \quad \cos \theta = \frac{5}{13} \quad \tan \theta = \frac{-12}{5}$$

$$\csc \theta = -\frac{13}{12} \quad \sec \theta = \frac{13}{5} \quad \cot \theta = -\frac{5}{12}$$

21	Sin	Cos	Tan	Csc	Sec	Cot
0	0	1	0	∞	1	∞
90°	1	0	∞	1	∞	0
180°	0	-1	0	∞	-1	∞
270°	-1	0	∞	-1	∞	0
360°	0	1	0	∞	1	∞

$$25. \frac{2\pi}{3} = \frac{\pi}{3}$$

$$31. \sin(-120) = -\frac{\sqrt{3}}{2}$$

38. $\sin \frac{\pi}{3} = \pi/3$

48. $\csc \pi \rightarrow \text{undef}(\infty)$

55. $\theta = 30^\circ \quad \phi = 150^\circ$

64. $\sqrt{11^2 + 6^2} = 12$

$x = 71$

$\cos \theta = -\frac{11}{12}, \sin \theta = -\frac{60}{71}$

70. $\sin^2 \theta + \cos^2 \theta = 1$

$\cos^2 \theta = 1 - (\frac{3}{4})^2$

$= -\frac{15}{17}$

80. $\sin(180^\circ + \theta)$
 $= -\sin \theta \text{ true}$

86. $\cos 45^\circ \cdot \sin 240^\circ \cdot \tan 135^\circ \times \csc 60^\circ$
 $= \frac{\sqrt{2}}{2} \cdot \frac{\sqrt{3}}{2} \cdot -1 \cdot \frac{\sqrt{3}}{3}$

95. $\sin 30^\circ = \frac{1}{2}$

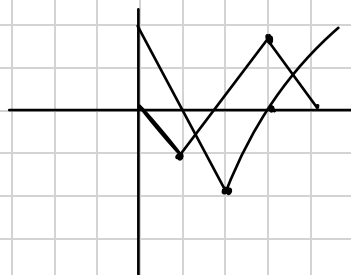
5.5

9. $-y = \sin(x)$

10. $-y = \cos(x)$

19. $-y = 5 \cos(x)$

24. $-y = 3 \sin(x)$



26. a. 6π

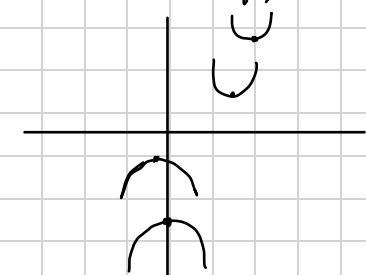
29. $-y = 4 \sin \frac{\pi}{3} x$

32. $-y = \cos(-\frac{1}{2}x)$

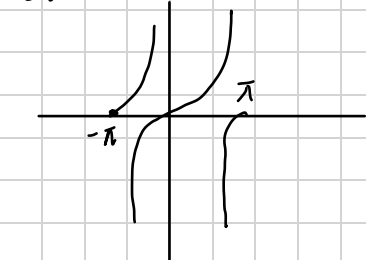


5.6

19. $-y = -\sec(x)$
 $-y = \csc(x - \frac{\pi}{4})$

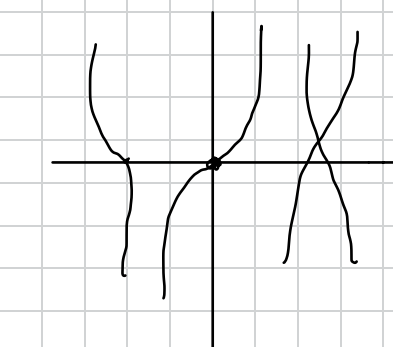


39.



43. $-y = \tanh x$

52. $-y = 5 \cot(\frac{\pi}{4}x)$



66. As $x \rightarrow 0^-$, $f(x) \rightarrow -\infty$
 $x \rightarrow 0^+$, $f(x) \rightarrow \infty$

5.7

1. $\sin^{-1}(\frac{\sqrt{2}}{2}) = \frac{\pi}{4}$

9. $\sin^{-1} \pi = \text{undefined}$

13. $\sin^{-1} \frac{\sqrt{3}}{2} + \sin^{-1} \frac{1}{2}$

$\frac{\pi}{3} + \frac{\pi}{6}$

18. $\tan^{-1}(-\sqrt{3}) = -\frac{\pi}{3}$

22. $\cos \frac{\pi}{2} = \text{undef}$

26. $\tan(-\frac{\sqrt{3}}{3}) = -\frac{\pi}{6}$

37. $2 \cos^{-1}(-\frac{\sqrt{3}}{2}) - \tan^{-1}(\frac{\sqrt{3}}{3})$
 $= 2 \cdot \frac{2\pi}{3} - \frac{\pi}{6}$

$= \frac{7\pi}{6}$

38. $\sin^{-1}(-\frac{4}{5}) = -53^\circ$
 $\theta = 180^\circ + 53^\circ$
 $= 233^\circ$