AI1103: Assignment 2

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and latex-tikz codes from

https://github.com/ASHWITHA-11008/ Assignment-2/blob/main/Assignment-2.tex

1 Problem

X(t) is a random process with a constant mean value of 2 and the autocorrelation function $R_x(\tau) = 4\left(e^{-0.2|\tau|} + 1\right)$. Let Y and Z be the random variables obtained by sampling X(t) at t=2 and t=4 respectively. Let W=Y-Z. The variance of W is

2 Solution

Let
$$t_1 = 2$$
 and $t_2 = 4$ (2.0.1)

$$\implies Y = X(t_1)$$
 (2.0.2)

$$\implies Z = X(t_2)$$
 (2.0.3)

We know,

$$\Longrightarrow R_X(\tau) = E[X(t)X(t+\tau)]$$
 (2.0.4)

$$\Longrightarrow R_X(0) = E[X^2(t)] \tag{2.0.5}$$

So,

$$\sigma_W^2 = E[X^2(t_1)] + E[X^2(t_2)] - 2E[X(t_1)X(t_2)]$$

$$= 2E[X^2(t_1)] - 2E[X(t_1)X(t_1 + 2)]$$

$$= 2R_X(0) - 2R_X(2)$$

$$= 8(e^{-0.2|0|} + 1) - 2 \times 4(e^{-0.2|2|} + 1)$$

$$= 8(2) - 2[4(0.67 + 1)]$$

$$= 2.64$$
(2.0.10)

So, option c is correct.