AI1103: Assignment 2

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and latex-tikz codes from

https://github.com/ASHWITHA-11008/ Assignment-1/blob/main/Assignment 2.tex

1 Problem

X(t) is a random process with a constant mean value of 2 and the autocorrelation function $R_x(\tau) = 4\left(e^{-0.2|\tau|} + 1\right)$. Let Y and Z be the random variables obtained by sampling X(t) at t=2 and t=4 respectively. Let W=Y-Z. The variance of W is

2 Solution

Given W = Y - Z

Variance of W

$$\sigma_W^2 = E[Y - Z]^2 - (E[Y - Z])^2$$
$$= E[Y^2] + E[Z^2] - 2E[YZ]$$

Since given mean value is constant

$$E[Y-Z] = \mu_Y - \mu_Z = 0$$

We know,

$$R_X(\tau) = E[(X)(X + \tau)]$$

 $E[X^2(t)] = R_X(0)$
 $E[X^2(2)] = E[X^2(4)] = R_X(0)$

So,

$$\sigma_W^2 = R_X(0) + R_X(0) - 2R_X(2)$$

$$= 4\left(e^{-0.2|0|} + 1\right) + 4\left(e^{-0.2|0|} + 1\right) - 2 \times 4\left(e^{-0.2|2|} + 1\right)$$

$$= 8 + 8 - 2[4(0.67 + 1)]$$

$$= 2.64$$

So, option c is correct.