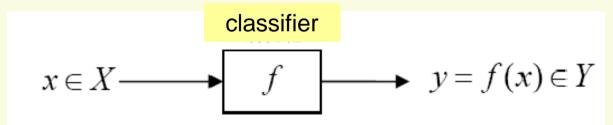
# Intro to Classification

### Definition of Classification

- A classifier is a function or an algorithm that maps every possible input (from a legal set of inputs) to a finite set of categories.
- X input space,  $x \in X$  sample from an input space.
- A typical input space is high-dimensional, for example  $x = \{x_1,...,x_d\} \in R^d$ , d > 1. We also call x a feature vector.
- $\Omega$  is a finite set of categories to which the input samples belong:  $\Omega = \{1,2,...,C\}$ .
- $w_i \in \Omega$  are called labels.

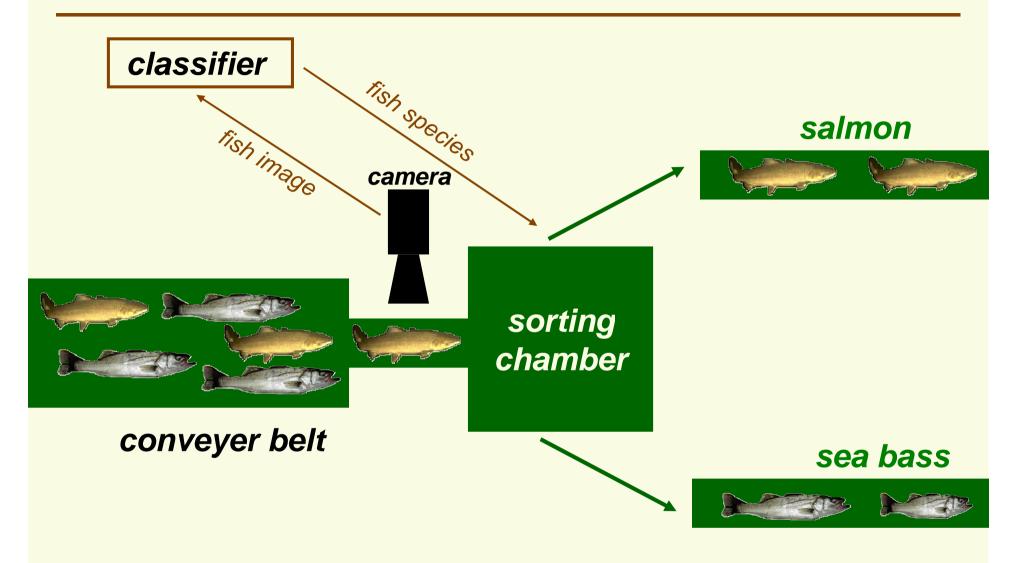
#### Definition of Classification

- Y is a finite set of decisions the output set of the classifier.
- Usually  $Y=\Omega$ , but it can also contain other decisions, such as "no decision", "reject" (doesn't belong to any category from  $\Omega$ ).
- A classifier is a function  $f: X \to Y$



Classification is also called Pattern Recognition.

# Our Toy Application: fish sorting



# How to design a PR system?

Collect data and classify by hand



Preprocess by segmenting fish from background

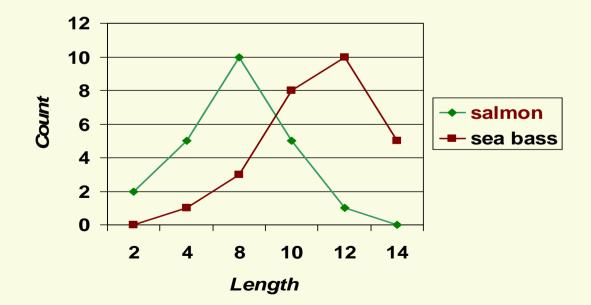


- Extract possibly discriminating features
  - length, lightness, width, number of fins, etc.
- Classifier design
  - Choose model
  - Train classifier on part of collected data (training data)
- Test classifier on the rest of collected data (test data)
  i.e. the data not used for training
  - Should classify new data (new fish images) well

# Classifier design

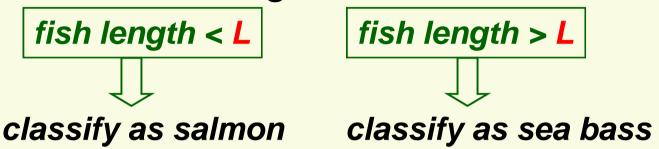
- Notice salmon tends to be shorter than sea bass
- Use fish length as the discriminating feature
- Count number of bass and salmon of each length

	2	4	8	10	12	14
bass	0	1	3	8	10	5
salmon	2	5	10	5	1	0



## Fish length as discriminating feature

Find the best length L threshold

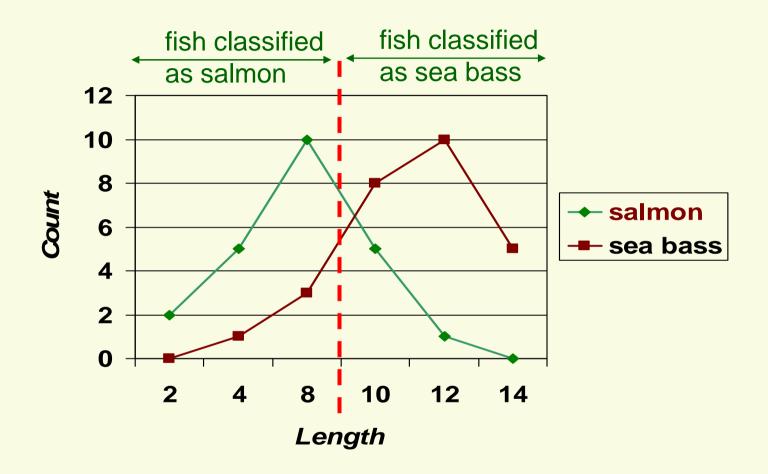


- For example, at L = 5, misclassified:
  - 1 sea bass
  - 16 salmon

	2	4	8	10	12	14	
bass	0	1	3	8	10	5	
salmon	2	5	10	5	1	0	

• Classification error (total error):  $\frac{17}{50} = 34\%$ 

## Fish Length as discriminating feature



After searching through all possible thresholds L,
 the best L= 9, and still 20% of fish is misclassified

# Next Step

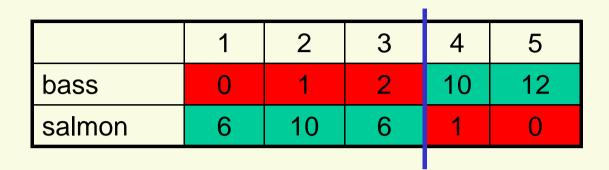
- Lesson learned:
  - Length is a poor feature alone!
- What to do?
  - Try another feature

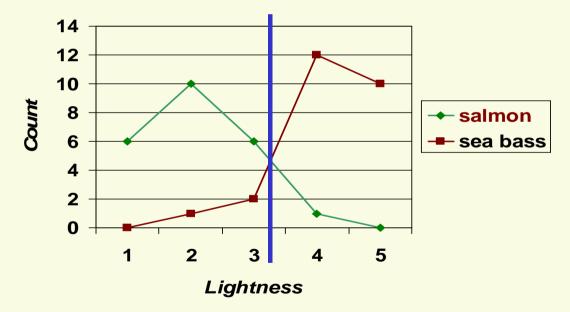




- Salmon tends to be lighter
- Try average fish lightness

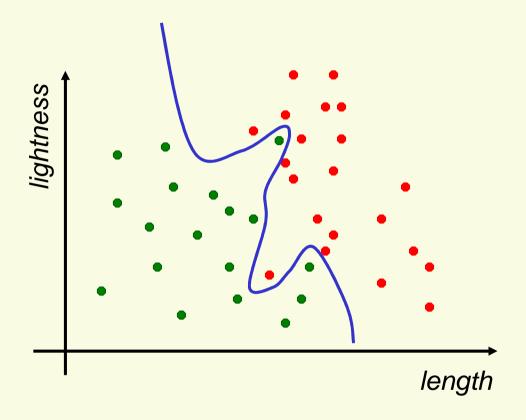
# Fish lightness as discriminating feature





 Now fish are well separated at lightness threshold of 3.5 with classification error of 8%

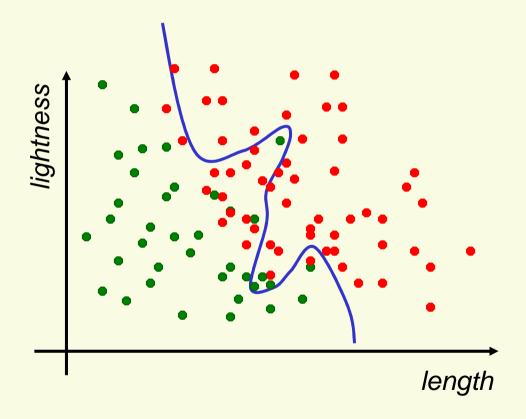
# Better decision boundary



Ideal decision boundary, 0% classification error

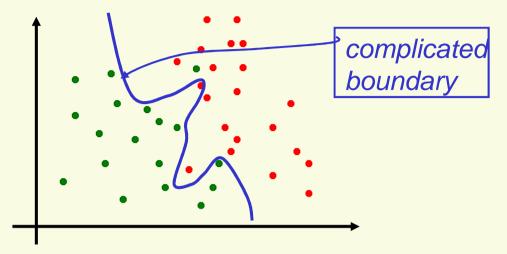
### Test Classifier on New Data

- Classifier should perform well on new data
- Test "ideal" classifier on new data: 25% error



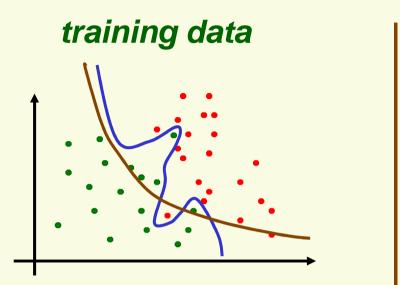
# What Went Wrong?

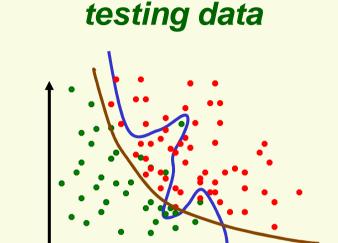
Poor generalization



- Complicated boundaries do not generalize well to the new data, they are too "tuned" to the particular training data, rather than some true model which will separate salmon from sea bass well.
  - This is called overfitting the data

### Generalization





- Simpler decision boundary does not perform ideally on the training data but generalizes better on new data
- Favor simpler classifiers

### Classification Overview

a lot is known "easier" little is known "harder"

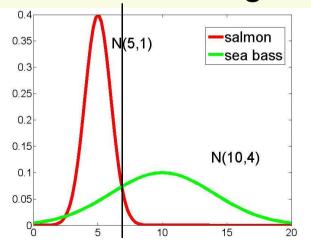
# Bayesian Decision theory

- Known probability distribution of the categories
  - never happens in real world
- Do not need training data
- Can design optimal classifier

### Example

respected fish expert says that salmon's length has distribution N(5,1) and sea bass's length

has distribution N(10,4)



a lot is known "easier" little is known

"harder"

### ML and Bayesian parameter estimation

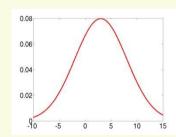
- Shape of probability distribution is known
  - Happens sometimes
- Labeled training data
  - salmon bass salmon salmon

- a lot is known "easier"
- Need to estimate parameters of probability distribution from the training data

#### Example

respected fish expert says salmon's length has distribution  $N(\mu_1, \sigma_1^2)$  and sea bass's length has distribution  $N(\mu_2, \sigma_2^2)$ 

- Need to estimate parameters  $\mu_1, \sigma_1^2, \mu_2, \sigma_2^2$
- Then can use the methods from the Bayesian decision theory



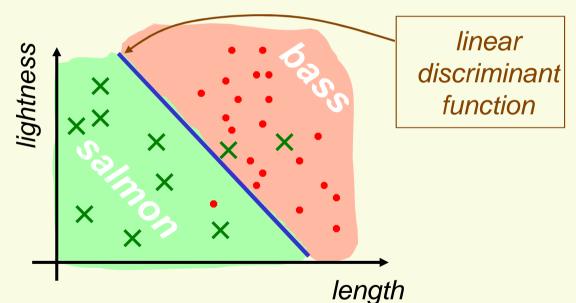
little is known "harder"

#### Linear discriminant functions and Neural Nets

 No probability distribution (no shape or parameters are known)

a lot is known

- Labeled data salmon bass salmon salmon
- The shape of discriminant functions is known



 Need to estimate parameters of the discriminant function (parameters of the line in case of linear discriminant)

little is known

#### Non-Parametric Methods

 Neither probability distribution nor discriminant function is known

a lot is known "easier"

- Happens quite often
- All we have is labeled data



 Estimate the probability distribution from the labeled data

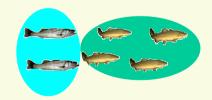
> little is known "harder"

# Unsupervised Learning and Clustering

- Data is not labeled
  - Happens quite often



- 1. Estimate the probability distribution from the *unlabeled* data
- 2. Cluster the data



a lot is known "easier"

> little is known "harder"

# Classification Summary

- 1. Bayesian Decision theory (rare case)
  - Know probability distribution of the categories
  - Do not even need training data
  - Can design optimal classifier
- 2. ML and Bayesian parameter estimation
  - Need to estimate Parameters of probability dist.
  - Need training data
- 3. Linear discriminant functions and Neural Nets
  - The shape of discriminant functions is known
  - Need to estimate parameters of discriminant functions
- 4. Non-Parametric Methods
  - No probability distribution, labeled data
- 5. Unsupervised Learning and Clustering
  - No probability distribution and unlabeled data

a lot is known

little is known